

# The $H_0$ Olympics: a fair ranking of proposed models

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Based on:

arXiv:2102.12498 (PRD in press)

arXiv:2008.09615 (PRD in press)

arXiv:2009.10733 PRD 103 (2020)

arXiv:2107.10291, submitted to Physics Reports

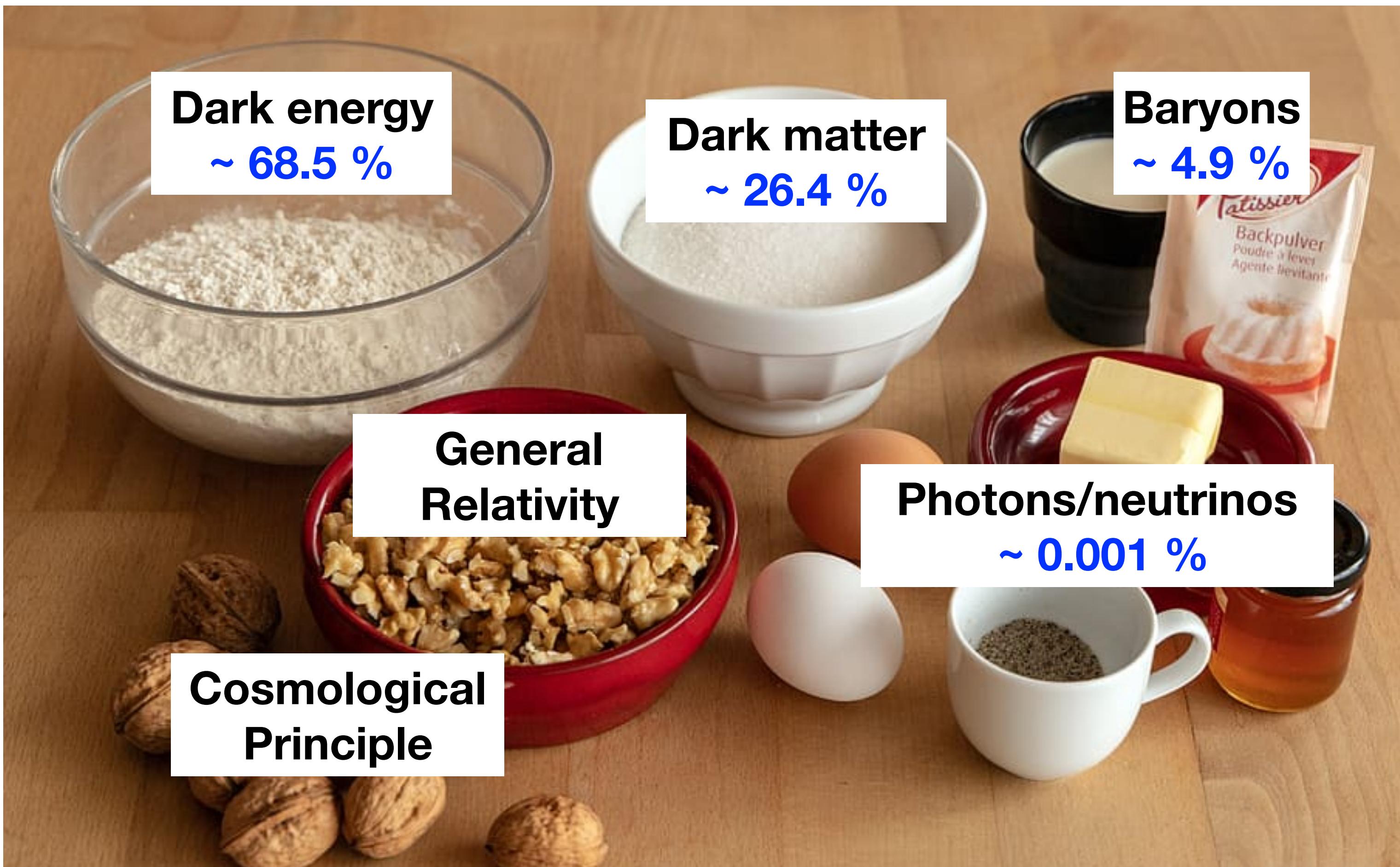


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- I. Cosmic concordance and discordance
- II. The  $H_0$  Olympics: quantifying the success of a resolution
- III. Explaining the  $S_8$  tension with Decaying Dark matter
- IV. Conclusions

