

| Algorithmics | Student information   | Date | Number of session |
|--------------|-----------------------|------|-------------------|
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## Activity 1. Tromino Times

| $N$                       | $T$ Tromino           |
|---------------------------|-----------------------|
| 16                        | 1                     |
| ...                       | (0 or 1 until next n) |
| 1024                      | 16                    |
| 2048                      | 30                    |
| 4096                      | 140                   |
| 8192                      | 447                   |
| Heap Overflow (n = 16384) | 1627                  |

- What should be the time complexity of the algorithm?

The complexity of the algorithm is calculated the following way:

$$a = 4$$

$$b = 2 \text{ (by division)}$$

$$k = 0$$

So, the complexity is:  $O(n^{\log_b(a)})$  which is  $O(n^{\log_2(4)}) = O(n^2)$

The time complexity of the Tromino algorithm is  $O(n^2)$

- Check if the time obtained in the previous section does or does not meet the theoretical complexity of the algorithm.

For a complexity  $O(n^2)$  we would have the theoretical values:

(Note  $K$  is  $n_2^2/n_1^2$ , and since  $n_1 = 2 \cdot n_2$  in our case,  $K = n_2^2/2n_2^2 \rightarrow \frac{1}{4} = 0,25$ )

$$N = 1024 \quad T = 1024^2/2048^2 * 30 = 7,5$$

$$N = 2048 \quad T = 2048^2/4096^2 * 140 = 35$$

$$N = 4096 \quad T = 4096^2/8192^2 * 447 = 111.75$$

$$N = 8192 \quad T = 8192^2/16384^2 * 1627 = 406,75$$

And thus the ties meet approximately the complexity of the algorithm.