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# **kafe Documentation**

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**kafe** is a data fitting framework designed for use in undergraduate physics lab courses. It provides a basic *Python* toolkit for fitting and plotting using already available *Python* packages such as *NumPy* and *matplotlib*, as well as CERN *ROOT*'s version of the *Minuit* minimizer.

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## SUMMARY

The package provides a simple approach to fitting using variance-covariance matrices, thus allowing for error correlations to be taken into account. This implementation's error model assumes the measurement data (dependent variable) is distributed according to a *Gaussian* distribution centered at its "true" value. The spread of the distribution is given as a  $(1\sigma)$ -error.

An "errors-in-variables" model is also implemented to take uncertainties in the independent variable ( $x$  errors) into account. This is done by specifying/constructing a separate variance-covariance matrix for the  $x$  axis and "projecting" it onto the  $y$  error matrix. If the fit function is approximated in each point by its tangent line, the *Gaussian* errors in the  $x$  direction are not warped by this projection.

For examples on how to use **kafe**, see the `examples` folder. Consulting the [API](#) can also be helpful.





# API DOCUMENTATION

## 2.1 kafe Package

### 2.1.1 kafe Package

#### kafe

A Python package for fitting and plotting for use in physics lab courses.

This Python package allows fitting of user-defined functions to data. A dataset is represented by a *Dataset* object which stores measurement data as *NumPy* arrays. The uncertainties of the data are also stored in the *Dataset* as an *error matrix*, allowing for both correlated and uncorrelated errors to be accurately represented.

The constructor of a *Dataset* object accepts several keyword arguments and can be used to construct a *Dataset* out of data which has been loaded into *Python* as *NumPy* arrays. Alternatively, a plain-text representation of a *Dataset* can be read from a file.

Also provided are helper functions which construct a *Dataset* object from a file containing column data (one measurement per row, column order can be specified).

### 2.1.2 \_version\_info Module

### 2.1.3 constants Module

**F\_SIGNIFICANCE = 2**

Set significance for returning results and errors  $N$  = rounding error to  $N$  significant digits and value to the same order of magnitude as the error.

**G\_PADDING\_FACTOR\_X = 1.2**

factor by which to expand  $x$  data range

**G\_PADDING\_FACTOR\_Y = 1.2**

factor by which to expand  $y$  data range

**G\_PLOT\_POINTS = 200**

number of plot points for plotting the function

**M\_CONFIDENCE\_LEVEL = 0.05**

Confidence level for hypothesis test

**M\_MAX\_ITERATIONS = 6000**

Maximum *Minuit* iterations until abort

**M\_MAX\_X\_FIT\_ITERATIONS = 2**

Maximum additional iterations for  $x$  fit

**M\_TOLERANCE = 0.1**

Minuit tolerance level

## 2.1.4 dataset Module

**class Dataset** (*input\_file=None, data=None, cov\_mats=None, title='Untitled Dataset', basename=None, axis\_labels=['x', 'y'], axis\_units=['', '']*)

Bases: object

The *Dataset* object is a data structure for storing measurement and error data. In this implementation, the *Dataset* has the compulsory field *data*, which is used for storing the measurement data, and another field *cov\_mats*, used for storing the covariance matrix for each axis.

There are two ways a *Dataset* can be constructed. The most straightforward way is to specify an input file containing a plain-text representation of the dataset:

```
>>> my_dataset = Dataset(input_file='/path/to/file')
```

or

```
>>> my_dataset = Dataset(input_file=my_file_object)
```

If an *input\_file* argument is provided, the *data* and *cov\_mats* arguments are ignored. The *Dataset* plain-text representation format is as follows:

```
# x data
x_1  sigma_x_1
x_2  sigma_x_2  cor_x_12
...  ...      ...
x_N  sigma_x_N  cor_x_1N  ...  cor_x_NN

# y data
y_1  sigma_y_1
y_2  sigma_y_2  cor_y_12
...  ...      ...
y_N  sigma_y_N  cor_y_1N  ...  cor_y_NN
```

Here, the *sigma\_...* represents the fully uncorrelated error of the data point and *cor\_...\_ij* is the correlation coefficient between the *i*-th and *j*-th data point.

Alternatively, field data can be set by passing iterables as arguments. Available arguments for this purpose are:

**data** : tuple/list of tuples/lists/arrays of floats

a tuple/list of measurement data. Each element of the tuple/list must be iterable and be of the same length. The first element of the **data** tuple/list is assumed to be the  $x$  data, and the second to be the  $y$  data:

```
>>> my_dataset = Dataset(data=([0., 1., 2.], [1.23, 3.45, 5.62]))
```

Alternatively,  $x$ - $y$  value pairs can also be passed as **data**. The following is equivalent to the above:

```
>>> my_dataset = Dataset(data=([0.0, 1.23], [1.0, 3.45], [2.0, 5.62]))
```

In case the *Dataset* contains two data points, the ordering is ambiguous. In this case, the first ordering ( $x$  data first, then  $y$  data) is assumed.