# **I. Cosmic concordance and discordance**

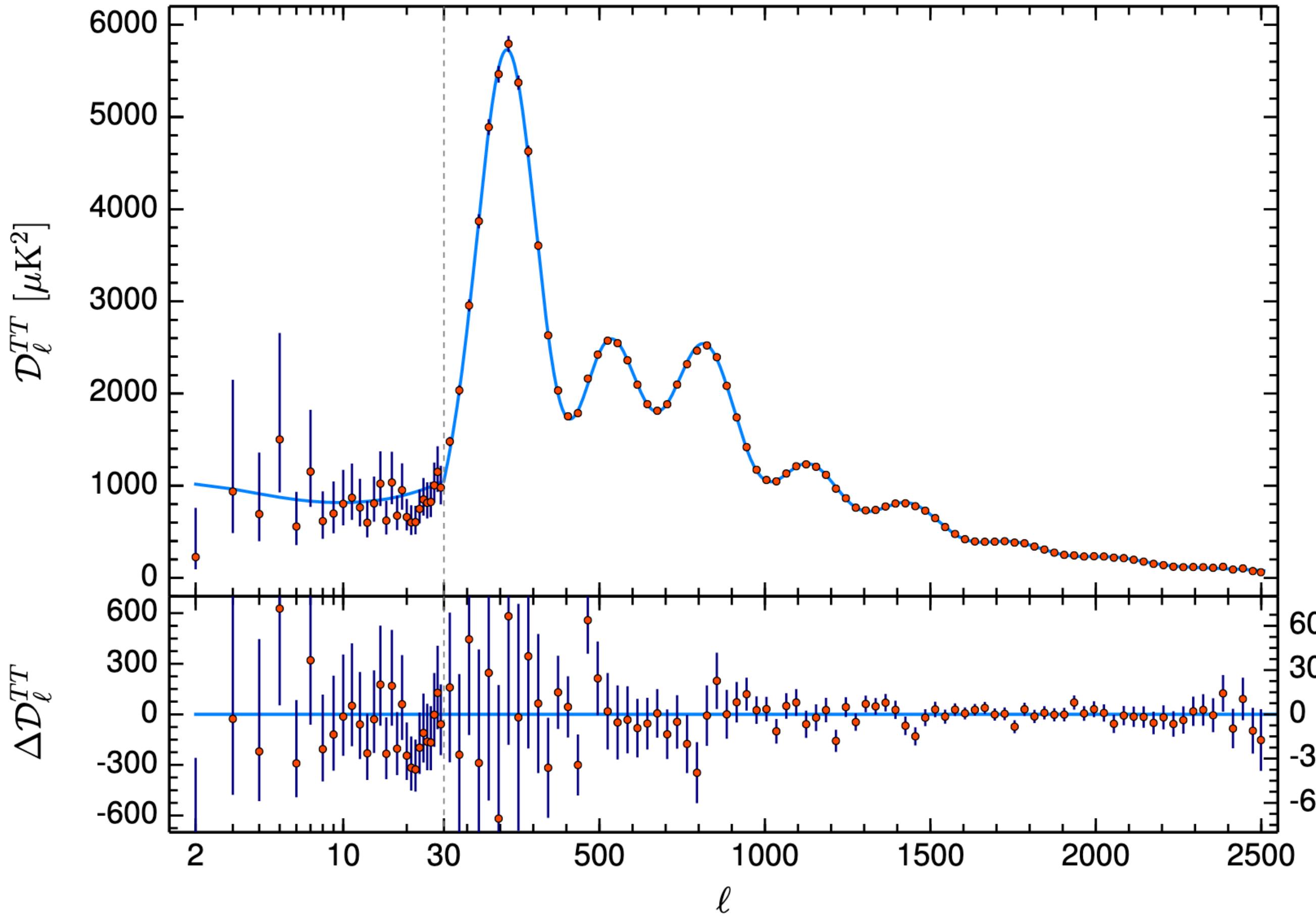
# Cosmic recipe



$\Lambda$ CDM model fully specified by  $\{\Omega_c, \Omega_b, H_0, A_s, n_s, \tau_{reio}\}$

# The era of precision cosmology

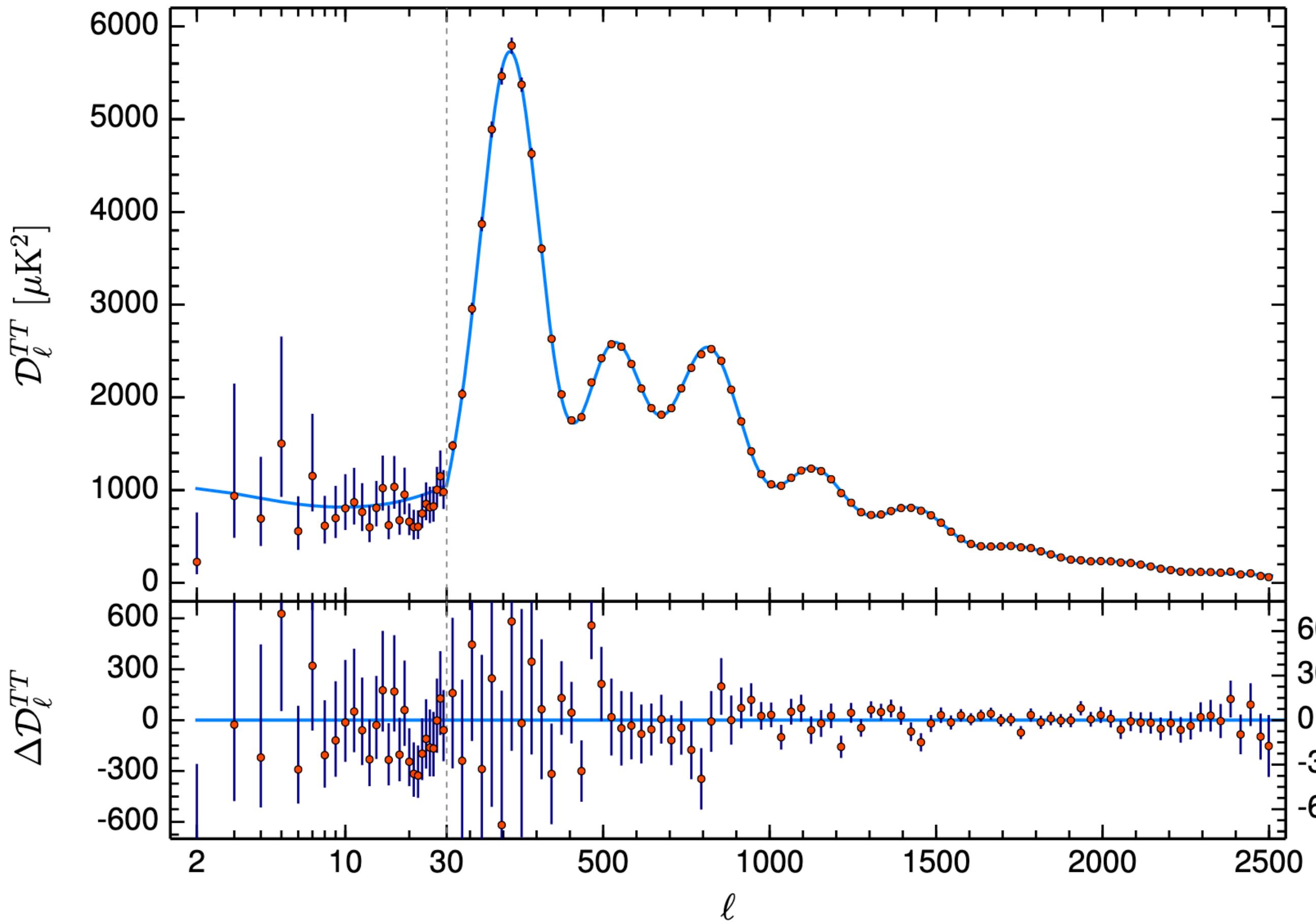
$\Lambda$ CDM gives excellent fit to CMB anisotropy spectra



Planck 2018, 1807.06209

# The era of precision cosmology

$\Lambda$ CDM gives excellent fit to CMB anisotropy spectra



Also explains:

- Baryon acoustic oscillations,
- Supernovae Ia,
- Light element abundances,
- Large Scale Structure, etc

# Challenges to the $\Lambda$ CDM paradigm

## 1. What is dark matter? And dark energy?

---

- Are they made of **particles**?
- Are they made of **single species**?
- How are they **produced**?
- What is their **lifetime**?
- And their **mass**?

# Challenges to the $\Lambda$ CDM paradigm

## 2. Several discrepancies emerged in recent years

---

- $S_8$  with weak-lensing data  
[KiDS-1000 2007.15632](#)
- $H_0$  with local measurements  
[Riess++ 2012.08534](#)

# Challenges to the $\Lambda$ CDM paradigm

## 2. Several discrepancies emerged in recent years

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- $S_8$  with weak-lensing data  
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### *Unaccounted systematics?*

