

# Deep learning the invisible universe

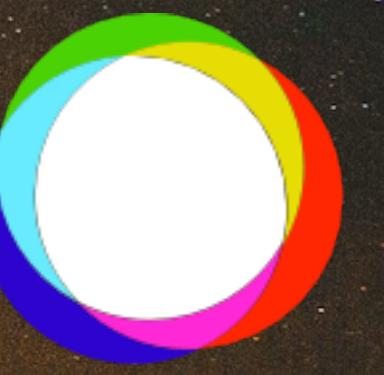
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**Guillermo Franco Abellán**

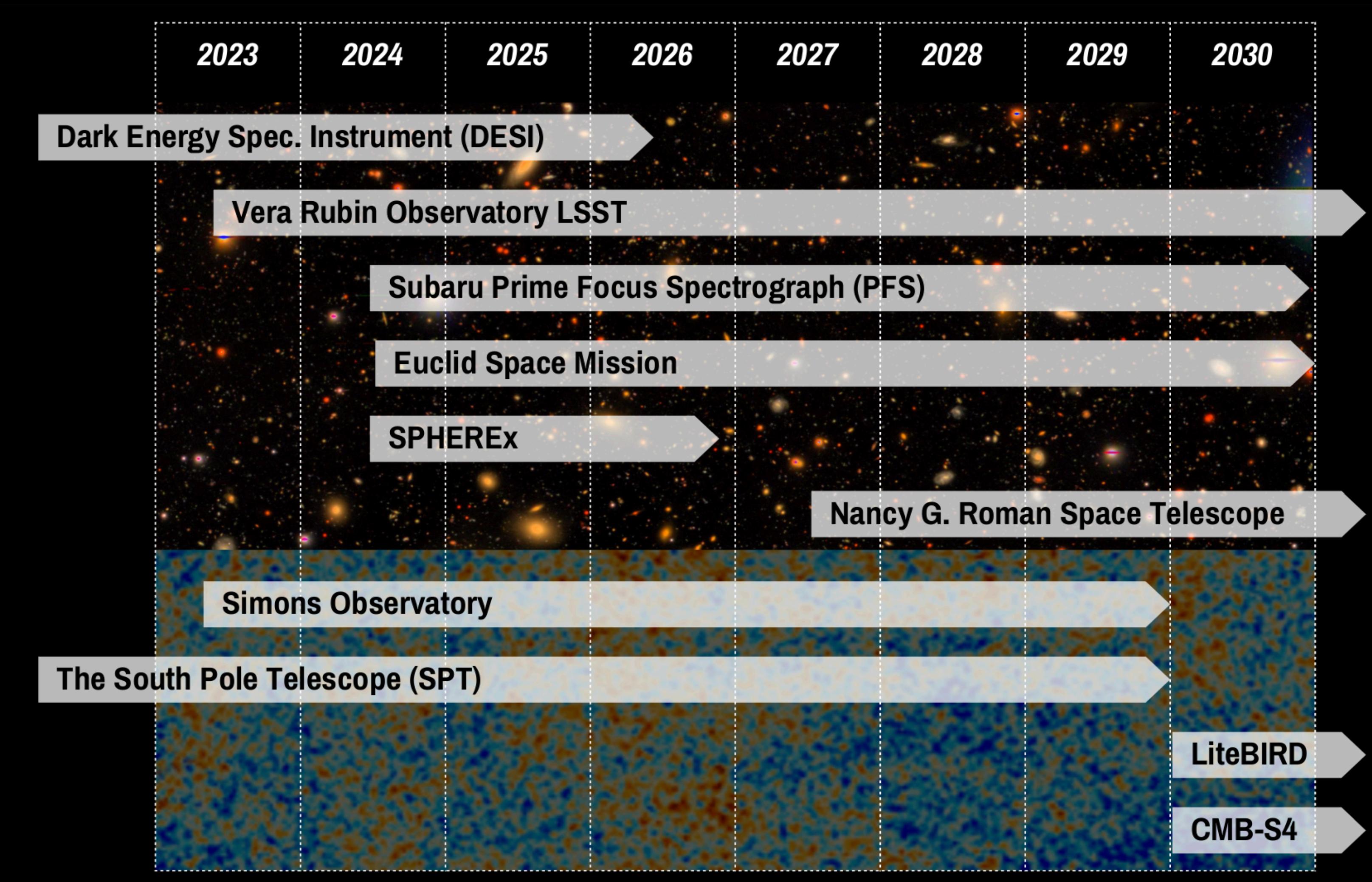
**GRAPPA, University of Amsterdam**

**21<sup>st</sup> May 2025**

**CEICO Cosmology Seminar**

**GRAPPA**   
GRavitation AstroParticle Physics Amsterdam

# We are entering in the era of **ultra-high precision cosmology**

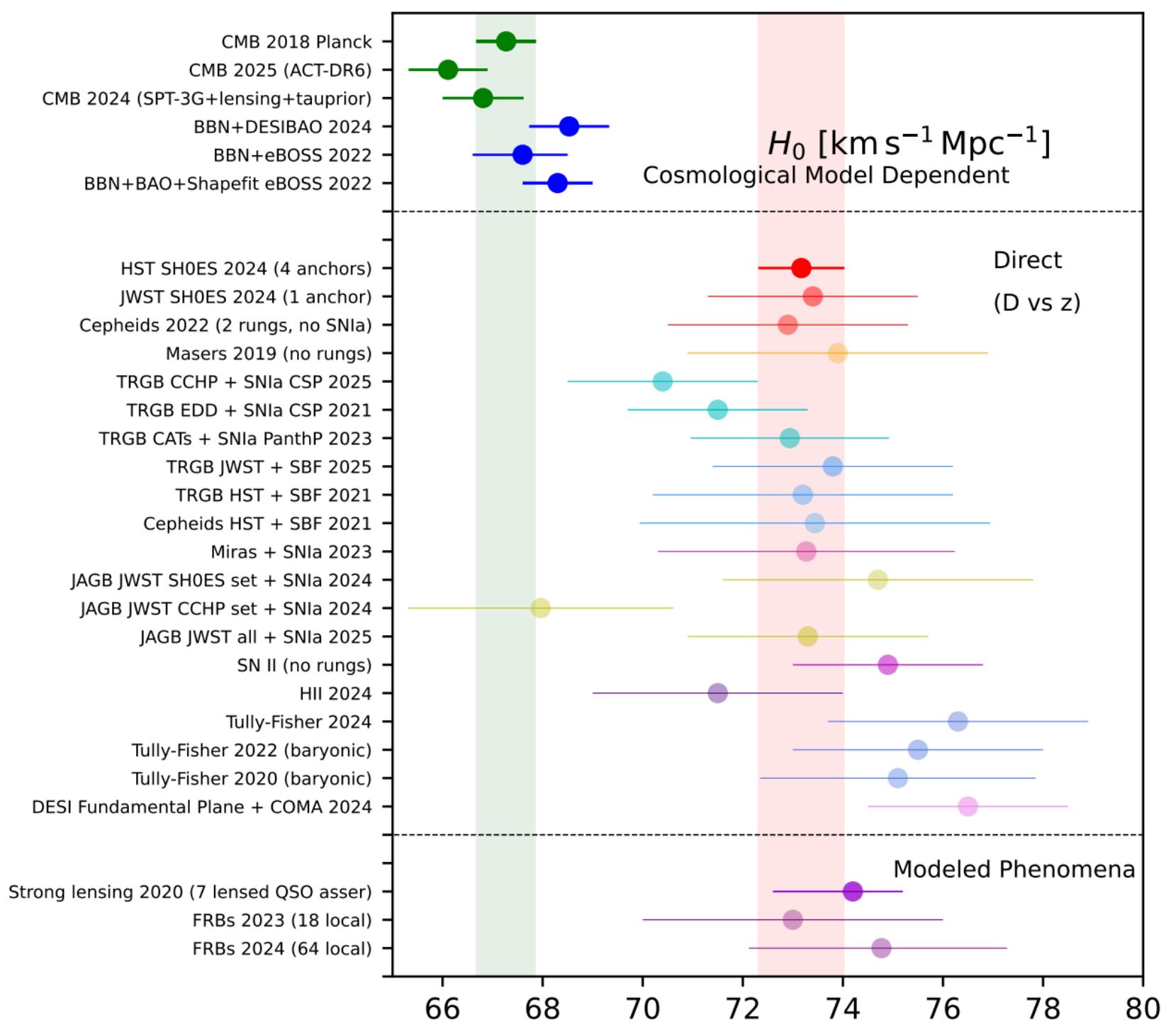


[Credit A. Bayer]

Various datasets point at **cracks in the  $\Lambda$ CDM model**

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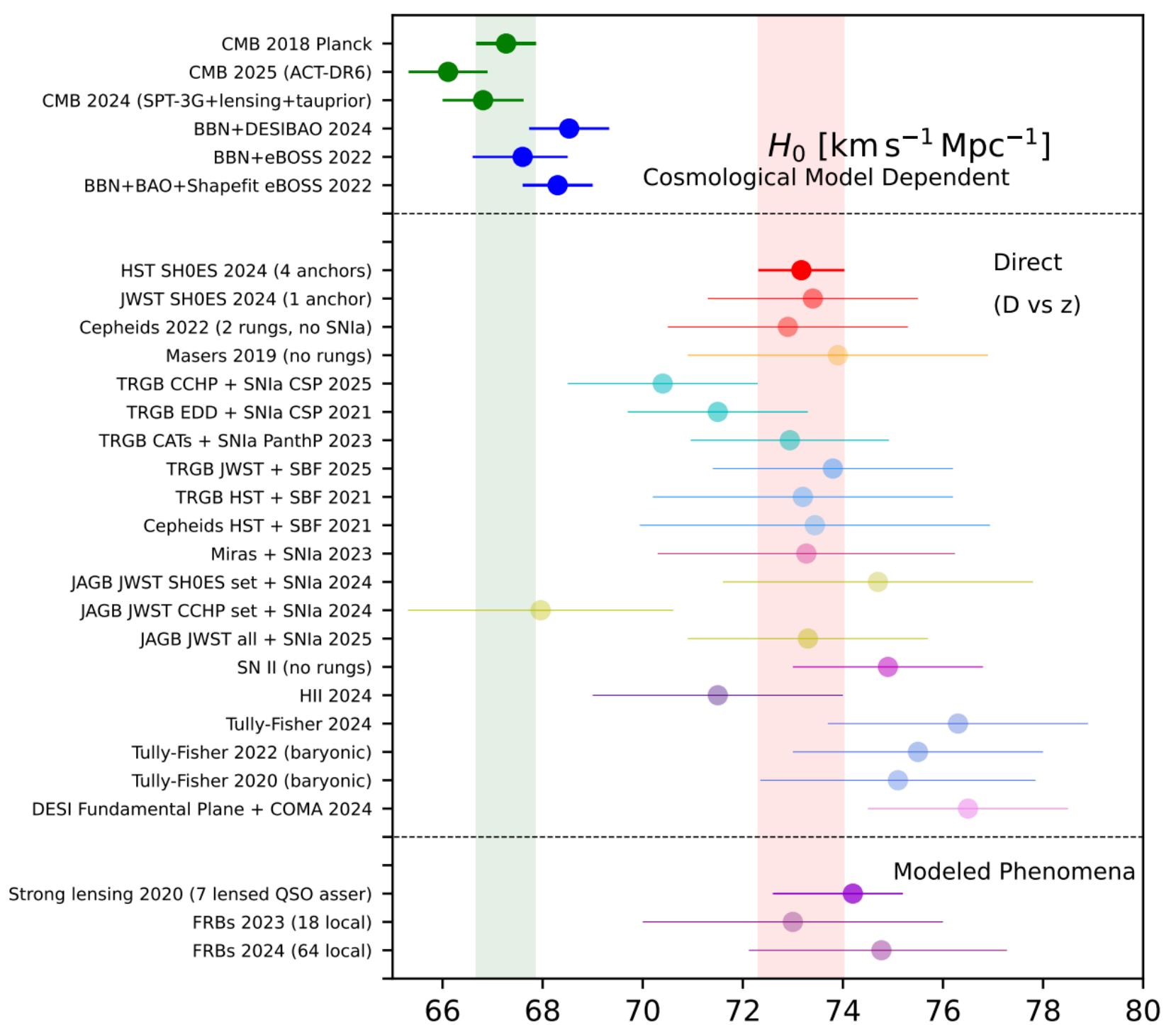
## $H_0$ tension



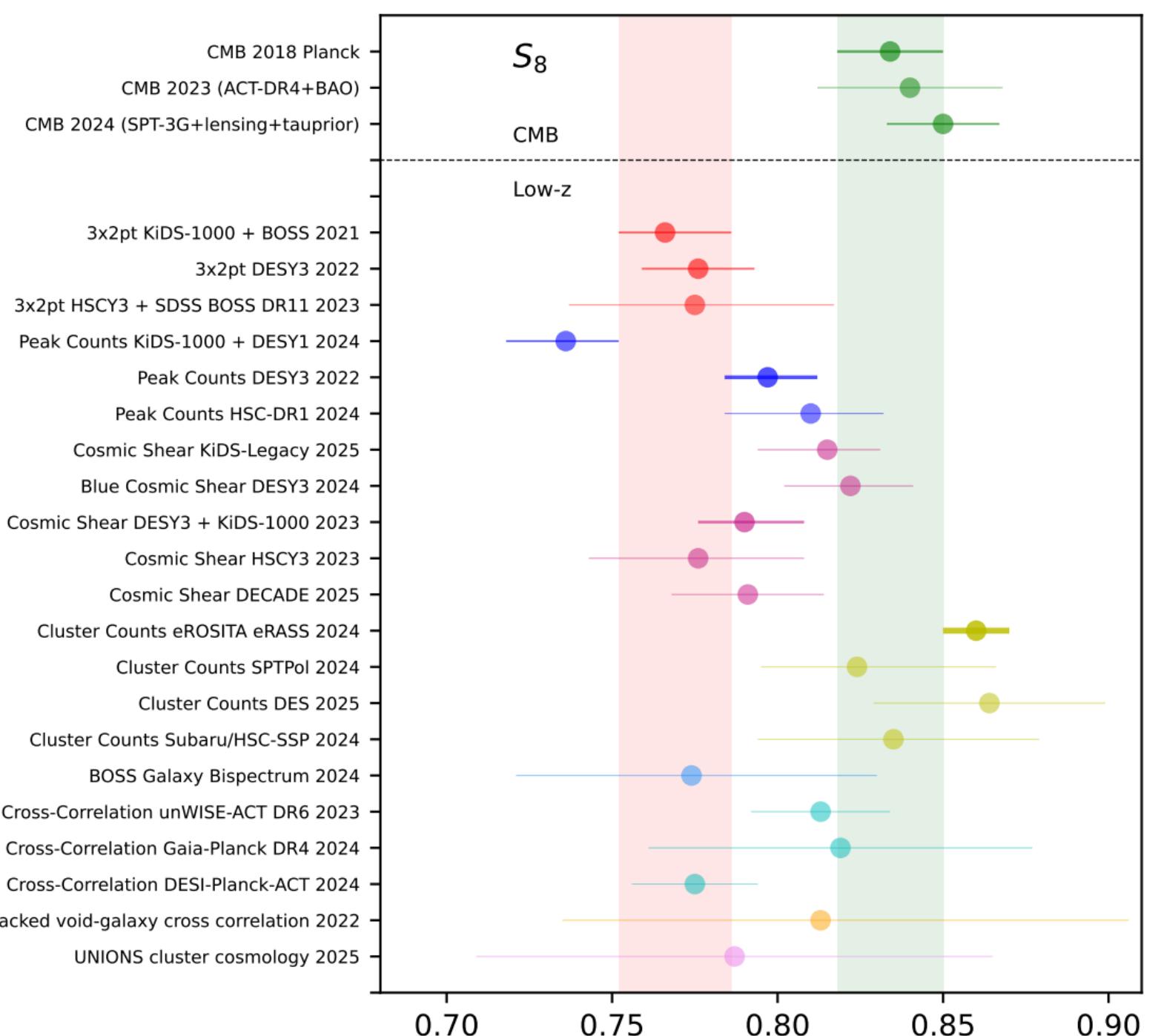
[CosmoVerse White  
Paper: 2504.01669]

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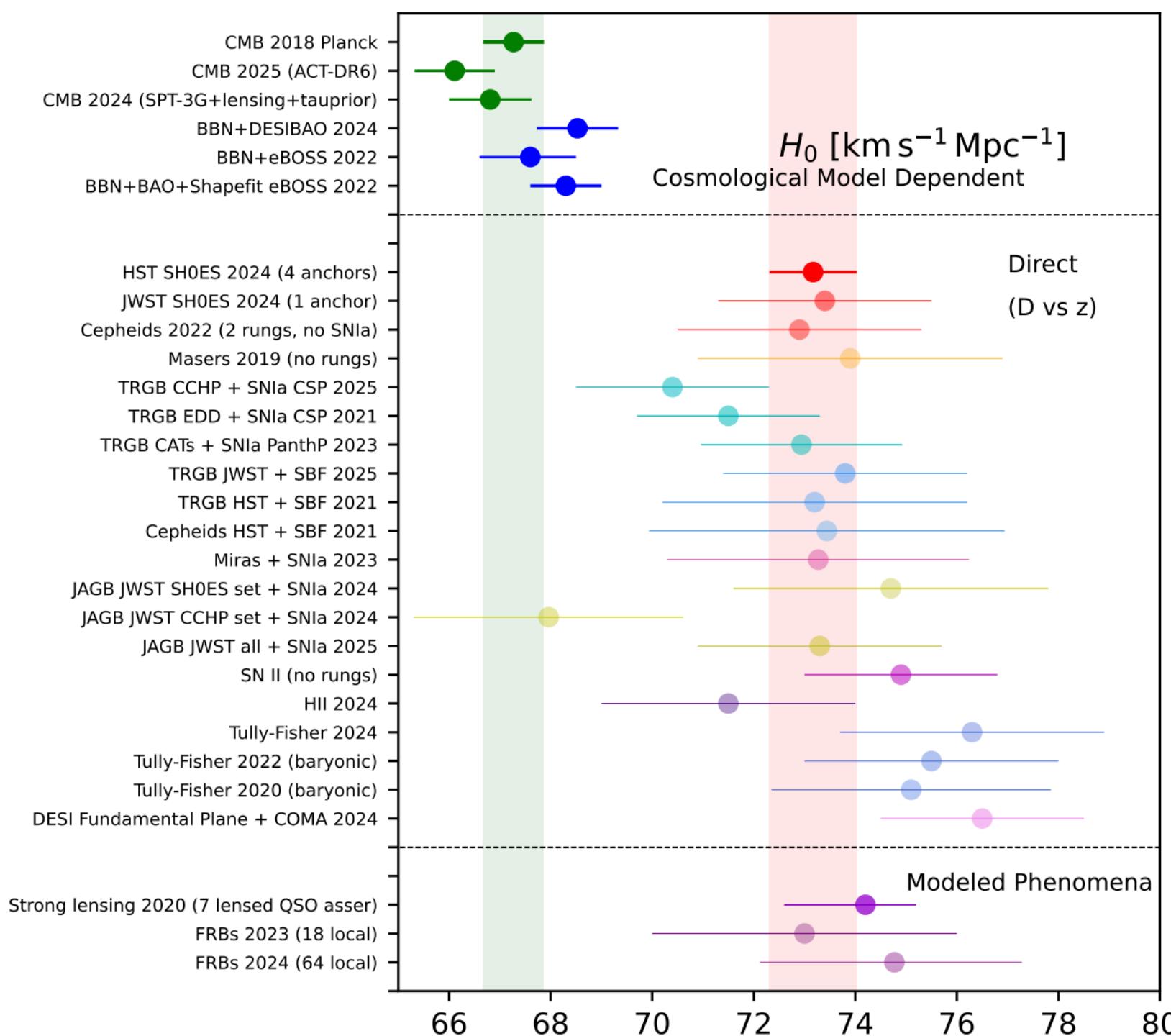
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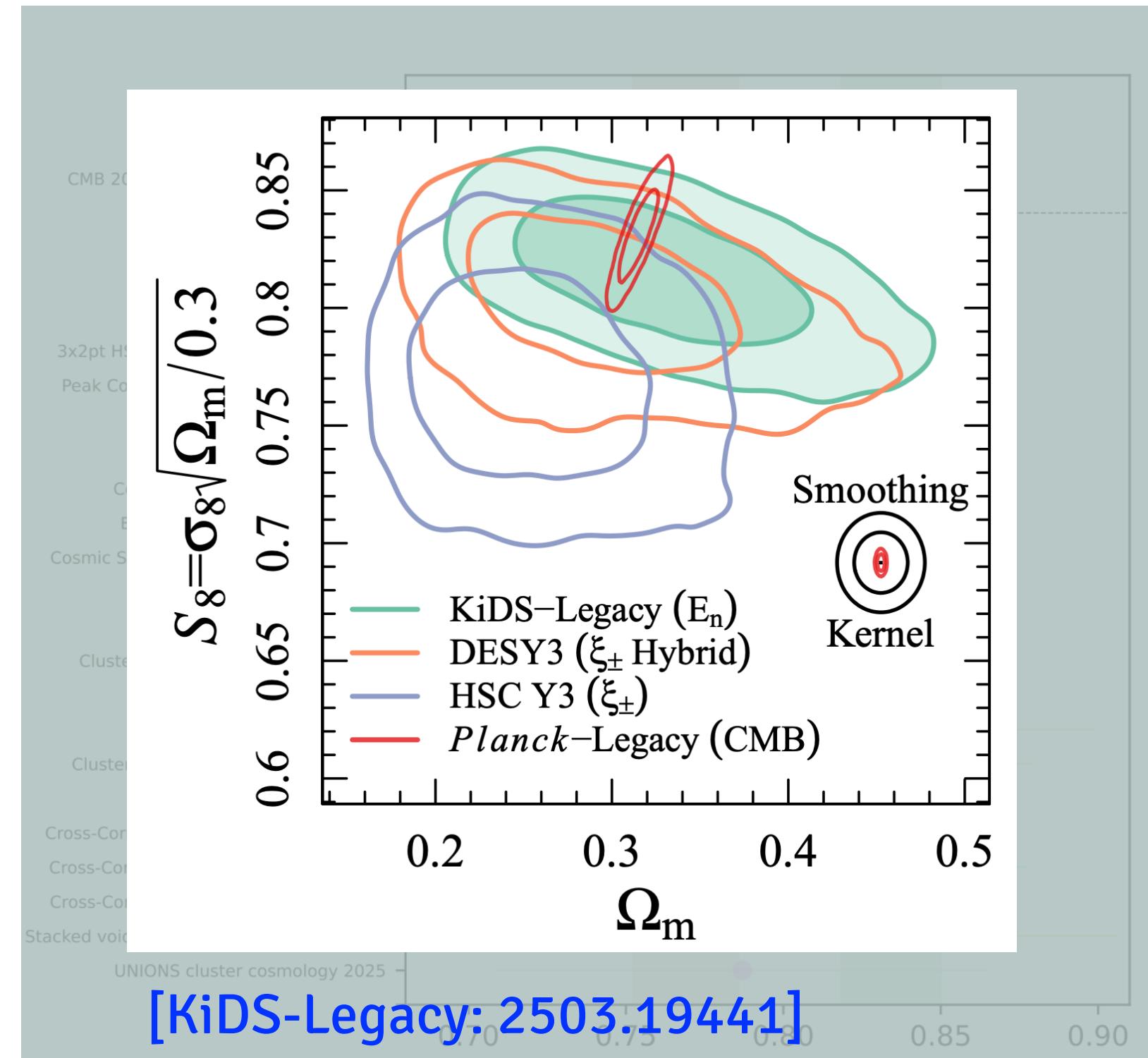
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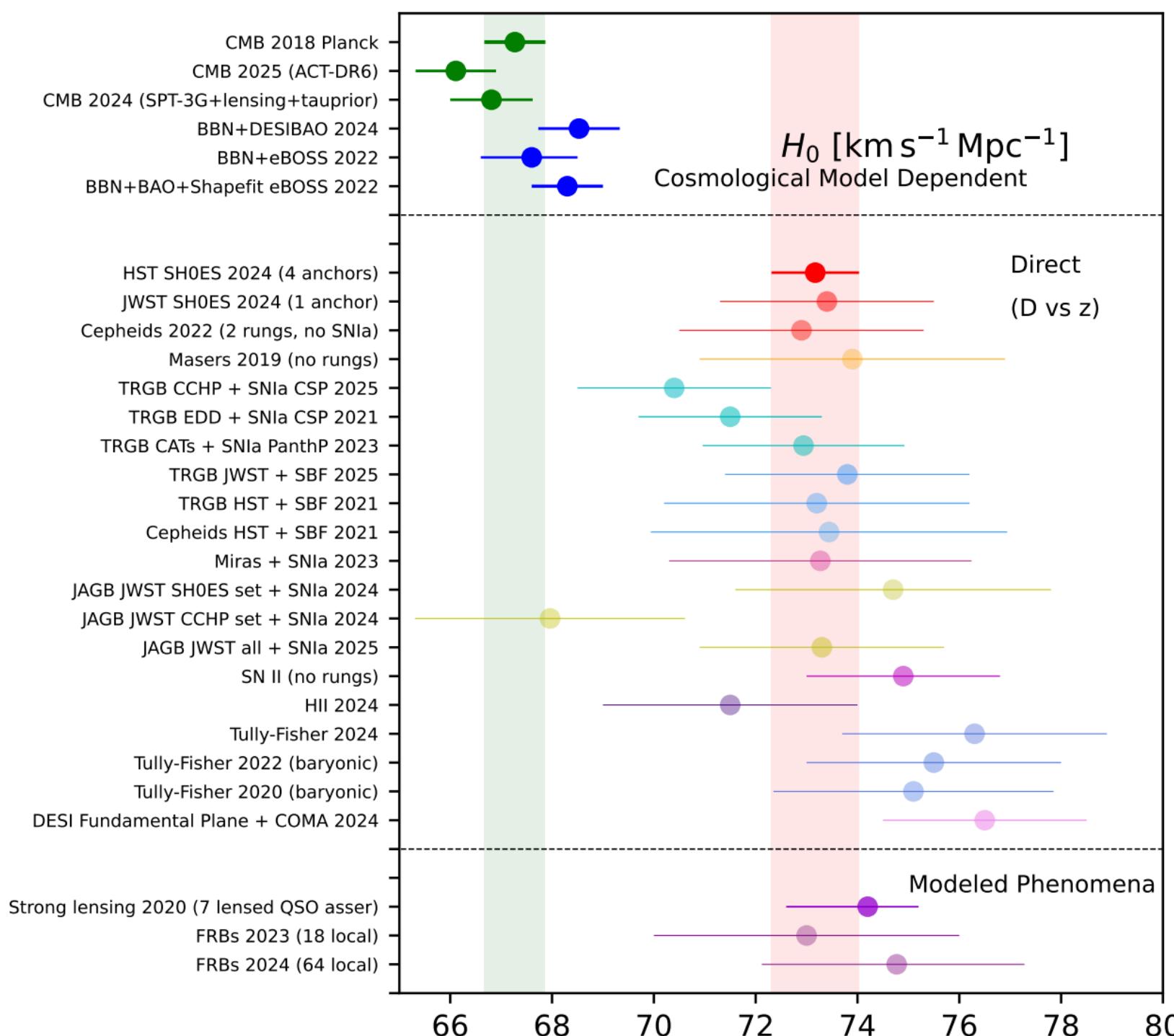
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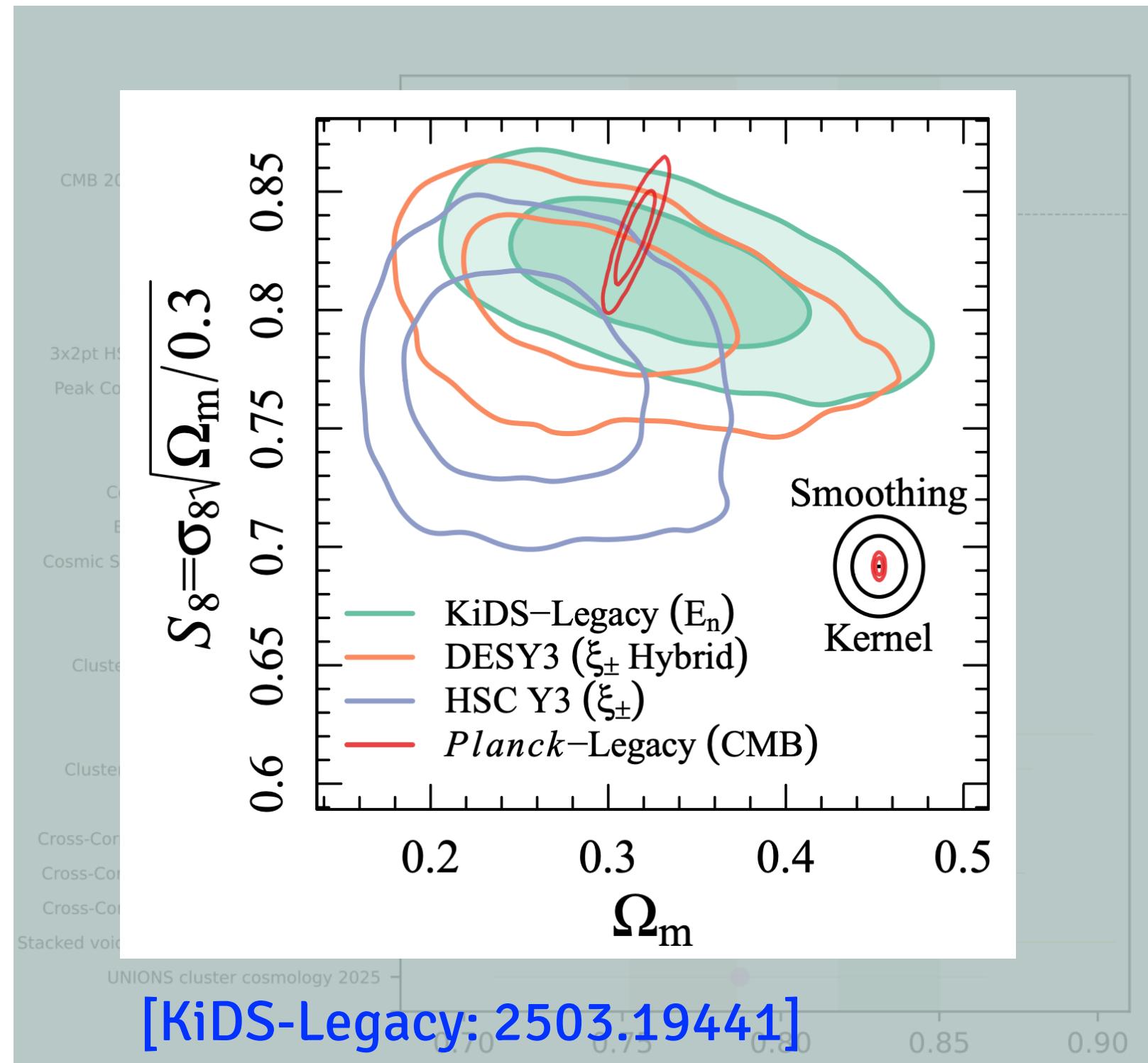
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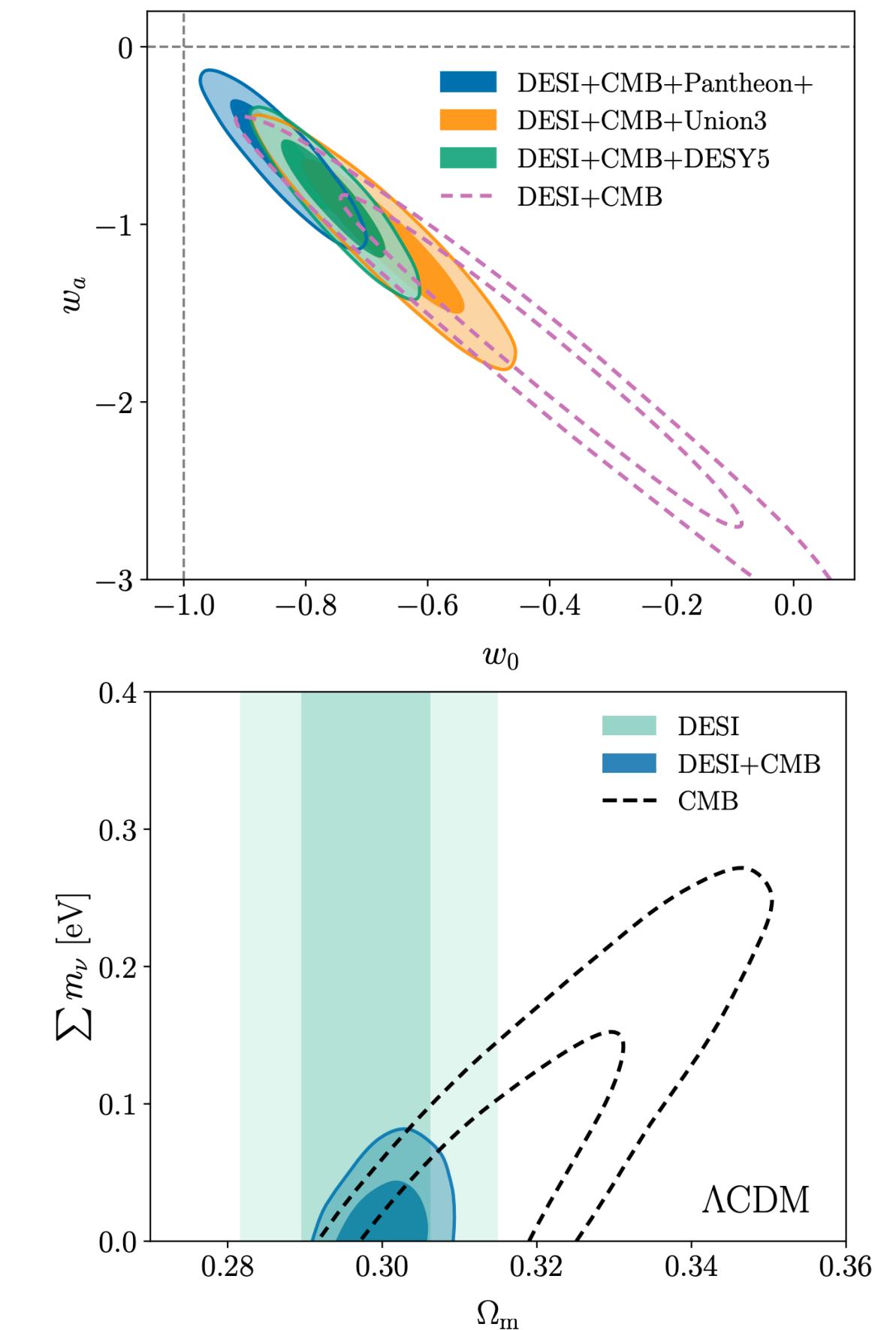
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## Latest DESI results



[DESI BAO DR2: 2503.14738]

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## Data

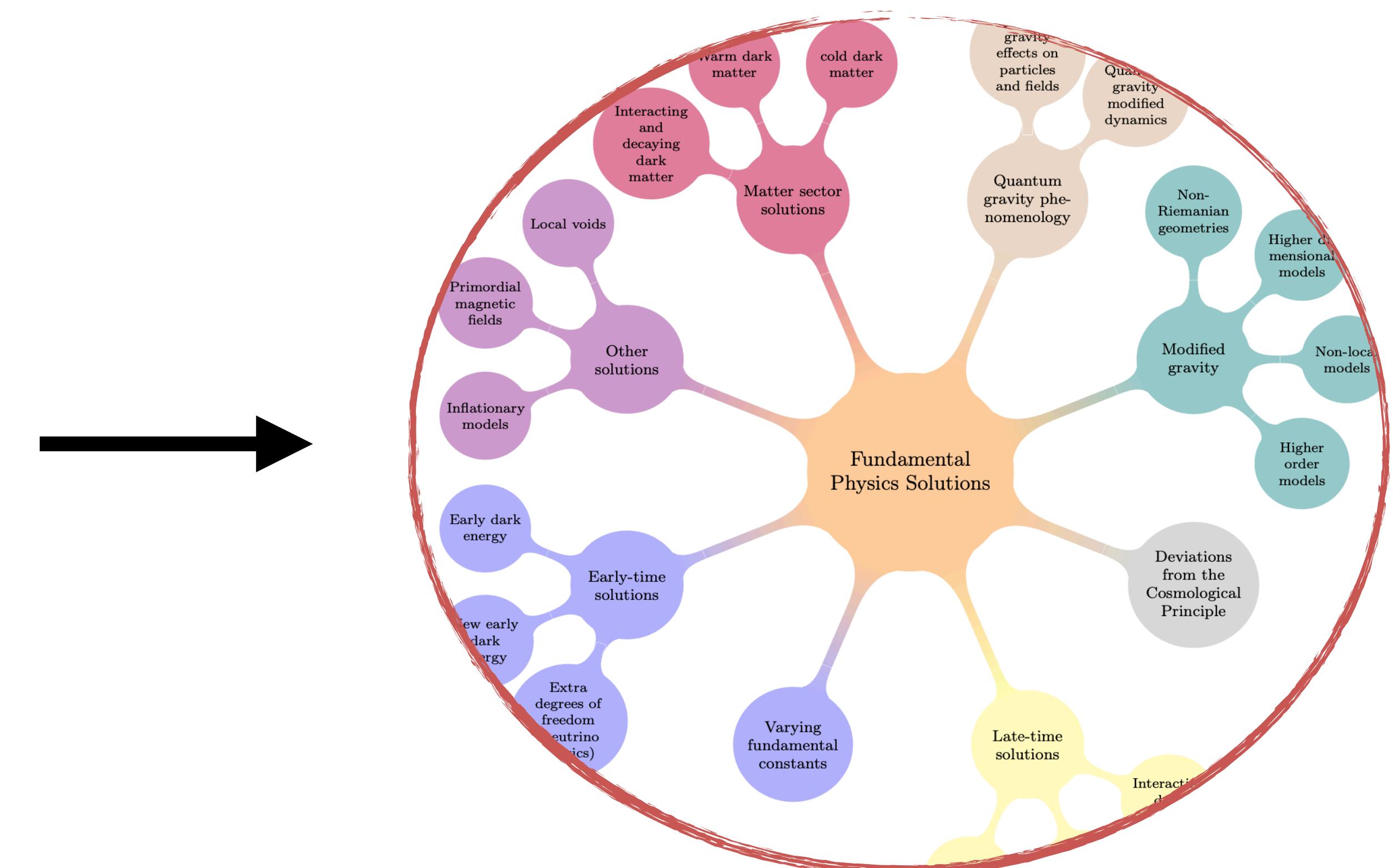


To learn about the universe, we need to **solve the inverse problem**

## Data



## Theory



# Some $\Lambda$ CDM extensions I studied in the past

## Decaying DM

[[GFA+](#) 2008.09615]  
[[GFA+](#) 2102.12498]  
[Simon, [GFA+](#) 2203.07440]