*cov\_mats* : tuple/list of *numpy.matrix* (optional)

a tuple/list of two-dimensional iterables containing the covariance matrices for *x* and *y*, in that order. Covariance matrices can be any sort of two-dimensional NxN iterables, assuming N is the number of data points.

```
>>> my_dataset = Dataset(data=([0., 1., 2.], [1.23, 3.45, 5.62]), cov_mats=(my_cov_mat_x, my_cov_mat_y))
```

This keyword argument can be omitted, in which case covariance matrices of zero are assumed. To specify a covariance matrix for a single axis, replace the other with *None*.

```
>>> my_dataset = Dataset(data=([0., 1., 2.], [1.23, 3.45, 5.62]), cov_mats=(None, my_cov_mat_y))
```

*title* : string (optional)

the name of the *Dataset*. If omitted, the *Dataset* will be given the generic name 'Untitled Dataset'.

*axis\_labels* : list of strings (optional)

labels for the *x* and *y* axes. If omitted, these will be set to 'x' and 'y', respectively.

*axis\_units* : list of strings (optional)

units for the *x* and *y* axes. If omitted, these will be assumed to be dimensionless, i.e. the unit will be an empty string.

*cov\_mat\_is\_regular*(*axis*)

Returns *True* if the covariance matrix for an axis is regular and *False* if it is singular.

**axis** ['x' or 'y'] Axis for which to check for regularity of the covariance matrix.

*cov\_mats* = *None*

list of covariance matrices

*get\_axis*(*axis\_alias*)

Get axis id from an alias.

**axis\_alias** [string or int] Alias of the axis whose id should be returned. This is for example either '0' or 'x' for the *x*-axis (id 0).

*get\_cov\_mat*(*axis*, *fallback\_on\_singular*=*None*)

Get the error matrix for an axis.

**axis** ['x' or 'y'] Axis for which to load the error matrix.

**fallback\_on\_singular** [*numpy.matrix* or string (optional)] What to return if the matrix is singular. If this is *None* (default), the matrix is returned anyway. If this is a *numpy.matrix* object or similar, that is returned instead. Alternatively, the shortcuts 'identity' or 1 and 'zero' or 0 can be used to return the identity and zero matrix respectively.

*get\_data*(*axis*)

Get the measurement data for an axis.

**axis** [string] Axis for which to get the measurement data. Can be 'x' or 'y'.

*get\_data\_span*(*axis*, *include\_error\_bars*=*False*)

Get the data span for an axis. The data span is a tuple (*min*, *max*) containing the smallest and highest coordinates for an axis.

**axis** ['x' or 'y'] Axis for which to get the data span.

**include\_error\_bars** [boolean (optional)] True if the returned span should be enlarged to contain the error bars of the smallest and largest datapoints (default: *False*)

`get_formatted(format_string='.06e', delimiter='t')`

Returns the dataset in a plain-text format which is human-readable and can later be used as an input file for the creation of a new *Dataset*. The format is as follows:

```
# x data
x_1  sigma_x_1
x_2  sigma_x_2  cor_x_12
...  ...      ...      ...
x_N  sigma_x_N  cor_x_1N  ...  cor_x_NN

# y data
y_1  sigma_y_1
y_2  sigma_y_2  cor_y_12
...  ...      ...      ...
y_N  sigma_y_N  cor_y_1N  ...  cor_y_NN
```

Here, the  $x_i$  and  $y_i$  represent the measurement data, the  $\sigma_{x_i}$  are the statistical uncertainties of each data point, and the  $cor_{x_{ij}}$  are the correlation coefficients between the  $i$ -th and  $j$ -th data point.

If the  $x$  or  $y$  errors are not correlated, then the entire correlation coefficient matrix can be omitted. If there are no statistical uncertainties for an axis, the second column can also be omitted. A blank line is required at the end of each data block!

**format\_string** [string (optional)] A format string with which each entry will be rendered. Default is `' .06e '`, which means the numbers are represented in scientific notation with six significant digits.

**delimiter** [string (optional)] A delimiter used to separate columns in the output.

`get_size()`

Get the size of the *Dataset*. This is equivalent to the length of the  $x$ -axis data.

`has_correlations(axis)`

Returns *True* if the specified axis has correlation data, *False* if not.

**axis** [`'x'` or `'y'`] Axis for which to check for correlations.

`has_errors(axis)`

Returns *True* if the specified axis has statistical error data.

**axis** [`'x'` or `'y'`] Axis for which to check for error data.

`n_axes = None`

dimensionality of the *Dataset*. Currently, only 2D *Datasets* are supported

`n_datapoints = None`

number of data points in the *Dataset*

`read_from_file(input_file)`

Reads the *Dataset* object from a file.

**returns** [boolean] *True* if the read succeeded, *False* if not.

`set_cov_mat(axis, mat)`

Set the error matrix for an axis.

**axis** [`'x'` or `'y'`] Axis for which to load the error matrix.

**mat** [*numpy.matrix* or *None*] Error matrix for the axis. Passing *None* unsets the error matrix.

`set_data(axis, data)`

Set the measurement data for an axis.