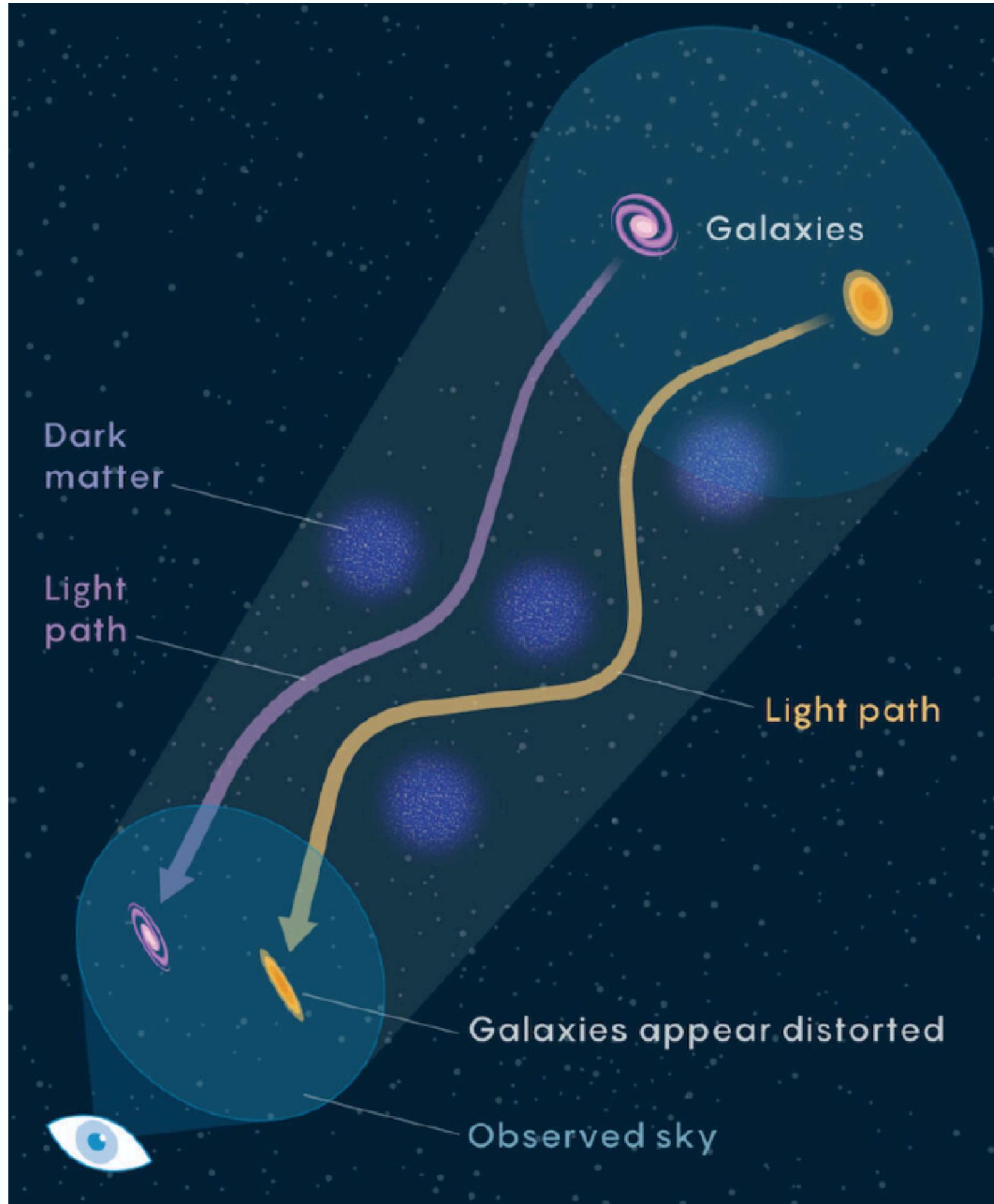
- Less exotic explanation
- Difficult to account for all discrepancies

### *Physics beyond $\Lambda$ CDM?*

- Reveal properties about the dark sector
- Very challenging

# The $S_8$ tension

Weak-lensing surveys are mainly sensible to  $S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3}$



KiDS+BOSS+2dfLenS\*:

$$S_8 = 0.766^{+0.020}_{-0.014}$$

Planck (*under  $\Lambda$ CDM*):

