

5)

$$\begin{aligned}
 1) \quad & (P \rightarrow Q) \wedge (P \rightarrow \perp) \Leftrightarrow P \rightarrow Q \wedge \perp \\
 & (\sim P \vee Q) \wedge (\sim P \vee \perp) \Leftrightarrow \\
 & \sim P \vee (Q \wedge \perp) \Leftrightarrow \\
 & \sim P \vee Q \wedge \perp \Leftrightarrow \\
 & P \rightarrow Q \wedge \perp \Leftrightarrow \\
 & \#
 \end{aligned}$$

$$6) \quad P \uparrow Q \Leftrightarrow ((P \downarrow P) \downarrow (Q \downarrow Q)) \downarrow ((P \downarrow P) \downarrow (Q \downarrow Q))$$

$$((P \downarrow P) \downarrow (Q \downarrow Q)) \downarrow ((P \downarrow P) \downarrow (Q \downarrow Q)) \Leftrightarrow$$

$$[(\sim P \wedge \sim P) \downarrow (\sim Q \wedge \sim Q)] \downarrow [(\sim P \wedge \sim P) \downarrow (\sim Q \wedge \sim Q)] \Leftrightarrow$$

$$[(\sim(P \wedge P) \downarrow (\sim(Q \wedge Q)))] \downarrow [(\sim(P \wedge P) \downarrow (\sim(Q \wedge Q)))] \Leftrightarrow$$

$$[(\sim P) \downarrow (\sim Q)] \downarrow [(\sim P) \downarrow (\sim Q)] \Leftrightarrow$$

$$[P \wedge Q] \downarrow [P \wedge Q] \Leftrightarrow$$

$$[\sim(p \wedge q)] \wedge [\sim(p \wedge q)] \Leftrightarrow$$

$$[\sim p \vee \sim q] \wedge [\sim p \vee \sim q] \Leftrightarrow$$

$$(p \uparrow q) \wedge (p \uparrow q) \Leftrightarrow$$

$$(p \uparrow q) \Leftrightarrow$$

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