**axis** [`'x'` or `'y'`] Axis for which to set the measurement data.

**data** [iterable] Measurement data for axis.

**write\_formatted**(*file\_path*, *format\_string*='%.06e', *delimiter*='t')

Writes the dataset to a plain-text file. For details on the format, see [get\\_formatted](#).

**file\_path** [string] Path of the file object to write. **WARNING:** *overwrites existing files!*

**format\_string** [string (optional)] A format string with which each entry will be rendered. Default is ' %.06e ', which means the numbers are represented in scientific notation with six significant digits.

**delimiter** [string (optional)] A delimiter used to separate columns in the output.

**build\_dataset**(*xdata*, *ydata*, *cov\_mats*=None, *xabserr*=0.0, *xrelerr*=0.0, *xabscor*=0.0, *xrelcor*=0.0, *yabserr*=0.0, *yrelerr*=0.0, *yabscor*=0.0, *yrelcor*=0.0, *title*=None, *basename*=None, *axis\_labels*=None, *axis\_units*=None)

This helper function creates a *Dataset* from a series of keyword arguments.

Valid keyword arguments are:

**xdata and ydata** [list/tuple/*np.array* of floats] These keyword arguments are mandatory and should be iterables containing the measurement data.

**cov\_mats** [None or 2-tuple (optional)] This argument defaults to None, which means no covariance matrices are used. If covariance matrices are needed, a tuple with two entries (the first for *x* covariance matrices, the second for *y*) must be passed.

Each element of this tuple may be either None or a NumPy matrix object containing a covariance matrix for the respective axis.

**error specification keywords** [iterable or numeric (see below)] In addition to covariance matrices, errors can be specified for each axis (*x* or *y*) according to a simplified error model.

In this respect, a valid keyword is composed of an axis, an error relativity specification (*abs* or *rel*) and error correlation type (*err* or *cor*). The errors are then set as follows:

1. For totally uncorrelated errors (*err*):

- if keyword argument is iterable, the error list is set to that
- if keyword argument is a number, an error list with identical entries is generated

2. For fully correlated errors (*cor*):

- keyword argument *must* be a single number. The global correlated error for the axis is then set to that.

So, for example:

```
>>> myDataset = build_dataset(..., yabserr=0.3, yrelcor=0.1)
```

creates a *Dataset* with an uncorrelated error of 0.3 for each *y* coordinate and a fully correlated (systematic) error of *y* of 0.1.

**title** [string (optional)] The title of the *Dataset*.

**basename** [string or None (optional)] A basename for the *Dataset*. All output files related to this dataset will use this as a basename. If this is None (default), the basename will be inferred from the filename.

**axis\_labels** [2-tuple of strings (optional)] a 2-tuple containing the axis labels for the *Dataset*. This is relevant when plotting *Fits* of the *Dataset*, but is ignored when plotting more than one *Fit* in the same *Plot*.

**axis\_units** [2-tuple of strings (optional)] a 2-tuple containing the axis units for the *Dataset*. This is relevant when plotting *Fits* of the *Dataset*, but is ignored when plotting more than one *Fit* in the same *Plot*.

## 2.1.5 file\_tools Module

**parse\_column\_data**(*file\_to\_parse*, *field\_order*='x,y', *delimiter*=' ', *cov\_mat\_files*=None, *title*='Untitled Dataset', *basename*=None, *axis\_labels*=['x', 'y'], *axis\_units*=['', ''])

Parses a file which contains measurement data in a one-measurement-per-row format. The field (column) order can be specified. It defaults to *x,y*. Valid field names are *x*, *y*, *xabserr*, *yabserr*, *xrelerr*, *yrelerr*. Another valid field name is *ignore* which can be used to skip a field.

A certain type of field can appear several times. If this is the case, all specified errors are added in quadrature:

$$\sigma_{\text{tot}} = \sqrt{\sigma_1^2 + \sigma_2^2 + \dots}$$

Every valid measurement data file *must* have an *x* and a *y* field.

For more complex error models, errors and correlations may be specified as covariance matrices. If this is desired, then any number of covariance matrices (stored in separate files) may be specified for an axis by using the *cov\_mat\_files* argument.

Additionally, a delimiter can be specified. If this is a whitespace character or omitted, any sequence of whitespace characters is assumed to separate the data.

**file\_to\_parse** [file-like object or string containing a file path] The file to parse.

**field\_order** [string (optional)] A string of comma-separated field names giving the order of the columns in the file. Defaults to 'x,y'.

**delimiter** [string (optional)] The field delimiter used in the file. Defaults to any whitespace.

**cov\_mat\_files** [*several* (see below, optional)] This argument defaults to None, which means no covariance matrices are used. If covariance matrices are needed, a tuple with two entries (the first for *x* covariance matrices, the second for *y*) must be passed.

Each element of this tuple may be either None, a file or file-like object, or an iterable containing files and file-like objects. Each file should contain a covariance matrix for the respective axis.

When creating the *Dataset*, all given matrices are summed over.

**title** [string (optional)] The title of the *Dataset*.

**basename** [string or None (optional)] A basename for the *Dataset*. All output files related to this dataset will use this as a basename. If this is None (default), the basename will be inferred from the filename.