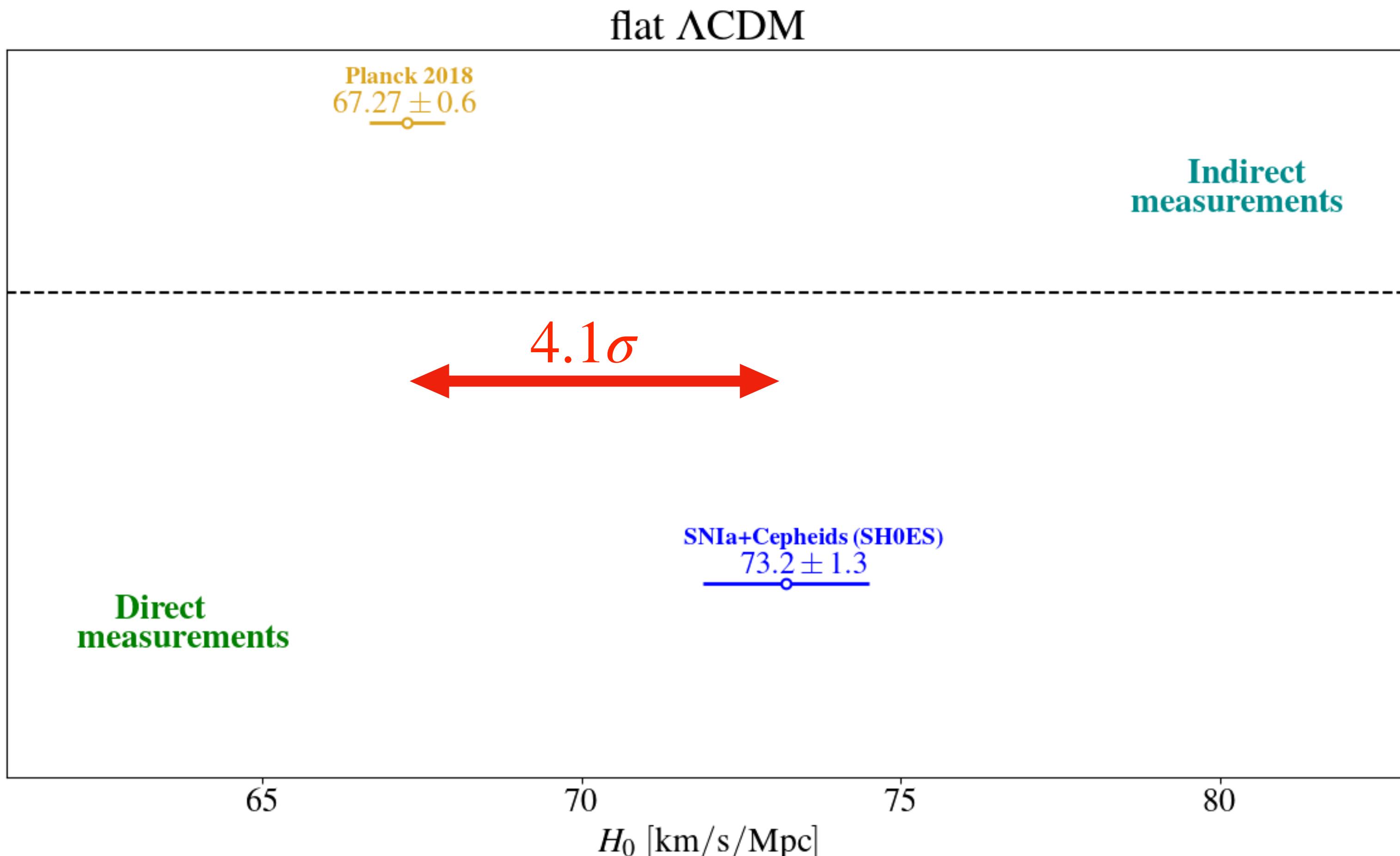
$$S_8 = 0.830 \pm 0.013$$

→  $\sim 2 - 3\sigma$  tension

\*Other surveys such as DES, CFHTLens or HSC yield similar results

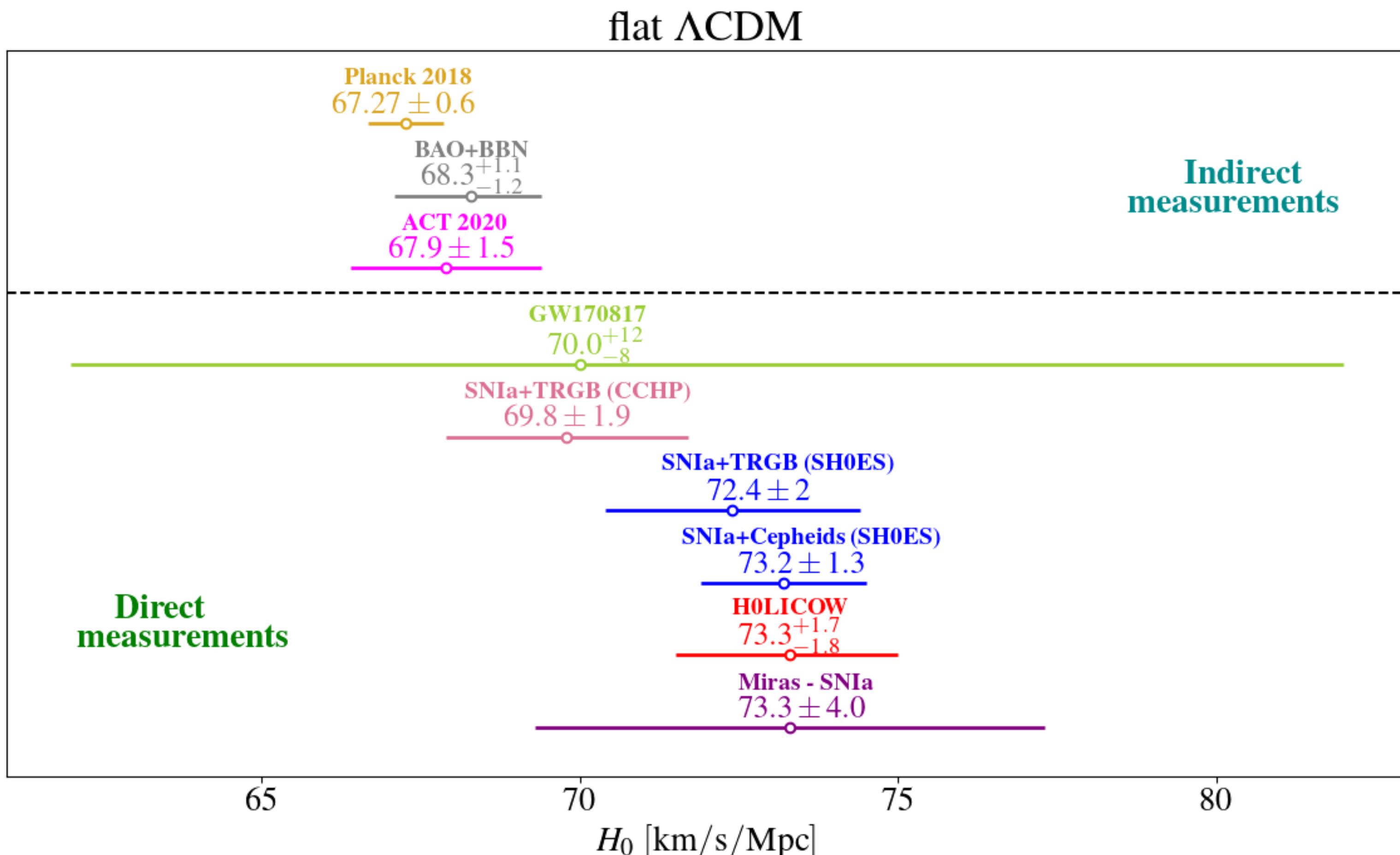
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# The $H_0$ tension

Planck (*under  $\Lambda$ CDM*) and SHoES measurements are in  **$4.1\sigma$  tension**  
High- and low-redshift probes are typically discrepant



# How does SH0ES determine $H_0$ ?

$$v = H_0 D$$

From spectrometry

$$1 + z = \frac{\lambda_{obs}}{\lambda_{emit}}$$

Distance to some standard candle, e.g. supernovae Ia

$$\text{Flux} = \frac{L}{4\pi D_L^2}$$

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$$\text{Flux} = \frac{L}{4\pi D_L^2}$$

Focus on small  $z^*$ , for which distances are approx. **model-independent**

$$D_L = (1 + z) \int_0^z \frac{cdz'}{H(z')} \xrightarrow{z \ll 1} czH_0^{-1} \simeq vH_0^{-1}$$

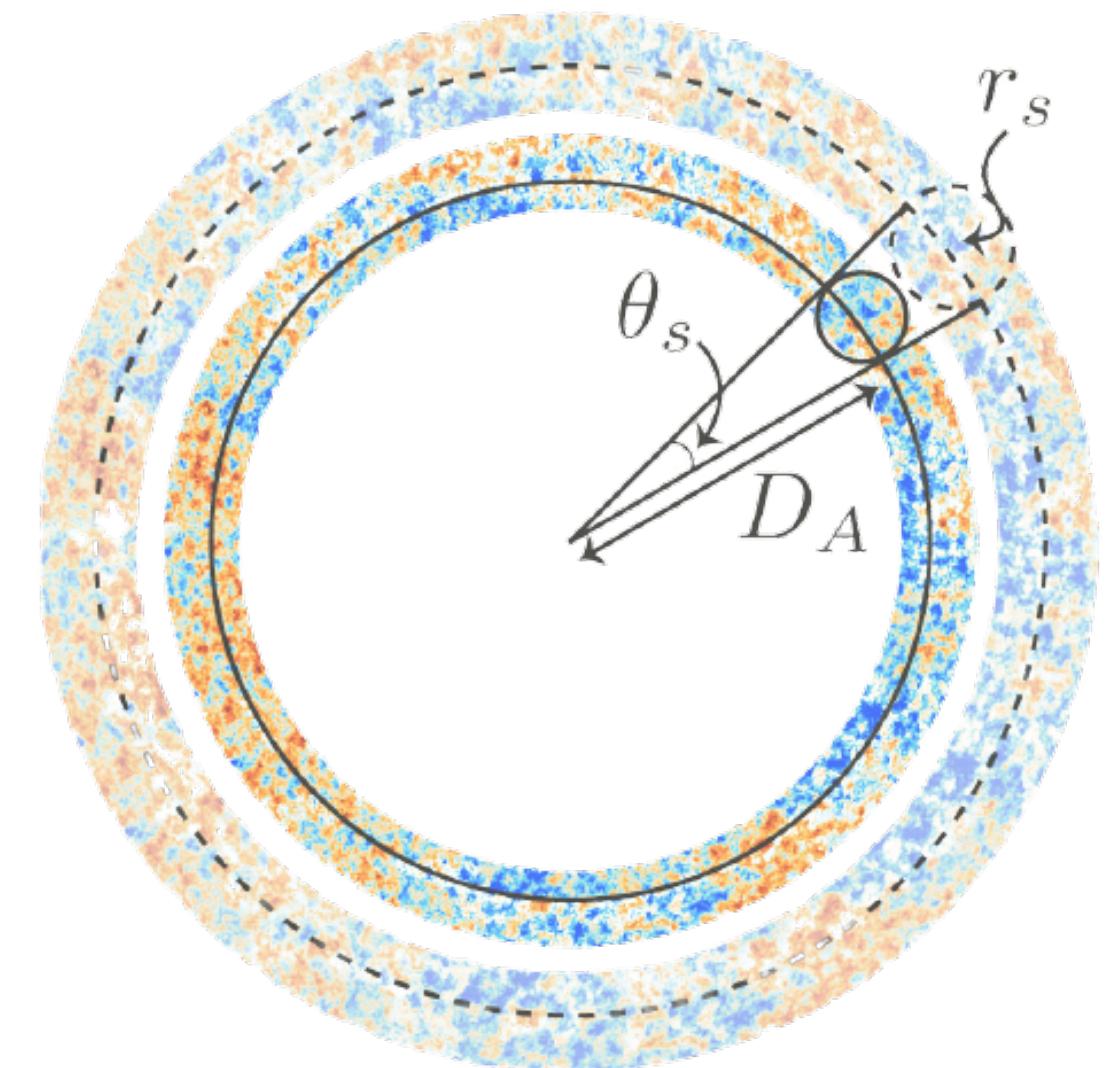
$$\text{where } H^2(z) = \frac{8\pi G}{3} \sum_i \rho_i(z)$$

