





Financial Mathematics and Statistics

MSc Finance Mock Exam

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Rules: there are two types of questions in this exam:

- Multiple choice questions but only one answer is possible.
- Questions where you have to provide the right figure in order to complete a table.

For MCQ: if a good answer if selected, you will have 1 point, if you do not answer to the question, you will zero point. In case you provide a wrong answer, you will have -0.5 points.

For the others questions, where you have to complete a table, there is no negative point.

Preliminaries

Financial market prices are subject to wide variations over time, and it is assumed that the values taken by the latter over time are distributed according to a centered normal distribution whose mean is equal to 7900 points. We know that 30% of the values taken by the CAC 40 price are below 7700 points and that 10% of the values taken are between 7850 and 7950. In what proportion does the share price take values between 7700 and 7850?
\square 15%
$\square 20\%$
$\square \ 25\%$
$\square \ 30\%$
In a study of salaries in the finance sector, the organization found that the distribution of salaries followed a normal distribution, with a mean gross salary equal to 100,000 and a standard deviation equal to 15,000.
Approximately what proportion of salaries lie in the interval [70,000; 130,000]?
\square 90%.
\square 95%.
\square 97.5%.
□ 99%.
It is customary to use a linear model to try and estimate the profits generated by a company on the basis of various criteria, such as sales, investment in research, investment in marketing, etc. In such a situation, what is the dependent variable?
1. In such a situation, what is the dependent variable?
\Box the generated profits.
\Box investment in marketing.
\Box investment in research.
\square sales.
2. What are the assumptions related to the linear models?

☐ the data are assumed to be independent and indentically distributed according to a normal distribution, the errors of the model are dependent to the others with different variances.	
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\Box the data are assumed to be independent and identically distributed according to a normal distribution, the errors of the model are independent with unequal variance.	
Hypothesis testing are mainly used to take decisions but also to lead to several conclusions of statiscal analysis, such as comparing the behavior. For this purpose, we usually introduce a coefficient α , called an <i>error rate</i> to conclude to our hypothesis testing.	
1. Let us imagine that we want to test if two means μ_1 and μ_2 are equal or not using a two tailed test, what are the hypothesis H_0 and H_1 :	
$ \Box H_0: \mu_1 \neq \mu_2 \text{ vs. } H_1: \mu_1 > \mu_2. $ $ \Box H_0: \mu_1 = \mu_2 \text{ vs. } H_1: \mu_1 > \mu_2 $ $ \Box H_0: \mu_1 \neq \mu_2 \text{ vs. } H_1: \mu_1 = \mu_2 $ $ \Box H_0: \mu_1 = \mu_2 \text{ vs. } H_1: \mu_1 \neq \mu_2 $	
2. Assuming that we are performing a two tailed test. If we denote U a random variable and u_{test} the value of the statistical test. How is defined the p -value?	
$ \Box \ 2\mathbb{P}[U \le t]. $ $ \Box \ 2\mathbb{P}[U \ge t]. $ $ \Box \ \mathbb{P}[U \le t]. $ $ \Box \ \mathbb{P}[U \ge t]. $	
3. What is the meaning of this value α ?	
 □ This is a risk of the first kind. It represents the greatest risk we are prepared to take for the rejection of the null hypothesis. □ This is a risk of the second kind. It represents the greatest risk we are prepared 	
to take for the rejection of the null hypothesis. ☐ This is a risk of the first kind. It represents the greatest risk we are prepared to take for the acceptation of the null hypothesis.	
☐ This is a risk of the second kind. It represents the greatest risk we are prepared to take for the acceptation of the null hypothesis.	
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A case study

A company specializing in finance is conducting an equal pay study. The human resources department and union representatives have been asked to conduct the study, which covers a number of points. To this end, a survey was carried out among a number of employees: workers and technicians, men and women in three different cities: Bordeaux, Marseille and Lyon. The study is made on two different years: 2020 and 2021 of data for a selected sample of employees. The study is conducted on a sample of 45 instances.

The test conducted in this part are two tail test using $\alpha = 0.025$.