**axis\_labels** [2-tuple of strings (optional)] a 2-tuple containing the axis labels for the *Dataset*. This is relevant when plotting *Fits* of the *Dataset*, but is ignored when plotting more than one *Fit* in the same *Plot*.

**axis\_units** [2-tuple of strings (optional)] a 2-tuple containing the axis units for the *Dataset*. This is relevant when plotting *Fits* of the *Dataset*, but is ignored when plotting more than one *Fit* in the same *Plot*.

**return** [*Dataset*] A *Dataset* built from the parsed file.

**parse\_matrix\_file**(*file\_like*, *delimiter*=None)

Read a matrix from a matrix file. The format of the matrix file should be:

```
# comment row
a_11 a_12 ... a_1M
a_21 a_22 ... a_2M
...   ...   ...
a_N1 a_N2 ... a_NM
```

**file\_like** [string or file-like object] File path or file object to read matrix from.

**delimiter** [None or string (optional)] Column delimiter use in the matrix file. Defaults to None, meaning any whitespace.

## 2.1.6 fit Module

**class Fit**(*dataset*, *fit\_function*, *external\_fcn*=<function chi2 at 0x300bb18>, *fit\_label*=None)

Bases: object

Object representing a fit. This object references the fitted *Dataset*, the fit function and the resulting fit parameters.

Necessary arguments are a *Dataset* object and a fit function (which should be fitted to the *Dataset*). Optionally, an external function *FCN* (whose minima should be located to find the best fit) can be specified. If not given, the *FCN* function defaults to  $\chi^2$ .

**dataset** [*Dataset*] A *Dataset* object containing all information about the data

**fit\_function** [function] A user-defined Python function to be fitted to the data. This function's first argument must be the independent variable *x*. All other arguments *must* be named and have default values given. These defaults are used as a starting point for the actual minimization. For example, a simple linear function would be defined like:

```
>>> def linear_2par(x, slope=1, y_intercept=0):
...     return slope * x + y_intercept
```

Be aware that choosing sensible initial values for the parameters is often crucial for a successful fit, particularly for functions of many parameters.

**external\_fcn** [function (optional)] An external *FCN* (function to minimize). This function must have the following call signature:

```
>>> FCN(xdata, ydata, cov_mat, fit_function, parameter_values)
```

It should return a float. If not specified, the default  $\chi^2$  *FCN* is used. This should be sufficient for most fits.

**fit\_label** [*LaTeX*-formatted string (optional)] A name/label/short description of the fit function. This appears in the legend describing the fitter curve. If omitted, this defaults to the fit function's *LaTeX* expression.

**call\_external\_fcn**(\**parameter\_names*)

Wrapper for the external *FCN*. Since the actual fit process depends on finding the right parameter values and keeping everything else constant we can use the *Dataset* object to pass known, fixed information to the external *FCN*, varying only the parameter values.

**parameter\_names** [sequence of values] the parameter values at which *FCN* is to be evaluated

**current\_cov\_mat** = None

the current covariance matrix used for the *Fit*

**dataset** = None

this *Fit* instance's child *Dataset*

**do\_fit**(*quiet*=False, *verbose*=False)

Runs the fit algorithm for this *Fit* object.

First, the *Dataset* is fitted considering only uncertainties in the *y* direction. If the *Dataset* has no uncertainties in the *y* direction, they are assumed to be equal to 1.0 for this preliminary fit, as there is no better information available.

Next, the fit errors in the *x* direction (if they exist) are taken into account by projecting the covariance matrix for the *x* errors onto the *y* covariance matrix. This is done by taking

the first derivative of the fit function in each point and “projecting” the  $x$  error onto the resulting tangent to the curve.

This last step is repeated until the change in the error matrix caused by the projection becomes negligible.

**quiet** [boolean (optional)] Set to True if no output should be printed.

**verbose** [boolean (optional)] Set to True if more output should be printed.

**external\_fcn** = **None**

the (external) function to be minimized for this *Fit*

**fit\_function** = **None**

the fit function used for this *Fit*

**fit\_one\_iteration**(*verbose=False*)

Instructs the minimizer to do a minimization.

**fix\_parameters**(\**parameters\_to\_fix*)

Fix the given parameters so that the minimizer works without them when *do\_fit* is called next. Parameters can be given by their names or by their IDs.

**get\_current\_fit\_function**()

This method returns a function object corresponding to the fit function for the current parameter values. The returned function is a function of a single variable.

**returns** [function] A function of a single variable corresponding to the fit function at the current parameter values.

**get\_error\_matrix**()

This method returns the covariance matrix of the fit parameters which is obtained by querying the minimizer object for this *Fit*

**returns** [*numpy.matrix*] The covariance matrix of the parameters.

**get\_parameter\_errors**(*rounding=False*)

Get the current parameter uncertainties from the minimizer.

**rounding** [boolean (optional)] Whether or not to round the returned values to significance.

**returns** [tuple] A tuple of the parameter uncertainties

**get\_parameter\_values**(*rounding=False*)

Get the current parameter values from the minimizer.