\*But not too small, to make sure peculiar velocities are negligible

# How does Planck determine $H_0$ ?

Angular size of the sound horizon is measured at the 0.04 % precision

$$\theta_s = \frac{r_s(z_{\text{rec}})}{D_A(z_{\text{rec}})} = \frac{\int_0^{\tau_{\text{rec}}} c_s(\tau) d\tau}{\int_{\tau_{\text{rec}}}^{\tau_0} c d\tau}$$



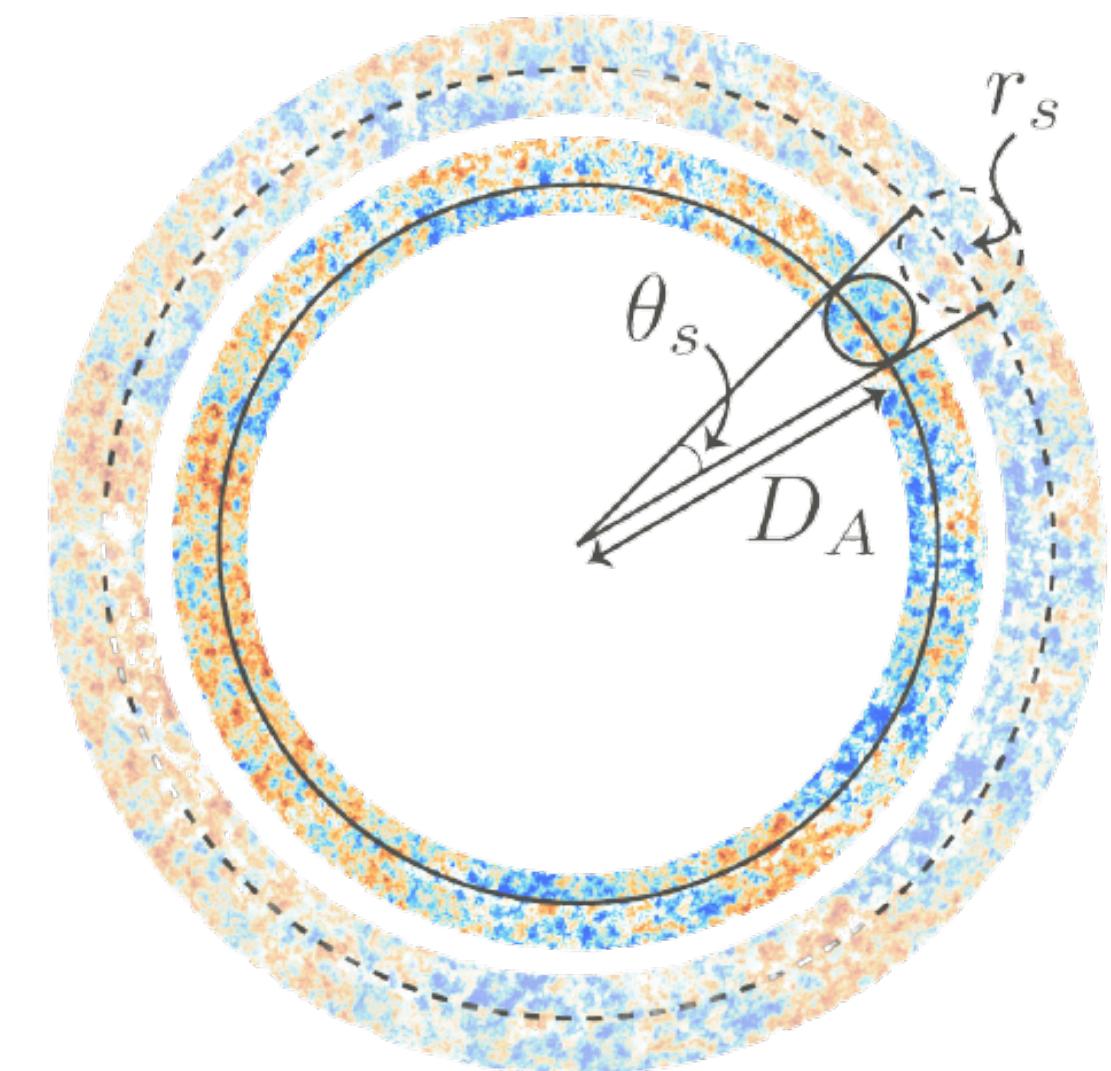
T. Smith

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with  $D_A \propto 1/H_0 = 1/\sqrt{\rho_{\text{tot}}(0)}$



