Solutions to Problem Set 2 (6.042J)

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Problem 1

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a)
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 $Members(p, a, b) ::= \forall z \in p. (z = a \text{ OR } z = b)$

b)

 $\operatorname{Pair}(p,a,b) ::= \operatorname{Members}(p,a) \text{ AND Members}(p,a,b)$

c)

Second(p, b) ::= pair(p, b)

Problem 2

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\begin{aligned} x &\in \overline{A \cap B} \\ \text{iff } x &\in \text{NOT } (A \cap B) \\ \text{iff } x &\in \text{NOT}(A) \text{ AND } x \in \text{NOT}(B) \\ \text{iff } x &\in \text{NOT}(A \text{ AND } B) \\ \text{iff } x &\in (\overline{A} \text{ OR } \overline{B}) \\ \text{iff } x &\in \overline{A} \text{ OR } x \in \overline{B} \\ \text{iff } x &\in \overline{A} \cup \overline{B} \end{aligned}
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