**rounding** [boolean (optional)] Whether or not to round the returned values to significance.

**returns** [tuple] A tuple of the parameter values

**latex\_parameter\_names** = **None**

L<sup>A</sup>T<sub>E</sub>X parameter names

**minimizer** = **None**

this *Fit*’s minimizer (*Minuit*)

**number\_of\_parameters** = **None**

the total number of parameters

**parameter\_names** = **None**

the names of the parameters

**print\_fit\_details**()

prints some fit goodness details

**print\_fit\_results**()

prints fit results



**print\_rounded\_fit\_parameters()**

prints the fit parameters

**project\_x\_covariance\_matrix()**

Project the  $x$  errors from the  $x$  covariance matrix onto the total matrix.

This is done elementwise, according to the formula:

$$C_{\text{tot},ij} = C_{y,ij} + C_{x,ij} \frac{\partial f}{\partial x_i} \frac{\partial f}{\partial x_j}$$

**release\_parameters(\*parameters\_to\_fix)**

Release the given parameters so that the minimizer begins to work with them when *do\_fit* is called next. Parameters can be given by their names or by their IDs. If no arguments are provided, then release all parameters.

**set\_parameters(\*args, \*\*kwargs)**

Sets the parameter values (and optionally errors) for this fit. This is usually called just before the fit is done, to establish the initial parameters. If a parameter error is omitted, it is set to 1/1000th of the parameter values themselves. If the default value of the parameter is 0, it is set, by exception, to 0.001.

This method accepts up to two positional arguments and several keyword arguments.

**args[0]** [tuple/list of floats (optional)] The first positional argument is expected to be a tuple/list containing the parameter values.

**args[1]** [tuple/list of floats (optional)] The second positional argument is expected to be a tuple/list of parameter errors, which can also be set as an approximate estimate of the problem's uncertainty.

**no\_warning** [boolean (optional)] Whether to issue warnings (False) or not (True) when communicating with the minimizer fails. Defaults to False.

Valid keyword argument names are parameter names. The keyword arguments themselves may be floats (parameter values) or 2-tuples containing the parameter values and the parameter error in that order:

**<parameter\_name>** [float or 2-tuple of floats (optional)] Set the parameter with the name **<'parameter\_name'>** to the value given. If a 2-tuple is given, the first element is understood to be the value and the second to be the parameter error.

**xdata = None**

the  $x$  coordinates of the data points used for this *Fit*

**ydata = None**

the  $y$  coordinates of the data points used for this *Fit*

**chi2(xdata, ydata, cov\_mat, fit\_function, parameter\_values)**

A simple  $\chi^2$  implementation. Calculates  $\chi^2$  according to the formula:

$$\chi^2 = \lambda^T C^{-1} \lambda$$

Here,  $\lambda$  is the residual vector  $\lambda = \vec{y} - \vec{f}(\vec{x})$  and  $C$  is the covariance matrix.

**xdata** [iterable] The  $x$  measurement data

**ydata** [iterable] The  $y$  measurement data

**cov\_mat** [numpy.matrix] The total covariance matrix

**fit\_function** [function] The fit function  $f(x)$

**parameter\_values** [list/tuple] The values of the parameters at which  $f(x)$  should be evaluated.

`round_to_significance(value, error, significance=2)`

Rounds the error to the established number of significant digits, then rounds the value to the same order of magnitude as the error.

**value** [float] value to round to significance

**error** [float] uncertainty of the value

**significance** [int (optional)] number of significant digits of the error to consider

## 2.1.7 function\_library Module

## 2.1.8 function\_tools Module

`ASCII(**kwargs)`

Optional decorator for fit functions. This overrides a FitFunction's plain-text (ASCII) attributes. The new values for these attributes must be passed as keyword arguments to the decorator. Possible arguments:

**name** [string] Plain-text representation of the function name.

**parameter\_names** [list of strings] List of plain-text representations of the function's arguments. The length of this list must be equal to the function's argument number. The argument names should be in the same order as in the function definition.

**x\_name** [string] Plain-text representation of the independent variable's name.

**expression** [string] Plain-text-formatted expression representing the function's formula.

`class FitFunction(f)`

Decorator class for fit functions. If a function definition is decorated using this class, some information is collected about the function which is relevant to the fitting process, such as the number of parameters, their names and default values. Some details pertaining to display and representation are also set, such as L<sup>A</sup>T<sub>E</sub>X representations of the parameter names and the function name. Other decorators can be applied to a function object to specify things such as a L<sup>A</sup>T<sub>E</sub>X or plain-text expression for the fit function.

`derive_by_parameters(x_o, derivative_spacing, parameter_list)`

Returns the gradient of *func* with respect to its parameters, i.e. with respect to every variable of *func* except the first one.

`derive_by_x(x_o, derivative_spacing, parameter_list)`

If *x\_o* is iterable, gives the array of derivatives of a function  $f(x, \text{par}_1, \text{par}_2, \dots)$  around  $x = x_i$  at every  $x_i$  in  $\vec{x}$ . If *x\_o* is not iterable, gives the derivative of a function  $f(x, \text{par}_1, \text{par}_2, \dots)$  around  $x = x_0$ .