model prediction of  $r_s$  + measurement of  $\theta_s \rightarrow H_0$

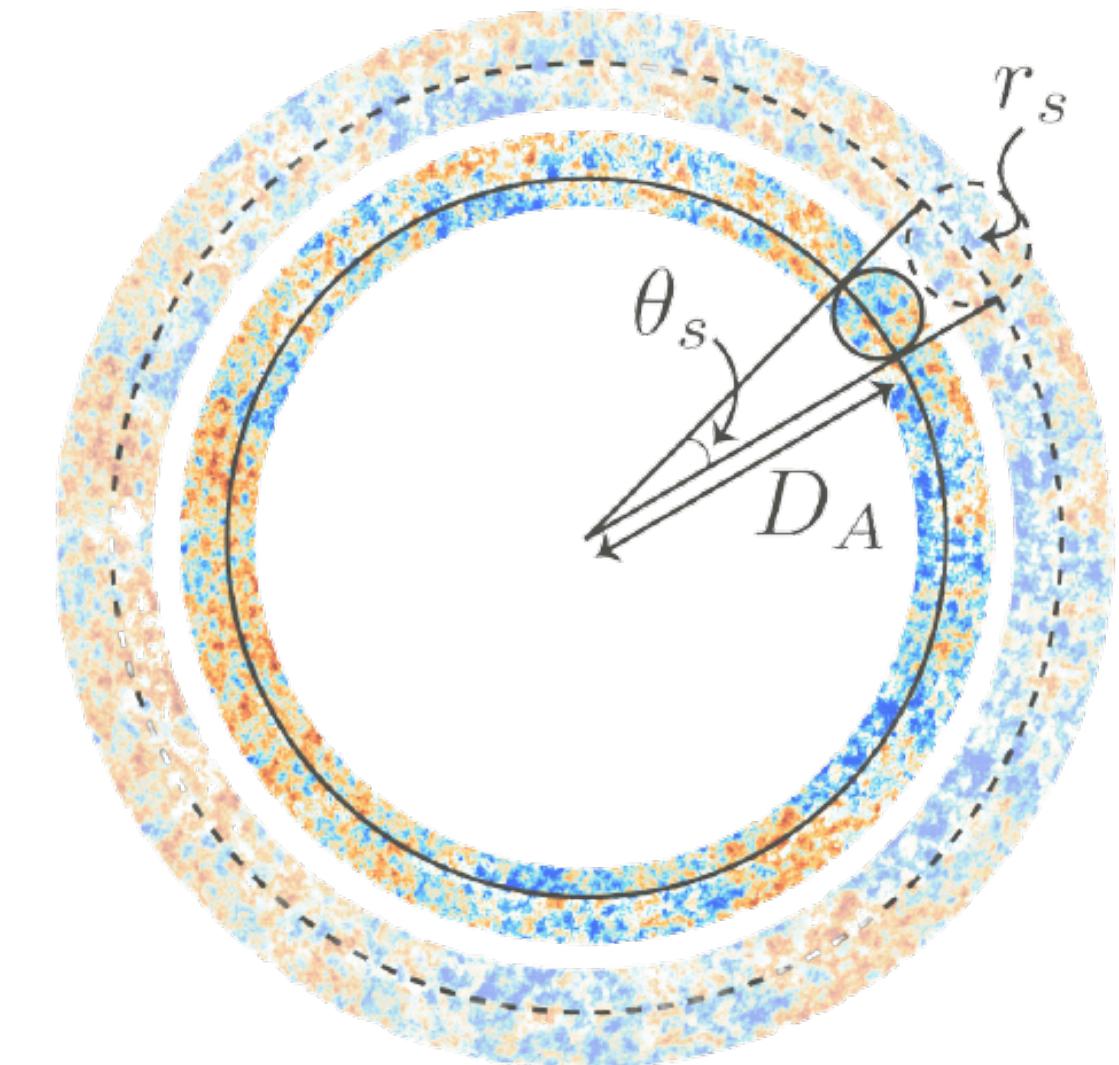
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model prediction of  $r_s$  + measurement of  $\theta_s \rightarrow H_0$

T. Smith

## *Early-time solutions*

Decrease  $r_s(z_{\text{rec}})$  at fixed  $\theta_s$  to decrease  $D_A(z_{\text{rec}})$  and increase  $H_0$

Ex :  $\Delta N_{\text{eff}} > 0$

## *Late-time solutions*

$r_s(z_{\text{rec}})$  and  $D_A(z_{\text{rec}})$  are fixed, but  $D_A(z < z_{\text{rec}})$  is changed to allow higher  $H_0$

Ex :  $w < -1$

## **II. The H<sub>o</sub> Olympics: quantifying the success of a resolution**

In collaboration with Nils Schöneberg, Andrea Pérez Sánchez,  
Samuel J. Witte, Vivian Poulin and Julien Lesgourges

# Lost in the landscape of solutions

- Cosmological tensions have become a **very hot topic** (specially the  $H_0$  tension)

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- Cosmological tensions have become a **very hot topic** (specially the  $H_0$  tension)
- [Di Valentino, Mena++ 2103.01183](#) → recent review of solutions, more than 1000 refs !

## Early Dark Energy Can Resolve The Hubble Tension

Vivian Poulin<sup>1</sup>, Tristan L. Smith<sup>2</sup>, Tanvi Karwal<sup>1</sup>, and Marc Kamionkowski<sup>1</sup>

## Relieving the Hubble tension with primordial magnetic fields

Karsten Jedamzik<sup>1</sup> and Levon Pogosian<sup>2,3</sup>

## The Neutrino Puzzle: Anomalies, Interactions, and Cosmological Tensions

Christina D. Kreisch,<sup>1,\*</sup> Francis-Yan Cyr-Racine,<sup>2,3,†</sup> and Olivier Doré<sup>4</sup>

## Rock ‘n’ Roll Solutions to the Hubble Tension

Prateek Agrawal<sup>1</sup>, Francis-Yan Cyr-Racine<sup>1,2</sup>, David Pinner<sup>1,3</sup>, and Lisa Randall<sup>1</sup>

## The Hubble Tension as a Hint of Leptogenesis and Neutrino Mass Generation

Miguel Escudero<sup>1,\*</sup> and Samuel J. Witte<sup>2,†</sup>

## Can interacting dark energy solve the $H_0$ tension?

Cleonora Di Valentino,<sup>1,2,\*</sup> Alessandro Melchiorri,<sup>3,†</sup> and Olga Mena<sup>4,‡</sup>

## Dark matter decaying in the late Universe can relieve the $H_0$ tension

Kyriakos Vattis, Savvas M. Koushiappas, and Abraham Loeb

## A Simple Phenomenological Emergent Dark Energy Model can Resolve the Hubble Tension

XIAOLEI LI<sup>1,2</sup> AND ARMAN SHAFIELOO<sup>1,3</sup>

## Early recombination as a solution to the $H_0$ tension

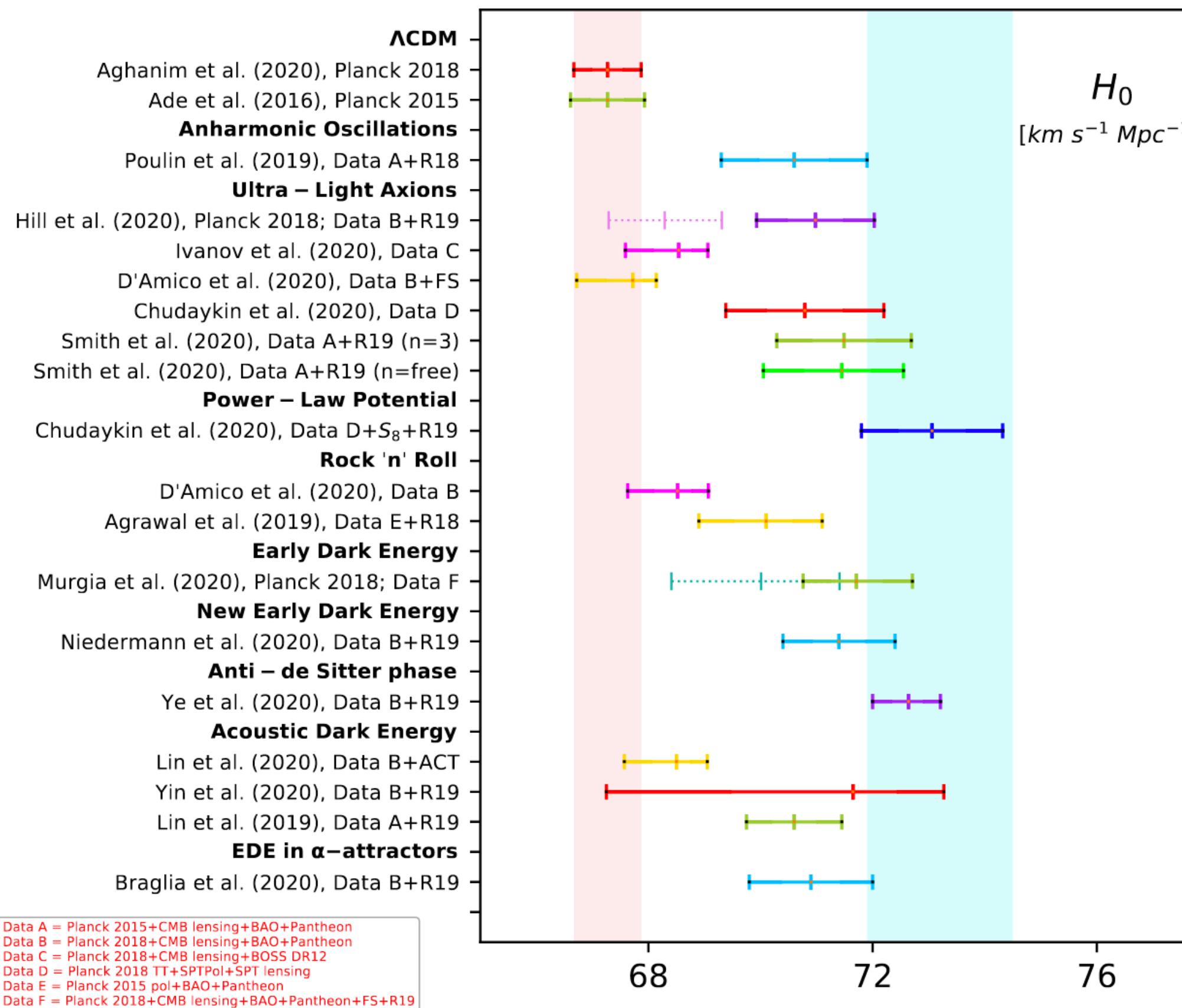
Toyokazu Sekiguchi<sup>1,\*</sup> and Tomo Takahashi<sup>2,†</sup>