## Early Modified Gravity /Early Dark Energy

[[GFA](#), Braglia+ 2308.12345]  
[Murgia, [GFA+](#) 2009.10733]

## Interacting Stepped DR

[Schöneberg & [GFA](#) 2206.11276]  
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## Hundreds of other models, e.g. see reviews:

“In the Realm of the Hubble tension - a Review of Solutions” Di Valentino+ [2103.01183]

“The  $H_0$  Olympics: a fair ranking of proposed models” Schöneberg, GFA+ [2107.10291]

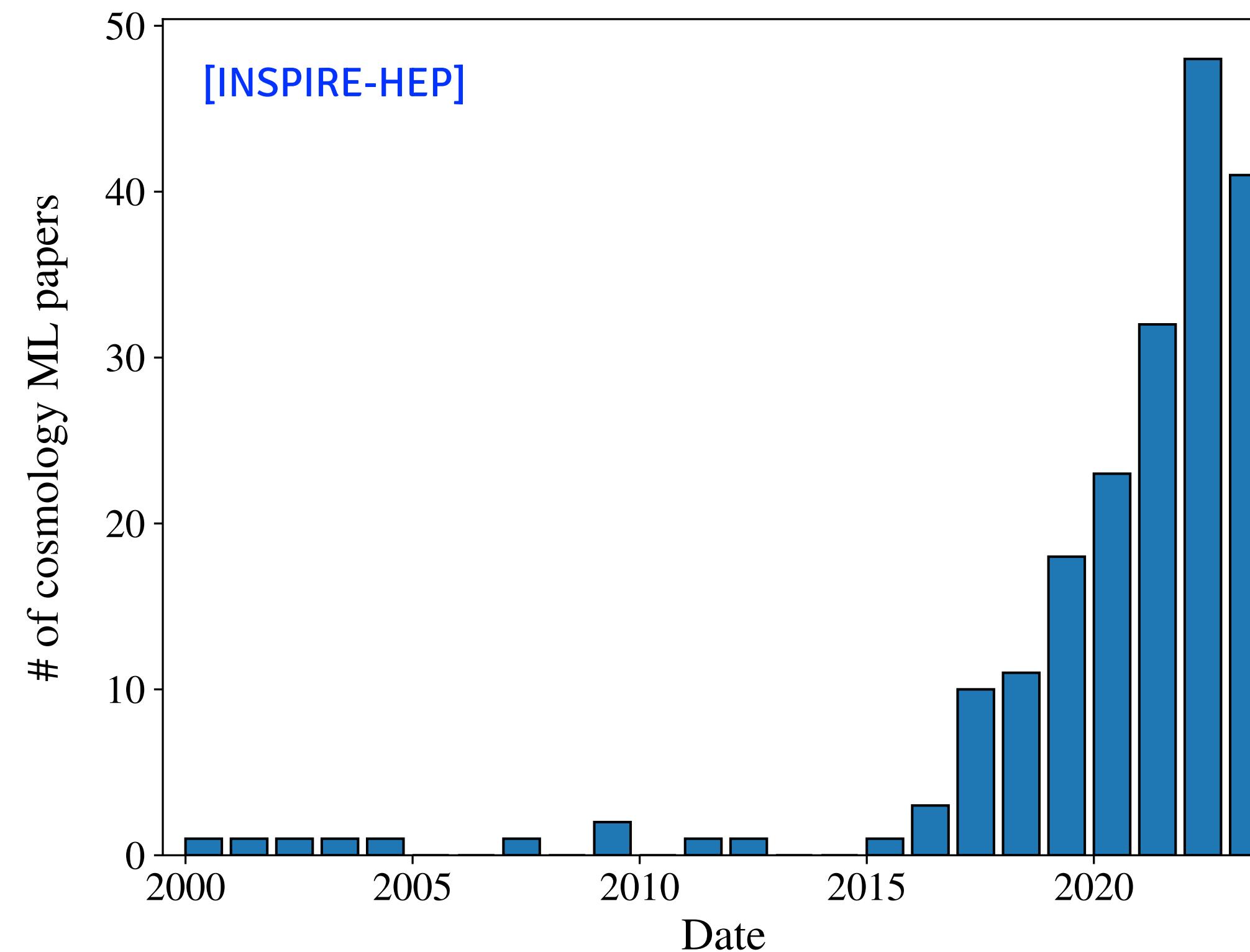
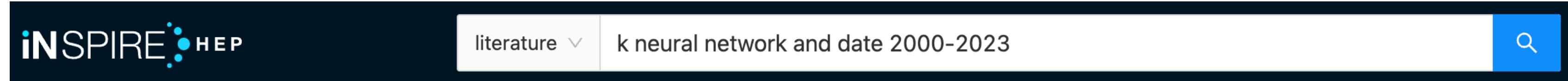
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- Expensive simulations

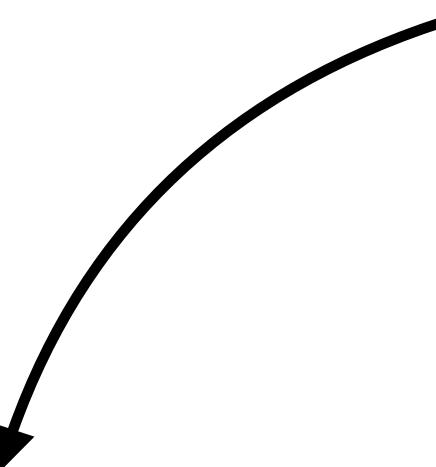
- High-dimensional parameter spaces



Machine learning is  
having a **strong impact**  
in cosmology

# **Two main approaches in ML**

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### **Emulators**

to speed up model evaluations of  
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### **Emulators**

to speed up model evaluations of cosmological observables

### **New statistical methods**

to improve the sampling in high-dimensional parameter spaces

## 1. Emulators

For testing **invisible neutrino decays** with latest cosmic data

## 2. Simulation-based inference

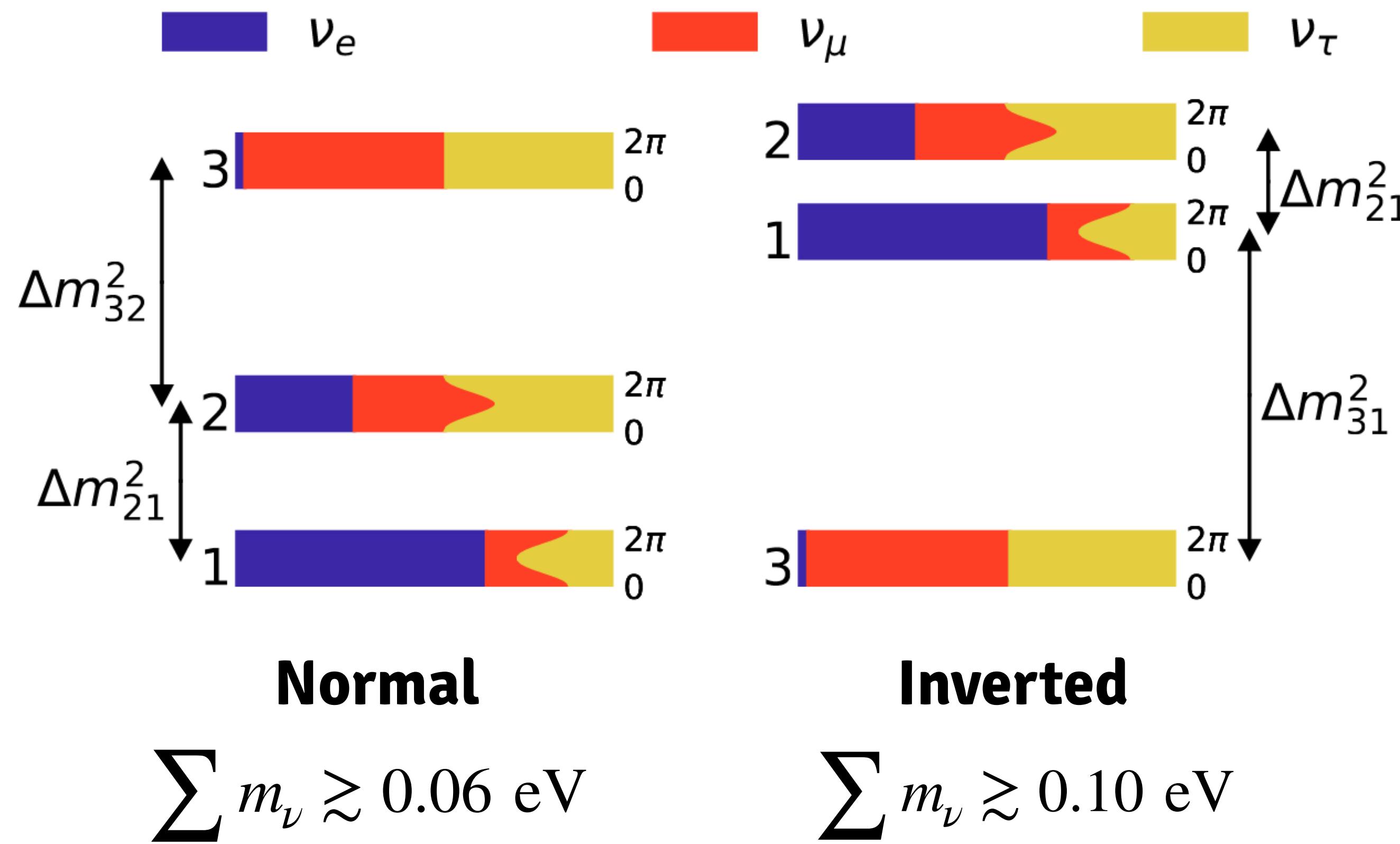
For efficient inference from **Euclid** data, with applications to **evolving dark energy**

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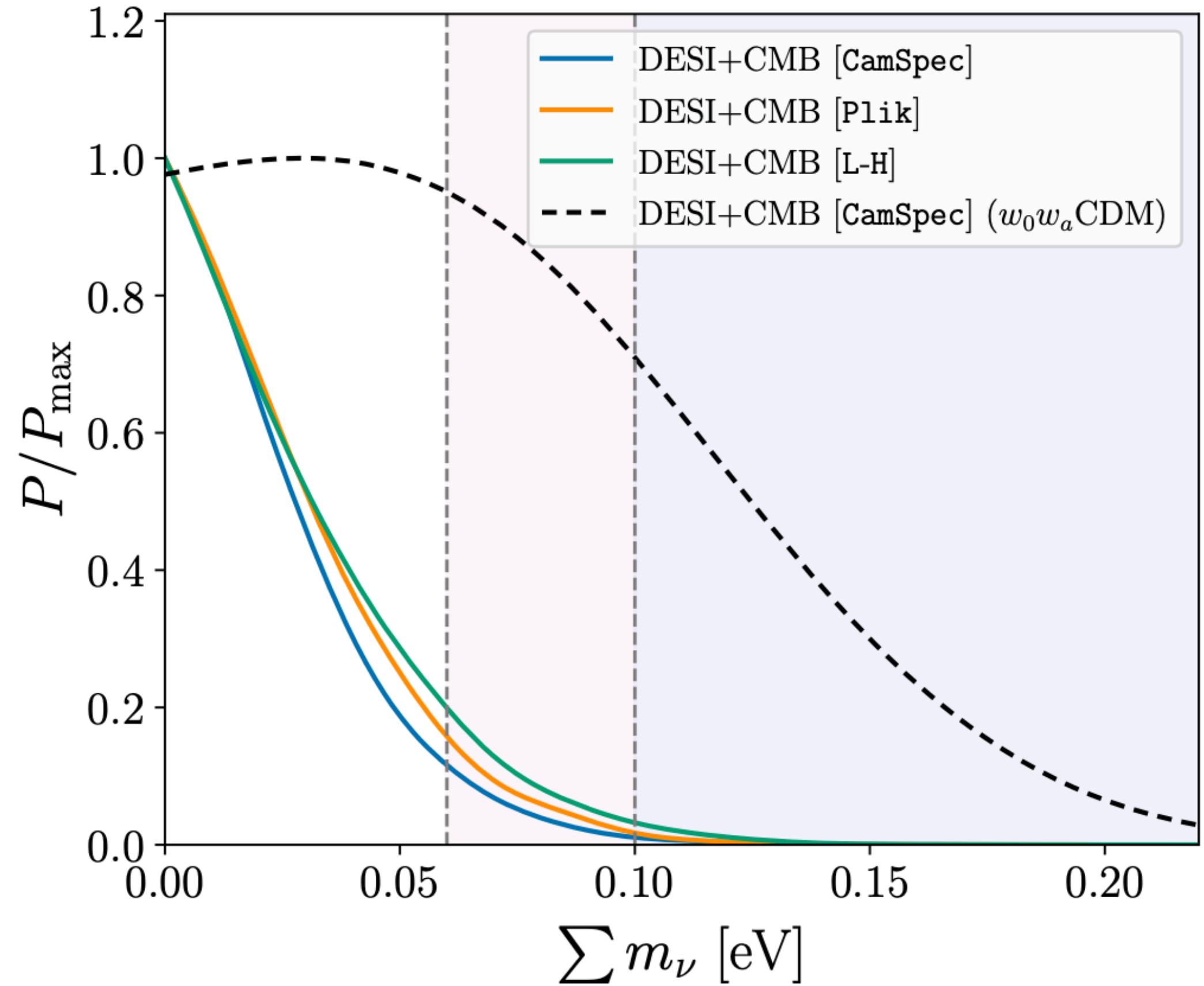
Ongoing work, to appear soon  
[arXiv:2506.XXXXX](https://arxiv.org/abs/2506.XXXXX)

Oscillation experiments have provided convincing evidence that **neutrinos have mass**



[Salas et al. 1806.11051]

# Cosmological bounds



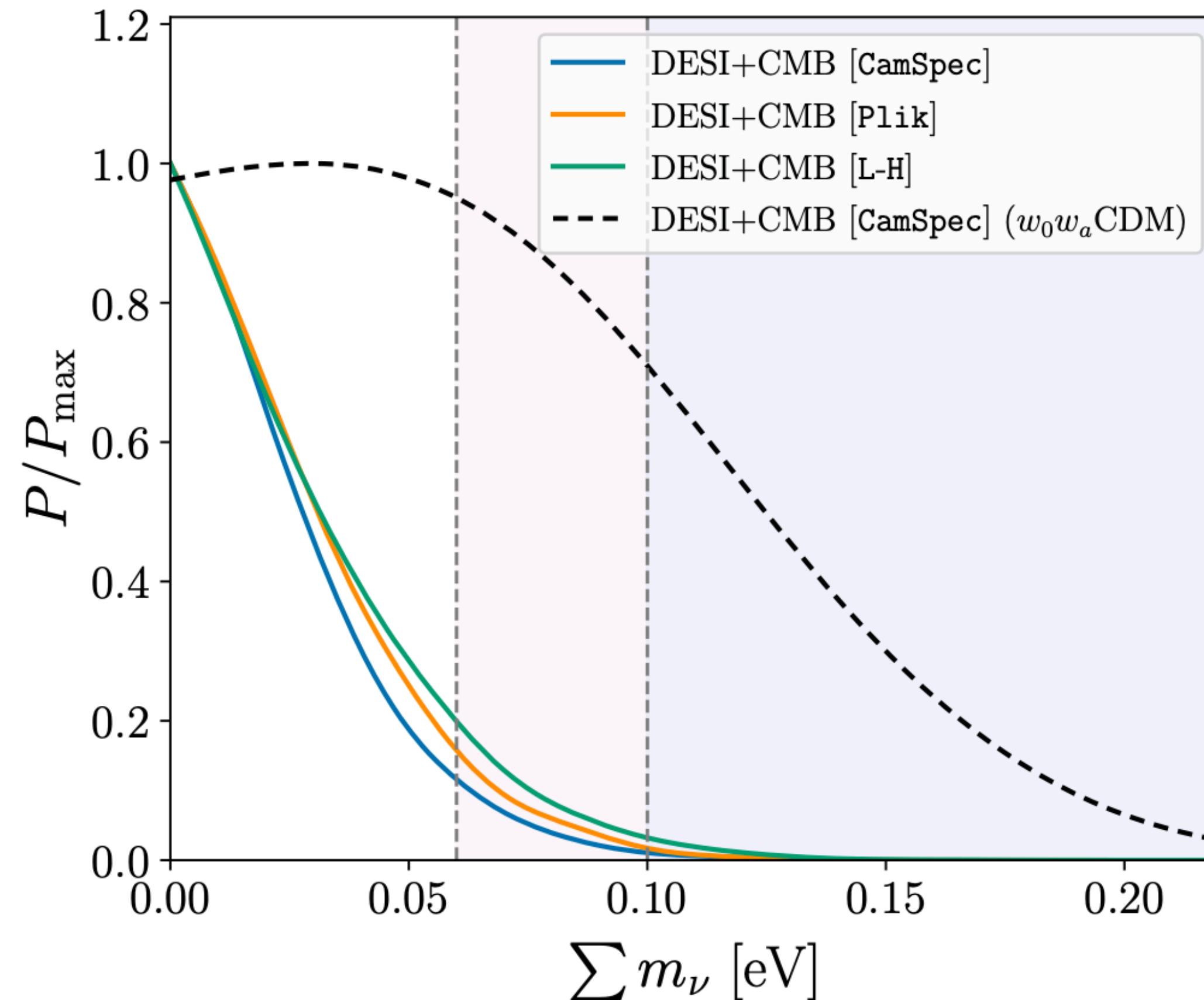
Cosmology has given tightest bound to date

$$\sum m_\nu < 0.064 \text{ eV}$$

(95%, DESI+CMB [CampSpec])

[DESI DR2 Results II \[2503.14738\]](#)

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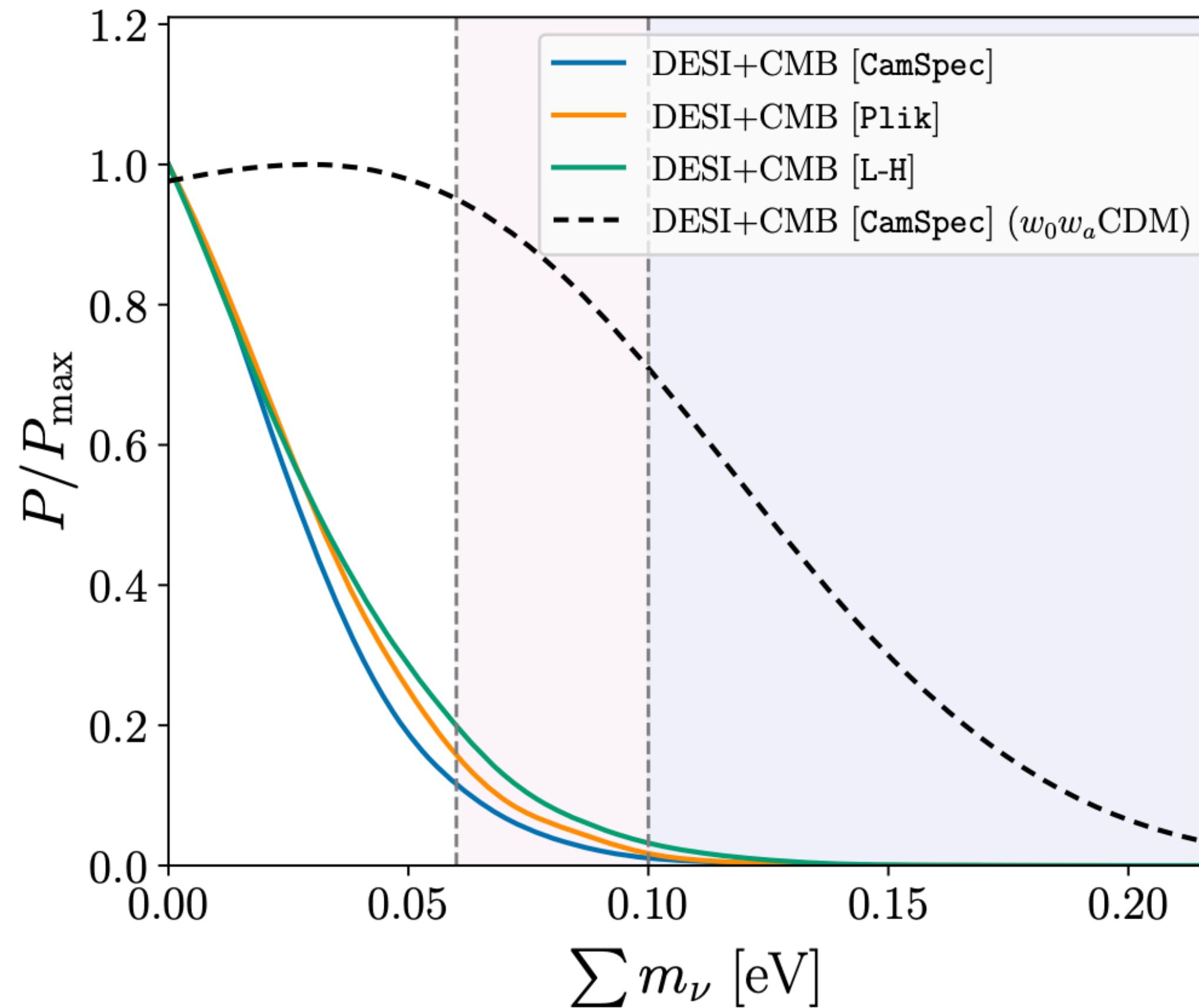
However, these bounds are **model dependent**

$$\sum m_\nu < 0.163 \text{ eV}$$

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What about changing **neutrino properties?**

[DESI DR2 Results II \[2503.14738\]](#)

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2 neutrinos decay **in the SM** but  $\tau_\nu \sim (G_F^2 m_\nu^5)^{-1} \gtrsim 10^{33}$  yr  $\gg t_U$

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Aalberts, Ando et al. [1803.00588]

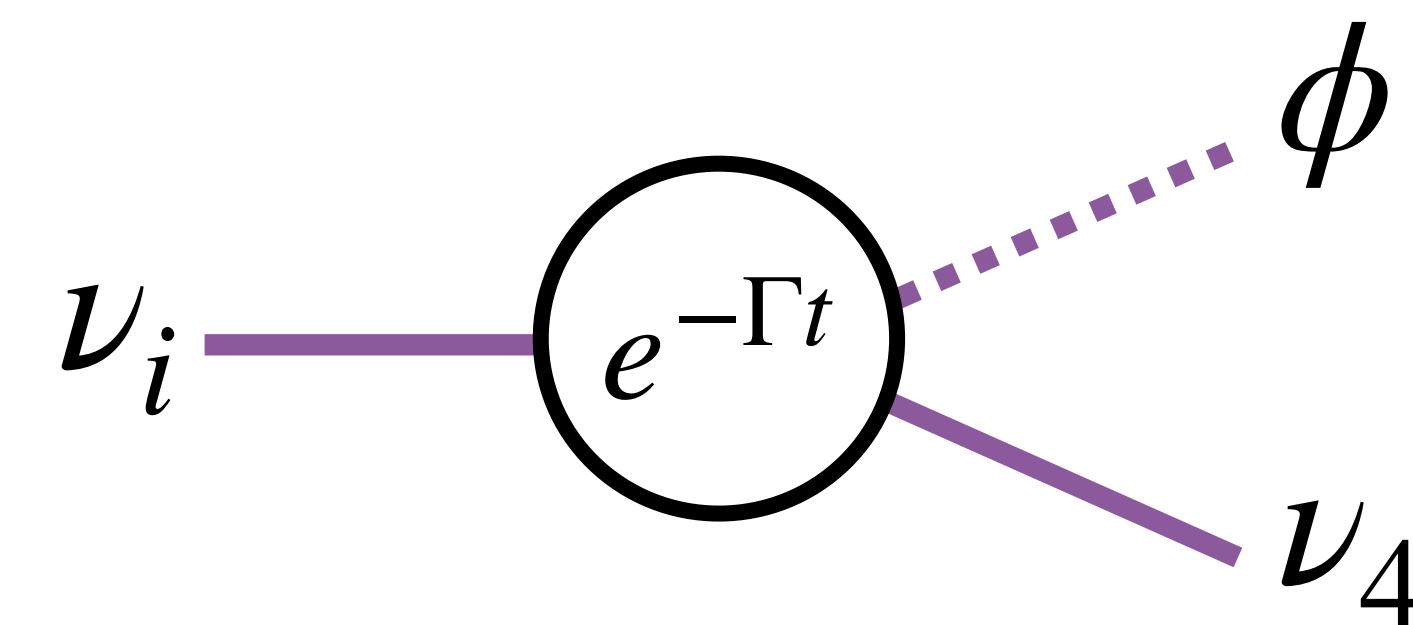
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Decays to **dark radiation**, much less constrained



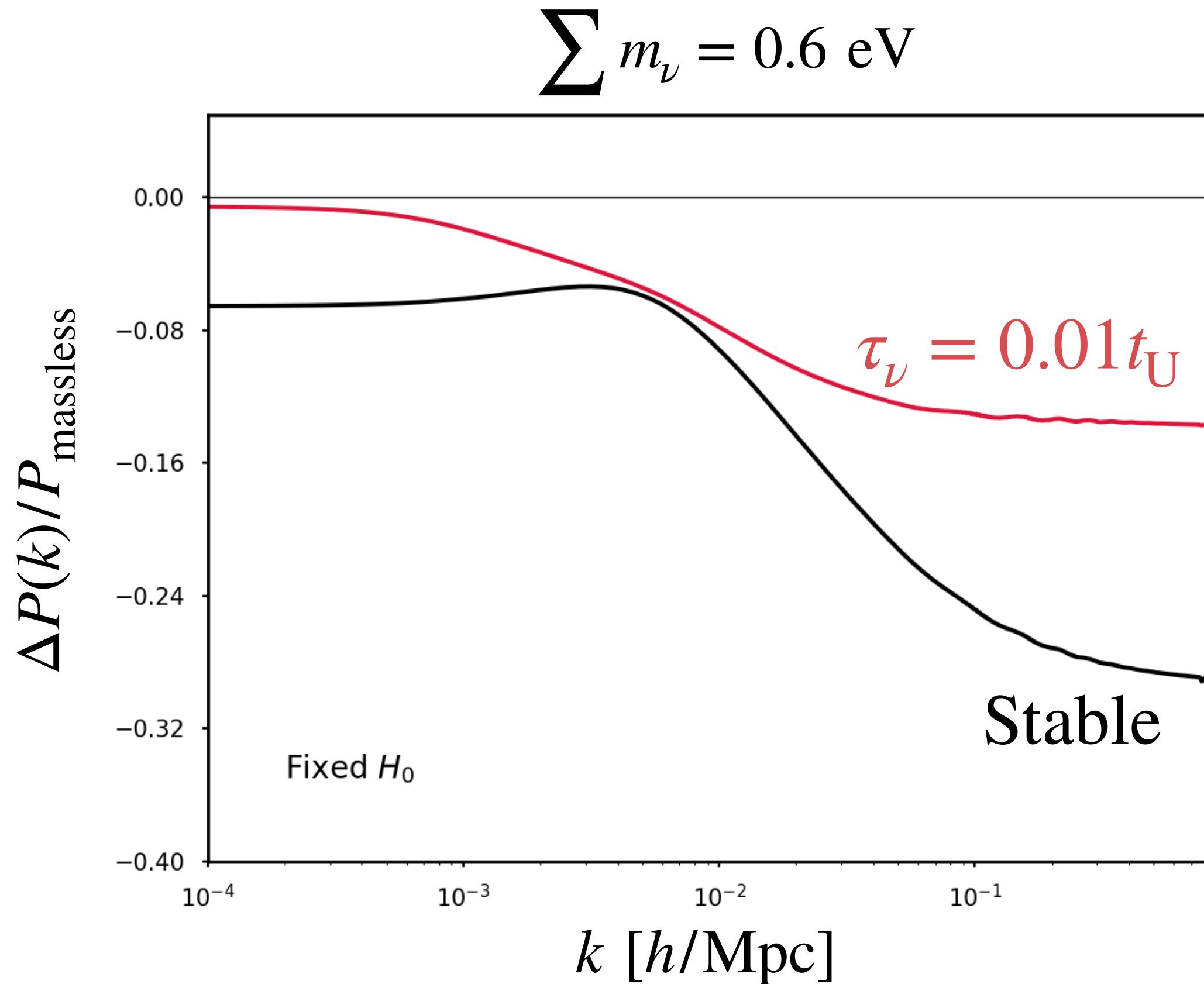
Appears naturally in many **simple extensions of the seesaw mechanism**

$$\mathcal{L}_{\text{int}} = \lambda i \phi \bar{\nu}_i \gamma_5 \nu_4 + \text{h.c.}$$

Escudero & Fairbairn [1907.05425]

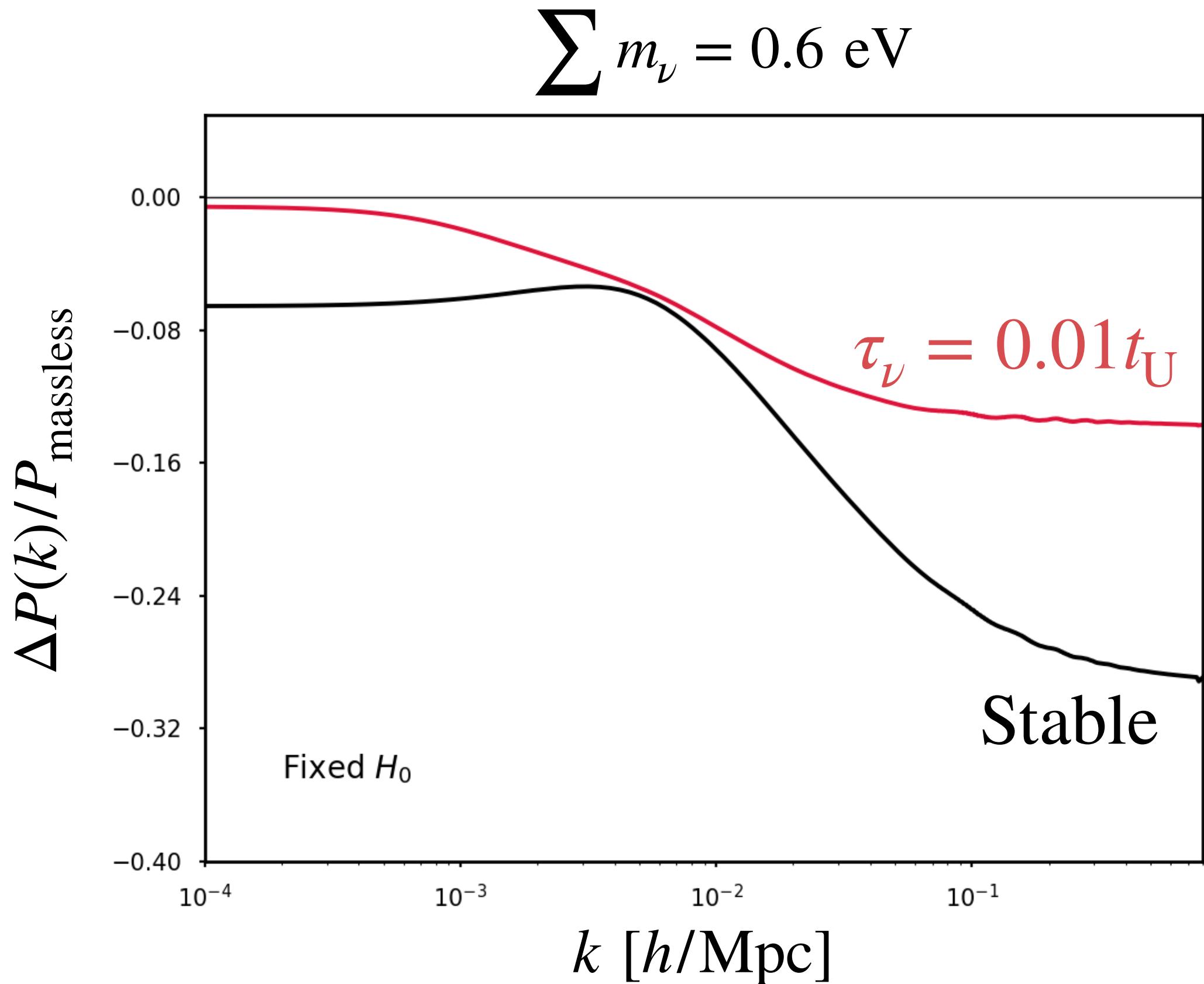
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# Decaying neutrinos



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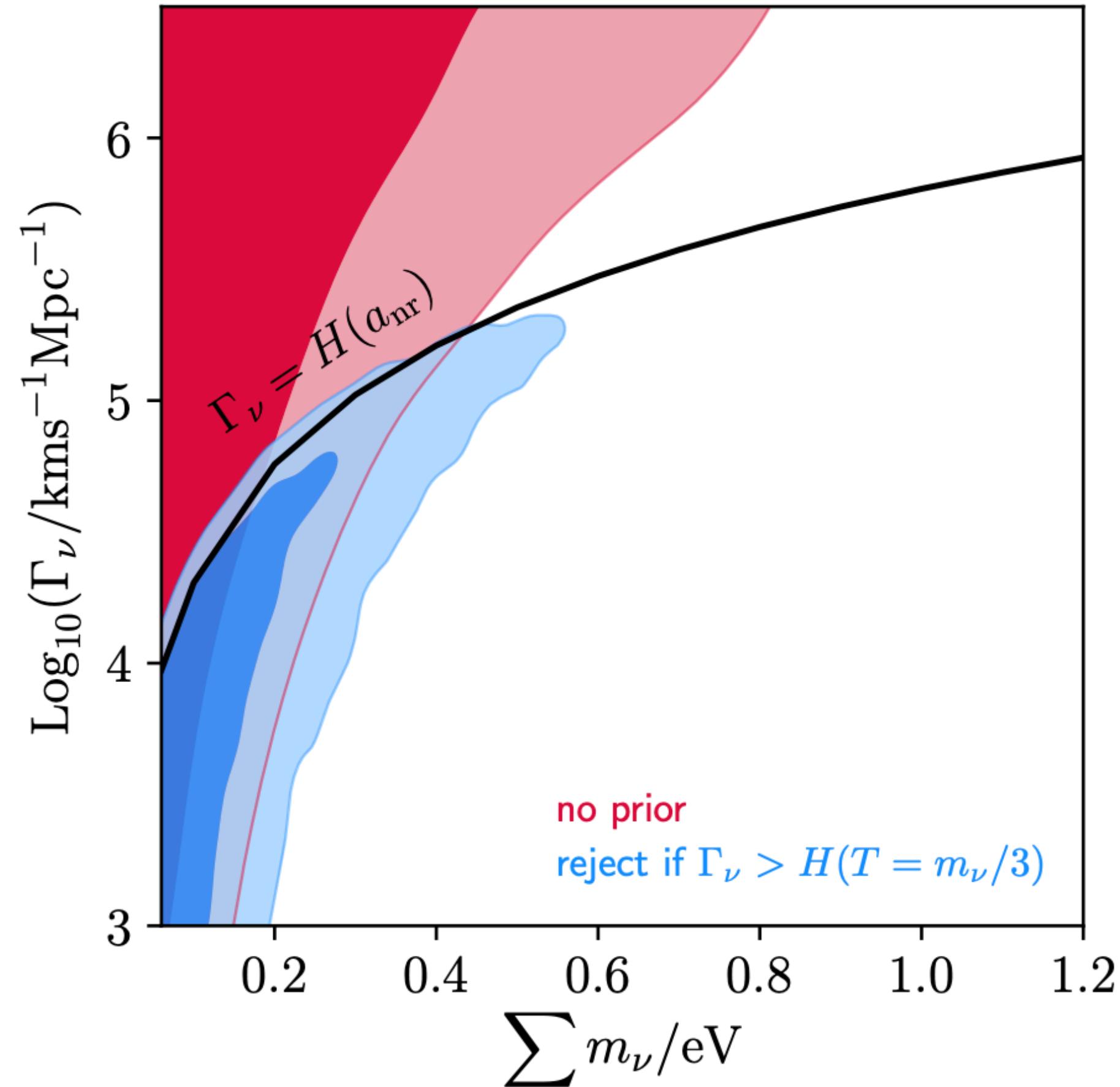