**expression = None**

a math expression (string) representing the function's result

`get_function_equation(equation_format='latex', equation_type='full', ensuremath=True)`

Returns a string representing the function equation. Supported formats are L<sup>A</sup>T<sub>E</sub>X and ASCII inline math. Note that L<sup>A</sup>T<sub>E</sub>X math is wrapped by default in an `\ensuremath{}` expression. If this is not desired behaviour, the flag `ensuremath` can be set to `False`.

**equation\_format** [string (optional)] Can be either "latex" (default) or "ascii".

**equation\_type** [string (optional)] Can be either "full" (default), "short" or "name". A "name"-type equation returns a representation of the function name:

*f*

A "short"-type equation limits itself to the function name and variables:

```
f(x, par1, par2)
```

A “full”-type equation includes the expression which the function calculates:

```
f(x, par1, par2) = par1 * x + par2
```

**ensuremath** [boolean (optional)] If a  $\LaTeX$  math equation is requested, True (default) will wrap the resulting expression in an `\ensuremath{}` tag. Otherwise, no wrapping is done.

**latex\_expression = None**

a  $\LaTeX$  math expression, the function’s result

**latex\_name = None**

The function’s name in  $\LaTeX$

**latex\_parameter\_names = None**

A list of parameter names in  $\LaTeX$

**latex\_x\_name = None**

A  $\LaTeX$  symbol for the independent variable.

**name = None**

The name of the function

**number\_of\_parameters = None**

The number of parameters

**parameter\_defaults = None**

The default values of the parameters

**parameter\_names = None**

The names of the parameters

**sourcelines = None**

string object holding the source code for the fit-function

**x\_name = None**

The name given to the independent variable

**$\LaTeX$ (\*\*kwargs)**

Optional decorator for fit functions. This overrides a FitFunction’s *latex\_* attributes. The new values for the *latex\_* attributes must be passed as keyword arguments to the decorator. Possible arguments:

**name** [string]  $\LaTeX$  representation of the function name.

**parameter\_names** [list of strings] List of  $\LaTeX$  representations of the function’s arguments. The length of this list must be equal to the function’s argument number. The argument names should be in the same order as in the function definition.

**x\_name** [string]  $\LaTeX$  representation of the independent variable’s name.

**expression** [string]  $\LaTeX$ -formatted expression representing the function’s formula.

**derivative**(func, derive\_by\_index, variables\_tuple, derivative\_spacing)

Gives  $\frac{\partial f}{\partial x_k}$  for  $f = f(x_0, x_1, \dots)$ . *func* is *f*, *variables\_tuple* is  $\{x_i\}$  and *derive\_by\_index* is *k*.

**outer\_product**(input\_array)

Takes a NumPy array and returns the outer (dyadic, Kronecker) product with itself. If *input\_array* is a vector *x*, this returns  $xx^T$ .

### 2.1.9 latex\_tools Module

`ascii_to_latex_math(str_ascii, monospace=True, ensuremath=True)`

Escapes certain characters in an ASCII input string so that the result can be included in math mode without error.

**str\_ascii** [string] A plain-text string containing characters to be escaped for L<sup>A</sup>T<sub>E</sub>X math mode.

**monospace** [boolean (optional)] Whether to render the whole expression as monospace. Defaults to True.

**ensuremath** [boolean (optional)] If this is True, the resulting formula is wrapped in an `\ensuremath{}` tag. Defaults to True.

### 2.1.10 minuit Module

`D_MATRIX_ERROR = {0: 'Error matrix not calculated', 1: 'Error matrix approximate!', 2: 'Error matrix forced positive d`  
Error matrix status codes

`class Minuit(number_of_parameters, function_to_minimize, parameter_names, start_parameters, parameter_errors, quiet=True, verbose=False)`

A class for communicating with ROOT's function minimizer tool Minuit.

`FCN_wrapper(number_of_parameters, derivatives, f, parameters, internal_flag)`

This is actually a function called in *ROOT* and acting as a C wrapper for our *FCN*, which is implemented in Python.

This function is called by *Minuit* several times during a fit. It doesn't return anything but modifies one of its arguments (*f*). This is *ugly*, but it's how *ROOT*'s *TMinuit* works. Its argument structure is fixed and determined by *Minuit*:

**number\_of\_parameters** [int] The number of parameters of the current fit

**derivatives** [C array] If the user chooses to calculate the first derivative of the function inside the *FCN*, this value should be written here. This interface to *Minuit* ignores this derivative, however, so calculating this inside the *FCN* has no effect (yet).

**f** [C array] The desired function value is in `f[0]` after execution.

**parameters** [C array] A C array of parameters. Is cast to a Python list

**internal\_flag** [int] A flag allowing for different behaviour of the function. Can be any integer from 1 (initial run) to 4(normal run). See *Minuit*'s specification.

`fix_parameter(parameter_number)`

Fix parameter number `<parameter_number>`.