## Early modified gravity in light of the $H_0$ tension and LSS data

Matteo Braglia,<sup>1,2,3,\*</sup> Mario Ballardini,<sup>1,2,3,†</sup> Fabio Finelli,<sup>2,3,‡</sup> and Kazuya Koyama<sup>4,§</sup>

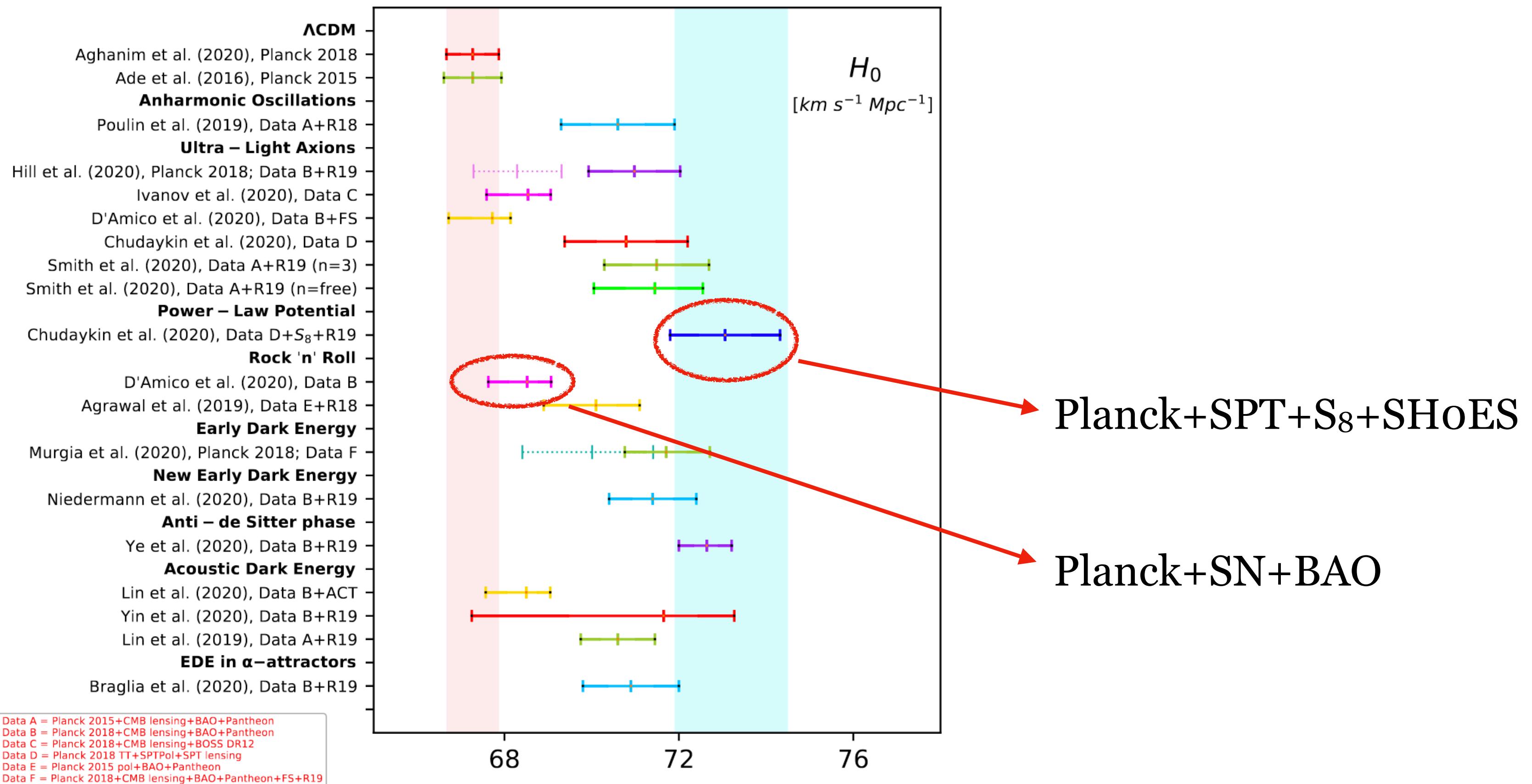
# Lost in the landscape of solutions

It proves difficult to compare success of the different proposed solutions, since authors typically use **differing and incomplete combinations of data**



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# The $H_0$ Olympics

**Goal:** Take a representative sample of proposed solutions, and quantify the relative success of each using certain metrics and a wide array of data

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## Early universe

### w Dark radiation

- $\Delta N_{\text{eff}}$
- Self-interacting DR
- Mixed DR
- DM-DR interactions
- Self-interacting  $v_s$ +DR
- Majoron- $v_s$  interactions

### wo Dark radiation

- Primordial B
- Varying  $m_e$
- Varying  $m_e + \Omega_k$
- Early Dark Energy
- New Early Dark Energy

### Late universe

- CPL dark energy
- PEDE
- MPEDE
- Fraction DM  $\rightarrow$  DR
- DM  $\rightarrow$  DR +WDM