A finite neutrino lifetime allows to **reduce their impact** on structure growth and expansion rate



This permits a **relaxation of neutrino mass bounds** from cosmology

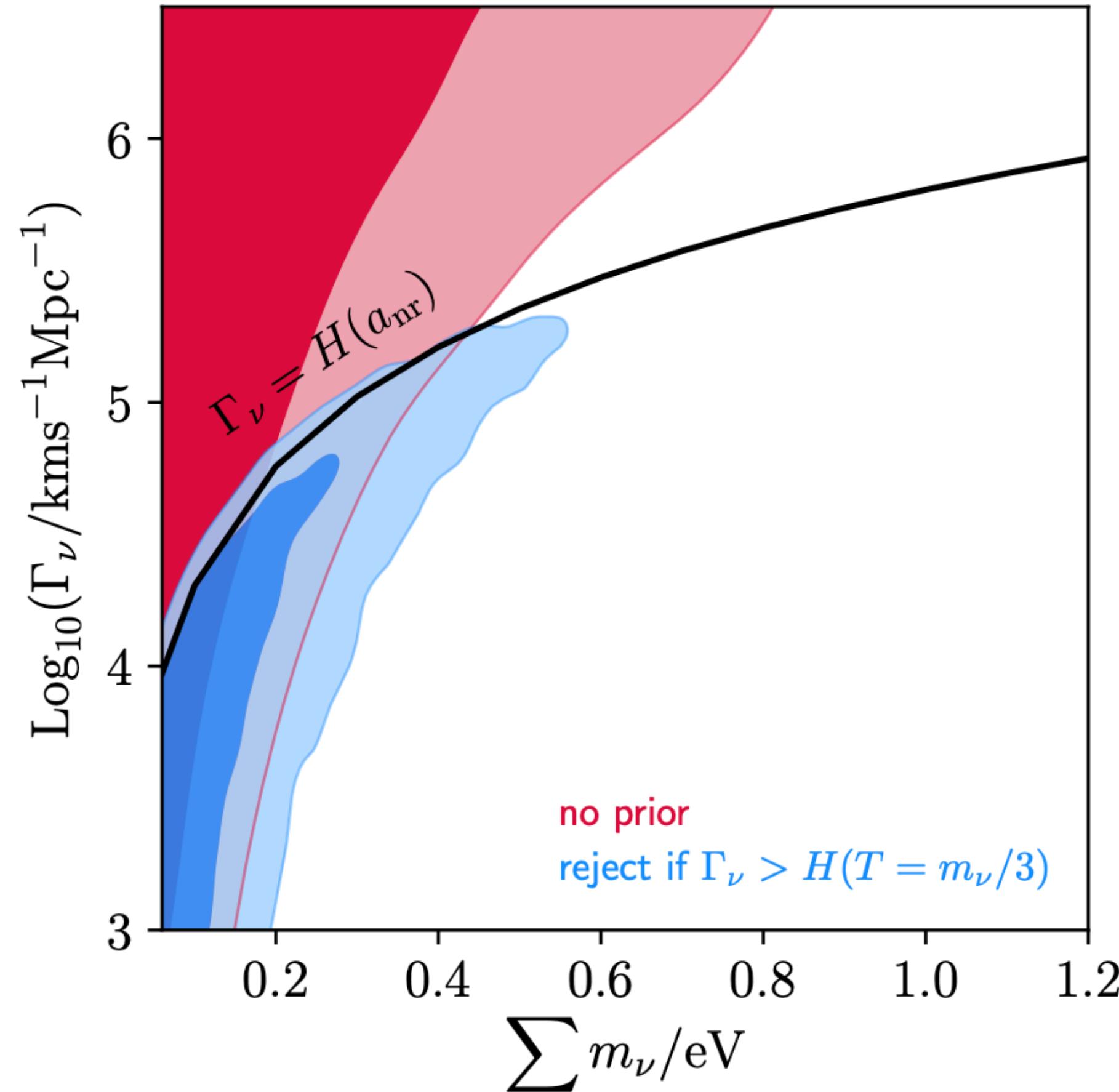
CMB+ BOSS + SNIa



Back in 2021, we showed that **non-relativistic neutrino decays to DR** can relax mass bounds up to  $\sum m_\nu < 0.4 \text{ eV}$

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## GOAL

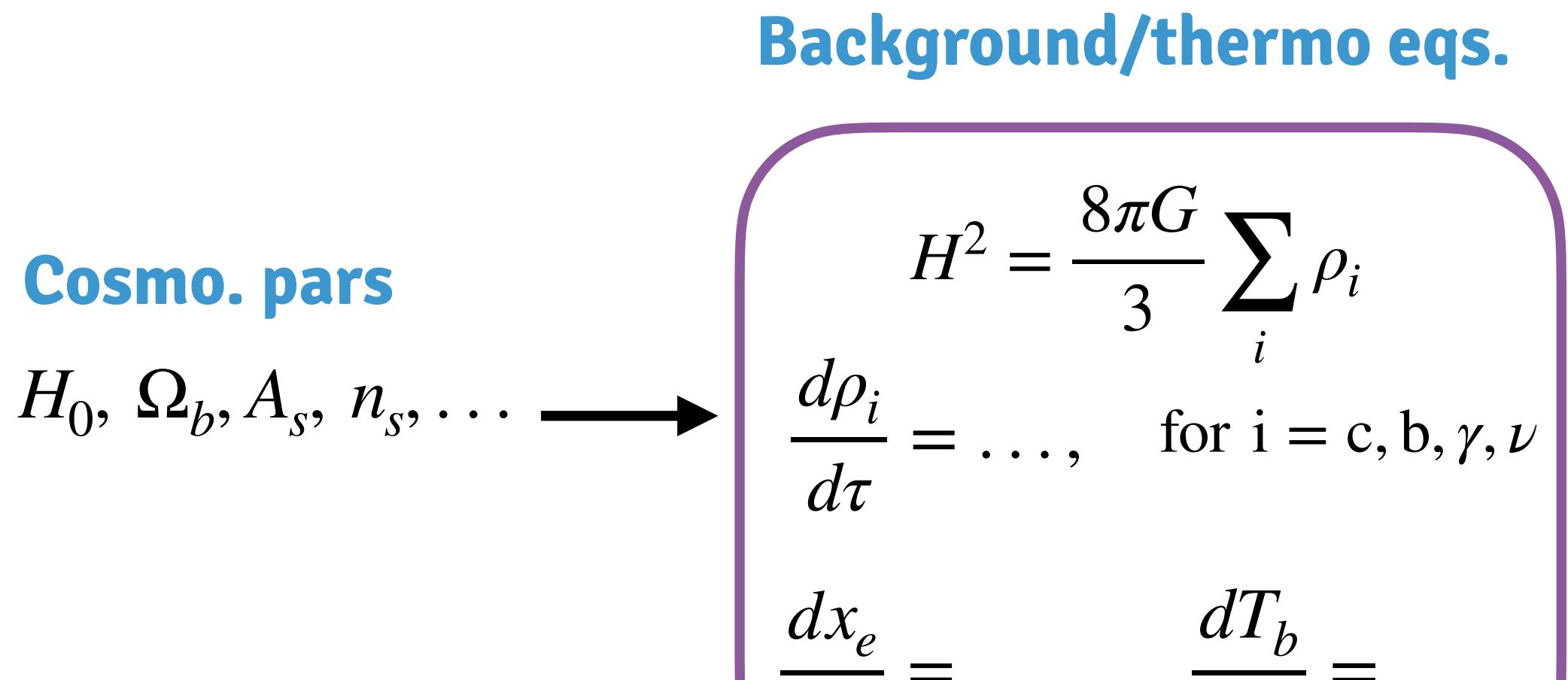
Build emulator for neutrino decay model, and use it to update mass bounds in light of latest DESI data

# Emulating an Einstein-Boltzmann Solver (EBS)

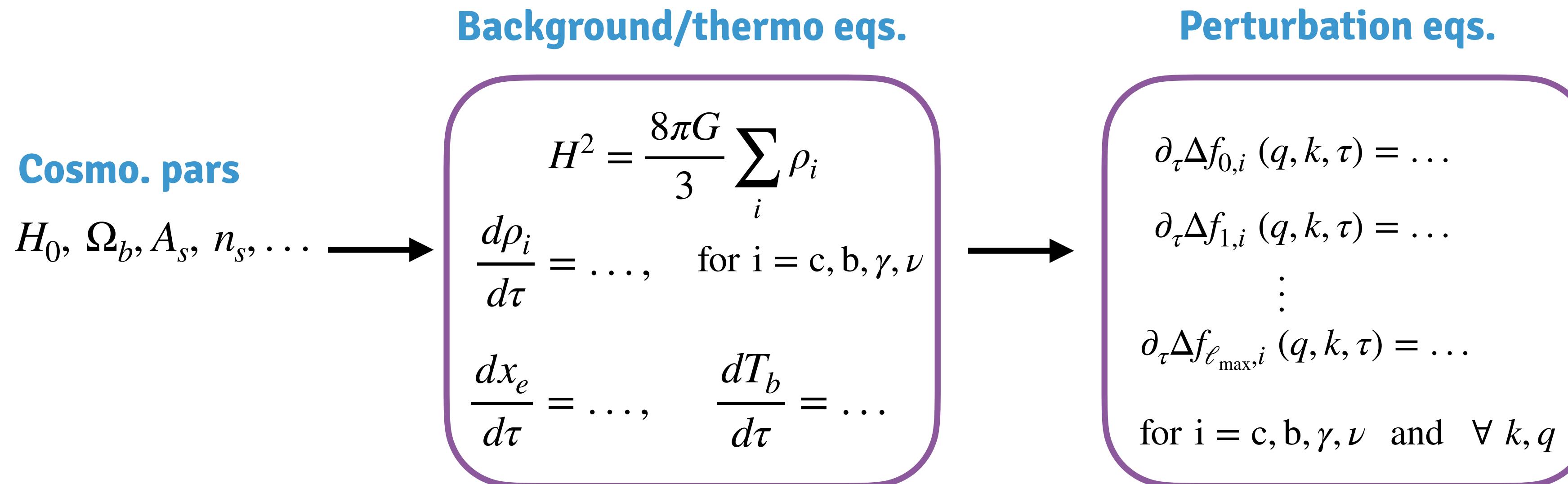
**Cosmo. pars**

$H_0, \Omega_b, A_s, n_s, \dots$

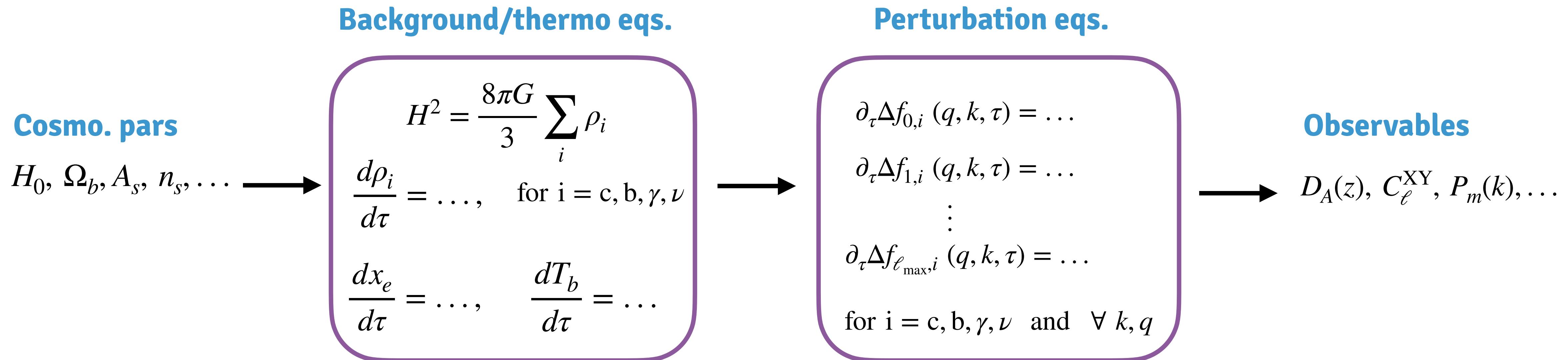
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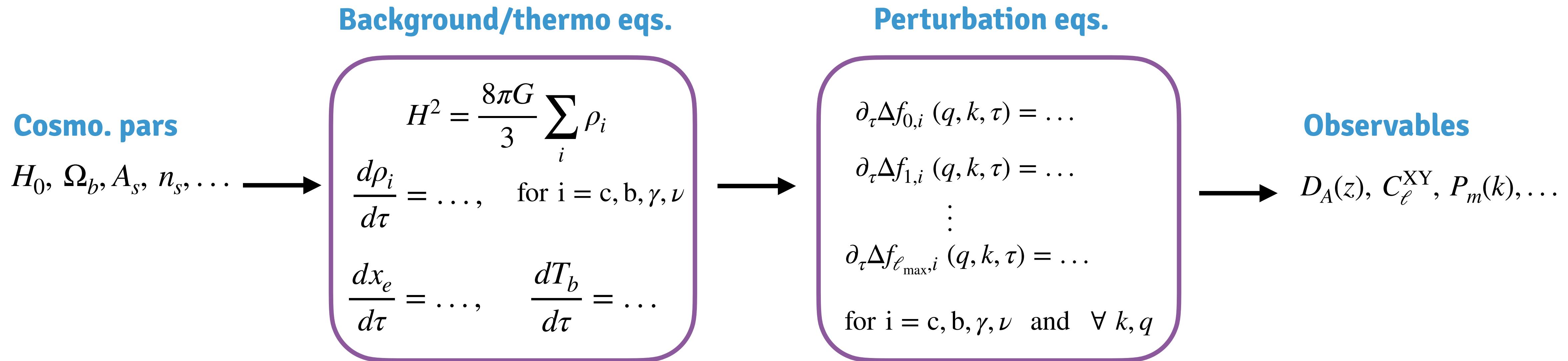
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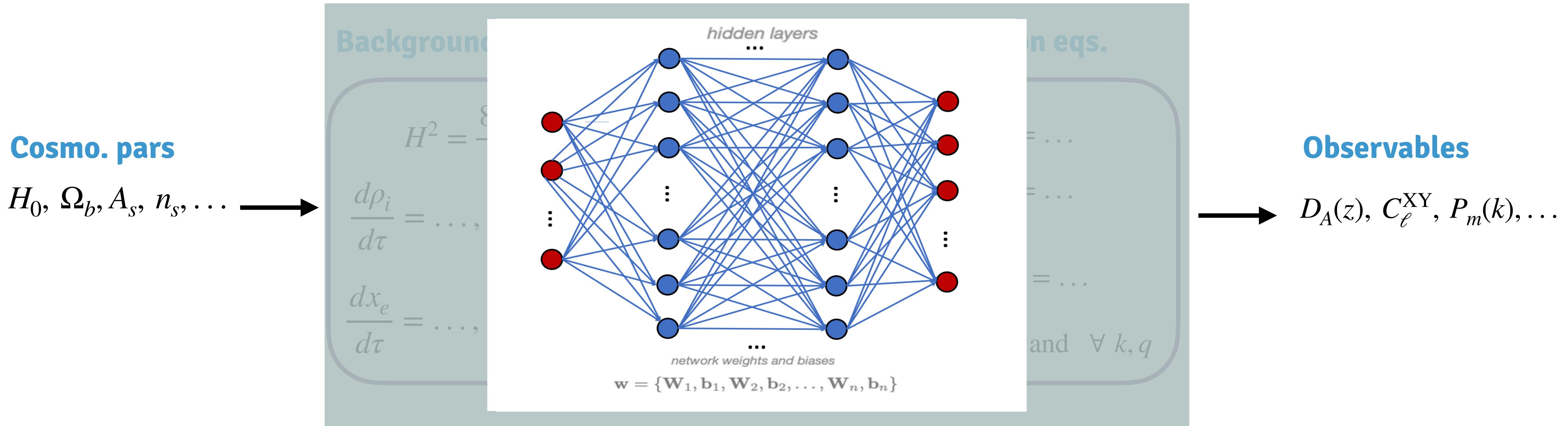


# Emulating an Einstein-Boltzmann Solver (EBS)



A single call to an EBS (e.g. CLASS) can be **time-consuming in  $\Lambda$ CDM extensions**. Moreover, one often needs  **$\sim 10^6$  model evaluations** for accurate inference.

# Emulating an Einstein-Boltzmann Solver (EBS)



**IDEA:** Replace the calculation of the full system of linear Einstein-Boltzmann eqs. by a **trained emulator**, e.g. a neural network (NN)

# Emulating an Einstein-Boltzmann Solver (EBS)

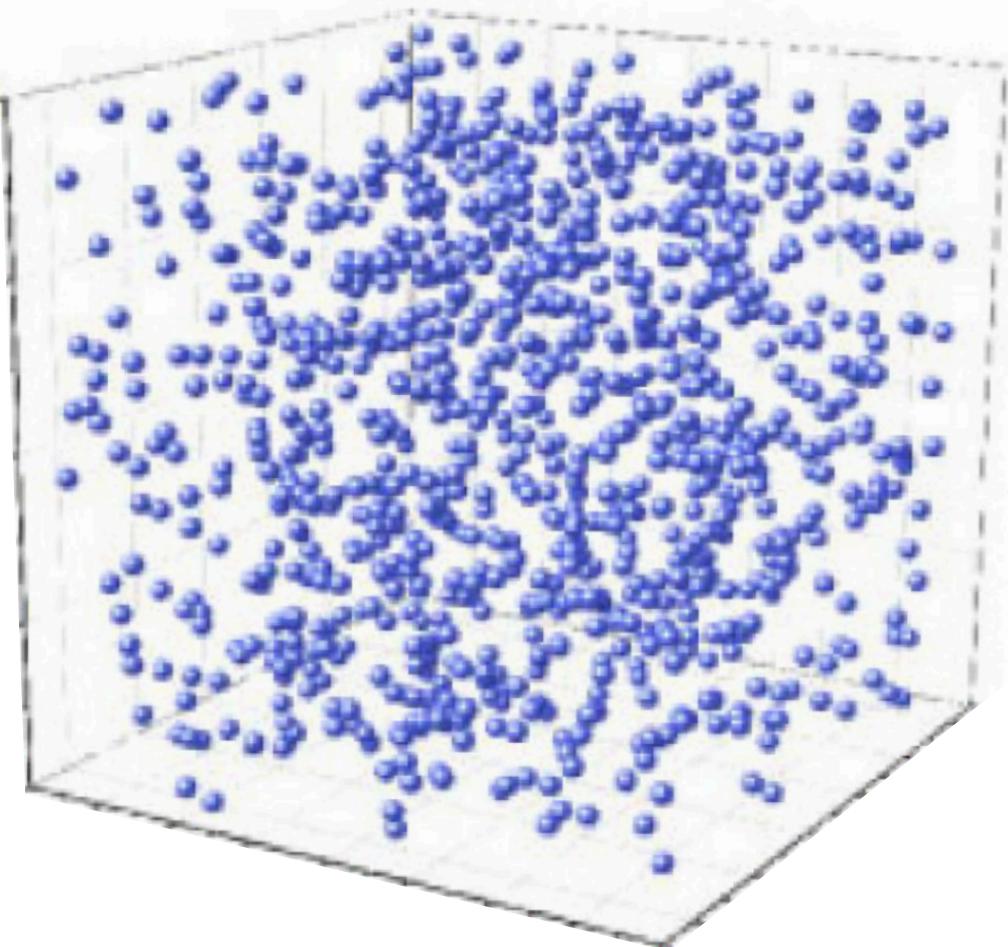
Many EBS emulators available on the market (e.g. [CosmoPower](#), [CosmicNet](#), [Capse.jl](#))

We rely on [CONNECT](#) [Nygaard et al. 2205.15726]

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## Latin Hypercube (LHC) sampling

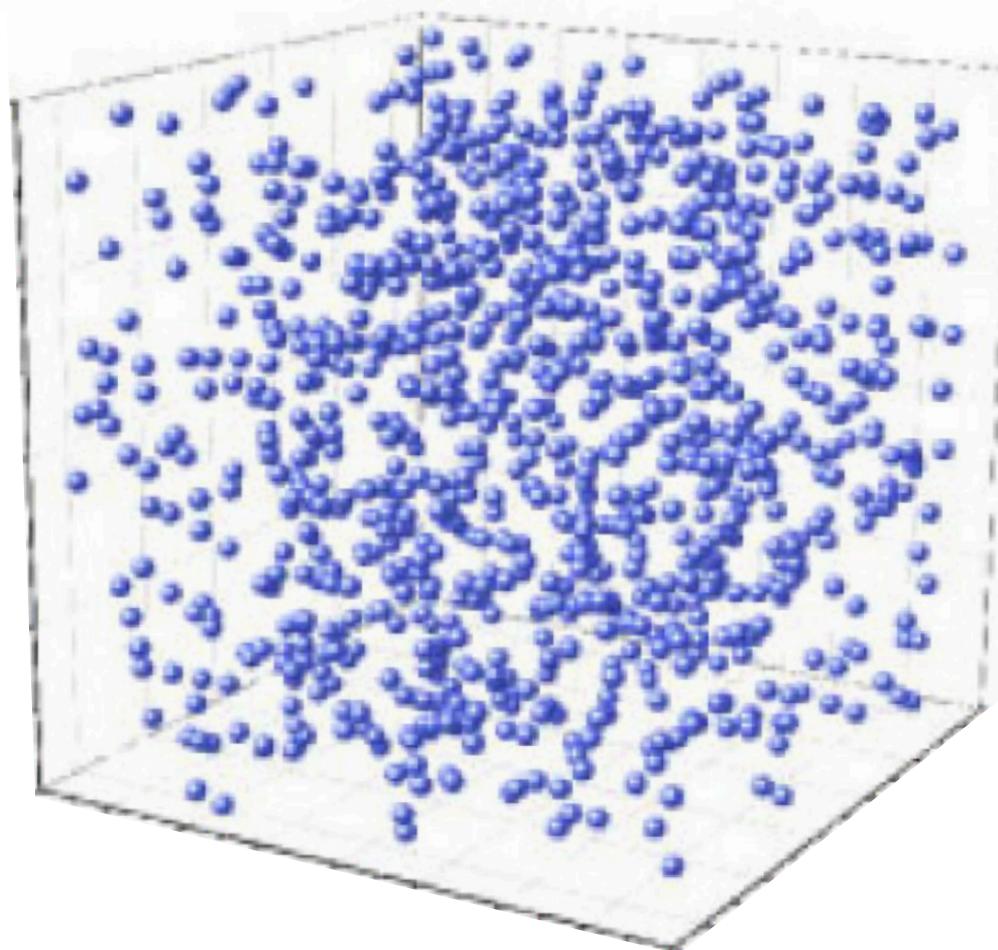


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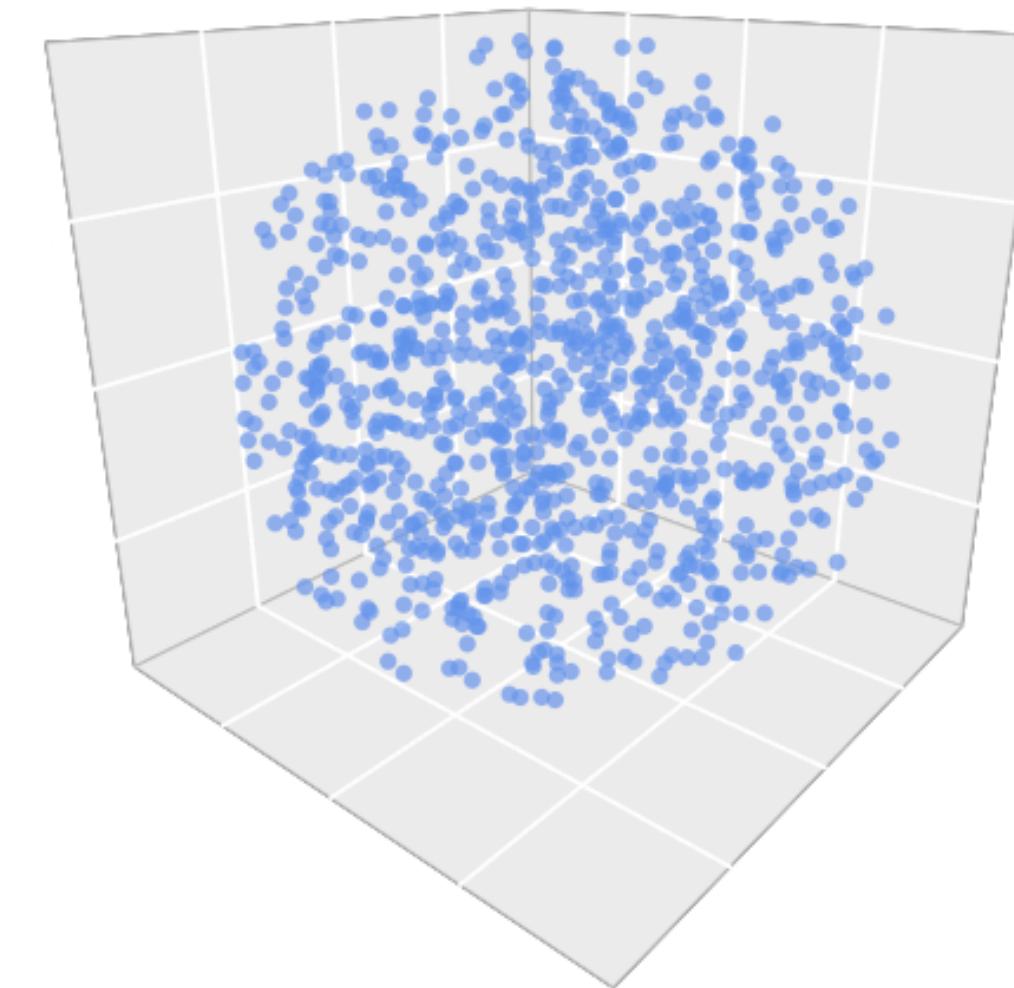
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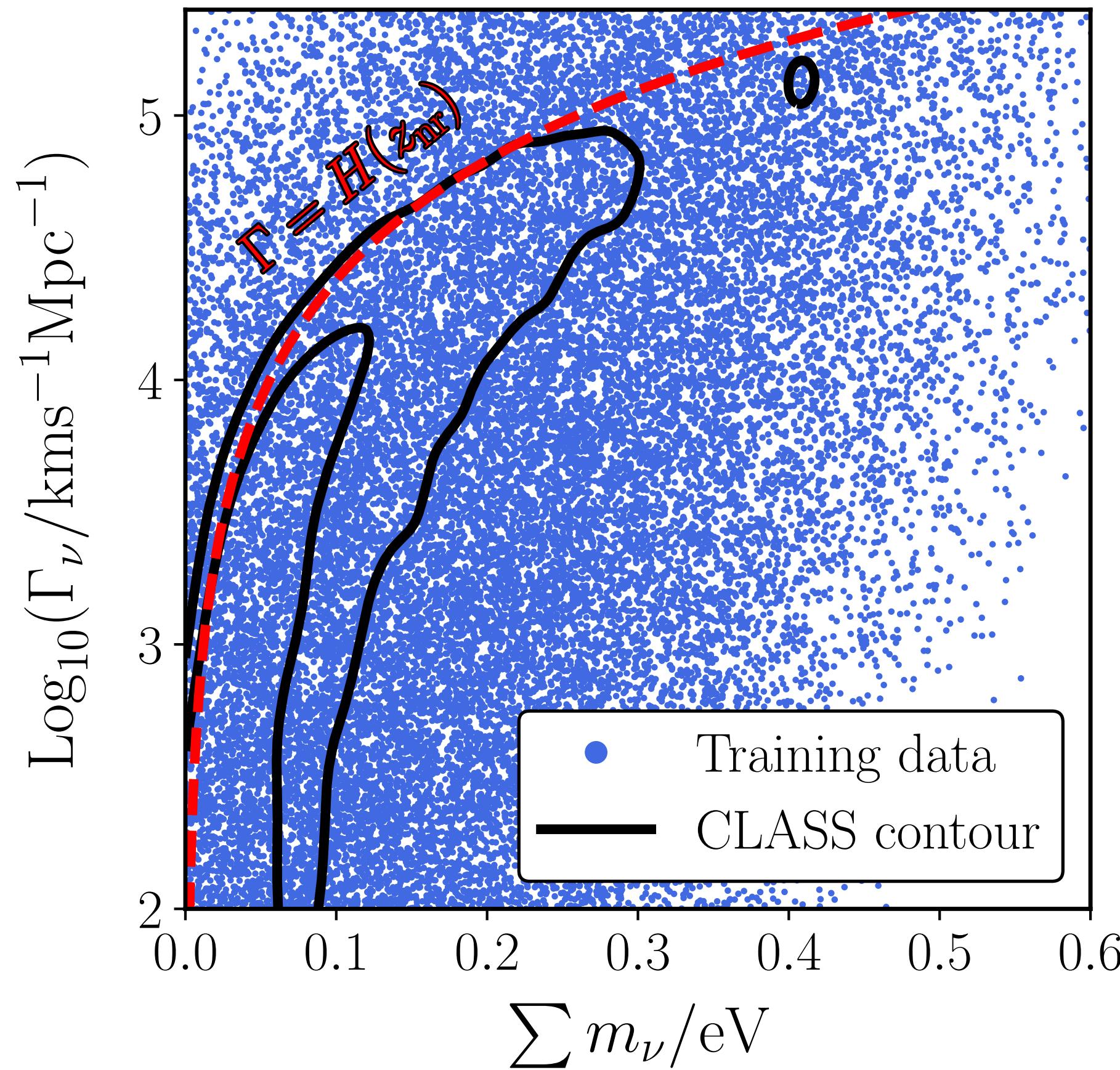
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**Hypersphere sampling**



Allows to concentrate points in  
**high-likelihood regions**  
→ more efficient and accurate

# Building emulator for decaying neutrinos

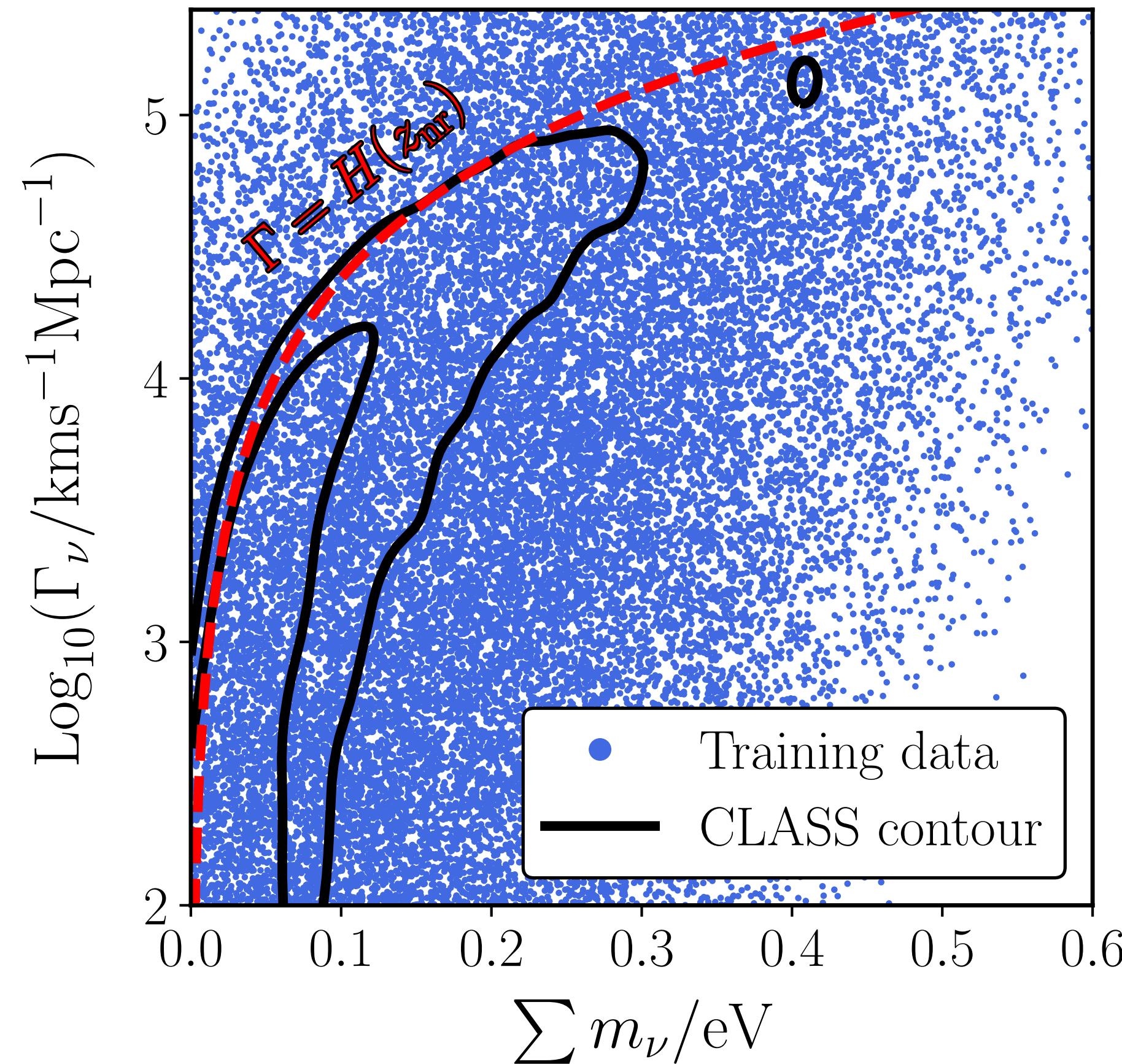


**Training data:**  $2.5 \times 10^4$  samples of  $\{\theta, x\}$  in the 8-dimensional hypersphere

$$\theta = \{\omega_b, \omega_c, H_0, \ln(10^{10} A_s), n_s, \tau_{\text{reio}}, m_\nu, \log_{10} \Gamma_\nu\}$$

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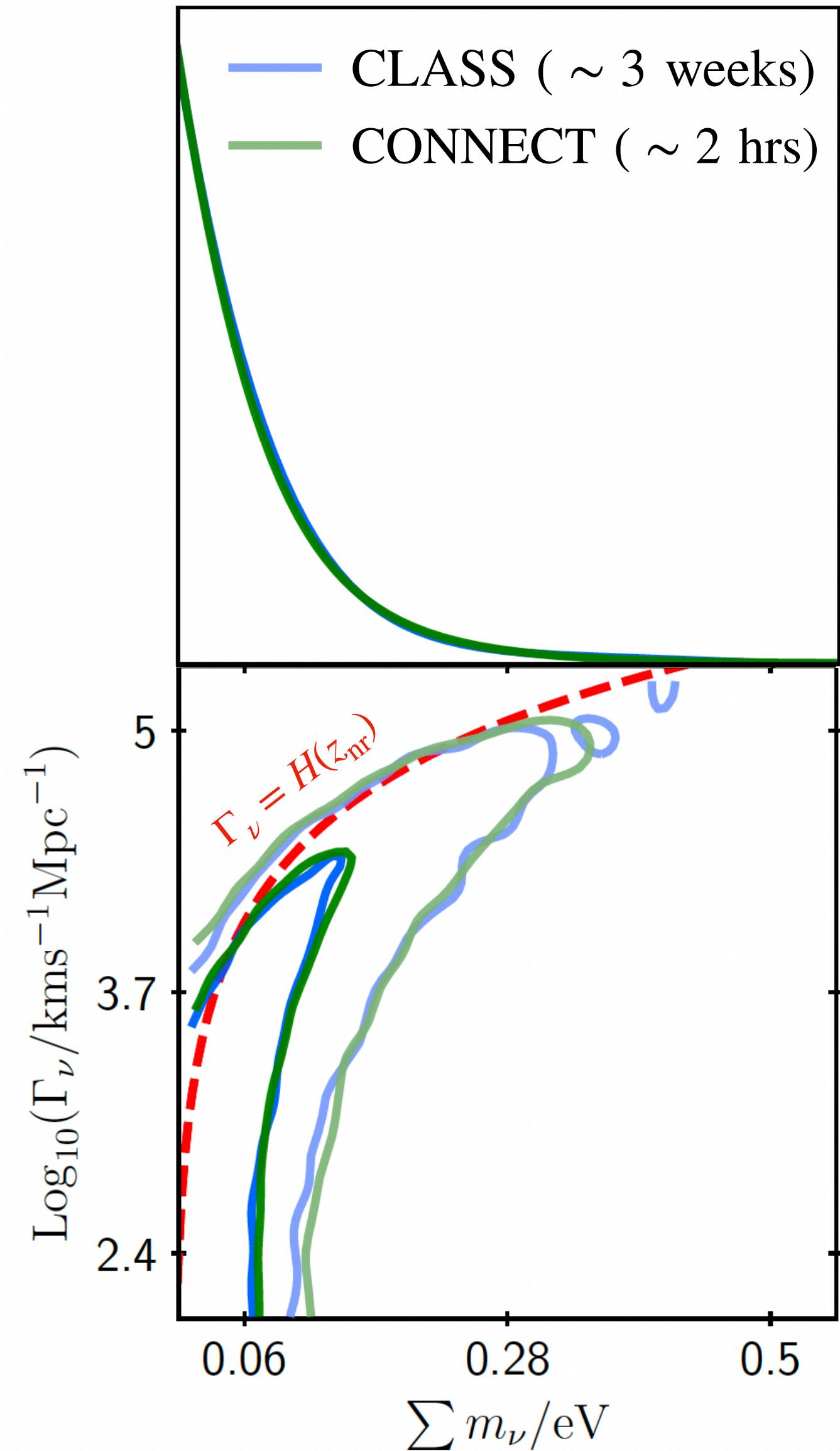


