Curso: Ensino Superior

Bacharelado em Ciência da Computação Disciplina: Cálculo Diferencial e Integral I Professora Me: Joelma Kominkiewicz Scolaro

Atividade 05 - Propriedades de Limites e limites no infinito

Data: 25/10/2021.

01- Calcule usando as propriedades:

Dado que

$$\lim_{x \to 2} f(x) = 4 \qquad \lim_{x \to 2} g(x) = -2 \qquad \lim_{x \to 2} h(x) = 0$$

encontre, se existir, o limite. Caso não exista, explique por quê.

(a)
$$\lim_{x \to 2} [f(x) + 5g(x)]$$
 (b) $\lim_{x \to 2} [g(x)]^3$

(c)
$$\lim_{x \to 2} \sqrt{f(x)}$$
 (d) $\lim_{x \to 2} \frac{3f(x)}{g(x)}$

(e)
$$\lim_{x \to 2} \frac{g(x)}{h(x)}$$
 (f)
$$\lim_{x \to 2} \frac{g(x)h(x)}{f(x)}$$

2) Calcule os seguintes limites pela substituição:

a)
$$\lim_{x \to 2} x =$$
 h) $\lim_{x \to 1} \frac{x^2 + 2x}{3x - 1} =$

b)
$$\lim_{x \to 2} x^3 =$$
 i) $\lim_{x \to 3} (4x^2 - 2x + 1) =$

c)
$$\lim_{x \to 1} 2x =$$
 j) $\lim_{x \to 1} (2x^3 + 3x^2 - x + 3) =$

d)
$$\lim_{x \to 1} x^6 =$$
 1) $\lim_{x \to 1} (3x^2 - 2x - 1) =$

e)
$$\lim_{x \to 3} (x^2 - x) =$$
 m) $\lim_{x \to 2} \frac{x+1}{x^2} =$

f)
$$\lim_{x \to 3} \frac{x+1}{x^2} =$$
 n) $\lim_{x \to 0} (4x^3 + 2x^2 + x + 2) =$

g)
$$\lim_{x \to 2} (3x + x^2) =$$
 o) $\lim_{x \to 1} (x^4 - x^3 + x^2 + x + 1) =$

p)
$$\lim_{x\to -1} (-2x^2 - x + 2) =$$

p)
$$\lim_{x \to 2} (x^3 - x^2 - 3)^{10} =$$

r)
$$\lim_{x \to 1} (x+2)^5 =$$

s)
$$\lim_{x \to 3} \frac{x^3 + x^2 + x + 1}{x^2 - 1} =$$

t)
$$\lim_{x \to 0} \frac{x^2 + x}{x^3 + x^2 + x + 1} =$$

u)
$$\lim_{x \to 1} \frac{3}{2x+1} =$$

v)
$$\lim_{x \to -1} \frac{3x^2 + x + 1}{2} =$$

x)
$$\lim_{x \to 0} \frac{x^3 + 2x^2 + 3x + 2}{2x^3 + x^2 + 2x + 4} =$$

3) Calcule os seguintes limites indeterminados:

a)
$$\lim_{x \to 3} \frac{x^2 - 9}{x - 3} =$$

e)
$$\lim_{x \to 0} \frac{x^3}{2x^2 - x} =$$

i)
$$\lim_{x \to 4} \frac{x^2 - 7x + 12}{x - 4} =$$

b)
$$\lim_{x \to -7} \frac{49 - x^2}{7 + x} =$$

f)
$$\lim_{x \to -7} \frac{49 + 14x + x^2}{7 + x} =$$

j)
$$\lim_{x\to 1} \frac{x-1}{x^2-3x+2} =$$

c)
$$\lim_{x \to 5} \frac{5 - x}{25 - x^2} =$$

g)
$$\lim_{x \to 3} \frac{x^2 - 6x + 9}{x - 3} =$$

$$1) \lim_{x \to 1} \frac{x^2 - 2x + 1}{x - 1} =$$

d)
$$\lim_{x\to 0} \frac{x^2 + x}{x^2 - 3x} =$$

h)
$$\lim_{x \to 1} \frac{x^2 - 4x + 3}{x - 1} =$$

m)
$$\lim_{x \to 2} \frac{x-2}{x^2-4} =$$

4-

Calcule os limites laterais:

a)
$$\lim_{x\to 6^+} \frac{4}{x-6} =$$

b)
$$\lim_{x\to 6^-} \frac{4}{x-6} =$$

c)
$$\lim_{x \to 1^+} \frac{3}{1-x} =$$

d)
$$\lim_{x\to 1^-} \frac{3}{1-x} =$$

e)
$$\lim_{x \to 0^+} \frac{x + 5}{x} =$$

f)
$$\lim_{x \to 0^-} \frac{x+5}{x} =$$

g)
$$\lim_{x \to 1^+} \frac{x^2}{x-1} =$$

h)
$$\lim_{x \to 1^-} \frac{x^2}{x-1} =$$

i)
$$\lim_{x\to 0^+} \frac{-1}{x^2} =$$

j)
$$\lim_{x\to 0^-} \frac{-1}{x^2} =$$

05- Calcule os limites, caso existam.

a)
$$\lim_{x\to +\infty} (2x+7)$$

b)
$$\lim_{x \to -\infty} (-4x + 1)$$

c)
$$\lim_{x \to +\infty} (3x^6 + 2x^3 - x + 4)$$

d)
$$\lim_{x \to \infty} (4x^7 + 2x^2 + \sqrt{3}x)$$
 e) $\lim_{x \to \infty} \frac{8x + 1}{4x - 5}$

e)
$$\lim_{x \to \infty} \frac{8x+1}{4x-5}$$

f)
$$\lim_{x \to -\infty} \frac{3x+2}{x^2-5x+6}$$

g)
$$\lim_{x \to \infty} \sqrt{2x^3 - x^2 + x + 1}$$
 h) $\lim_{x \to \infty} \sqrt{\frac{x^2 - 3x}{x^2 - 1}}$ i) $\lim_{x \to \infty} \left(\frac{6x - 1}{2x + 3}\right)^2$

h)
$$\lim_{x \to \infty} \sqrt{\frac{x^2 - 3x}{x^2 - 1}}$$

i)
$$\lim_{x \to \infty} \left(\frac{6x - 1}{2x + 3} \right)^2$$

j)
$$\lim_{x \to 0} \sqrt{x^2 - 5x + 7} - x$$

j)
$$\lim_{x \to \infty} \sqrt{x^2 - 5x + 7} - x$$
 k) $\lim_{x \to \infty} \frac{5x^2 - 3x + 1}{2x^2 + 4x - 7}$ l) $\lim_{x \to \infty} \frac{4 - 7x}{2 + 3x}$

1)
$$\lim_{x \to \infty} \frac{4-7x}{2+3x}$$

m)
$$\lim_{x \to \infty} \frac{-x^3 + 2x}{2x^2 - 3}$$
 n) $\lim_{x \to \infty} \frac{2 - x^2}{x + 3}$

n)
$$\lim_{x \to -\infty} \frac{2-x^2}{x+3}$$

$$o) \lim_{x \to \infty} \sqrt[3]{\frac{8+x^2}{x(x+1)}}$$

p)
$$\lim_{x\to\infty}\frac{3-2x}{5x+1}$$

q)
$$\lim_{x \to \infty} \frac{4x-3}{3x+2}$$

r)
$$\lim_{x \to \infty} \frac{x^2 - 4}{x + 1}$$

s)
$$\lim_{x \to -\infty} \frac{x^3 - 1}{x^2 + 1}$$

t)
$$\lim_{x \to \infty} \frac{x^2 - 3x + 4}{3x^3 + 5x^2 - 6x + 2}$$

u)
$$\lim_{x \to -\infty} \frac{x^2 + 4}{8x^3 - 1}$$

$$V) \lim_{x \to -\infty} \frac{x^2 + x + 1}{(x+1)^3 - x^3}$$

w)
$$\lim_{x\to\infty} \frac{(2x-3)^3}{x(x+1)(x+2)}$$

v)
$$\lim_{x \to \infty} \frac{x^2 + x + 1}{(x+1)^3 - x^3}$$
 w) $\lim_{x \to \infty} \frac{(2x-3)^3}{x(x+1)(x+2)}$ x) $\lim_{x \to \infty} \frac{(3x+2)^3}{2x(3x+1)(4x-1)}$

y)
$$\lim_{x\to\infty} \frac{(2x-3)^3(3x-2)^2}{x^5}$$

y)
$$\lim_{x \to \infty} \frac{(2x-3)^3(3x-2)^2}{x^5}$$
 z) $\lim_{x \to \infty} \frac{(x+2)^4 - (x-1)^4}{(2x+3)^3}$