1.	First of all, we want to know what is the distribution of employee salaries. How can
	the team in charge of this study verify that this distribution is indeed a gaussian distribution?
	\square We can only check if the distribution is symmetric.
	\square It is enough to see if there is only positive values.
	\square We can use a quantile-quantile or a normal probability plot to check this assumption.
	\square We can check if the the mode is equal to the mean and equal to the median of the distribution.
2.	Now, we want to to check if the wages have evolved between 2020 and 2021. What kind of test, the team shall perform for this purpose?
	\square A t-test without anymore assumption.
	\square A t-test with equal variance.
	\square A paired t-test.
	\Box A t-test with unequal variance.
	The appropriate two tailed test leads to the following table of results

t_{test}	-6.8838
df	
n voluo	1 60 10-8

3. What is the conclusion of this test?

$\hfill\Box$ We cannot conclude if the wages have evolved or not.
☐ We can say that the wages have evolved but we do not know if they have increased or decreased.
\square We can say that the wages have evolved but we can say that they have in creased.

☐ We can say tha	at the wages have evolve	ed but we can say they have decreased						
4. What is the number of degree of freedom related to this test.								
$egin{array}{l} & \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $								
5. To perform this test	, what are the statistica	al quantities computed by the team?						
\Box The mean of the	 □ The mean of the two groups and the variance of the two groups □ The mean of the two groups and the pooled variance. □ The mean of the difference of the groups and the variance of the sample 							
	he difference of the group	ps and the pooled variance.						
Now we want to find out whether men and women in this company earn the same wages or not in 2021. To do this, we specify that the sample studied comprises 28 men and 17 women. The conducted test leads to the following outputs. Test of the equality of the variances								
	variance mean man	5, 297, 043						
	variance mean women	2,304,340						
	F-test							
	degrees of freedom p -value	and 0.085						
 Complete the previous table by indicated the value of the F-test. Complete the values on the number of degrees of freedom. What is the conclusion of this test? 								
☐ We reject the of to proceed to a		s and to compare the wages we have t						

We do	onumber not onu	reject	the	equalit	y of	the	varian	ce	and	to	compare	the	wages	we
have to	to	procee	d to	a test t	est	with	equal	va	riano	ces.				

- \square We reject the equality of the variances and to compare the wages we have to to proceed to a t-test with unequal variances.
- \square We do not reject the equality of the variances and to compare the wages we have to a t-test with unequal variances.

Test of the equality of the means

sample mean man	23,389
sample mean women	20,503
t-test	5.0632
<i>p</i> -value	0.085

What is the conclusion of this test which consists in comparing the mean values?

Men	and	women	have	exactly	the	same	salary.

- \square Men have a higher wage than women.
- \square We cannot conclude.
- \square Men and women wages are statistically different.

We are now interested in the equal treatment of employees in the different cities studied. The result of the study is provided in the following table

Results of the analysis

	Degrees of Freedom	Sum of Squares	Mean Squares	Statistical Test	p-value
City		83,460,738			0.0004
Residuals		184, 487, 263		X	X

- 1. Complete the number of degrees freedom in the previous table.
- 2. Complete the Mean Squares values in the above table.
- $3.\,$ Complete the value of the Statistical test in the previous test.

4. What is used test for this study.
\square A t-test with equal variance.
\Box A paired t-test.
\Box A t-test with unequal variance.
$\hfill\Box$ A F-test based on the fisher distribution.
In the last part of their study, the team want to study if it is possible to predict the wages in 2021, using the wages in 2020.
The results of the linear regression is provided in the following table.

Results of the linear regression: about the coefficients

	Estimation	Standard Error	1
Intercept	20,067	3,513	 9.6×10^{-7}
Salary 2020	0.1164	0.1823	 0.526

Results of the linear regression: study the model

Residual Standard Error	2485
Degree of freedom of Residuals	
Degree of freedom of Regression	•••
Residual Sum of Squares	
Total Sum of Squares	268,000,000
Regression Sum of Squares	
R^2	
Adjusted R^2	
F-test	
<i>p</i> -value	0.531
P varae	0.001

1.	How	many	parameters	do you	have	in this	linear	model
		1.						
		2.						
		3.						
		1						

2. Complete the table Results of the linear regression: about the coefficients

- 3. Complete the number of degrees of freedom in the table Results of the linear regression: study the model
- 4. Complete the Residual and the Regression Sum of Squares in the **Results of the** linear regression: study the model
- 5. Complete the R^2 and the adjusted R^2 of the table Results of the linear regression: study the model
- 6. Complete the F-test of the table Results of the linear regression: study the model

7.	Is it po	ssible to	predict	the	wages	in	2021	using	the	wages	in	2020.
	□ Ye	es										
	□ No	0										