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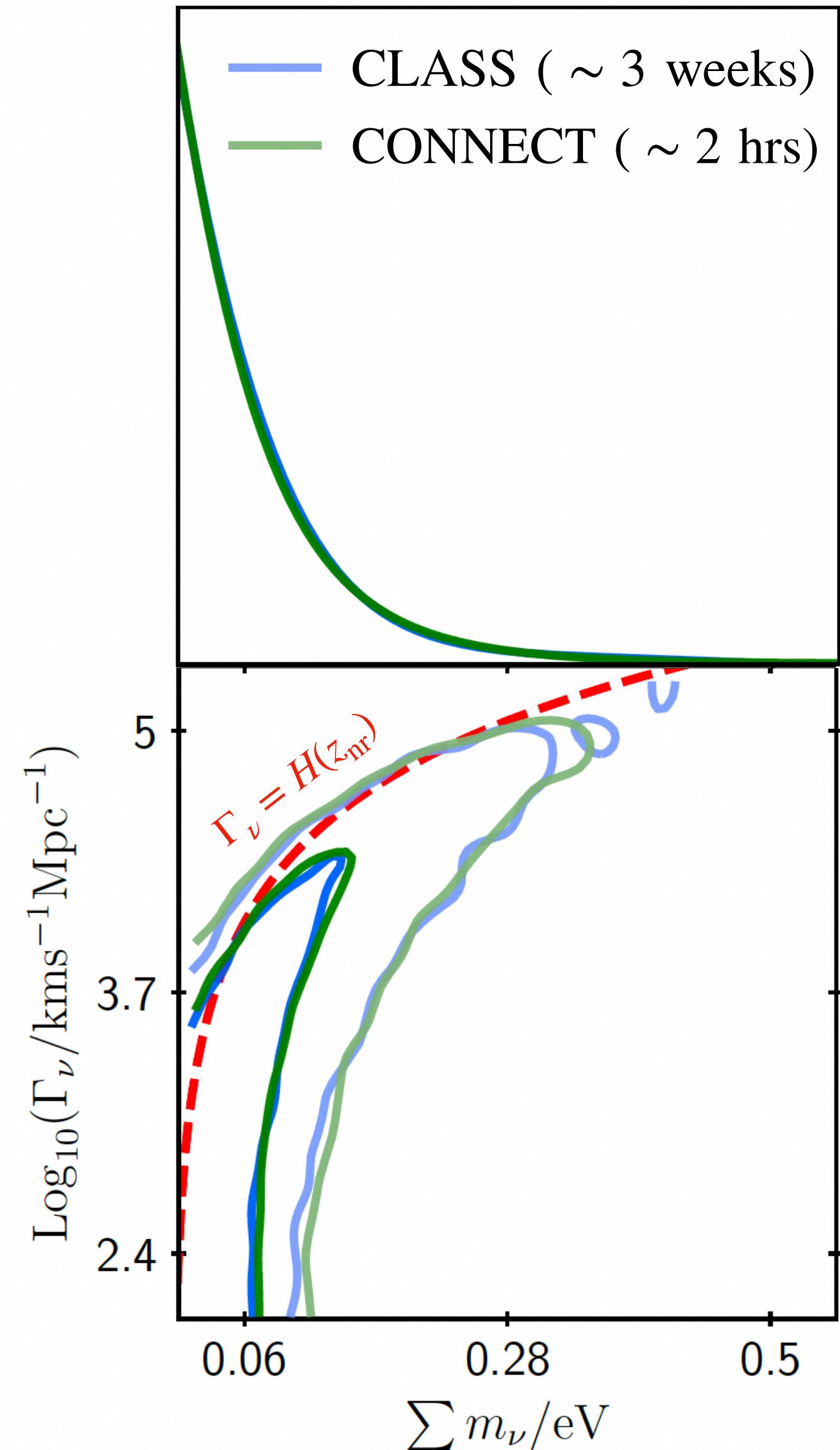
Data generation took  $\sim 1$  day on 128 CPUs  
(training the NNs was much faster)

# Cosmological constraints



CONNECT posteriors are in good agreement  
with CLASS, while being  $\times 250$  faster

# Cosmological constraints



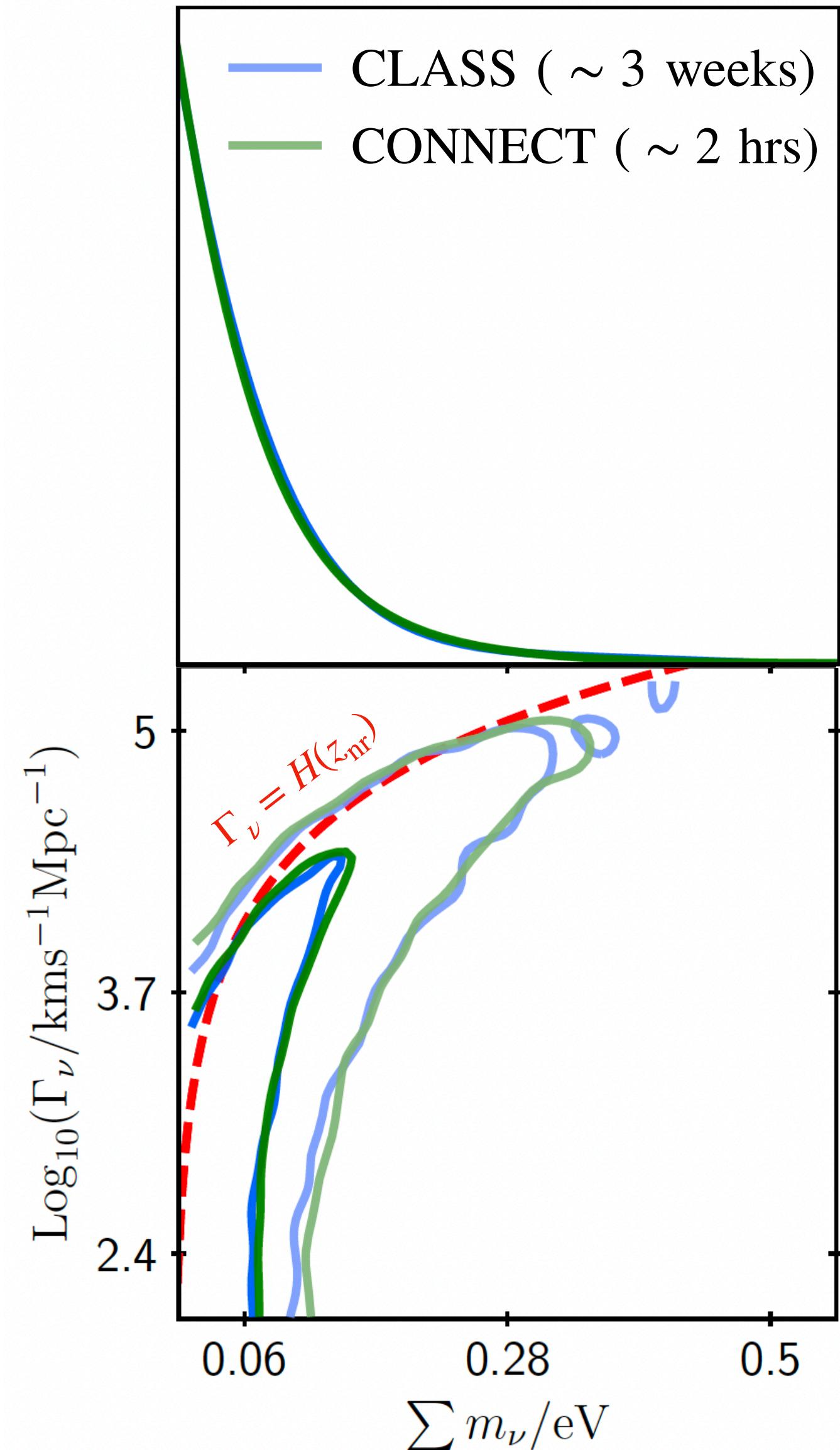
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**New mass bound:**

$$\sum m_\nu < 0.24 \text{ eV}$$

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**New mass bound:**

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**Next step:** derive bounds for neutrino decays with  
realistic mass splittings  $\nu_i \rightarrow \nu_j + \phi$

Based on arXiv:2403.14750  
arXiv:2506.XXXX

with Guadalupe Cañas-Herrera, Matteo  
Martinelli, Oleg Savchenko, Noemi Anau  
Montel & Christoph Weniger

## 2. **Simulation-based inference**

For efficient inference from  
**Euclid** data, with applications  
to **evolving dark energy**

# Bayesian inference

$\mathbf{x}_0$  : Data

$\theta$  : Parameters

Posterior	Likelihood	Prior
$p(\theta   \mathbf{x}_0)$	$\propto p(\mathbf{x}_0   \theta)p(\theta)$	

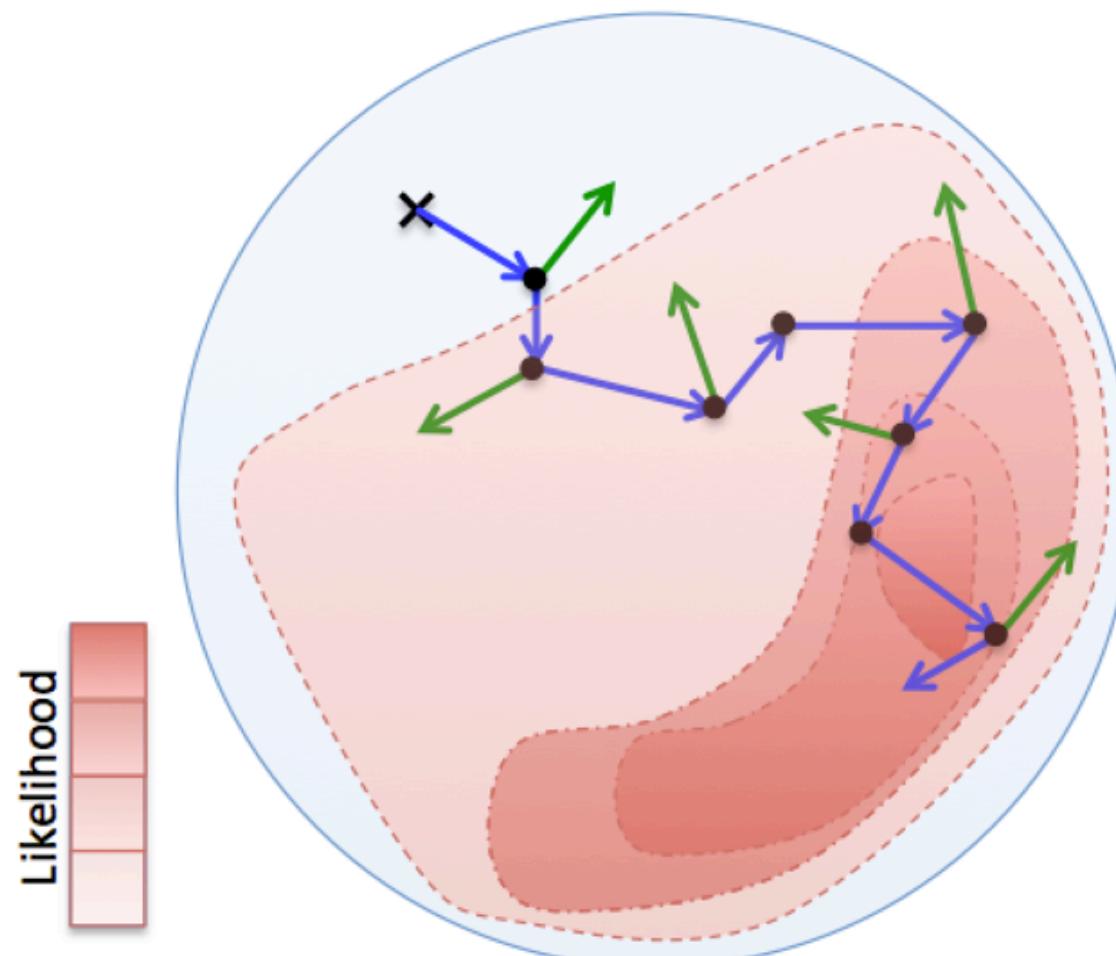
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Metropolis-Hastings algorithm

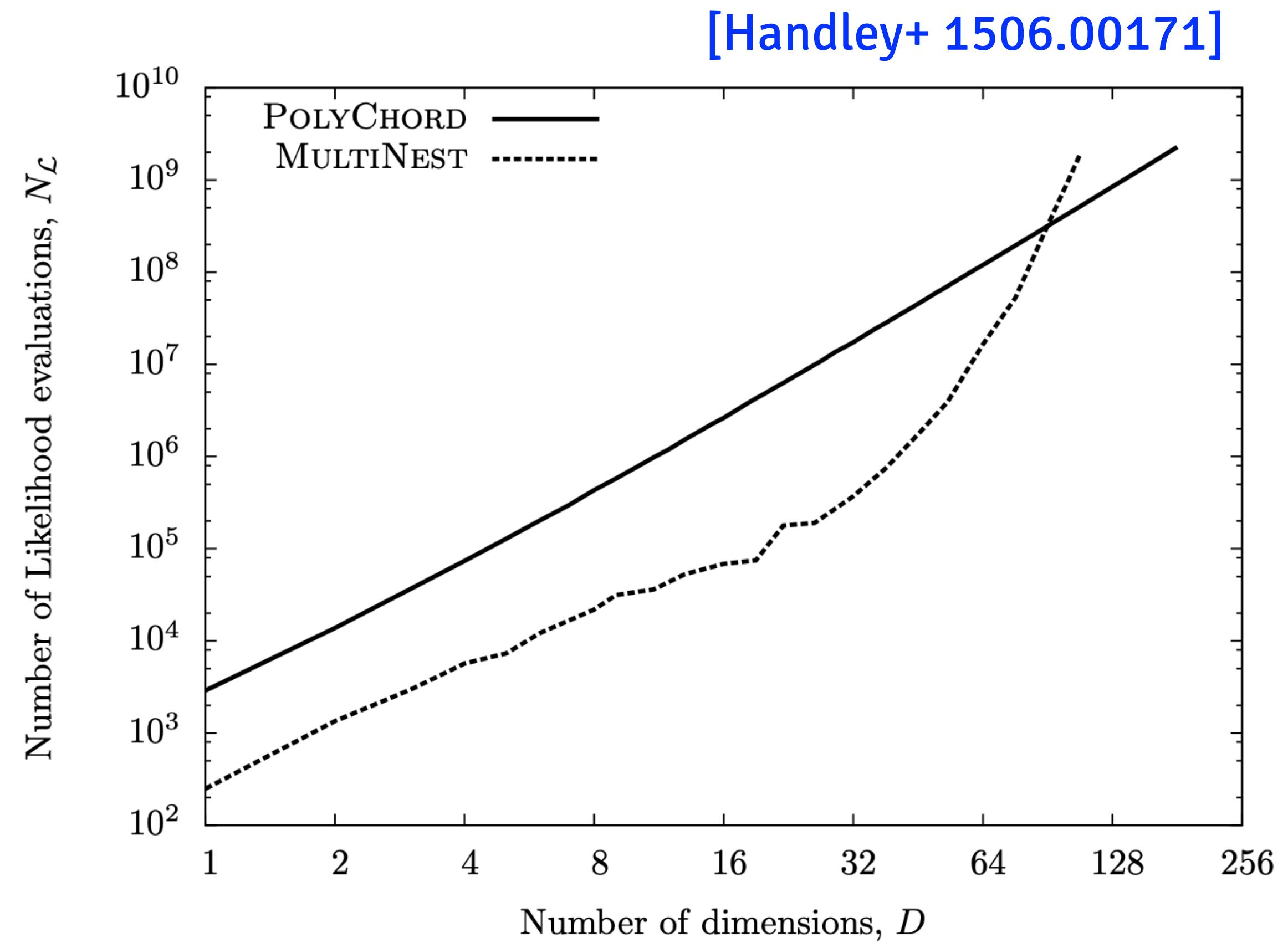


Traditional **likelihood-based** methods allow to get samples from the **full joint posterior** for some fixed data  $\mathbf{x}_0$

$$\theta \sim p(\theta | \mathbf{x}_0), \quad \text{for } \theta \in \mathbb{R}^D$$

# Current challenges

MCMC methods scale poorly with the dimensionality

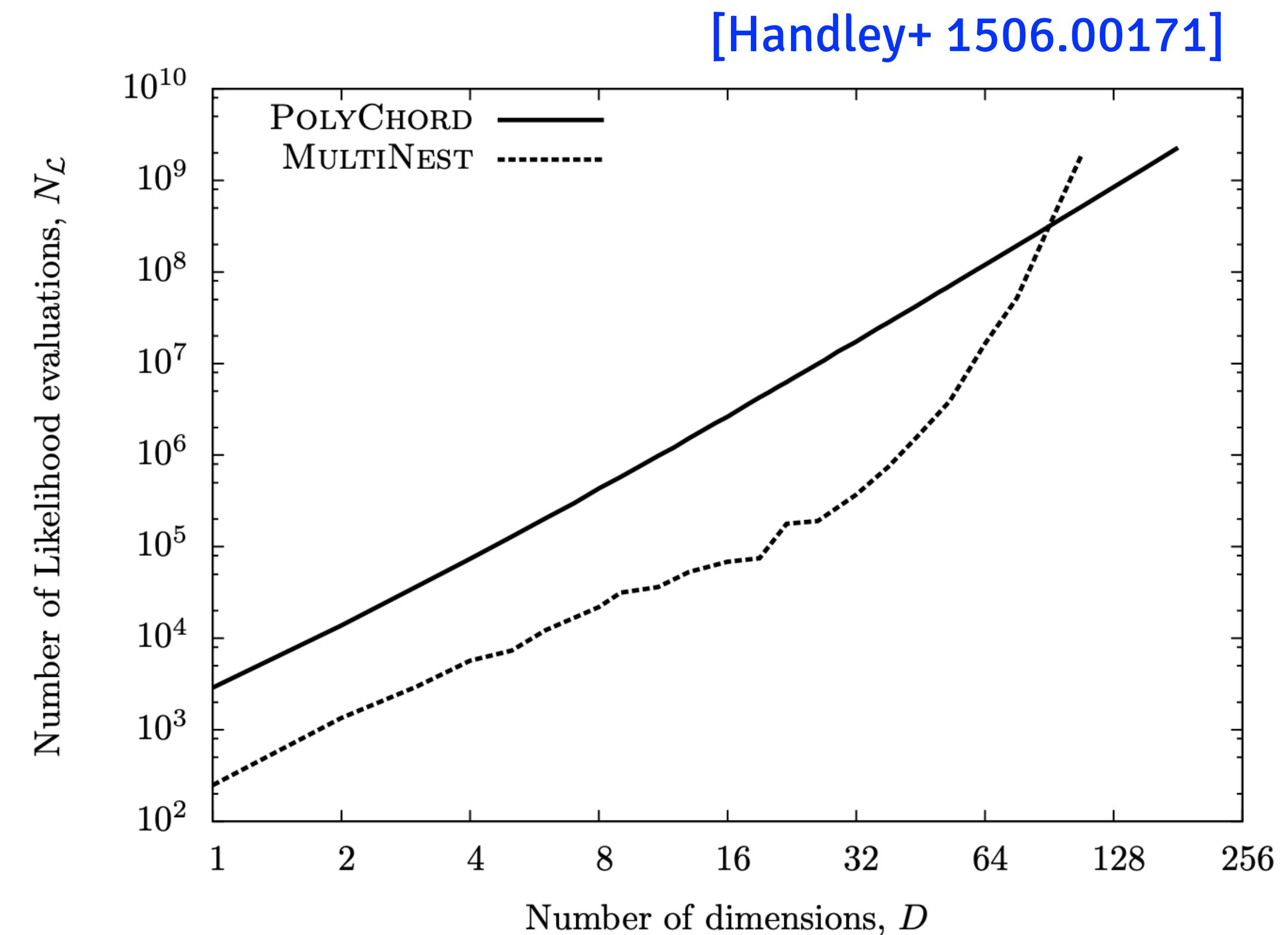


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 $\sim 50 - 100$  nuisance params!



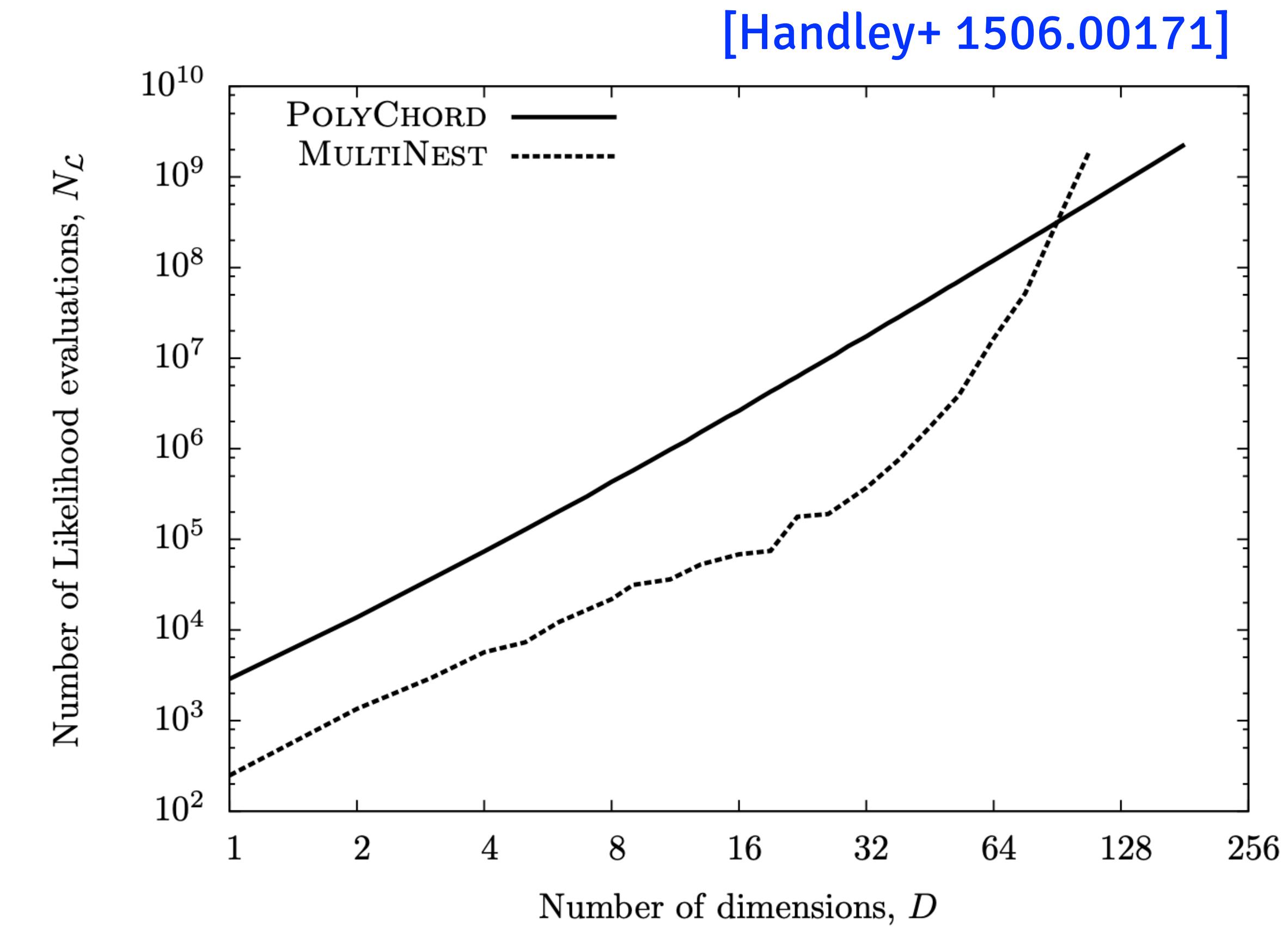
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Often the full **likelihood** function is **intractable**



# **Simulation-based inference (SBI)**

(a.k.a. likelihood-free or implicit inference)

“Can we still do Bayesian inference if all we can do is simulate the data?”

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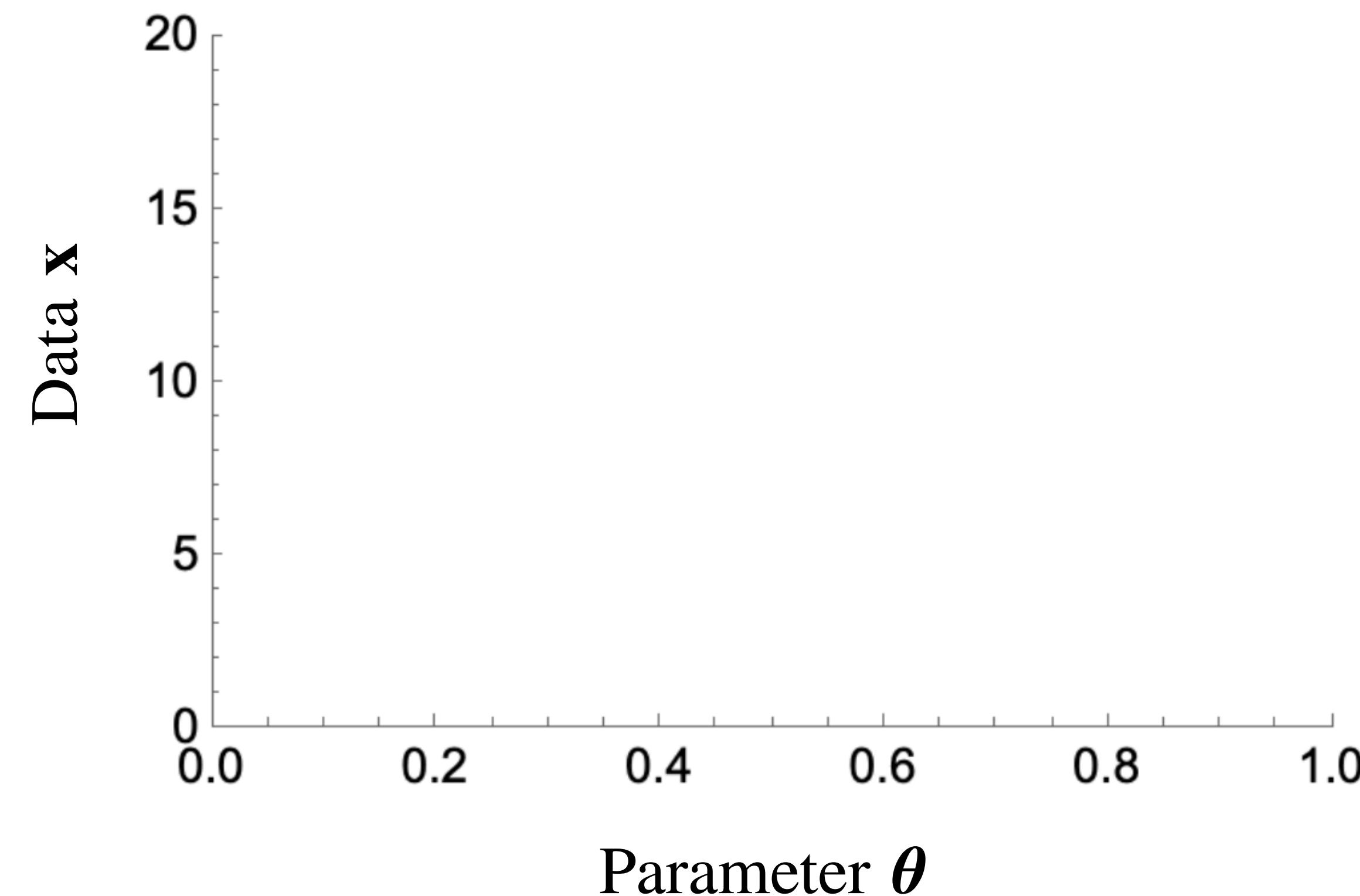
**Simulator** mapping from  
parameters  $\theta$  to data  $x$



$x \sim p(x | \theta)$   
**(implicit likelihood)**

# Simulation-based inference (SBI)

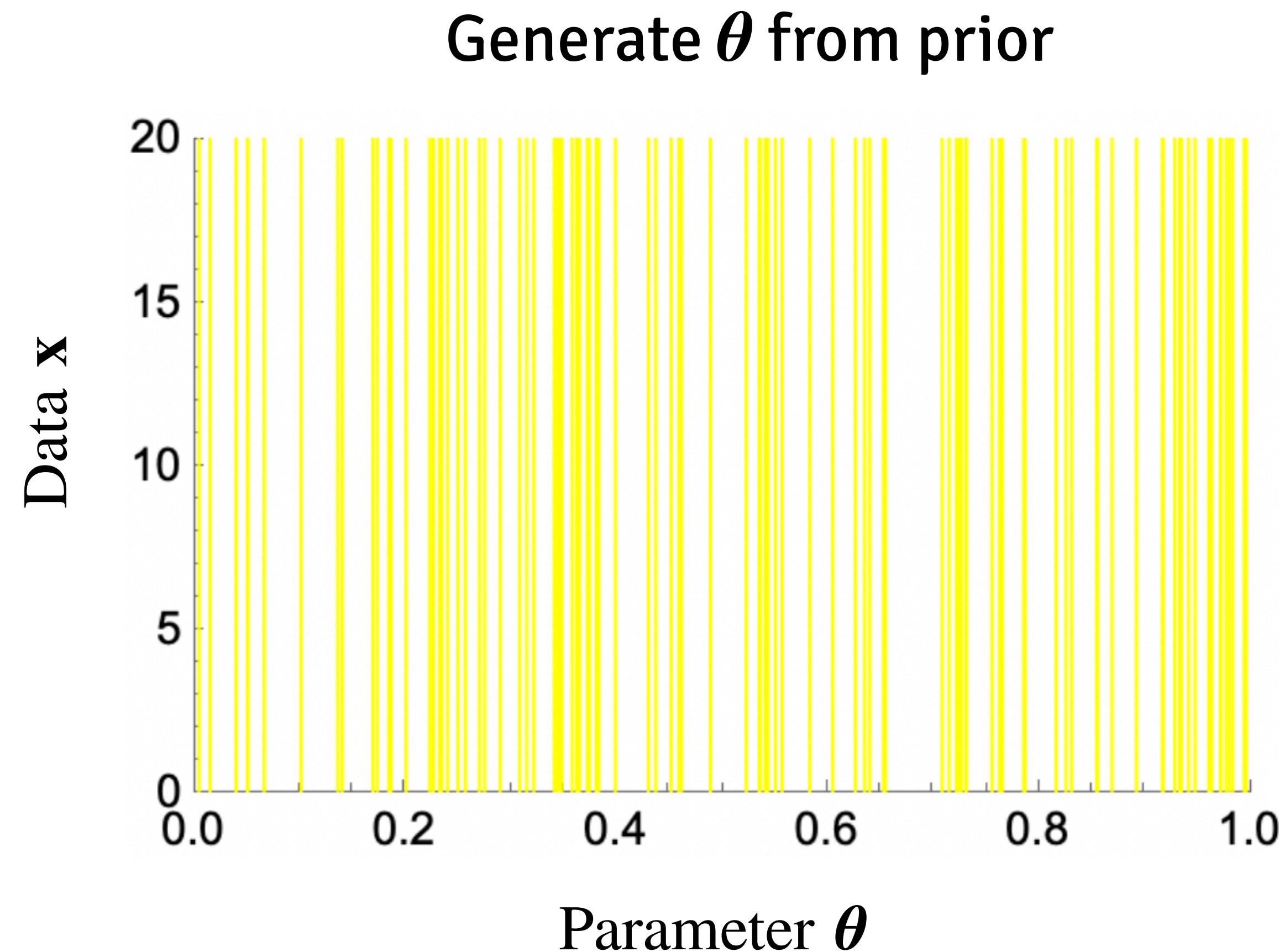
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[Credit: B. Wandelt]

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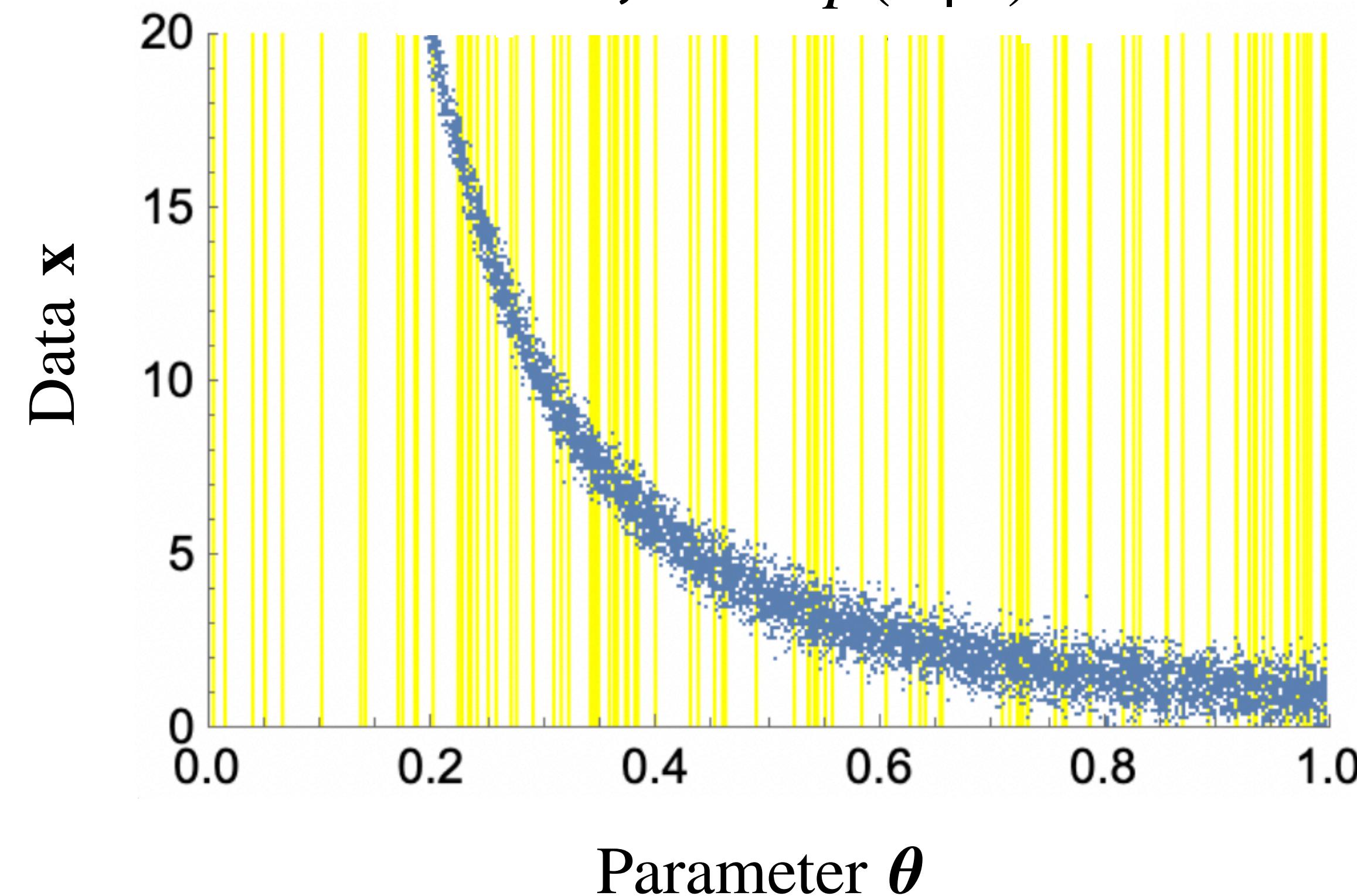