**parameter\_number** [int] Number of the parameter to fix.

`function_to_minimize = None`

the actual *FCN* called in *FCN\_wrapper*

`get_chi2_probability(n_deg_of_freedom)`

Returns the probability that an observed  $\chi^2$  exceeds the calculated value of  $\chi^2$  for this fit by chance, even for a correct model. In other words, returns the probability that a worse fit of the model to the data exists. If this is a small value (typically  $<5\%$ ), this means the fit is pretty bad. For values below this threshold, the model very probably does not fit the data.

**n\_def\_of\_freedom** [int] The number of degrees of freedom. This is typically `n_extdatapoints - n_extparameters`.

`get_contour(parameter1, parameter2, n_points=20)`

Returns a list of points (2-tuples) representing a sampling of the  $1\sigma$  contour of the *TMinuit* fit. The *FCN* has to be minimized before calling this.

**parameter1** [int] ID of the parameter to be displayed on the  $x$ -axis.

**parameter2** [int] ID of the parameter to be displayed on the  $y$ -axis.

**n\_points** [int (optional)] number of points used to draw the contour. Default is 20.

**returns** [2-tuple of tuples] a 2-tuple (x, y) containing **n\_points**+1 points sampled along the contour. The first point is repeated at the end of the list to generate a closed contour.

**get\_error\_matrix()**  
Retrieves the parameter error matrix from TMinuit.

return : *numpy.matrix*

**get\_fit\_info(info)**  
Retrieves other info from *Minuit*.

**info** [string] Information about the fit to retrieve. This can be any of the following:

- 'fcn': FCN value at minimum,
- 'edm': estimated distance to minimum
- 'err\_def': *Minuit* error matrix status code
- 'status\_code': *Minuit* general status code

**get\_parameter\_errors()**  
Retrieves the parameter errors from TMinuit.

return [tuple] Current *Minuit* parameter errors

**get\_parameter\_info()**  
Retrieves parameter information from TMinuit.

return [list of tuples] (parameter\_name, parameter\_val, parameter\_error)

**get\_parameter\_name(parameter\_nr)**  
Gets the name of parameter number **parameter\_nr**

**parameter\_nr** [int] Number of the parameter whose name to get.

**get\_parameter\_values()**  
Retrieves the parameter values from TMinuit.

return [tuple] Current *Minuit* parameter values

**max\_iterations = None**  
maximum number of iterations until TMinuit gives up

**minimize(log\_print\_level=3)**  
Do the minimization. This calls *Minuit*'s algorithms MIGRAD for minimization and HESSE for computing/checking the parameter error matrix.

**number\_of\_parameters = None**  
number of parameters to minimize for

**release\_parameter(parameter\_number)**  
Release parameter number <parameter\_number>.

**parameter\_number** [int] Number of the parameter to release.

**reset()**  
Execute TMinuit's *mnrset* method.

**set\_err(up\_value=1.0)**  
Sets the UP value for Minuit.

**up\_value** [float (optional, default: 1.0)] This is the value by which *FCN* is expected to change.

**set\_parameter\_errors**(*parameter\_errors=None*)

Sets the fit parameter errors. If *parameter\_values='None'*, sets the error to 1% of the parameter value.

**set\_parameter\_names**(*parameter\_names*)

Sets the fit parameters. If *parameter\_values='None'*, tries to infer defaults from the *function\_to\_minimize*.

**set\_parameter\_values**(*parameter\_values*)

Sets the fit parameters. If *parameter\_values='None'*, tries to infer defaults from the *function\_to\_minimize*.

**set\_print\_level**(*print\_level=1*)

Sets the print level for Minuit.

**print\_level** [int (optional, default: 1 (frugal output))] Tells TMinuit how much output to generate. The higher this value, the more output it generates.

**set\_strategy**(*strategy\_id=1*)

Sets the strategy Minuit.

**strategy\_id** [int (optional, default: 1 (optimized))] Tells TMinuit to use a certain strategy. Refer to TMinuit's documentation for available strategies.

**tolerance = None**

TMinuit tolerance

**update\_parameter\_data**(*show\_warnings=False*)

(Re-)Sets the parameter names, values and step size on the C++ side of Minuit.

**P\_DETAIL\_LEVEL = 1**

default level of detail for TMinuit's output (typical range: -1 to 3, default: 1)

## 2.1.11 numeric\_tools Module

**cor\_to\_cov**(*cor\_mat, error\_list*)

Converts a correlation matrix to a covariance matrix according to the formula

$$\text{Cov}_{ij} = \text{Cor}_{ij} \sigma_i \sigma_j$$

**cor\_mat** [*numpy.matrix*] The correlation matrix to convert.

**error\_list** [sequence of floats] A sequence of statistical errors. Must be of the same length as the diagonal of *cor\_mat*.

**cov\_to\_cor**(*cov\_mat*)

Converts a covariance matrix to a correlation matrix according to the formula

$$\text{Cor}_{ij} = \frac{\text{Cov}_{ij}}{\sqrt{\text{Cov}_{ii} \text{Cov}_{jj}}}$$

**cov\_mat** [*numpy.matrix*] The covariance matrix to convert.

**extract\_statistical\_errors**(*cov\_mat*)

Extracts the statistical errors from a covariance matrix. This means it returns the (elementwise) square root of the diagonal entries

**cov\_mat** The covariance matrix to extract errors from. Type: *numpy.matrix*

**make\_symmetric\_lower**(*mat*)

Copies the matrix entries below the main diagonal to the upper triangle half of the matrix. Leaves the diagonal unchanged. Returns a *NumPy* matrix object.

