

Universidad Nacional de Río Cuarto
Faculty of Engineering

Course: **Differential Equations**

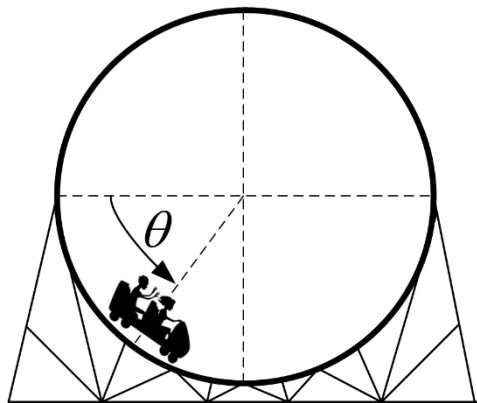
Date: **Second semester 2022**

Careers:

Mechanical Engineering
Chemical Engineering
Electrical Engineering
Telecommunications Engineering
Renewable Energy Engineering

Stability Analysis of Nonlinear Systems

A car slides down the curve shown in the figure. It corresponds to a circle of 6 m radius.



Considering the car as a point mass that moves on the curve:

- a) Find a dynamic model for the car as a function of θ .
- b) Find the critical points for $0 \leq \theta < 2\pi$.
- c) Classify the critical points considering that there is no damping.
- d) Classify critical points for different damping levels.
- e) Plot each case in the phase plane.