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# Simulation-based inference (SBI)

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Simulate  $\mathbf{x}$  for each  $\theta$   
i.e.,  $\mathbf{x} \sim p(\mathbf{x} | \theta)$

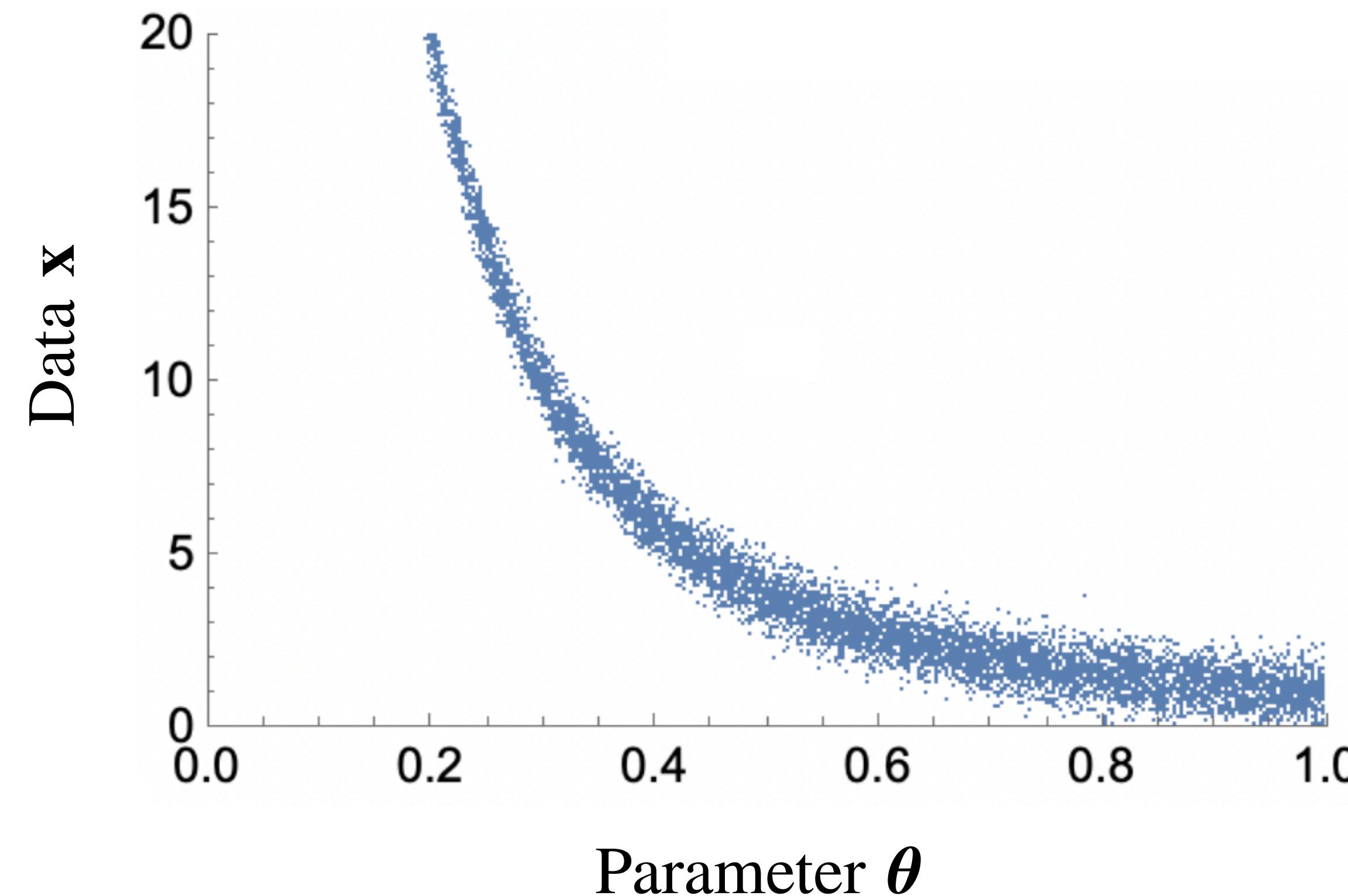


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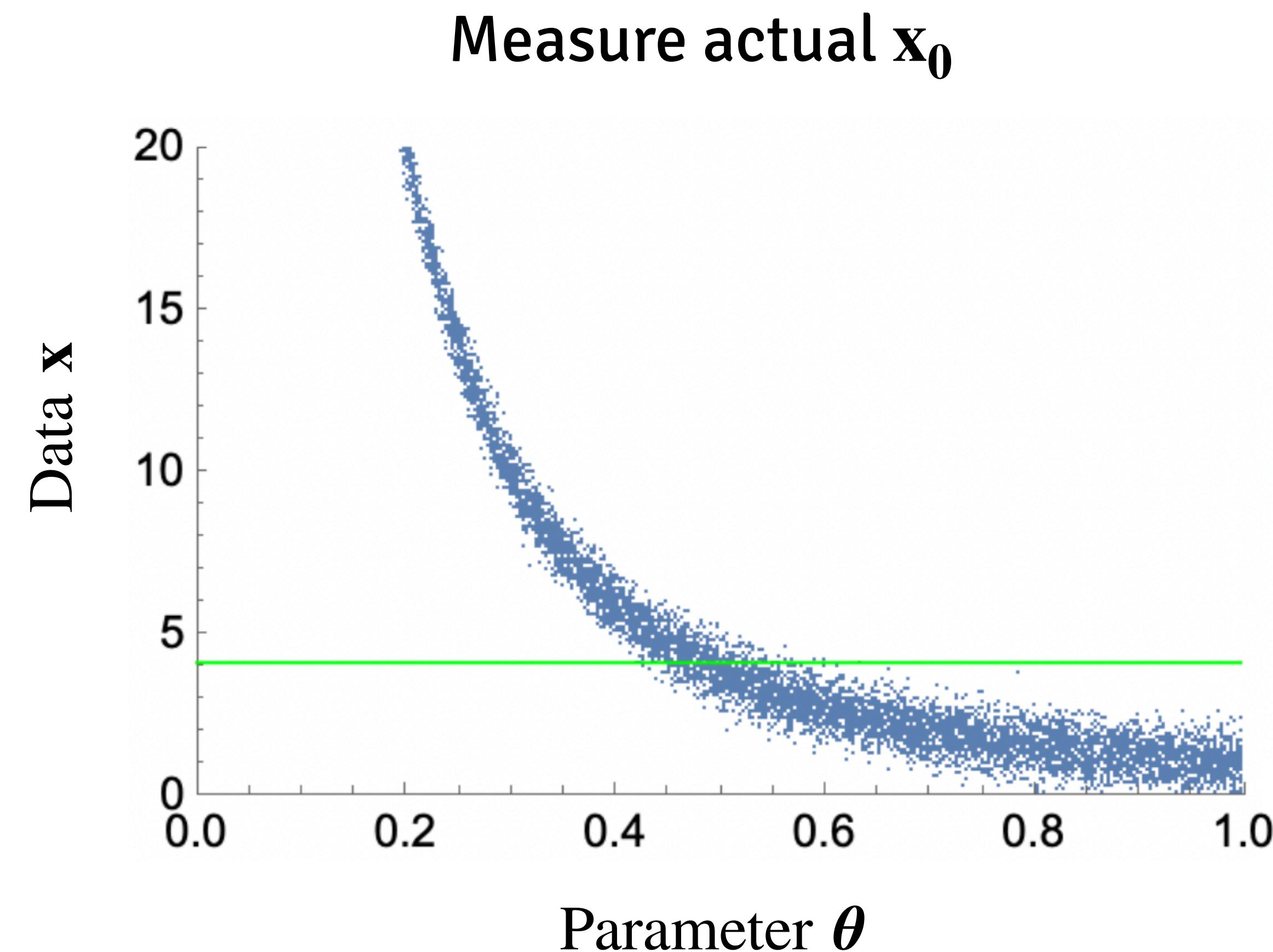
This is a sample from  $p(\theta, \mathbf{x})$



[Credit: B. Wandelt]

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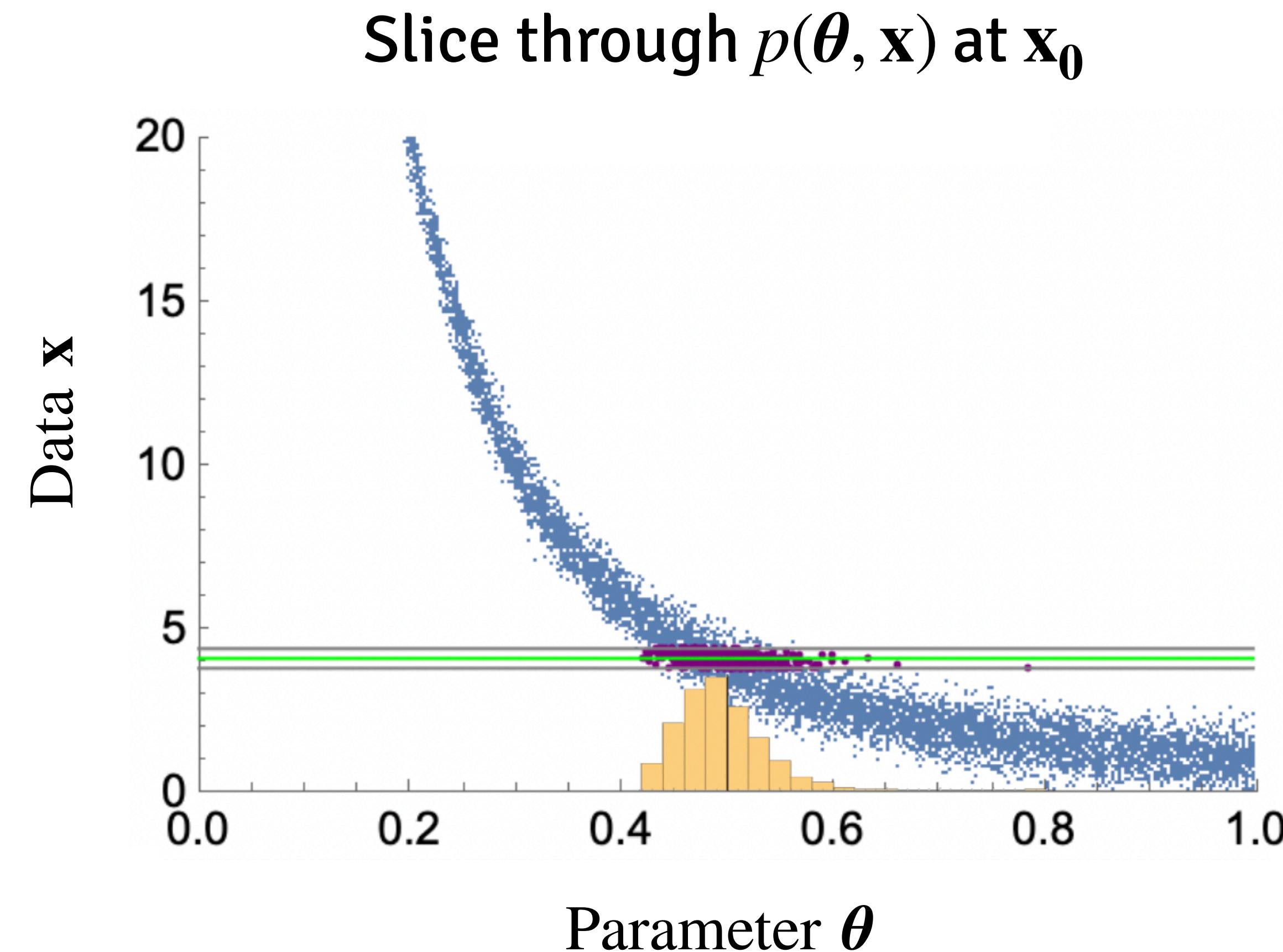
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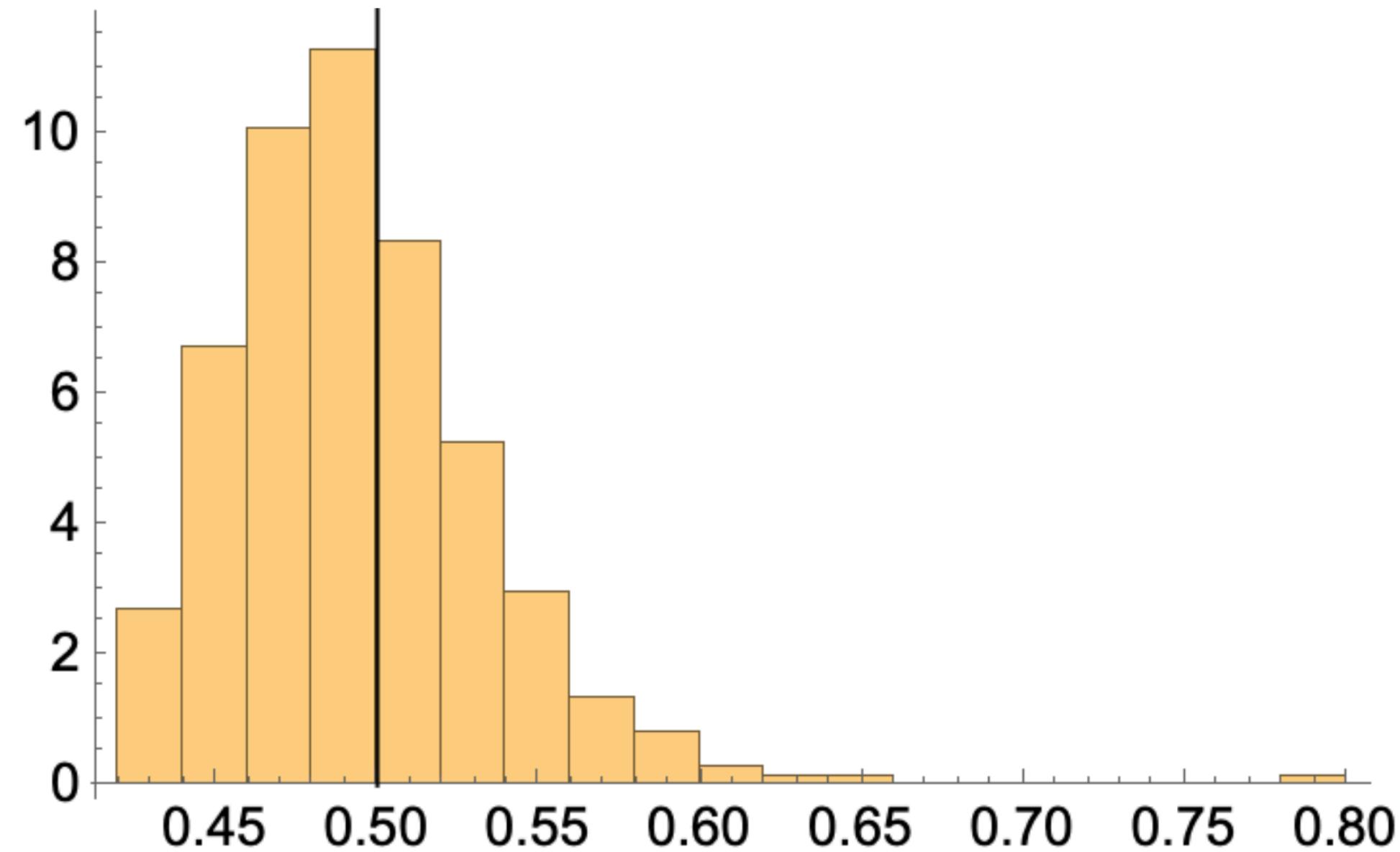


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Posterior  $p(\theta | \mathbf{x}_0)$



[Credit: B. Wandelt]

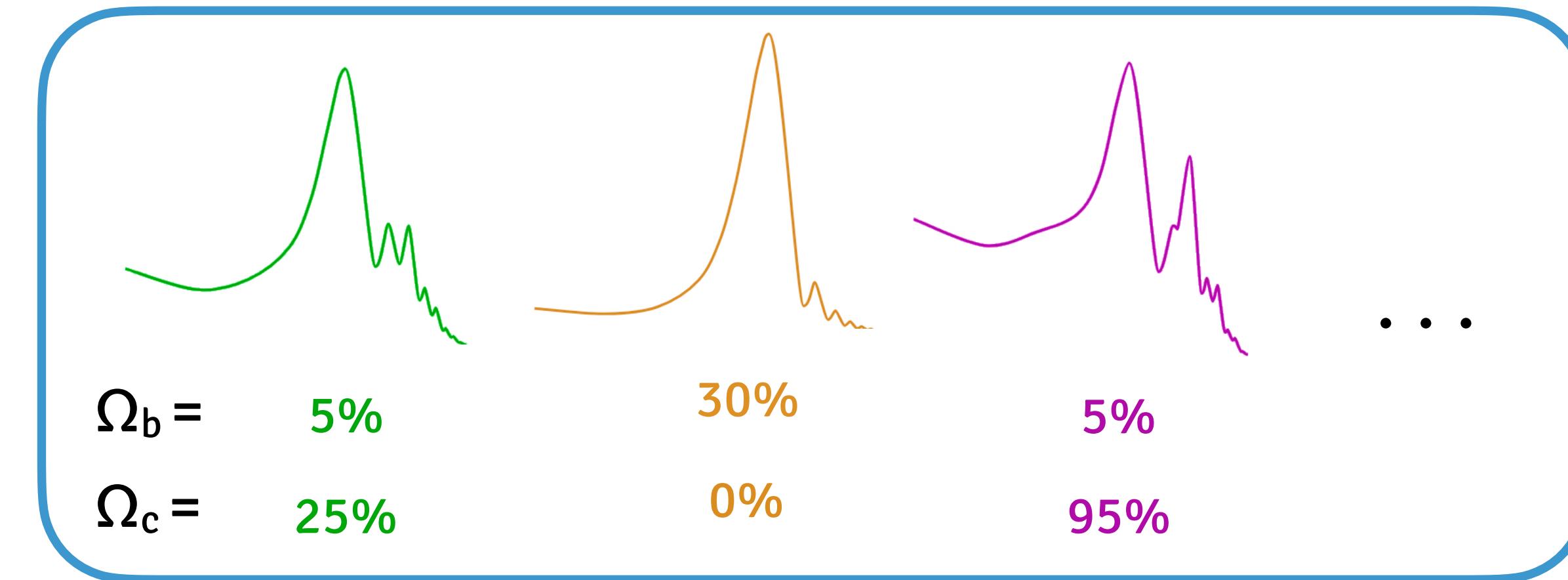
# Usual steps in SBI

I. **Simulation:** get  $N$  samples  $\{(\mathbf{x}^{(1)}, \boldsymbol{\theta}^{(1)}), (\mathbf{x}^{(2)}, \boldsymbol{\theta}^{(2)}), \dots, (\mathbf{x}^{(N)}, \boldsymbol{\theta}^{(N)})\}$

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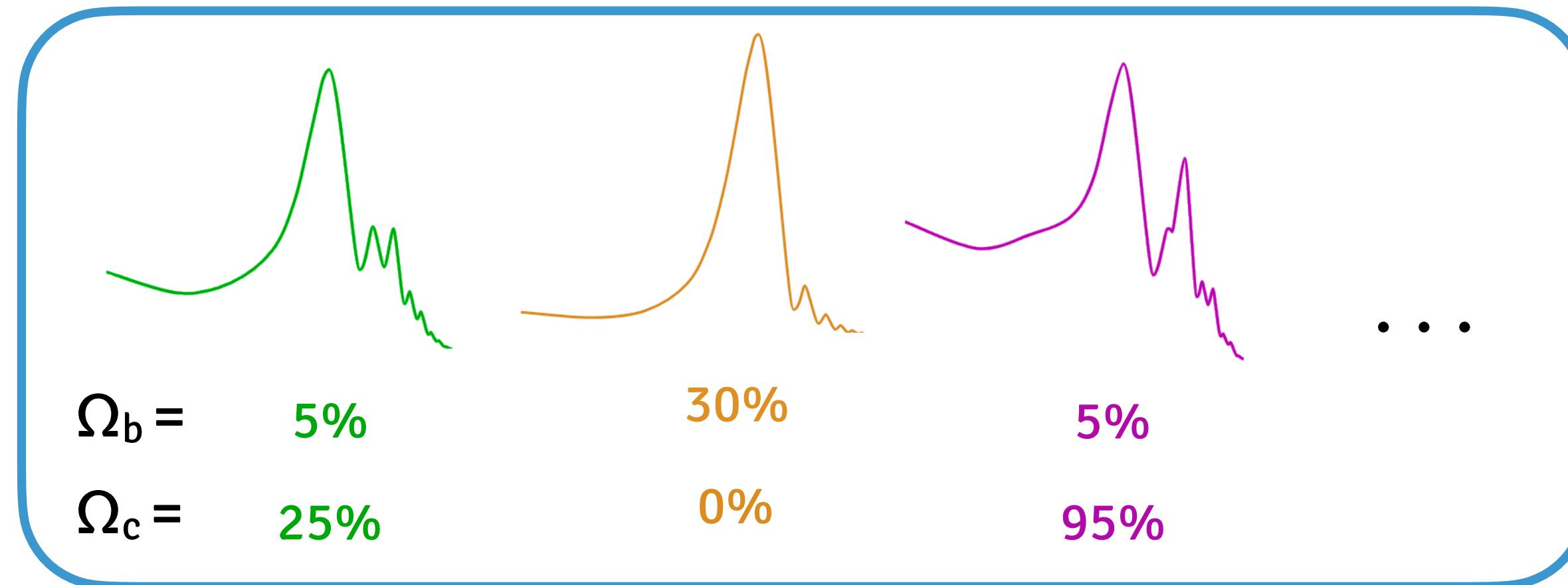
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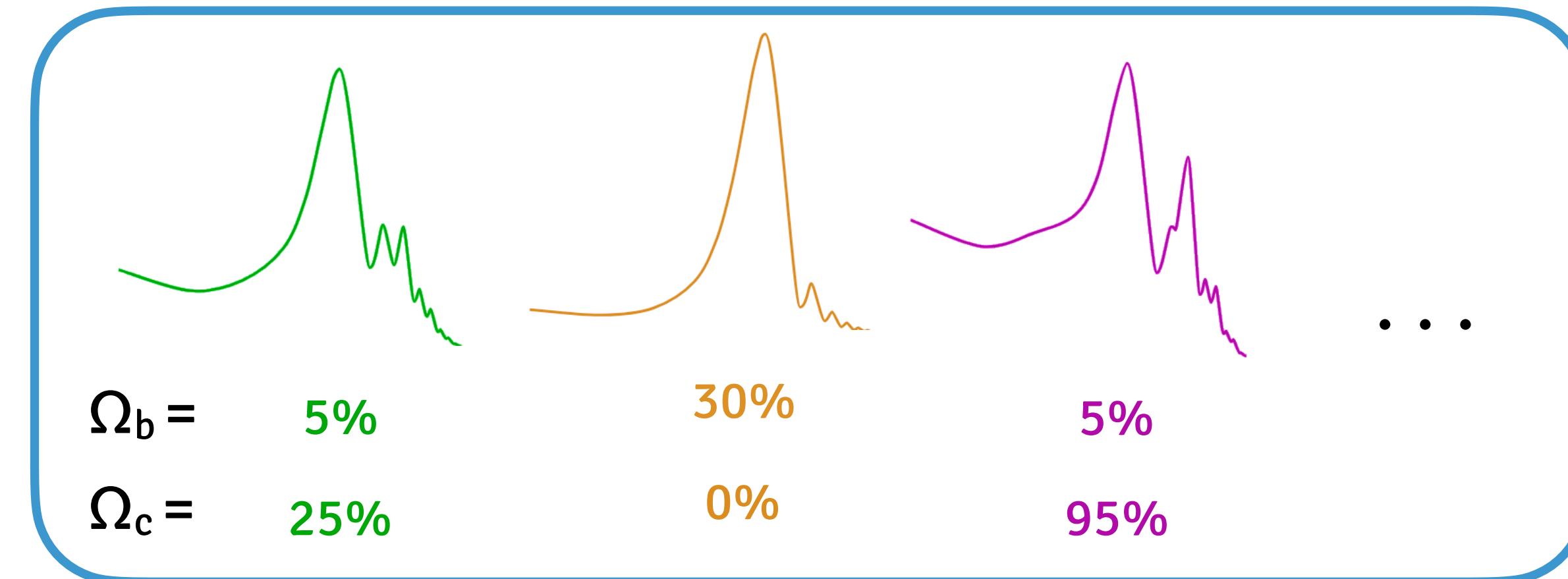


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II. **Training:** train a NN to learn posterior  $f_{\phi}(\boldsymbol{\theta}, \mathbf{x}) \simeq p(\boldsymbol{\theta} | \mathbf{x})$

III. **Inference:** evaluate trained network at  $\mathbf{x} = \mathbf{x}_0$  to get  $p(\boldsymbol{\theta} | \mathbf{x}_0)$

**Neural posterior estimation (NPE)**  $\longrightarrow p(\theta | \mathbf{x})$

SBI comes in many “flavors”:

**Neural likelihood estimation (NLE)**  $\longrightarrow p(\mathbf{x} | \theta)$

**Neural ratio estimation (NRE)**  $\longrightarrow p(\theta | \mathbf{x})/p(\theta)$

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Neural likelihood estimation (**NLE**)  $\rightarrow p(\mathbf{x} | \theta)$

Neural ratio estimation (**NRE**)  $\rightarrow p(\theta | \mathbf{x})/p(\theta)$

We focus on a recent algorithm:

**MNRE = Marginal Neural Ratio Estimation**

Implemented in [Swyft](#) [Miller et al. 2011.13951]

## Neural Ratio Estimation

$$\frac{p(\mathbf{x}, \theta)}{p(\mathbf{x})p(\theta)} = \frac{p(\theta | \mathbf{x})}{p(\theta)}$$

**MNRE**

**in a nutshell**

Train NNs to solve a **binary classification problem**:

$$(\mathbf{x}, \theta) \sim p(\mathbf{x}, \theta)$$

$$\begin{aligned}\Omega_b &= 5\% \\ \Omega_c &= 25\%\end{aligned}$$

$$\begin{aligned}30\% \\ 0\%\end{aligned}$$

$$\begin{aligned}5\% \\ 95\%\end{aligned}$$

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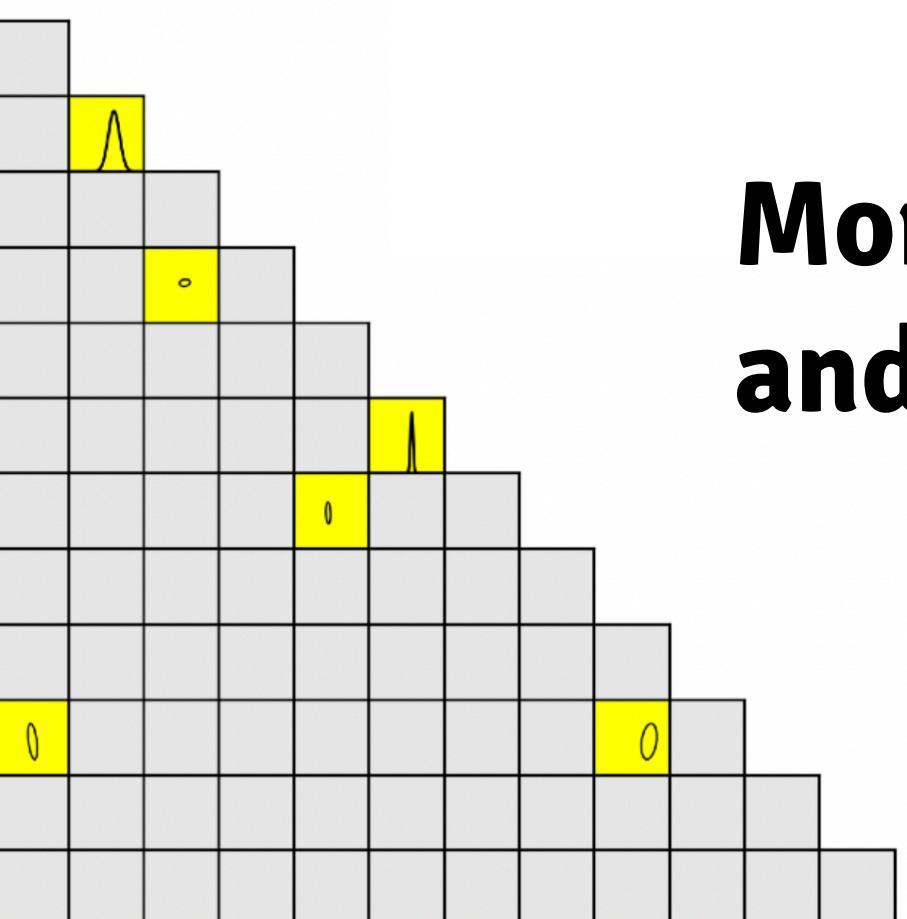
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**Focus on marginals**

Instead of estimating all parameters, **cherry-pick** the ones we care about



**More flexible  
and efficient!**

SBI has already been applied to different LSS surveys:

 **BOSS** [Lemos et al. 2310.15256]

 **DES** [Jeffrey et al. 2403.02314]

 **KiDS** [von Wietersheim-Kramsta et al. 2404.15402]

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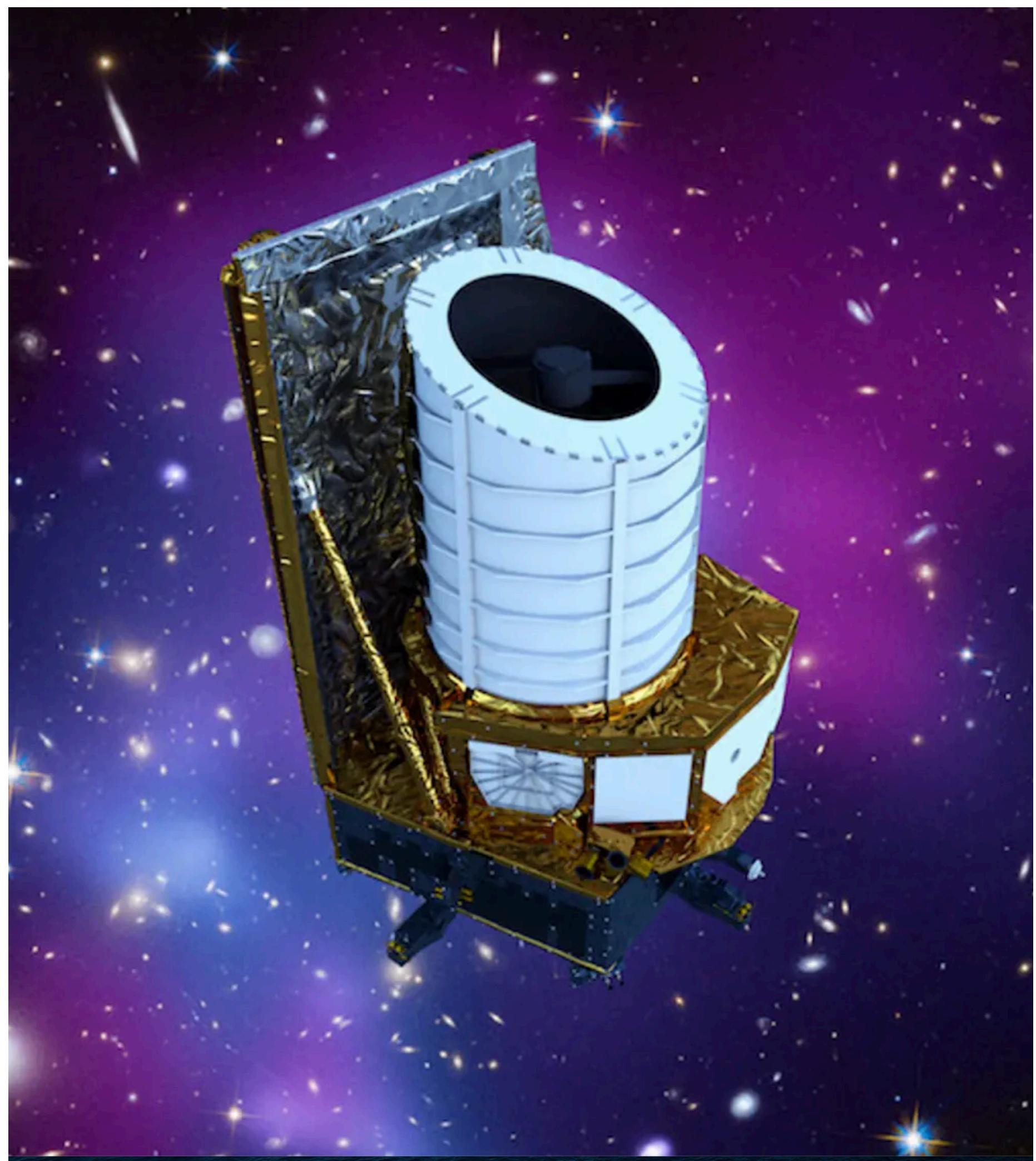
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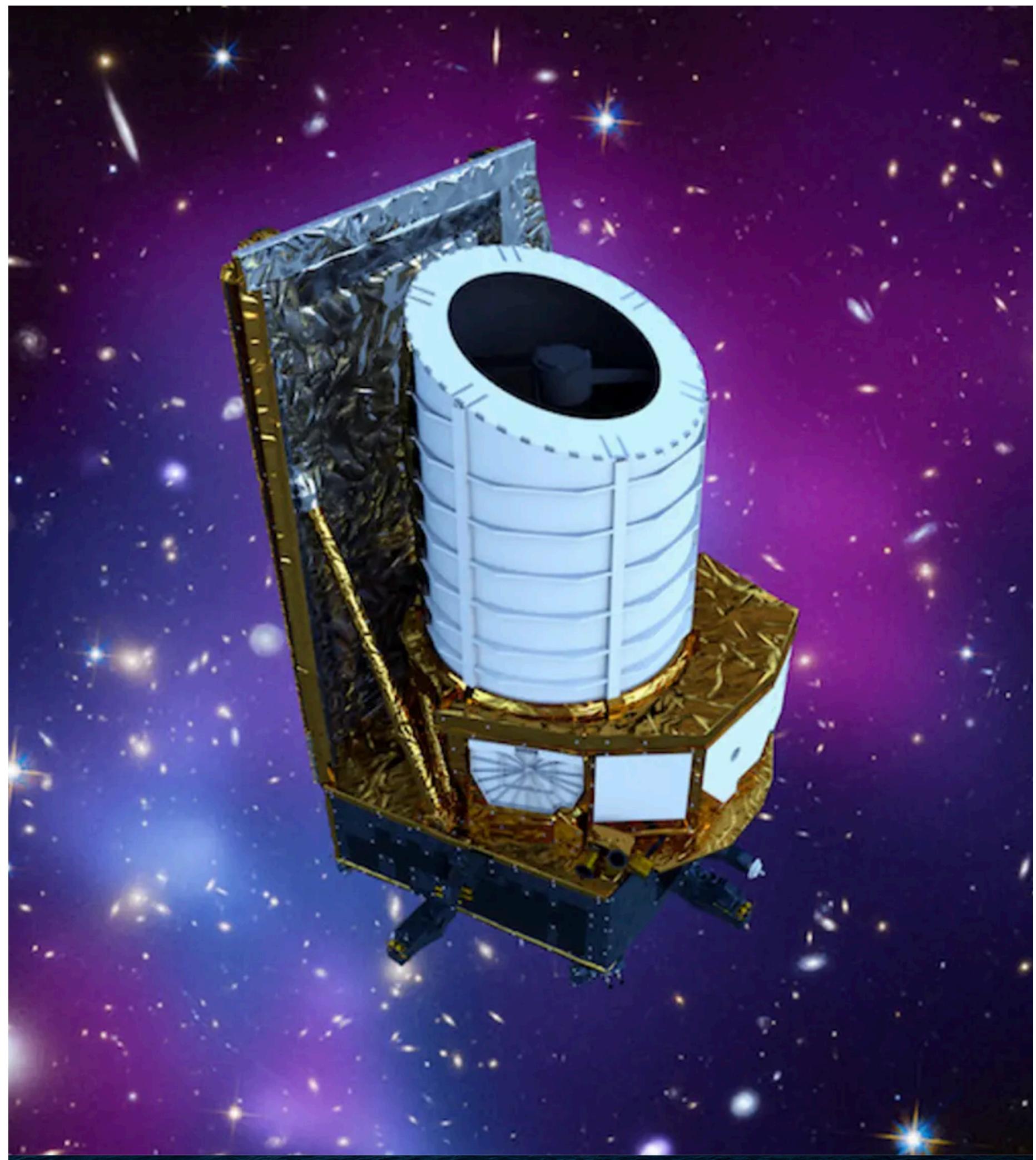
**Our goal:** apply MNRE to **Euclid** photometric observables

[ESA's Euclid space satellite]