**mat** [*numpy.matrix*] A lower diagonal matrix.

**returns** [*numpy.matrix*] The lower triangle matrix.

**zero\_pad\_lower\_triangle**(*triangle\_list*)

Converts a list of lists into a lower triangle matrix. The list members should be lists of increasing length from 1 to N, N being the dimension of the resulting lower triangle matrix. Returns a *NumPy* matrix object.

For example:

```
>>> zero_pad_lower_triangle([ [1.0], [0.2, 1.0], [0.01, 0.4, 3.0] ])
matrix([[ 1. ,  0. ,  0. ],
        [ 0.2 ,  1. ,  0. ],
        [ 0.01,  0.4 ,  3. ]])
```

**triangle\_list** [list] A list containing lists of increasing length.

**returns** [*numpy.matrix*] The lower triangle matrix.

## 2.1.12 plot Module

**class Plot**(\*fits, \*\*kwargs)

Bases: object

**axis\_labels** = None

axis labels

**compute\_plot\_range**(*include\_errorBars=True*)

Compute the span of all child datasets and sets the plot range to that

**draw\_fit\_parameters\_box**(*plot\_spec=o*)

Draw the parameter box to the canvas

**plot\_spec** [int, list of ints, string or None (optional, default: o)] Specify the plot id of the plot for which to draw the parameters. Passing o will only draw the parameter box for the first plot, and so on. Passing a list of ints will only draw the parameters for plot ids inside the list. Passing 'all' will print parameters for all plots. Passing None will return immediately doing nothing.

**draw\_legend**()

Draw the plot legend to the canvas

**extend\_span**(*axis, new\_span*)

Expand the span of the current plot.

This method extends the current plot span to include *new\_span*

**fits** = None

list of 'Fit's to plot

**init\_plots**()

Initialize the plots for each fit.

**plot**(*p\_id, show\_data=True, show\_function=True*)

Plot the *Fit* object with the number *p\_id* to its figure.

**plot\_all**(*show\_info\_for='all', show\_data\_for='all', show\_function\_for='all'*)

Plot every *Fit* object to its figure.

`plot_range = None`  
plot range

`plot_style = None`  
plot style

`save(output_file)`  
Save the *Plot* to a file.

`show()`  
Show the *Plot* in a matplotlib interactive window.

`show_legend = None`  
whether to show the plot legend (True) or not (False)

#### **class PlotStyle**

Class for specifying a style for a specific plot. This object stores a progression of marker and line types and colors, as well as preferences relating to point size and label size. These can be overridden by overwriting the instance variables directly. A series of *get\_...* methods are provided which go through these lists cyclically.

`get_line(idm)`  
Get a specific line type. This runs cyclically through the defined defaults.

`get_linecolor(idm)`  
Get a specific line color. This runs cyclically through the defined defaults.

`get_marker(idm)`  
Get a specific marker type. This runs cyclically through the defined defaults.

`get_markercolor(idm)`  
Get a specific marker color. This runs cyclically through the defined defaults.

`get_pointsize(idm)`  
Get a specific point size. This runs cyclically through the defined defaults.

#### **label\_to\_latex(label)**

Generates a simple LaTeX-formatted label from a plain-text label. This treats isolated characters and words beginning with a backslash as mathematical expressions and surround them with \$ signs accordingly.

**label** [string] Plain-text string to convert to LaTeX.

#### **pad\_span(span, pad\_coeff=1, additional\_pad=None)**

Enlarges the interval *span* (list of two floats) symmetrically around its center to length *pad\_coeff*. Optionally, an *additional\_pad* argument can be specified. The returned span is then additionally enlarged by that amount.

*additional\_pad* can also be a list of two floats which specifies an asymmetric amount by which to enlarge the span. Note that in this case, positive entries in *additional\_pad* will enlarge the span (move the interval end away from the interval's center) and negative amounts will shorten it (move the interval end towards the interval's center).

### **2.1.13 stream Module**

#### **class StreamDup(out\_file, suppress\_stdout=False)**

Bases: object

Object for simultaneous logging to stdout and files. This object provides a file/like object for the output to be written to. Writing to this object will write to stdout (usually the console) and to a file.



**out\_file** [file path or file-like object or list of file paths ...] File(s) to which to log the output, along with stdout. If a file exists on disk, it will be appended to.

**suppress\_stdout** [boolean] Whether to log to stdout simultaneously (False) or suppress output to stdout (True). Default to False.

**fileno()**

Returns the file handler id of the main (first) output file.

**flush()**

**write(message)**

**write\_timestamp(prefix)**

**write\_to\_file(message)**

**write\_to\_stdout(message, check\_if\_suppressed=False)**

Explicitly write to stdout. This method will not check by default whether `suppress_stdout` is set for this *StreamDup*. If `check_if_suppressed` is explicitly set to True, then this check occurs.

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