# **Charter Font Sample**Probability Cheatsheet Content

#### 1 Fundamental Definitions

**Random Variable** A function  $X : \Omega \to \mathbb{R}$  that assigns a real number to each outcome in the sample space  $\Omega$ .

**Independence** Events *A* and *B* are independent if:

$$P(A \cap B) = P(A)P(B)$$
$$P(A|B) = P(A)$$

### 2 Key Probability Rules

Bayes' Theorem:  $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$ 

**Law of Total Probability:** For partition  $\{B_i\}$ :  $P(A) = \sum_i P(A|B_i)P(B_i)$ 

## 3 Expected Value

The average value of a random variable:

$$E(X) = \sum_{x} x \cdot P(X = x)$$
 (discrete)

$$E(X) = \int_{-\infty}^{\infty} x f(x) dx$$
 (continuous)

Linearity: E(aX + bY + c) = aE(X) + bE(Y) + c

**Variance:**  $Var(X) = E(X^2) - [E(X)]^2$ 

#### 4 Common Distributions

**Binomial:**  $X \sim \text{Bin}(n, p)$  has PMF  $P(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$ 

Properties: E(X) = np, Var(X) = np(1-p)

**Poisson:**  $X \sim \operatorname{Pois}(\lambda)$  has PMF  $P(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}$ 

Properties:  $E(X) = \lambda$ ,  $Var(X) = \lambda$ Normal:  $X \sim \mathcal{N}(\mu, \sigma^2)$  has PDF:

 $f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$ 

Properties:  $E(X) = \mu$ ,  $Var(X) = \sigma^2$