On July 1<sup>st</sup> 2023, Euclid was launched to L2

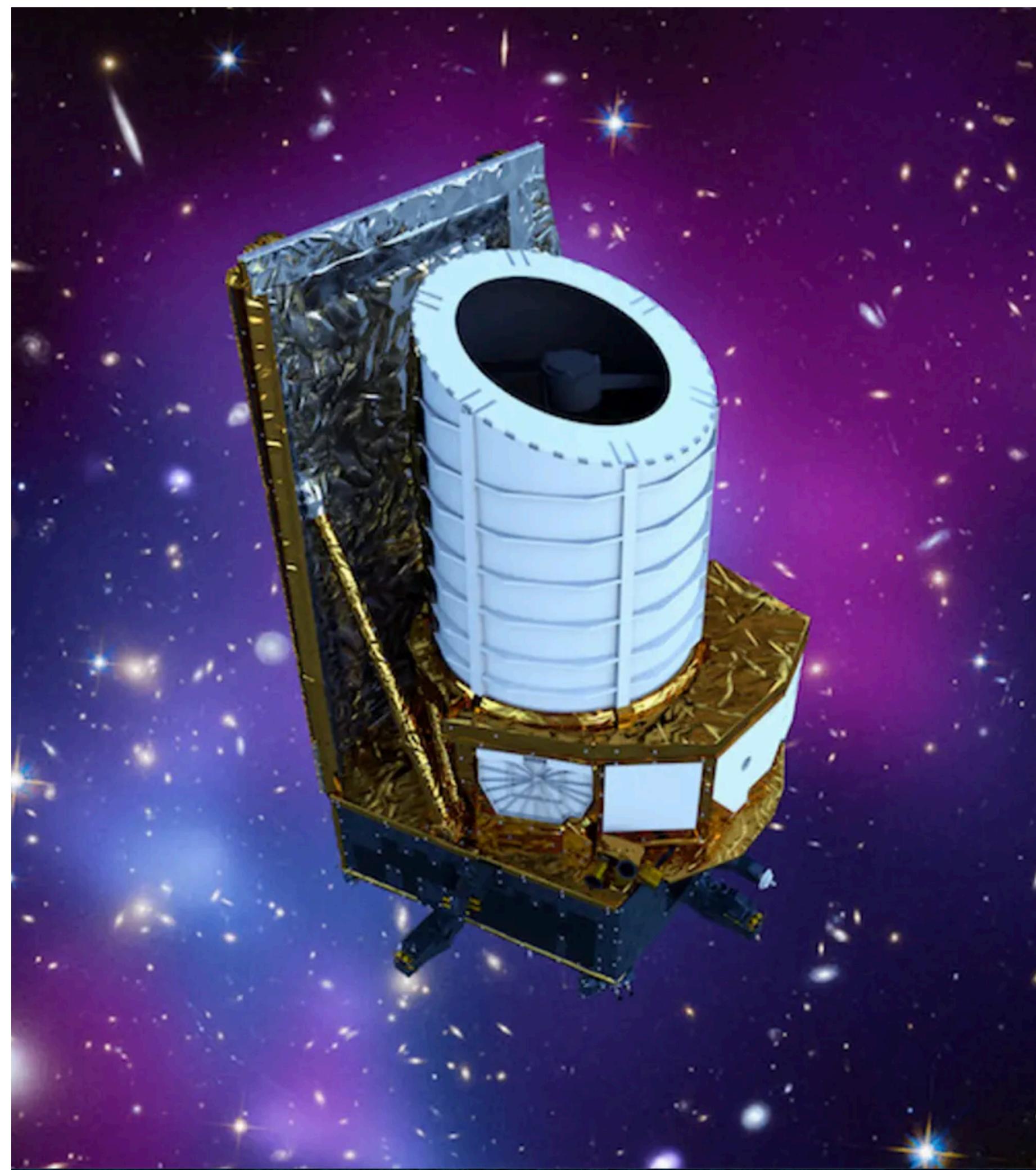
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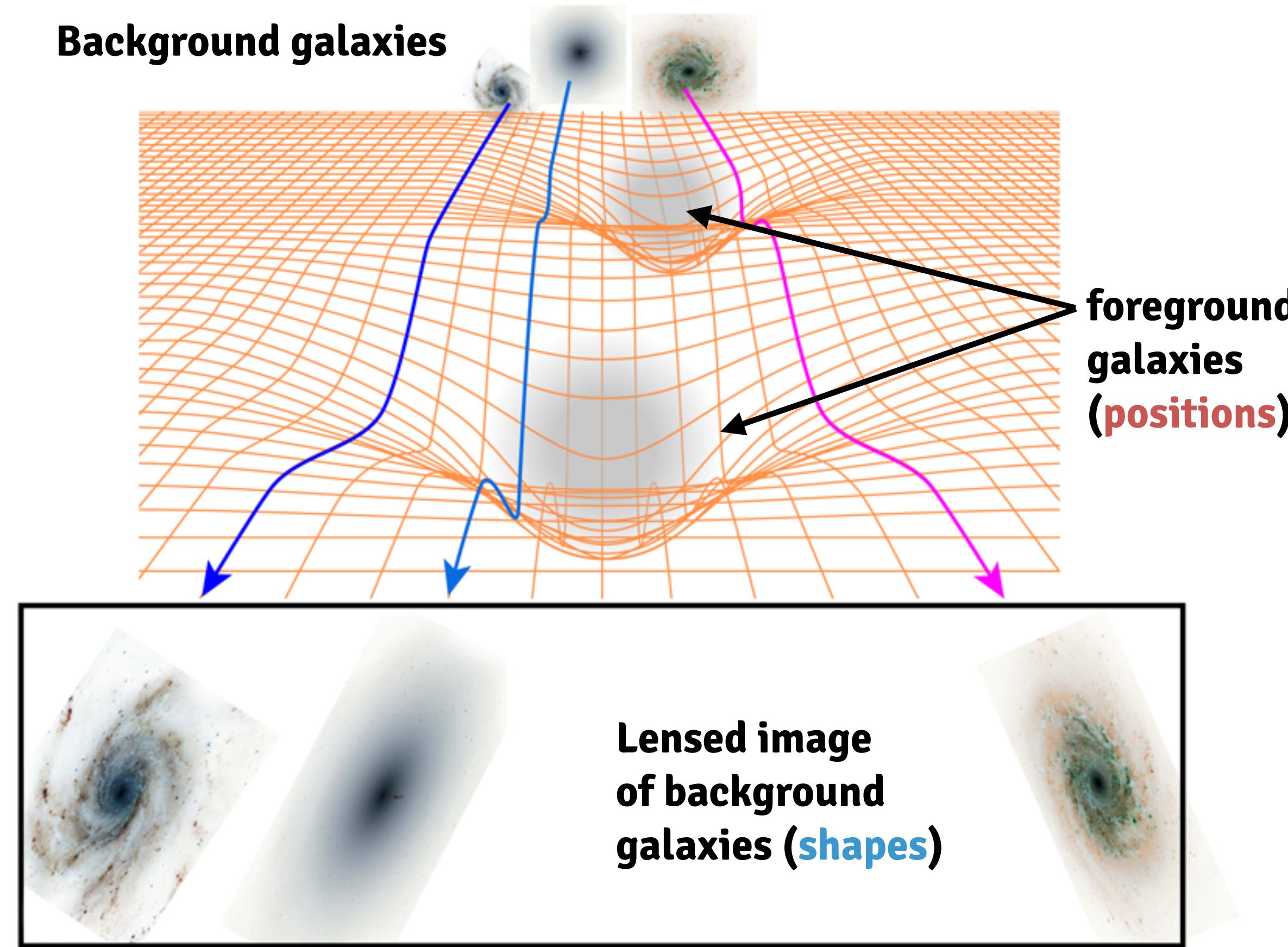


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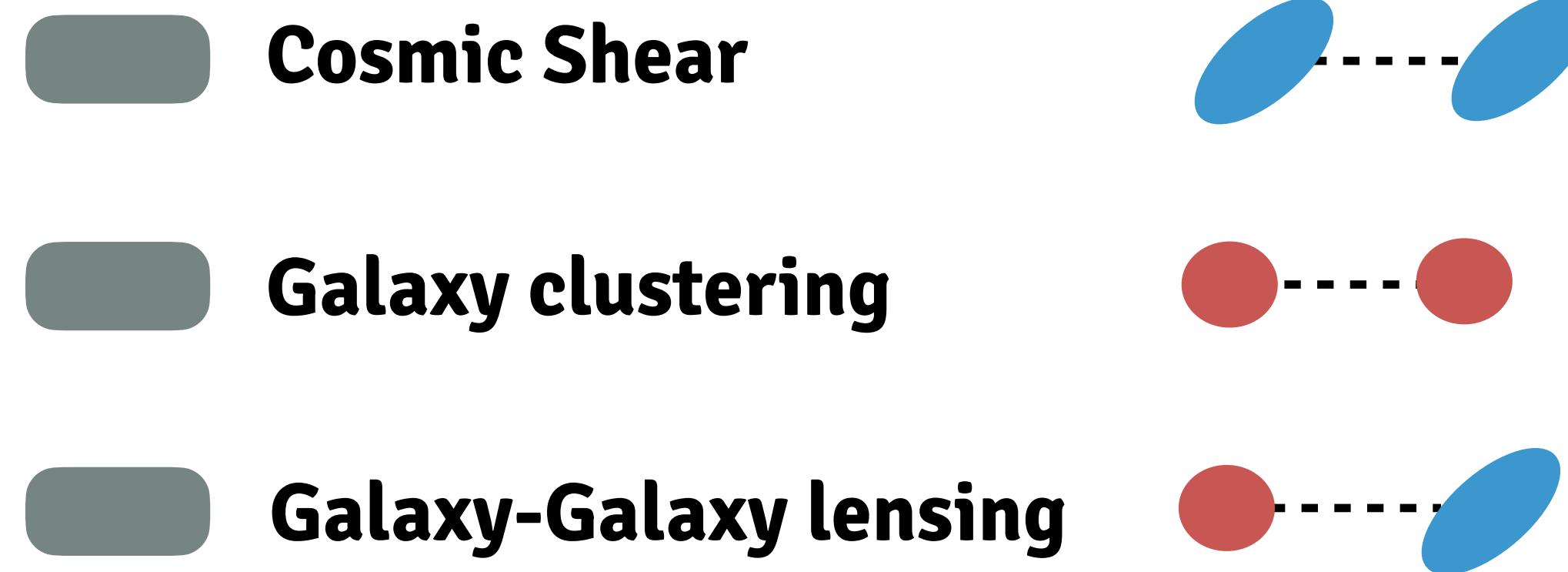
First public data release expected in 2026

# Which are the Euclid primary observables?



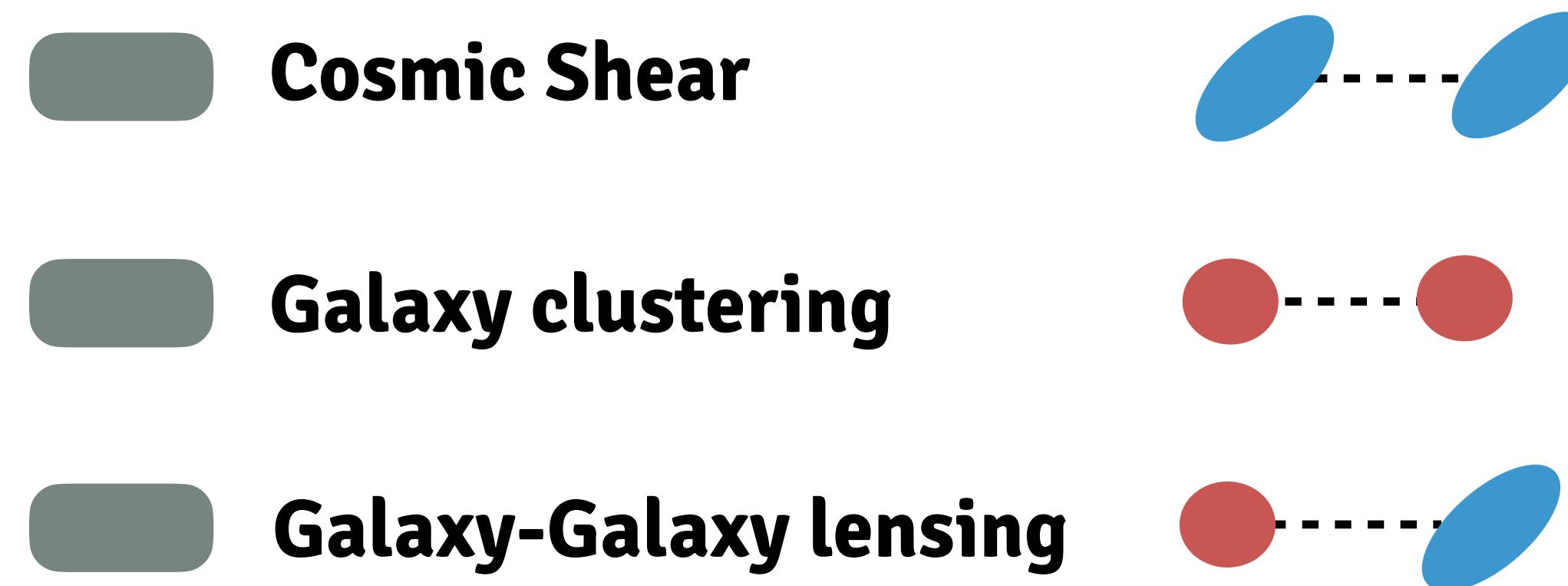
# 3x2pt photometric probes

Summarise maps of galaxy **positions/shapes** using three 2-point statistics (**3x2pt**) measured at 10 tomographic redshift bins



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Summarise maps of galaxy **positions/shapes** using three 2-point statistics (**3x2pt**) measured at **10 tomographic redshift bins**



...described by angular **power spectra**  $C_{ij}^{XY}(\ell) = \int dz W_i^X(z) W_j^Y(z) P_m(k_\ell, z)$

# Swyft analysis of Euclid 3x2pt

## 1. Simulator:

We generate **50k realisations** of  
3x2pt spectra with gaussian noise

$$\hat{C}_{ij}^{AB}(\ell) = C_{ij}^{AB}(\ell) + n_{ij}^{AB}(\ell)$$

$\mathcal{N}(0, \mathbf{C})$

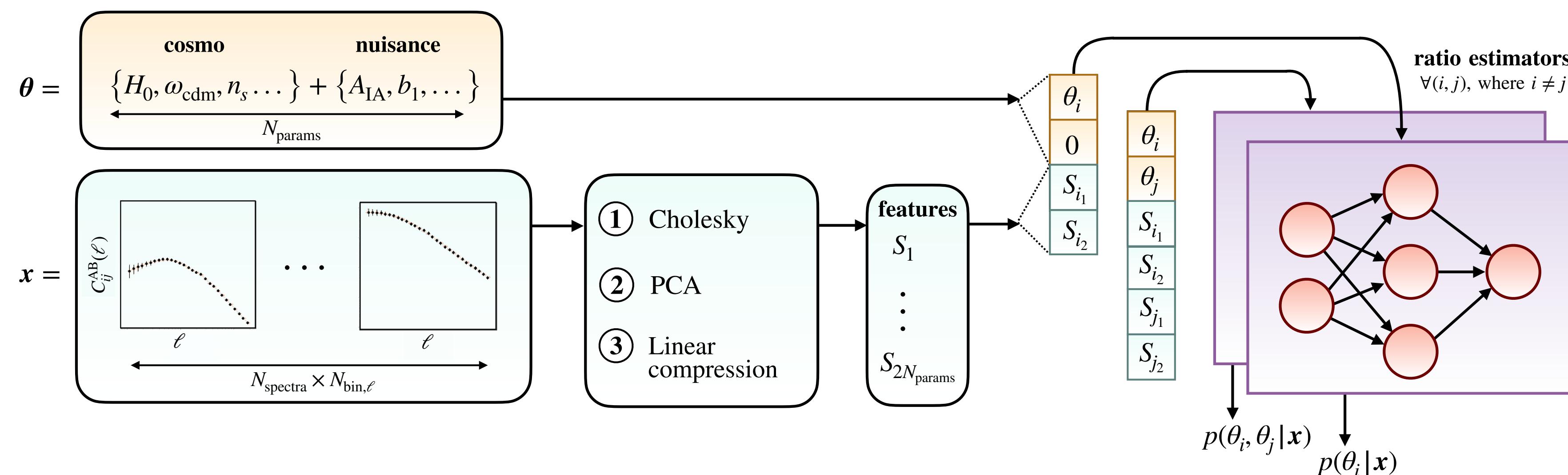
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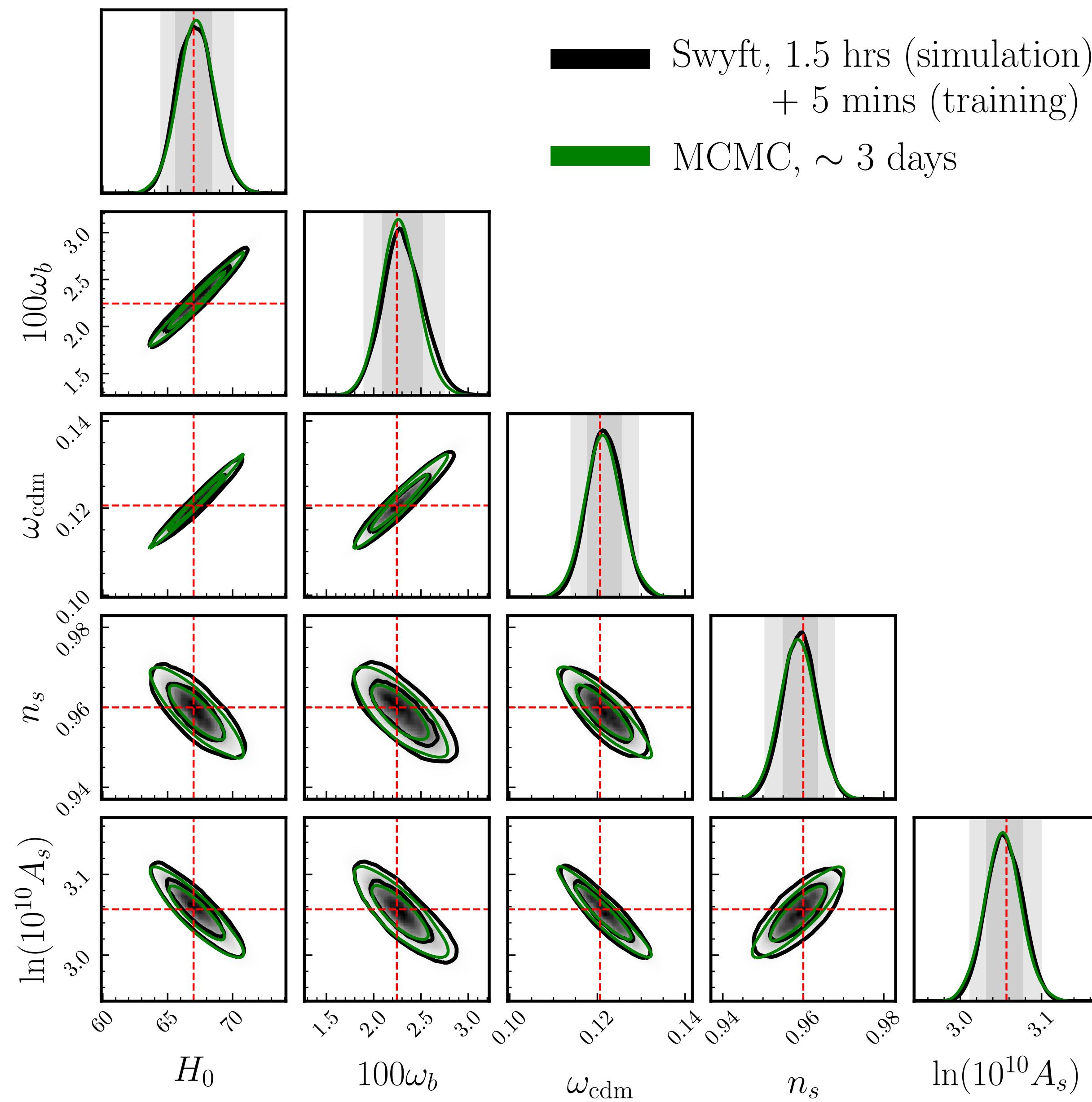
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$$\hat{C}_{ij}^{AB}(\ell) = C_{ij}^{AB}(\ell) + n_{ij}^{AB}(\ell) \sim \mathcal{N}(0, \mathbf{C})$$

## 2. Network: We pre-compress spectra into features

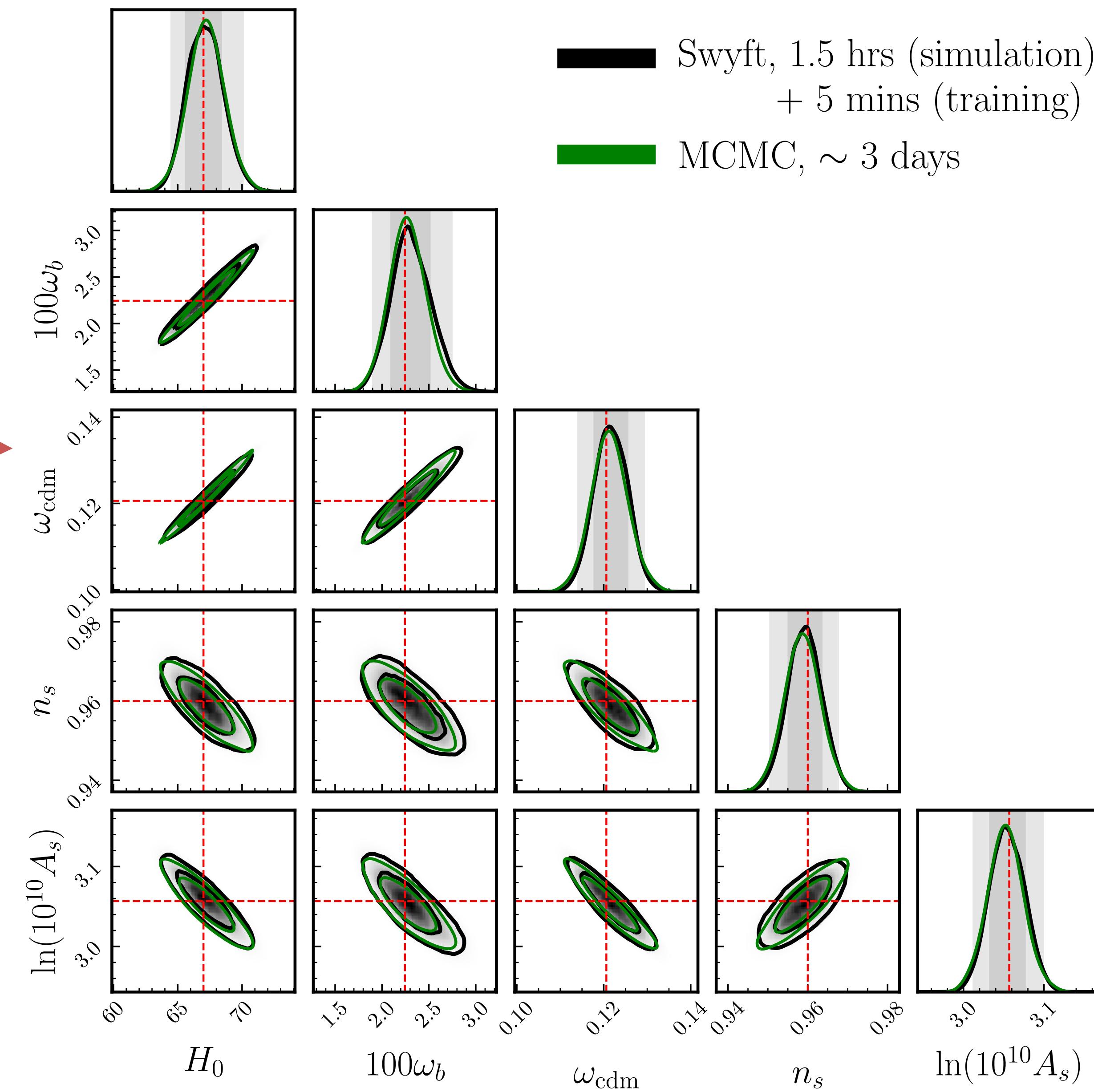


# Forecast $\Lambda$ CDM posteriors



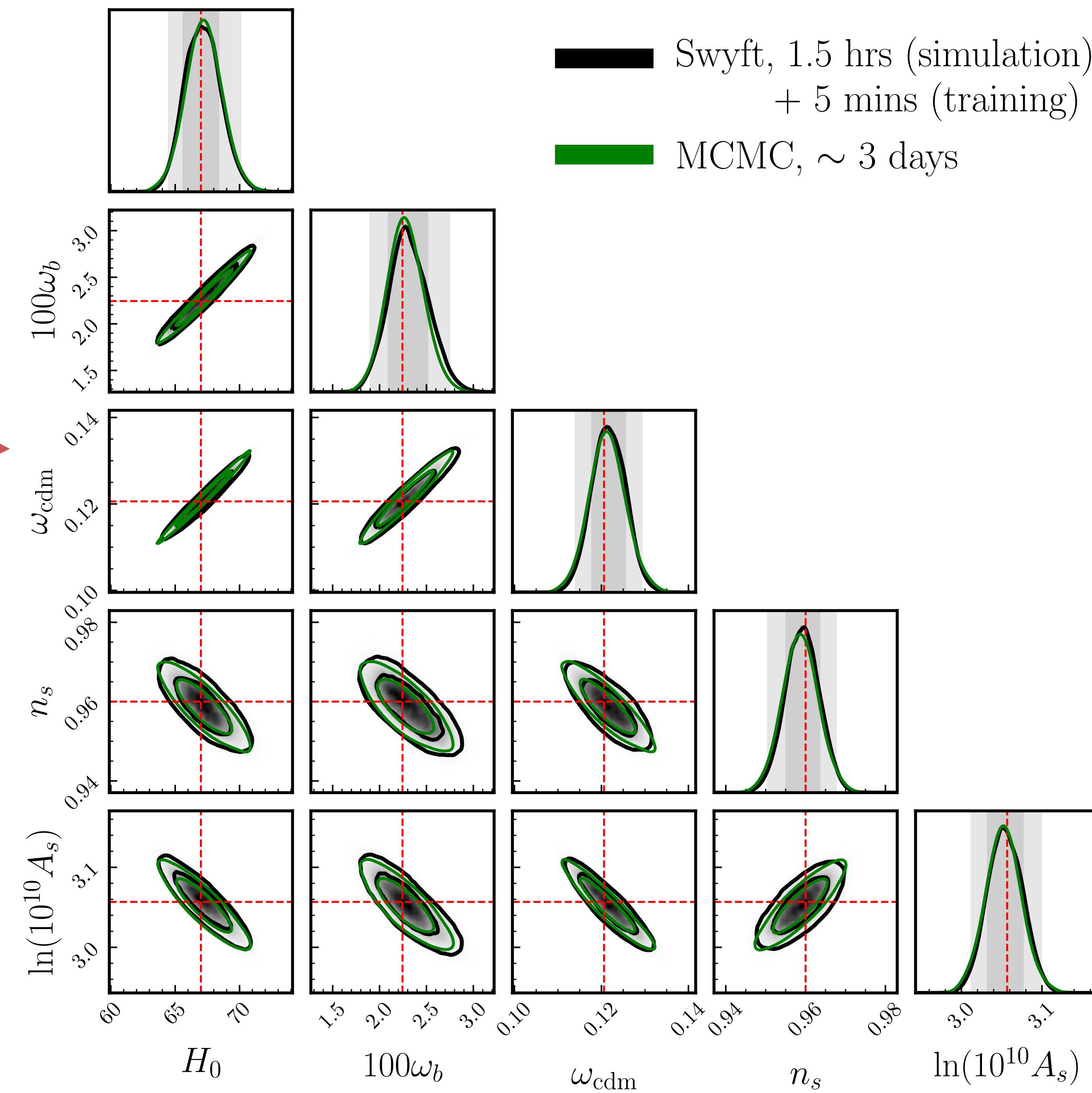
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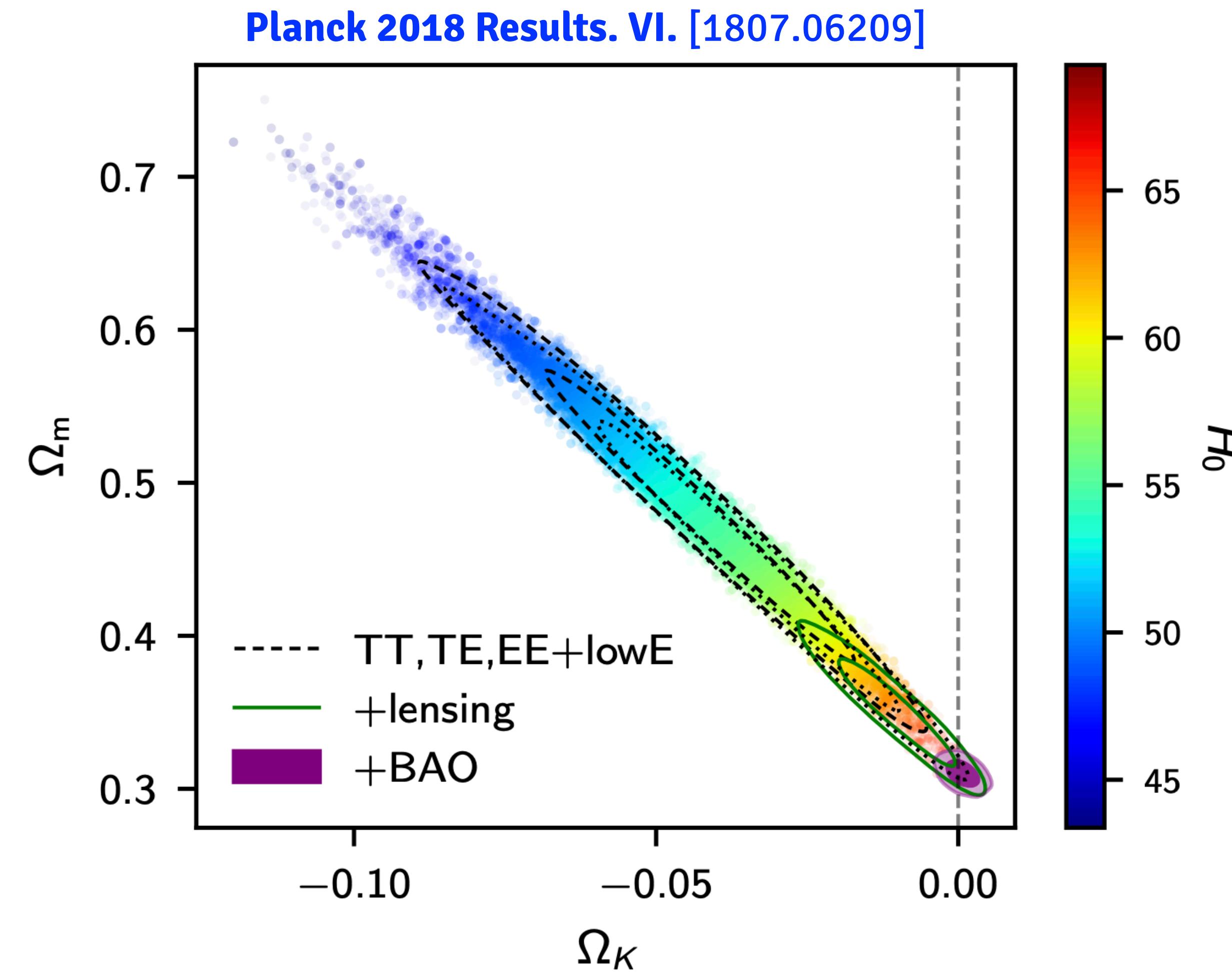
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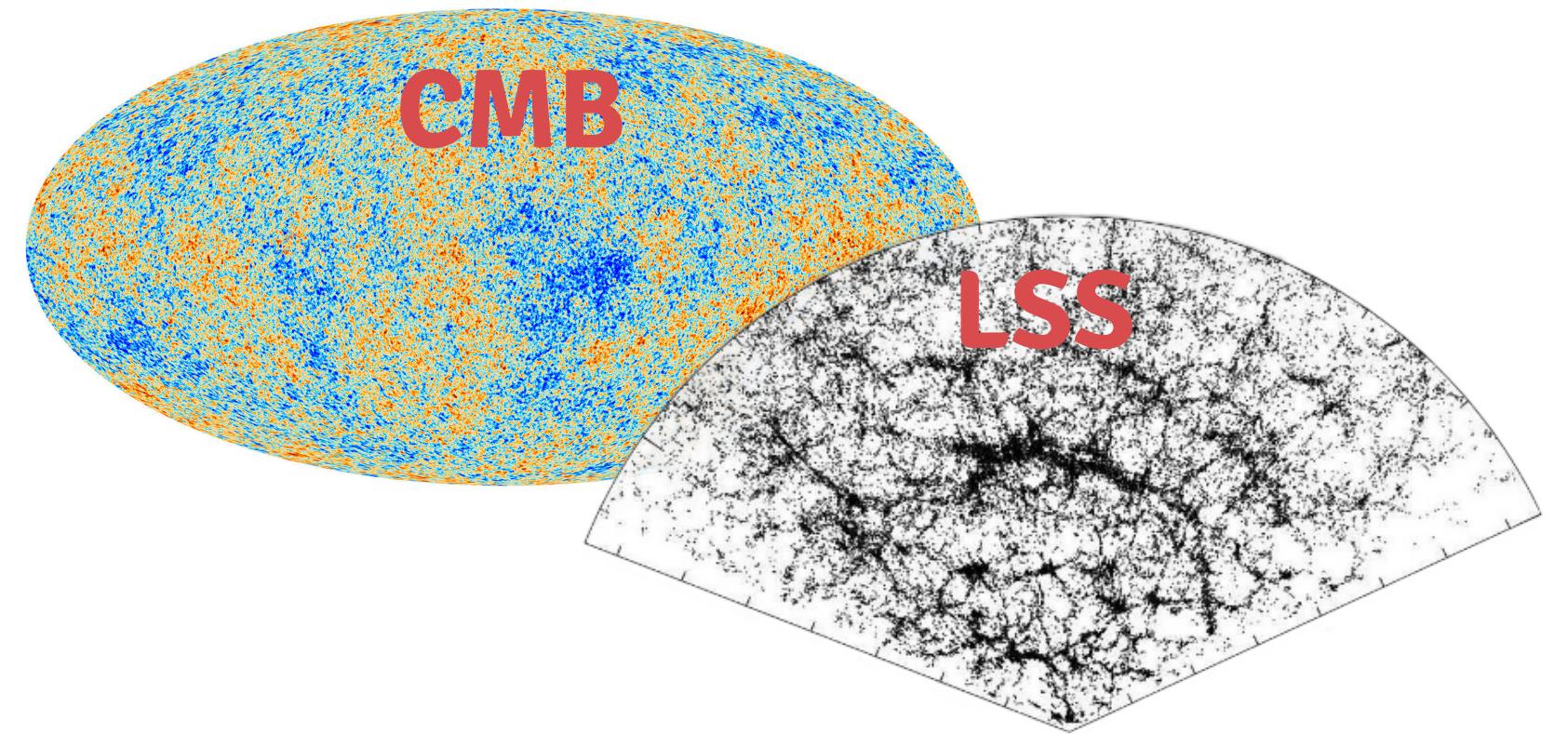
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**Canonical example:**

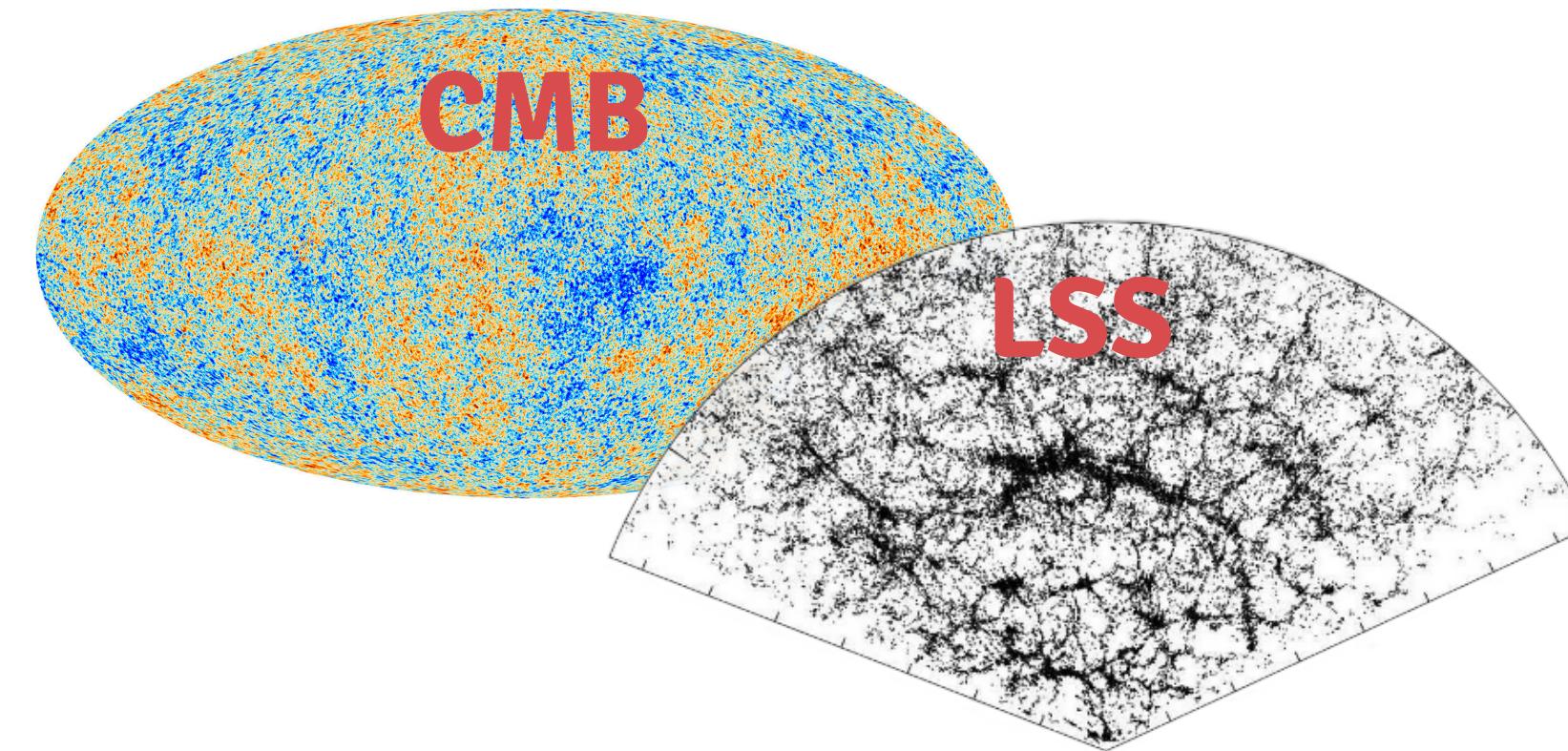


# Joint analyses of CMB & LSS



Very complementary  
(high- $z$  vs. low- $z$ , linear vs. non-linear)

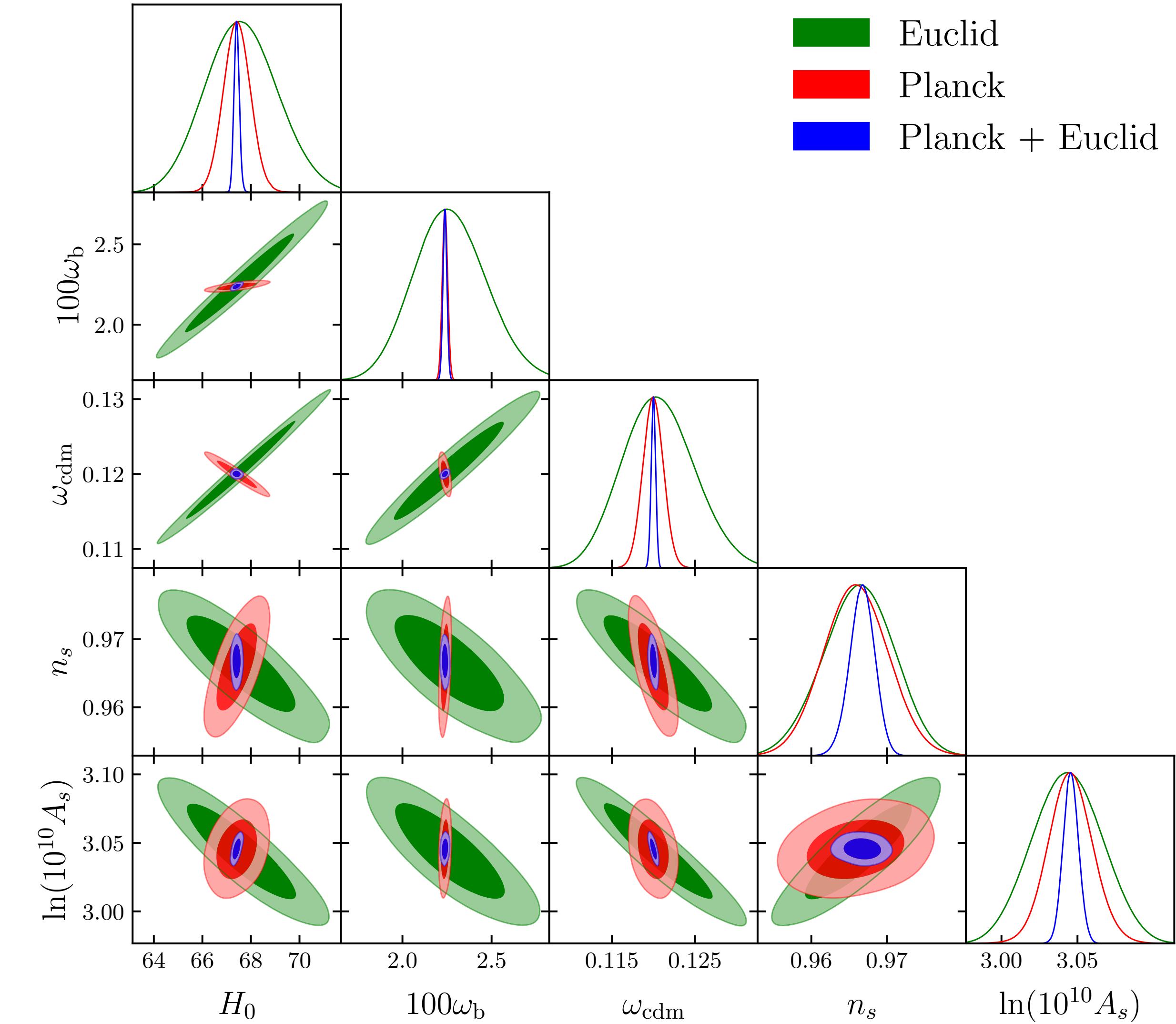
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Break parameter degeneracies



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## Can we do CMB+LSS analyses in SBI?

Unfortunately, building a realistic Planck simulator seems very challenging

**BUT** we can easily build an “effective”  
simulator using posterior samples  
from a previous MCMC run

$$a = \theta - \theta'$$

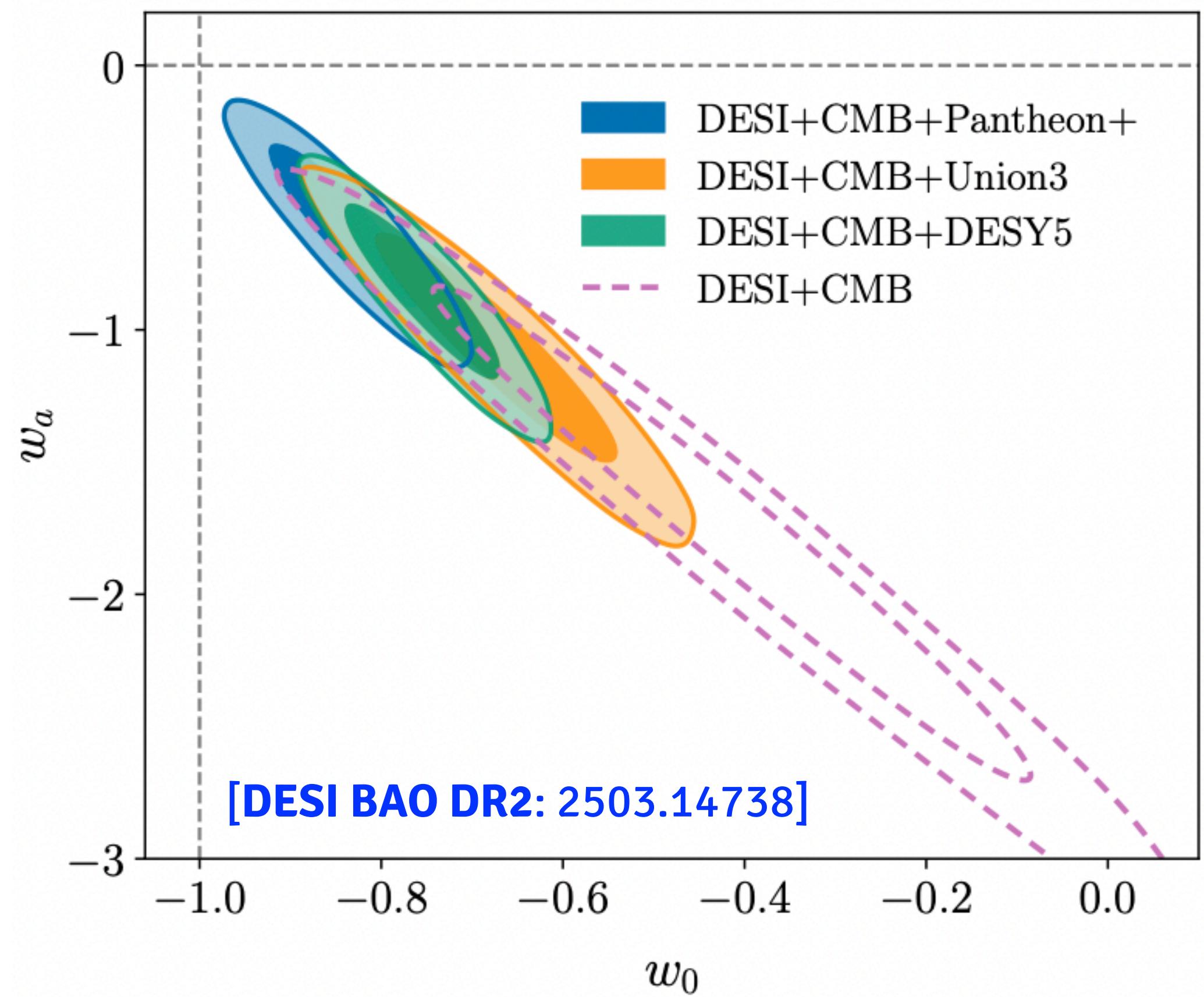
↑                      ↑

prior samples      posterior samples

$$f_\phi(\theta | a = 0) \simeq p(\theta | \mathbf{x}_0)$$

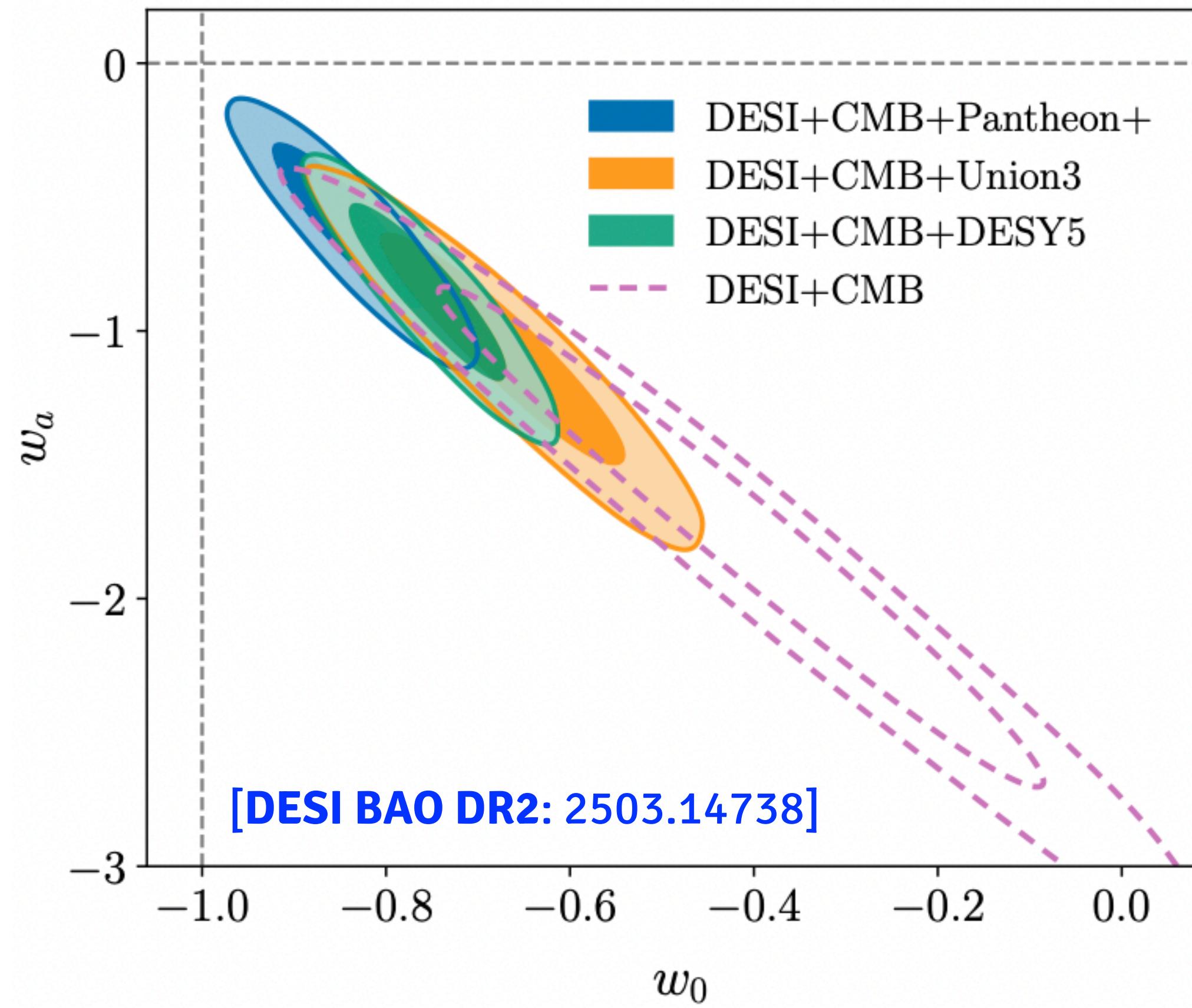
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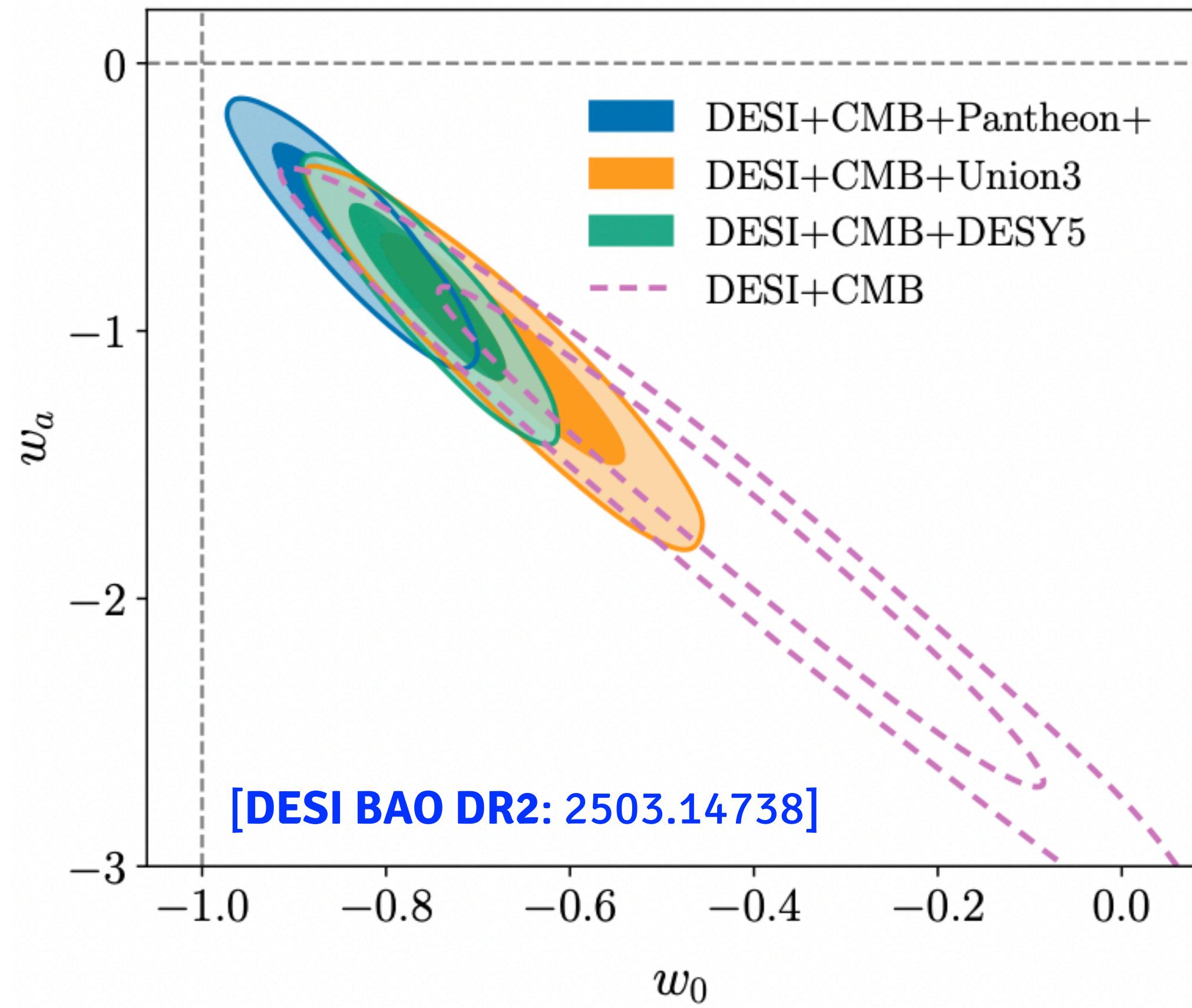
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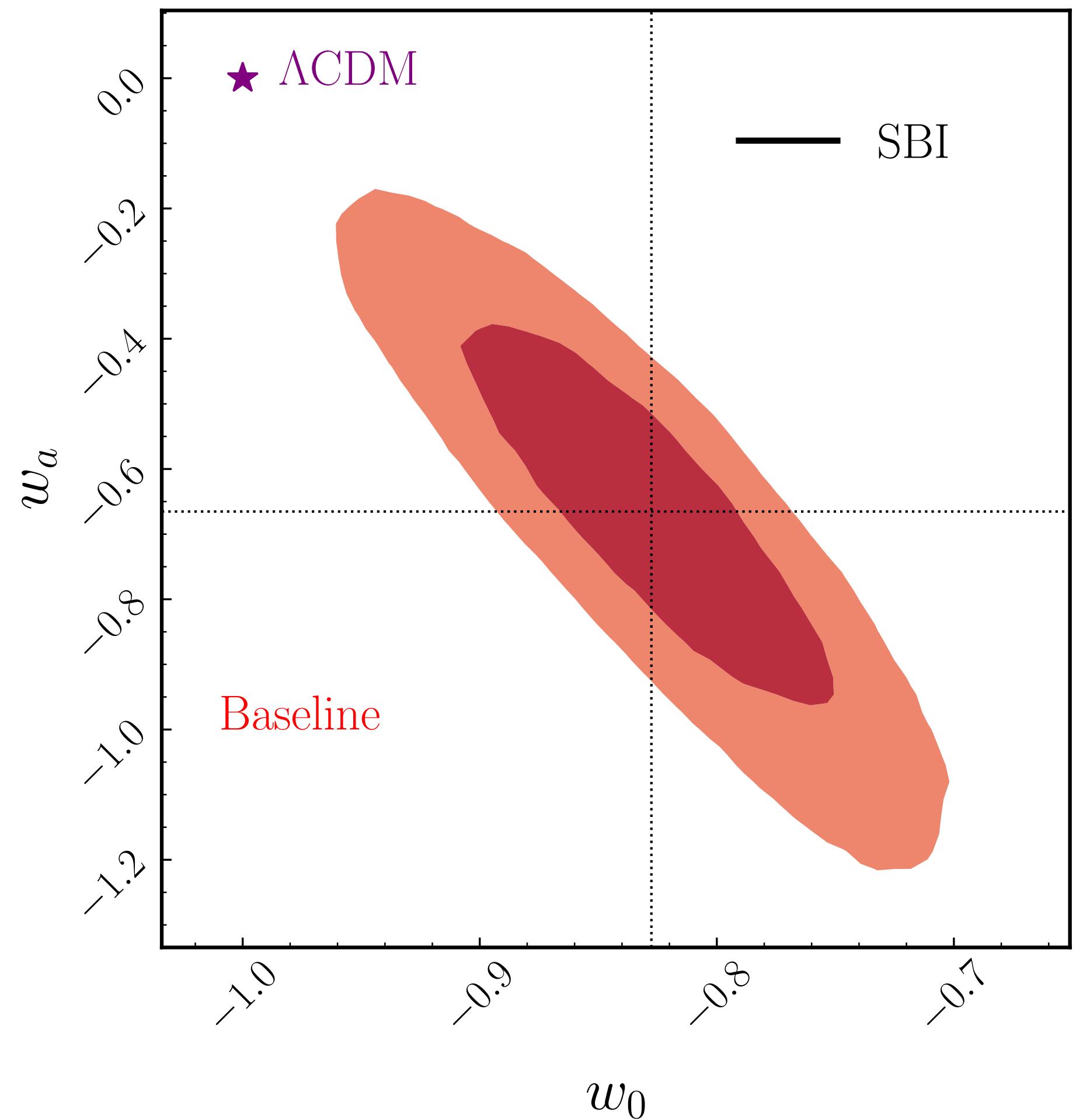
What can Euclid data (and its combination with current probes) tell us about this?



Perform forecast assuming the bestfit  $w_0 w_a$ CDM model hinted by DESI + CMB + Pantheon+

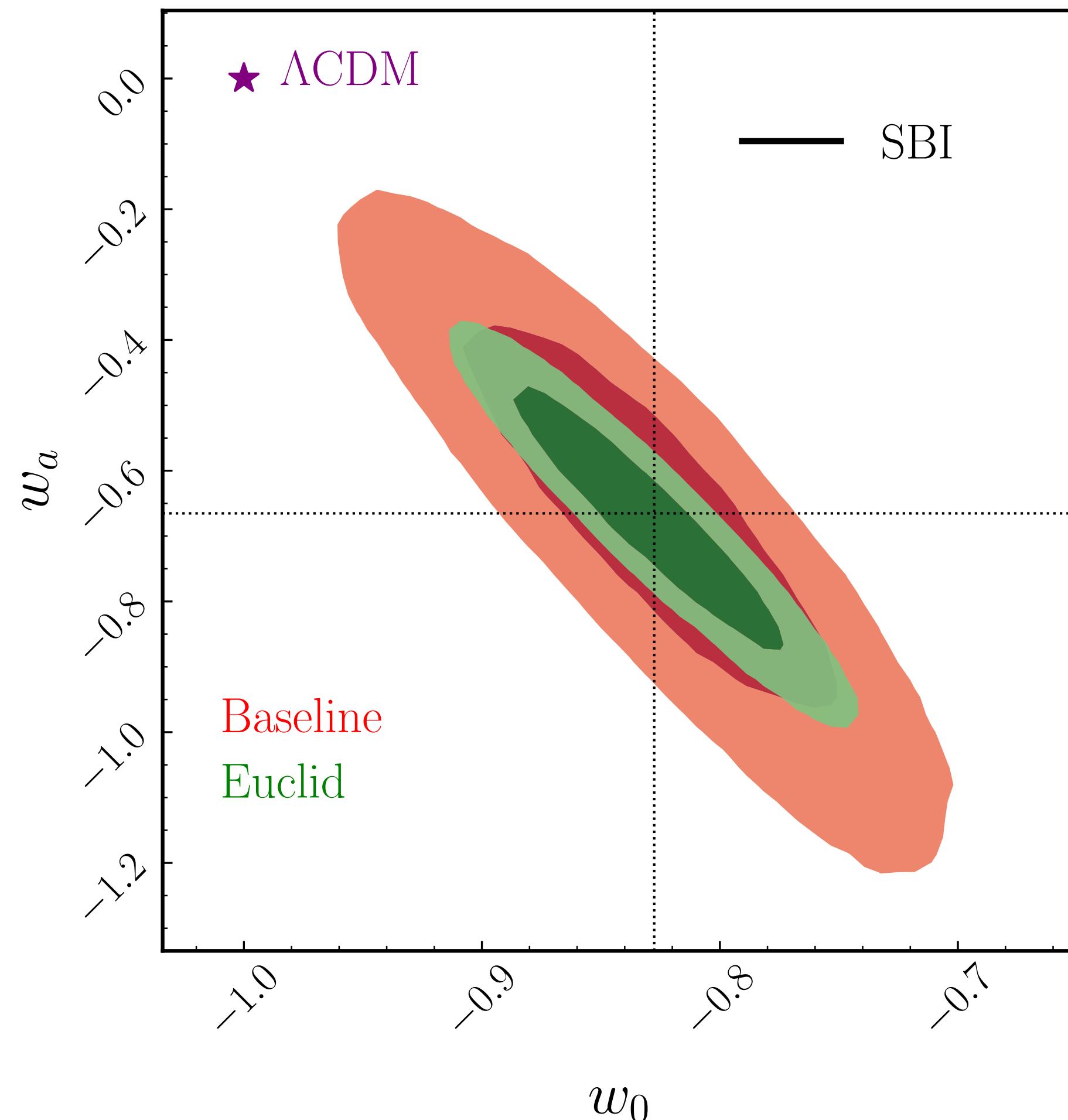
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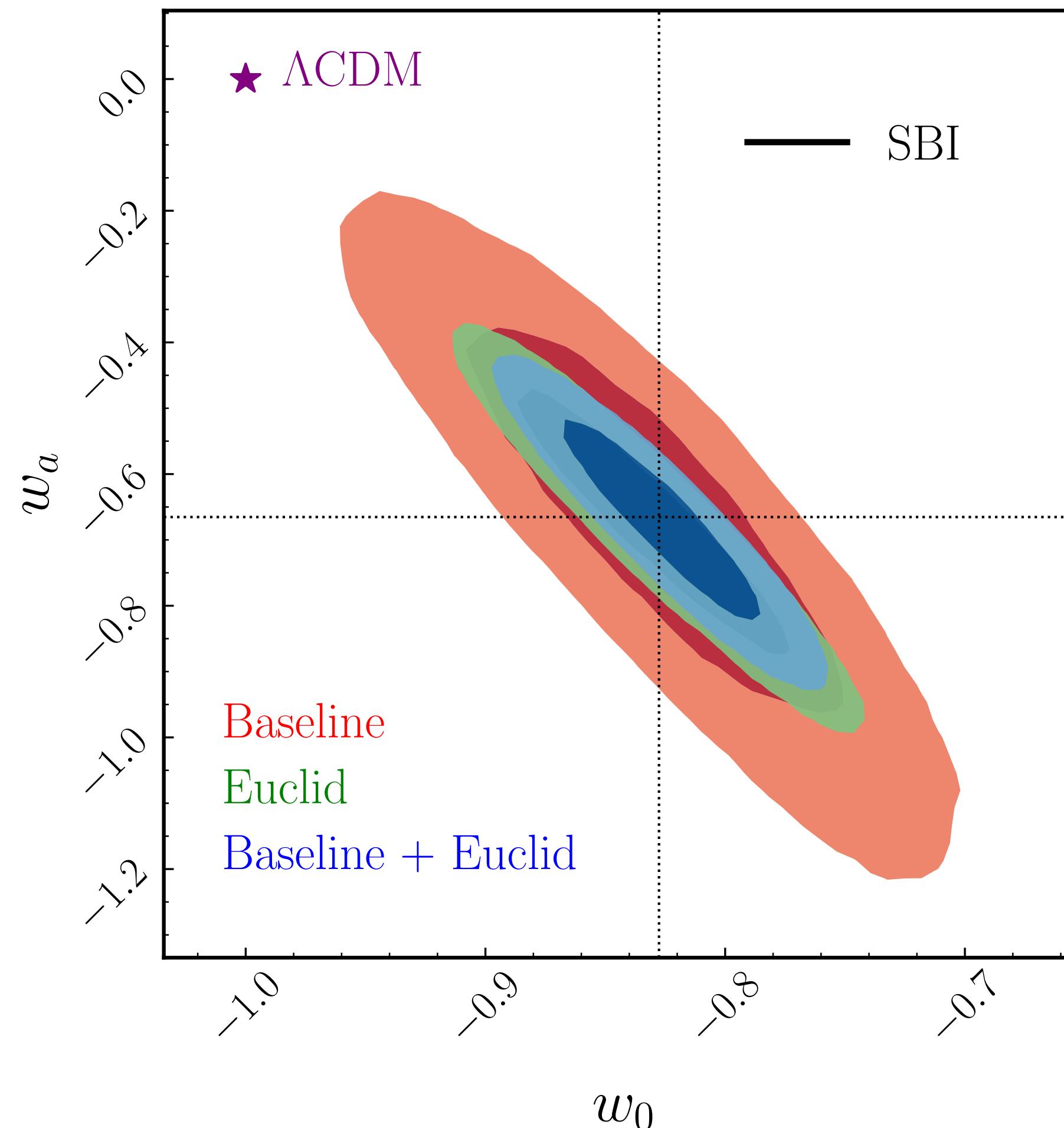
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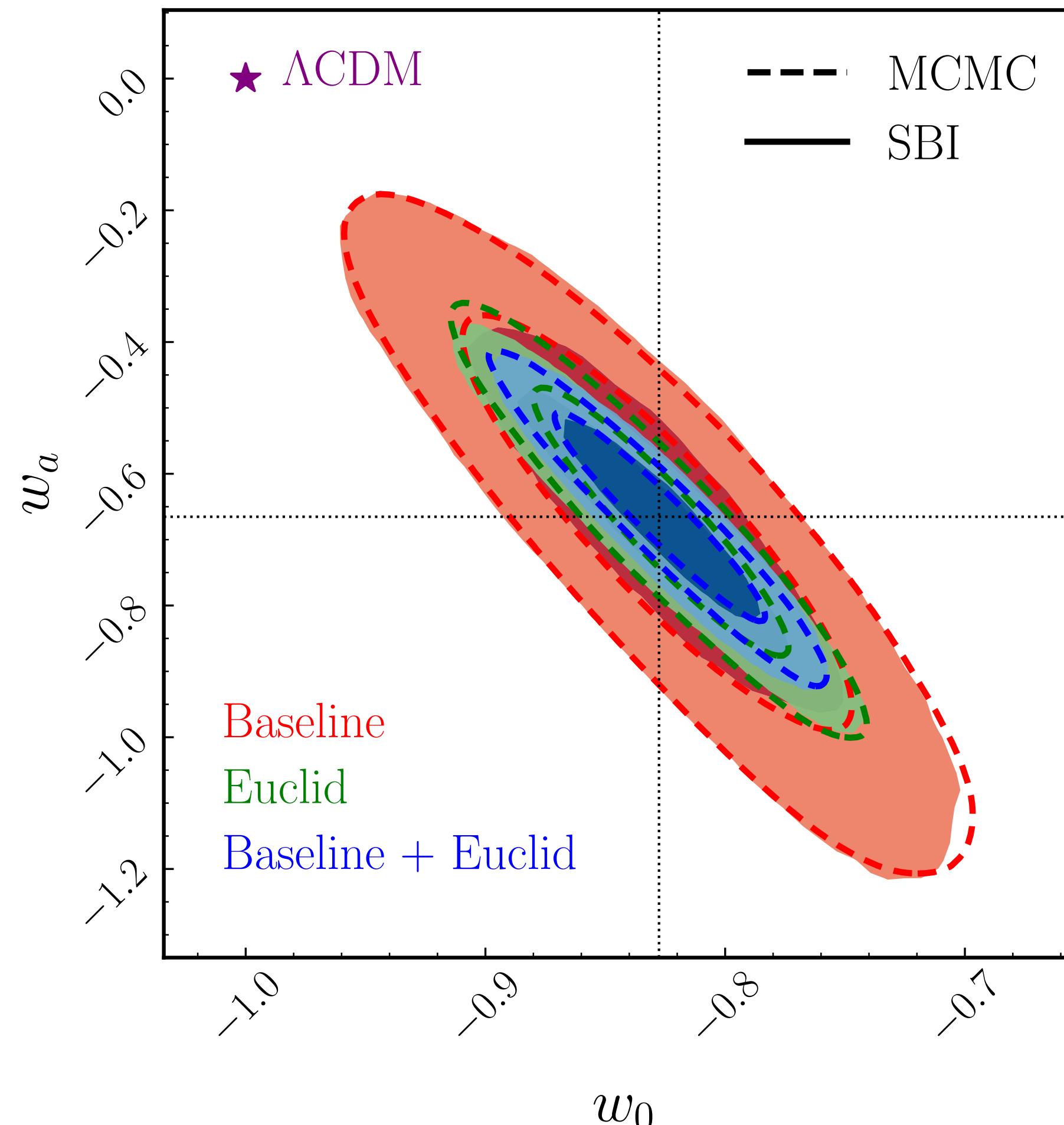


Euclid alone could detect the fiducial  $w_0w_a$ CDM model at the  $\sim 5\sigma$  level

The combination with Planck+DESI data would rise the detection to  $\sim 7\sigma$

# Forecast $w_0w_a$ CDM posteriors

Baseline = DESI + Planck + Pantheon+



SBI is in good agreement with MCMC,  
while requiring only  $\sim 3\%$  of the number  
of model evaluations used by MCMC

# Conclusions

- Modern **deep learning** techniques will be key to learn as much as we can about the dark sector and neutrinos from future data
- Emulators achieve **ultra-fast** model evaluations → applied to **decaying neutrino** models, these can relax current mass bounds up to  $\sum m_\nu < 0.24 \text{ eV}$
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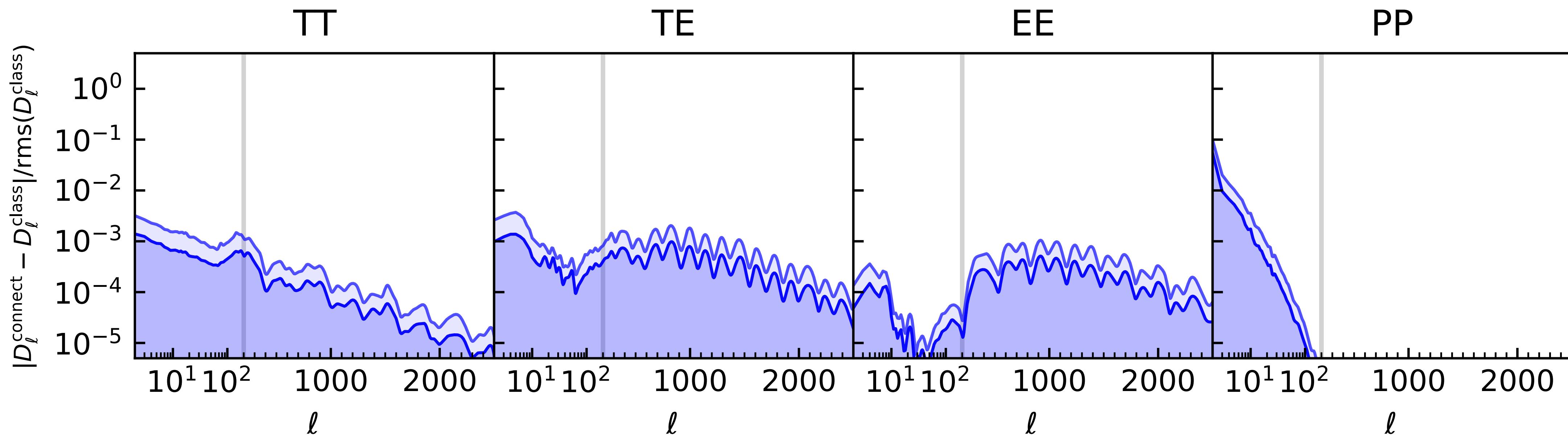
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**THANK YOU!**

[g.francoabellan@uva.nl](mailto:g.francoabellan@uva.nl)

# **BACK-UP**

# Errors in emulated CMB spectra for neutrino decays



The  $1\sigma$  and  $2\sigma$  percentile errors in the CMB spectra (from the test set) are almost always below 1%

**Strategy:** train a neural network  $d_\phi(\mathbf{x}, \theta) \in [0,1]$  as a binary classifier,  
so that

$$d_\phi(\mathbf{x}, \theta) \simeq 1 \quad \text{if} \quad (\mathbf{x}, \theta) \sim p(\mathbf{x}, \theta) = p(\mathbf{x} | \theta)p(\theta)$$

$$d_\phi(\mathbf{x}, \theta) \simeq 0 \quad \text{if} \quad (\mathbf{x}, \theta) \sim p(\mathbf{x})p(\theta)$$

**Note:**  $\Phi$  denotes all the network parameters

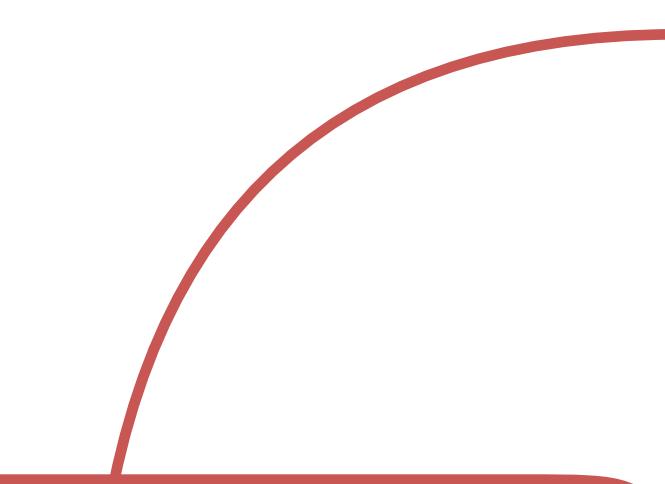
We have to **minimise a loss function** w.r.t. the network params.  $\Phi$

$$L[d_\phi(\mathbf{x}, \boldsymbol{\theta})] = - \int d\mathbf{x} d\boldsymbol{\theta} \left[ p(\mathbf{x}, \boldsymbol{\theta}) \ln(d_\phi(\mathbf{x}, \boldsymbol{\theta})) + p(\mathbf{x}) p(\boldsymbol{\theta}) \ln(1 - d_\phi(\mathbf{x}, \boldsymbol{\theta})) \right]$$

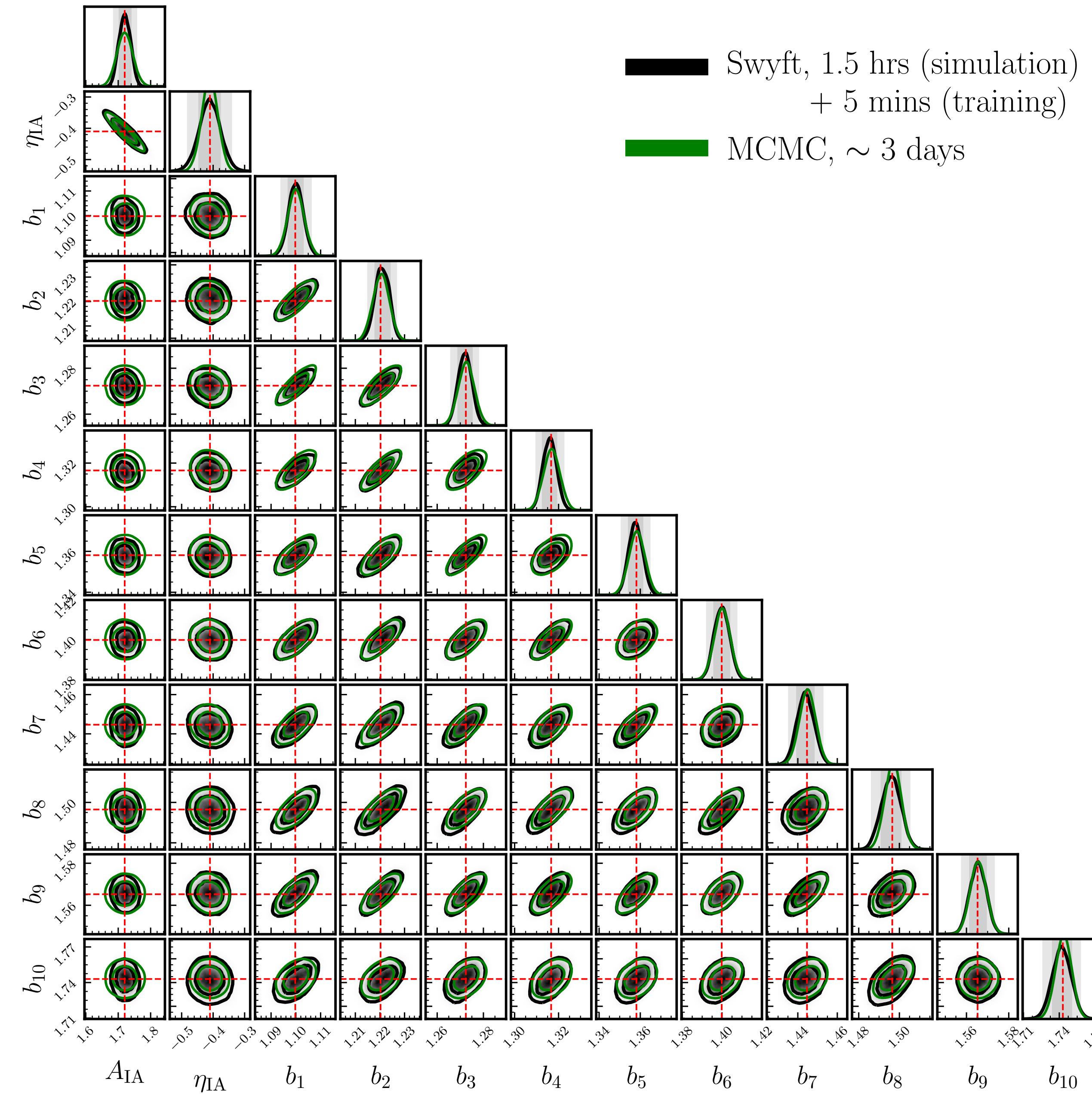
which yields

$$d_\phi(\mathbf{x}, \boldsymbol{\theta}) \simeq \frac{p(\mathbf{x}, \boldsymbol{\theta})}{p(\mathbf{x}, \boldsymbol{\theta}) + p(\mathbf{x}) p(\boldsymbol{\theta})} = \frac{r(\mathbf{x}; \boldsymbol{\theta})}{r(\mathbf{x}; \boldsymbol{\theta}) + 1}$$

# Posteriors for 3x2pt nuisance parameters



MNRE & MCMC are again  
in good agreement

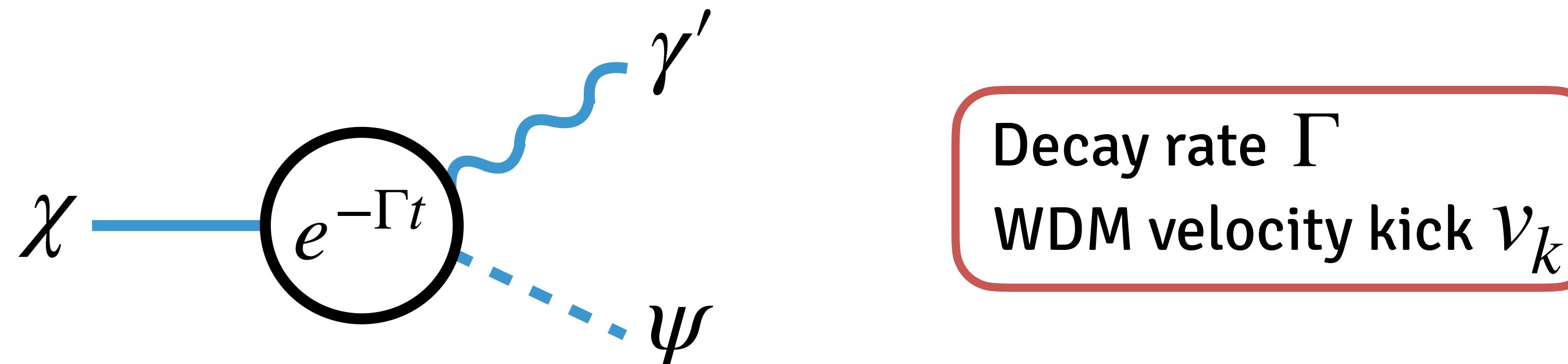


Does MNRE perform well with **highly non-Gaussian** posteriors?

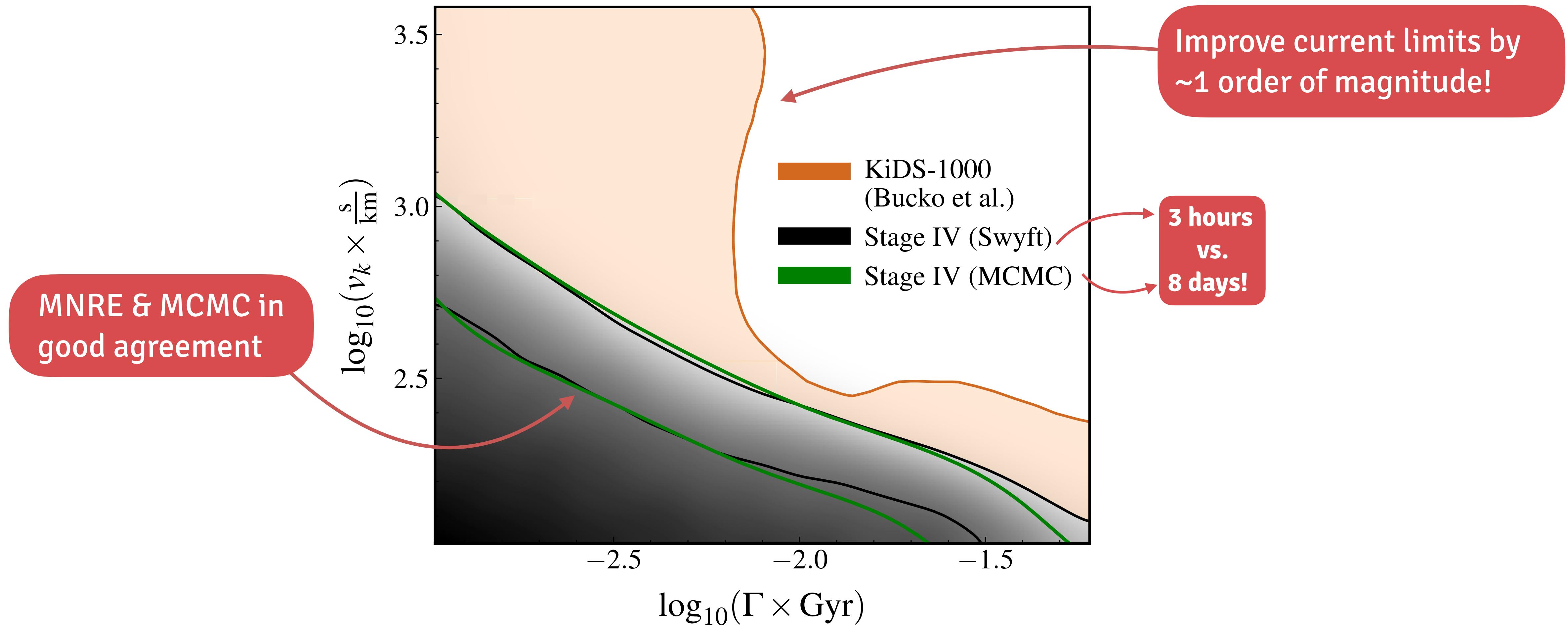
As an example, we test a model of **CDM decaying to DR + WDM**  
(proposed to explain the  $S_8$  tension)

[Abellán et al. 2102.12498]

[Bucko et al. 2307.03222]



# Forecast constraints on decaying DM



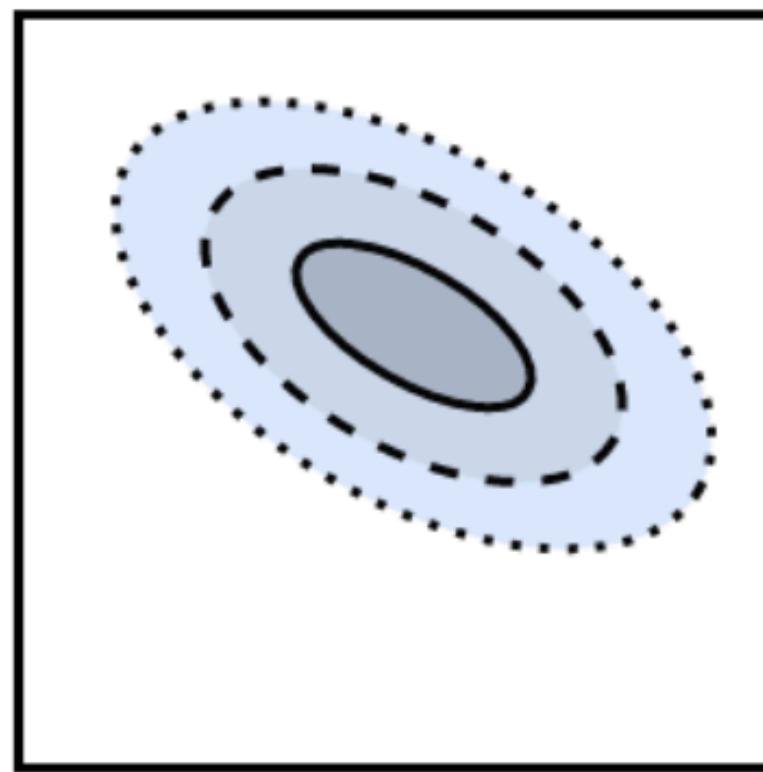
# But can we trust our results?



...even if NNs are often seen as "black boxes", it is possible to perform  
**statistical consistency tests** which are **impossible with MCMC**

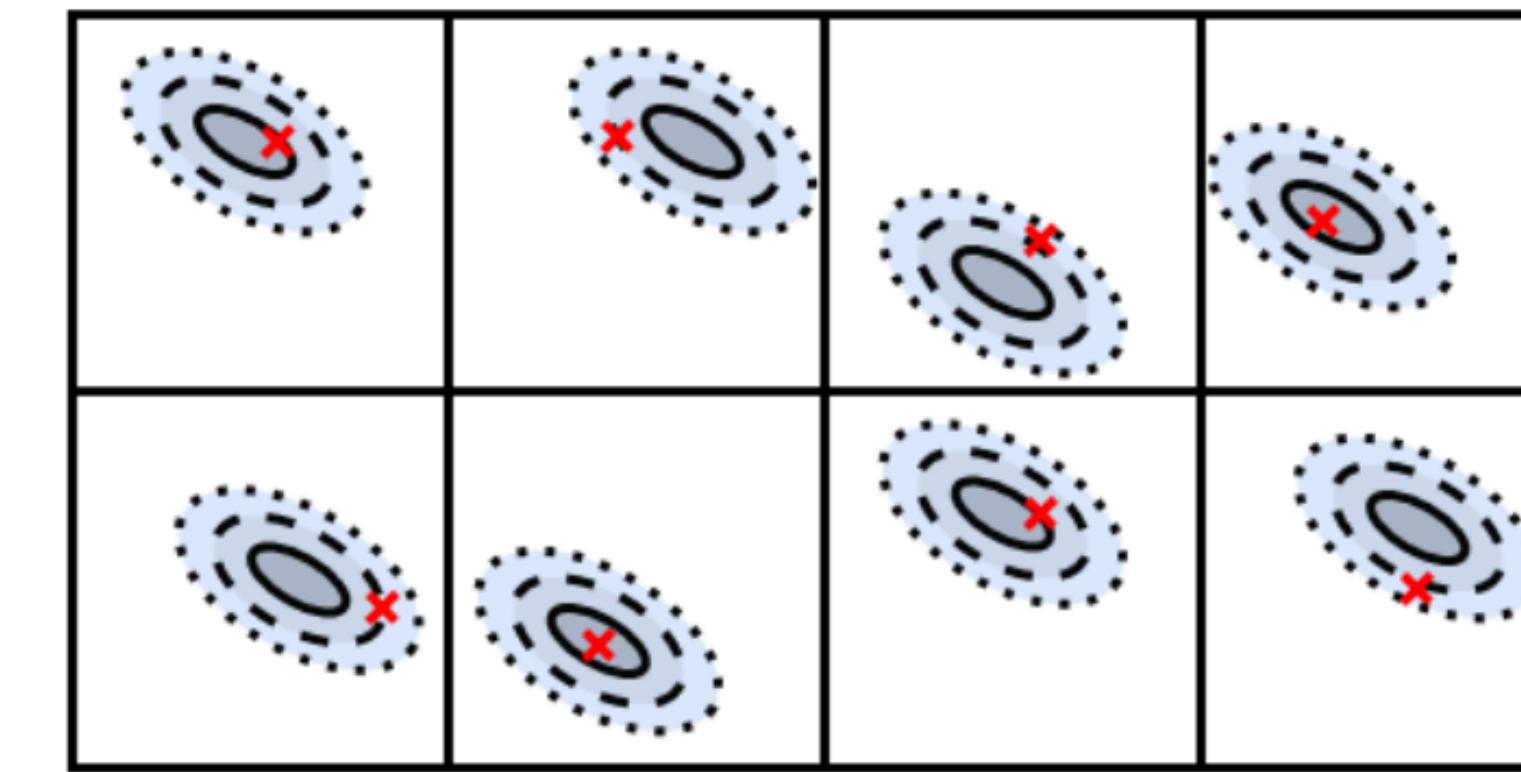
Trained networks can estimate effortlessly  
the posteriors for all simulated observations

MCMC



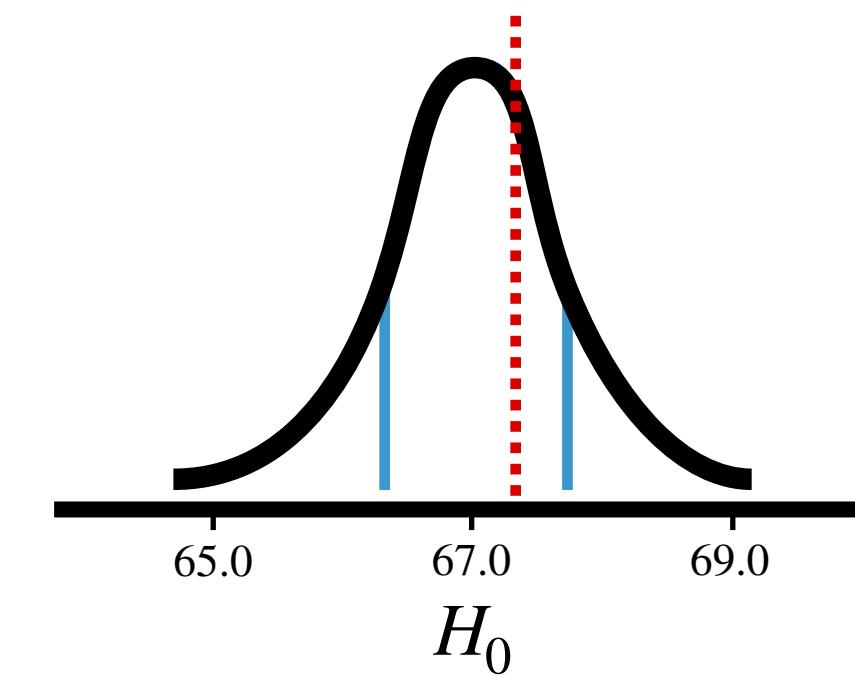
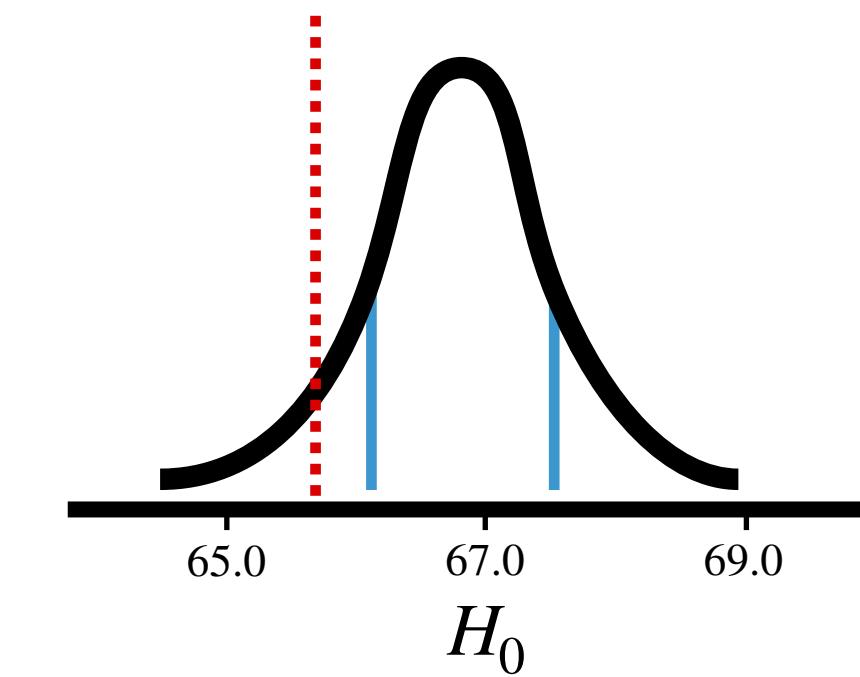
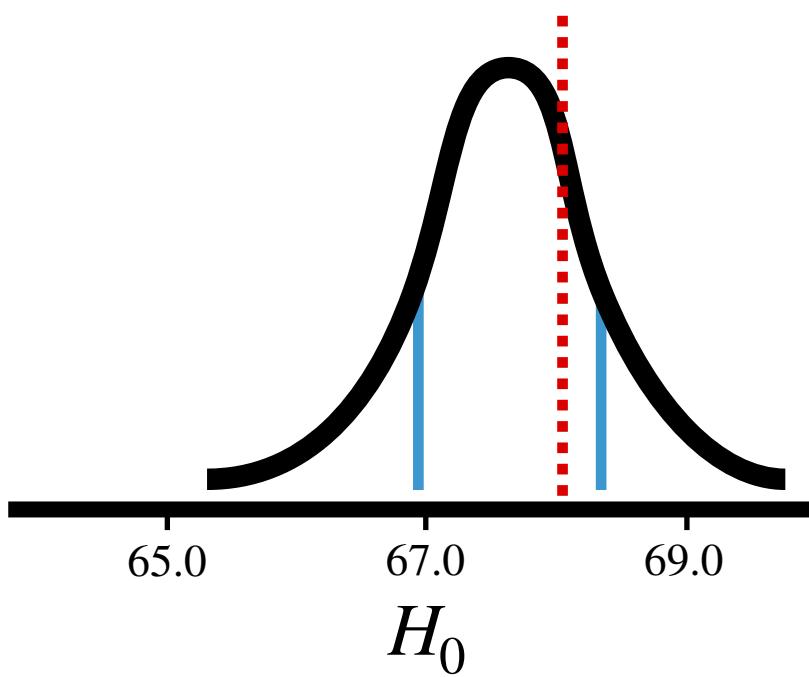
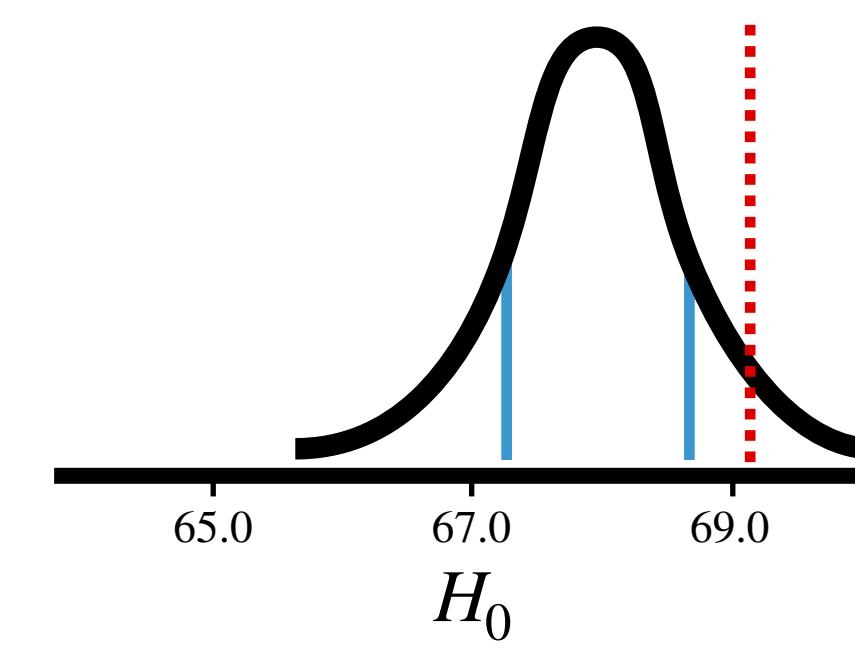
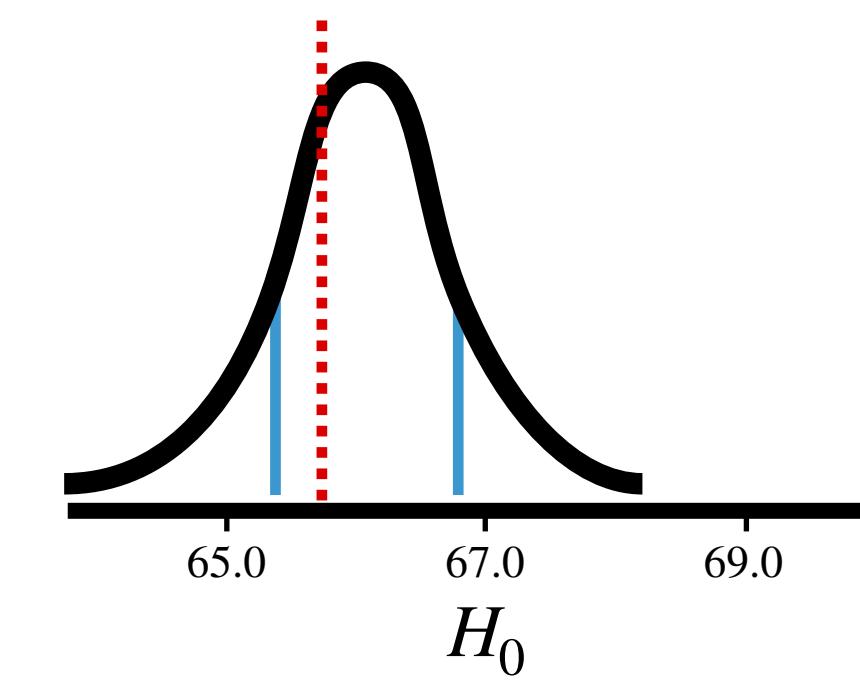
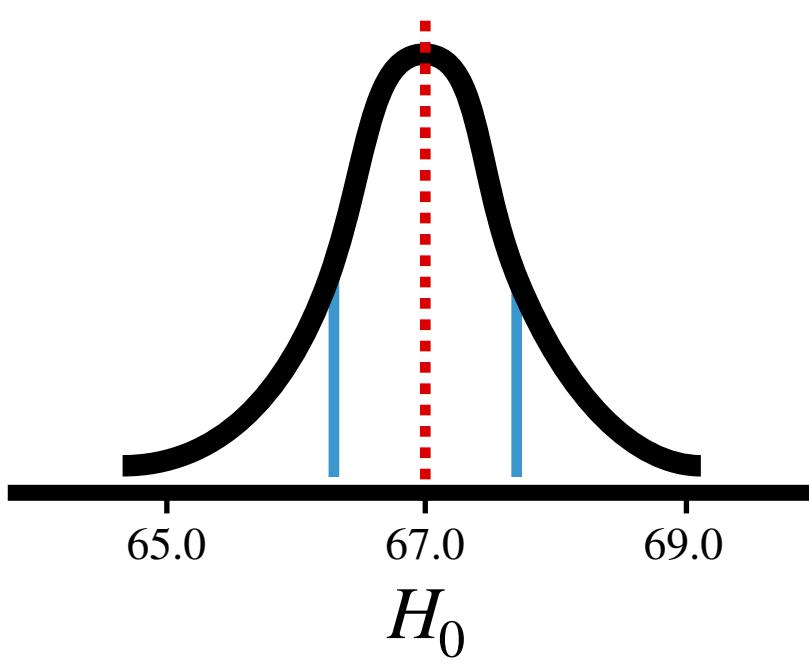
$$p(\theta|\mathbf{x}_o)$$

MNRE with swyft

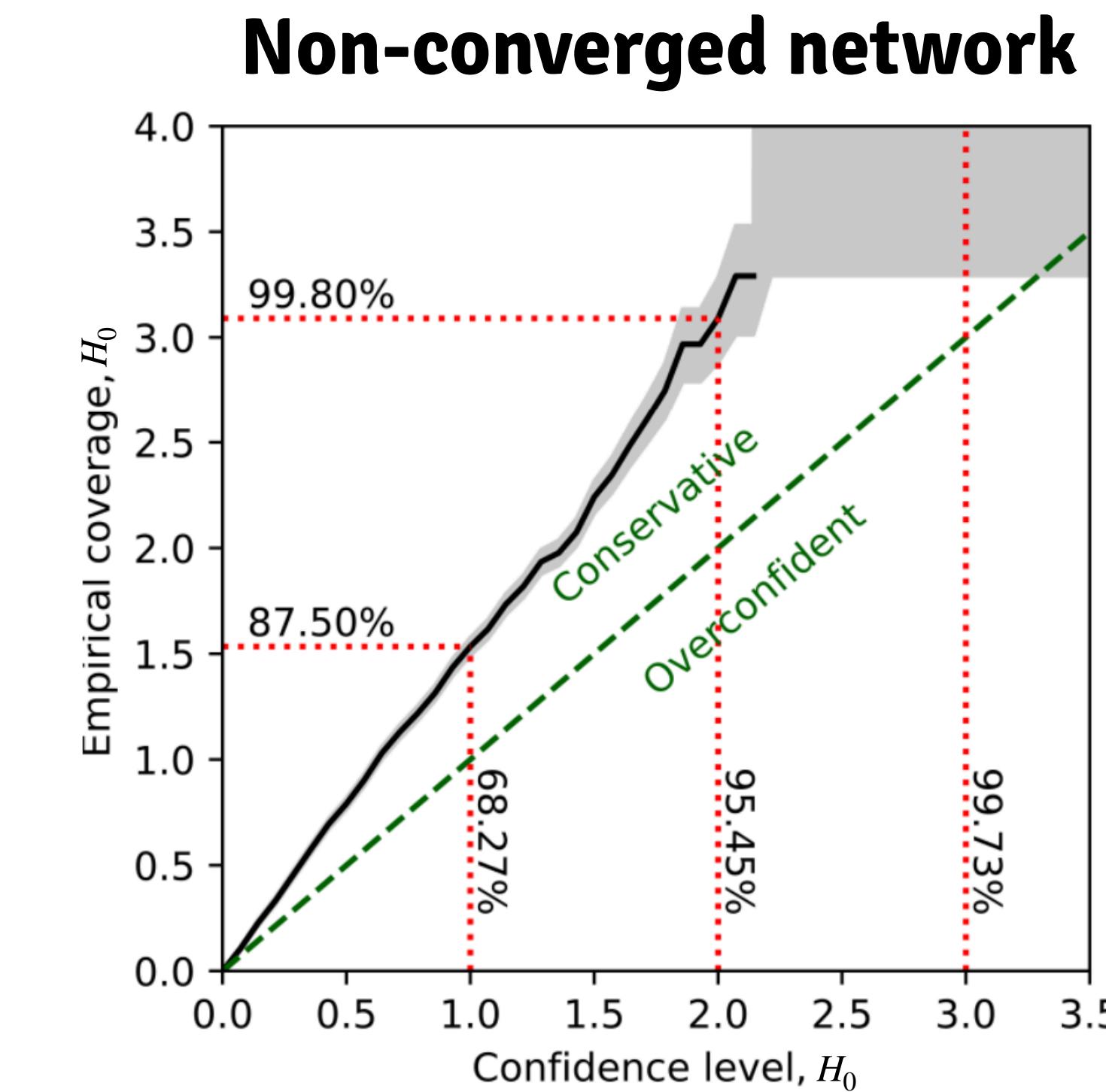
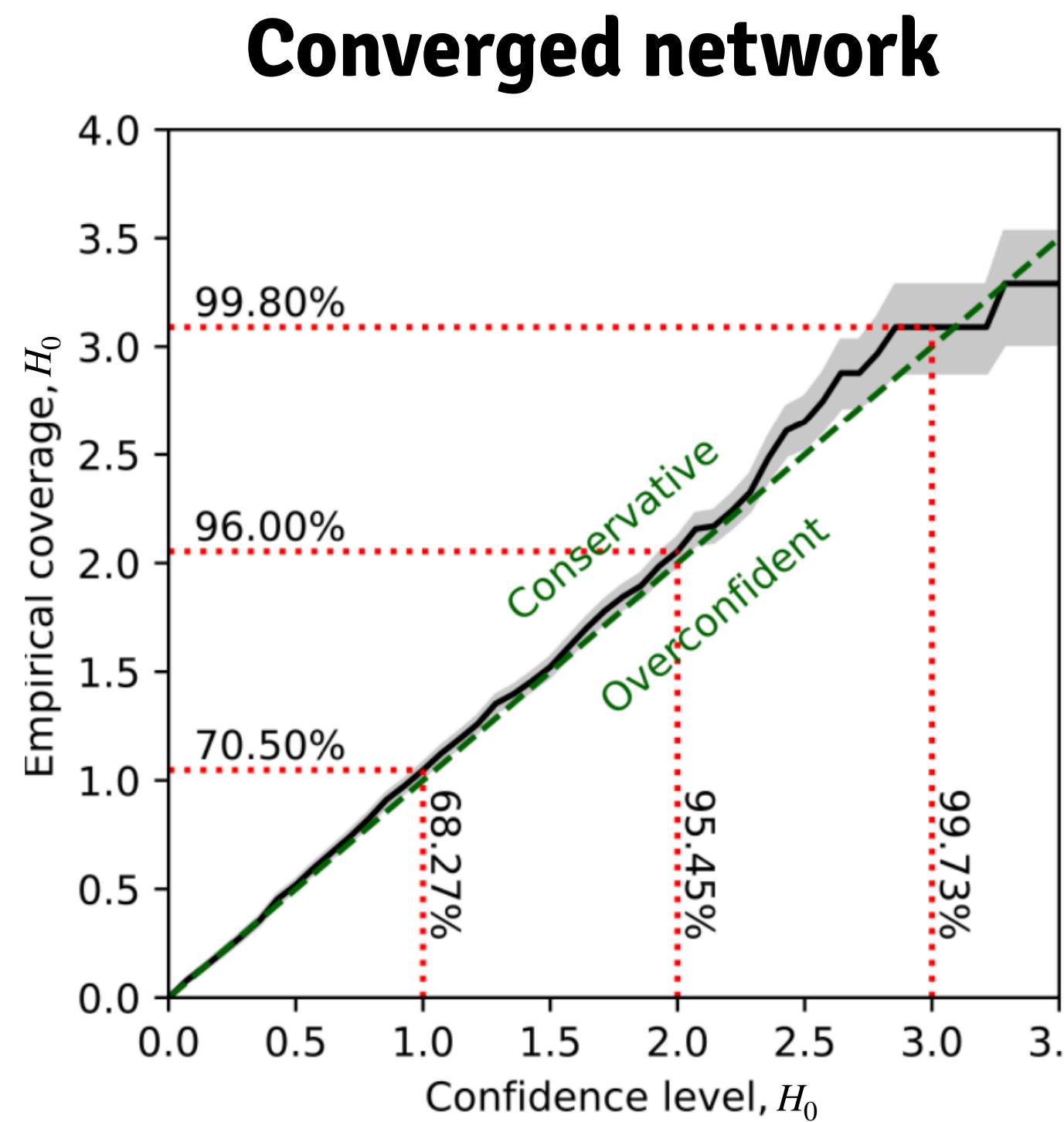


$$p(\theta|\mathbf{x}) \quad \forall \mathbf{x} \sim p(\mathbf{x})$$

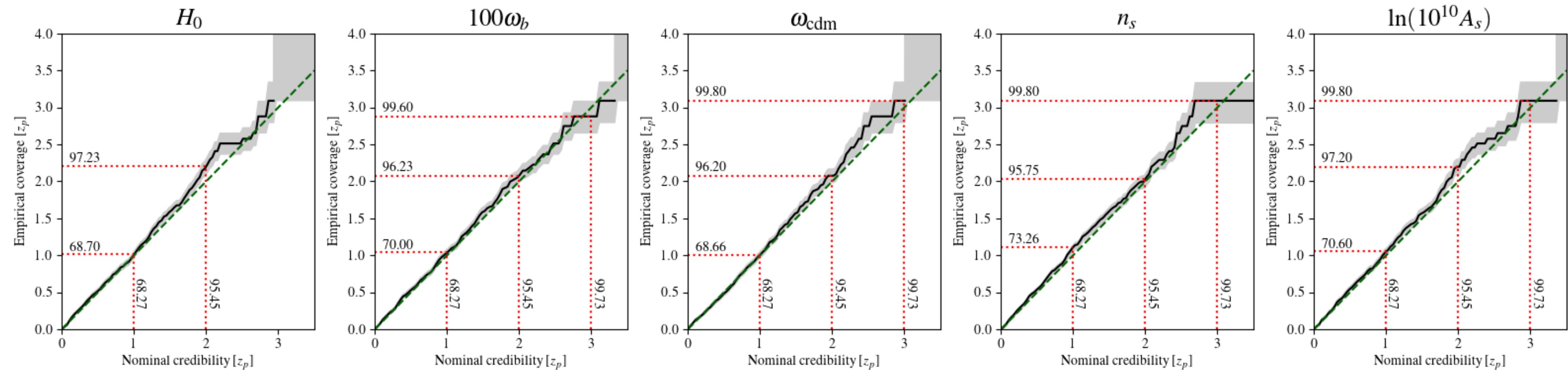
**Ex:** Is the estimated **68.27% interval** covering the ground truth in ~68% of the cases?



We can empirically estimate the Bayesian coverage



# Coverage test for Stage-IV 3x2pt



GFA++ 2403.14750

Empirical coverage and confidence level  
match to excellent precision!