# Model-independent treatment of the SH0ES data

The cosmic distance ladder method *doesn't directly measure  $H_0$ .*

It directly measures the intrinsic magnitude of SNIa  $M_b$  at redshifts  $0.02 \leq z \leq 0.15$ , and then obtains  $H_0$  by comparing with the apparent SNIa magnitudes  $m$

$$m(z) = M_b + 25 - 5\log_{10}H_0 + 5\log_{10}(\hat{D}_L(z))$$

where

$$\hat{D}_L(z) \simeq z \left( 1 + (1 - q_0) \frac{z}{2} - \frac{1}{6} (1 - q_0 - 3q_0^2 + j_0) z^2 \right)$$

$$q_0 = -0.53, \quad j_0 = 1 \quad (\Lambda\text{CDM assumed!})$$

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# Quantifying model success

**Criterion 1:** Can we get high values of  $H_0$  without the inclusion of a SHoES prior?

## Gaussian tension GT

$$\frac{\bar{x}_D - \bar{x}_{SH0ES}}{\sqrt{\sigma_D^2 + \sigma_{SH0ES}^2}} \text{ for } x = H_0 \text{ or } M_b$$

We demand  $GT < 3\sigma$

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We demand  $GT < 3\sigma$

## Caveats:

- Only valid for gaussian posteriors  $\times$
- Doesn't quantify quality of the fit  $\times$

Example:  $\Lambda$ CDM with fixed  $\Omega_{\text{cdm}}h^2 = 0.11$  yields  $H_0 = 71.84 \pm 0.16 \text{ km/s/Mpc}$  but has  $\Delta\chi^2 \simeq 106$

# Quantifying model success

**Criterion 2:** Can we get a good fit to all the data in a given model?

**Q<sub>DMAP</sub> tension**

$$\sqrt{\chi^2_{\min, \text{D+SH0ES}} - \chi^2_{\min, \text{D}}}$$

Raveri&Hu 1806.04649

We demand  $Q_{\text{DMAP}} < 3\sigma$

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Raveri&Hu 1806.04649

We demand  $Q_{\text{DMAP}} < 3\sigma$

**Caveats:**

- Accounts for non-gaussianity of posteriors
- Doesn't account for effects of over-fitting

# Quantifying model success

**Criterion 3:** Is a model M favoured over  $\Lambda$ CDM?

**Akaike Information Criterium  $\Delta$ AIC**

$$\chi^2_{\min, M} - \chi^2_{\min, \Lambda\text{CDM}} + 2(N_M - N_{\Lambda\text{CDM}})$$

We demand  $\Delta$ AIC < - 6.91 \*

\*Corresponds to weak preference according to Jeffrey's scale

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**Caveats:**

- Simple to use and prior-independent 

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# Steps of the contest

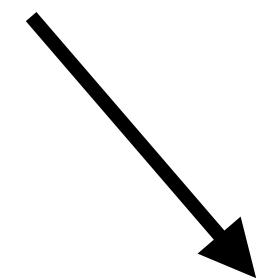
Compare all models against

- Planck 18 TTTEEE+lensing
- BAO (BOSS DR12+MGS+6dFGS)
- Pantheon SNIa catalog
- SHoES

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As long as  $\Delta\text{AIC} < 0$ , models go into  
finalist if criterium 2 or 3 are  
satisfied

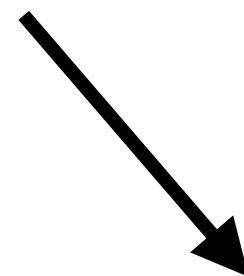
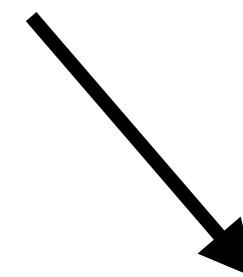
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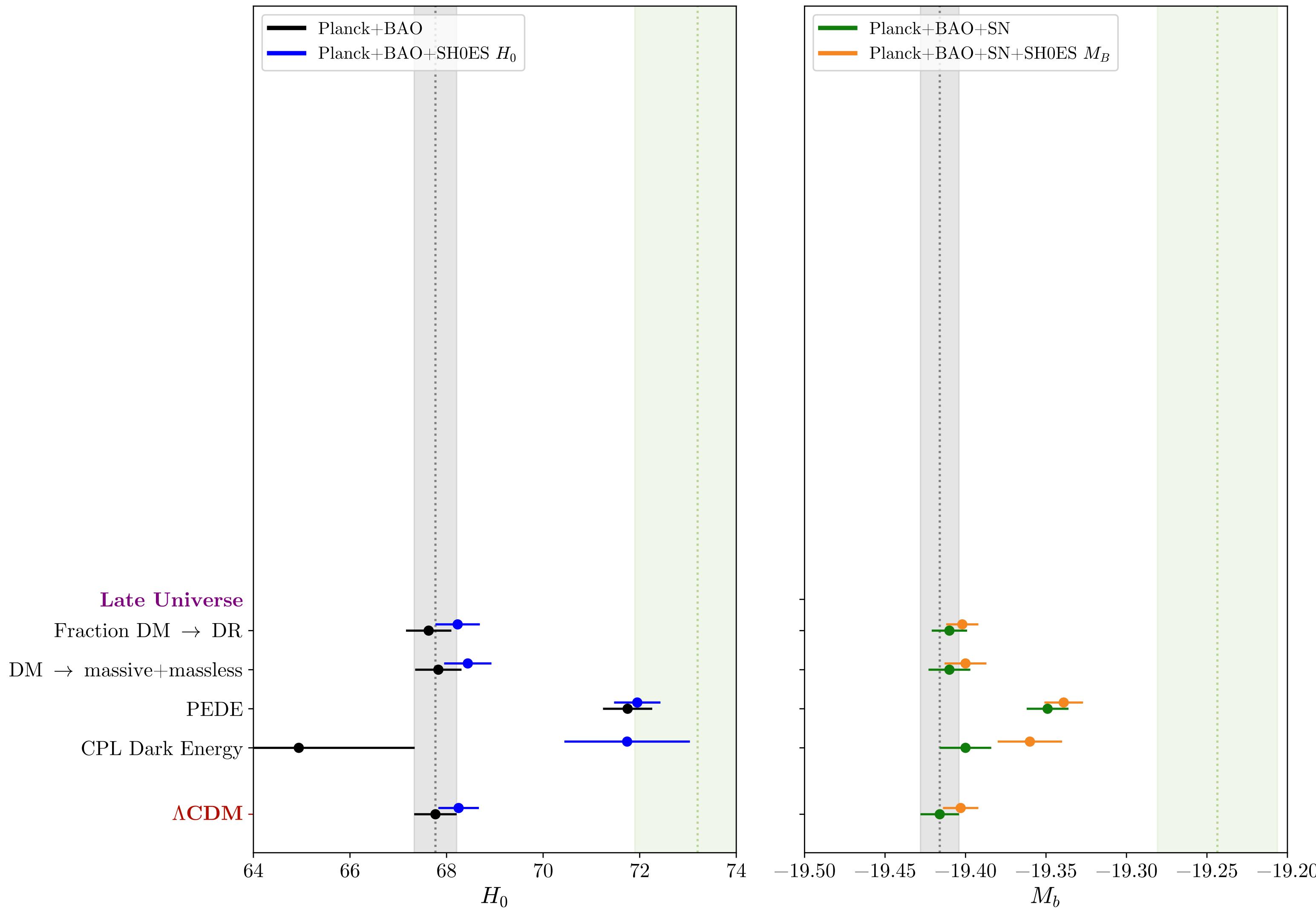
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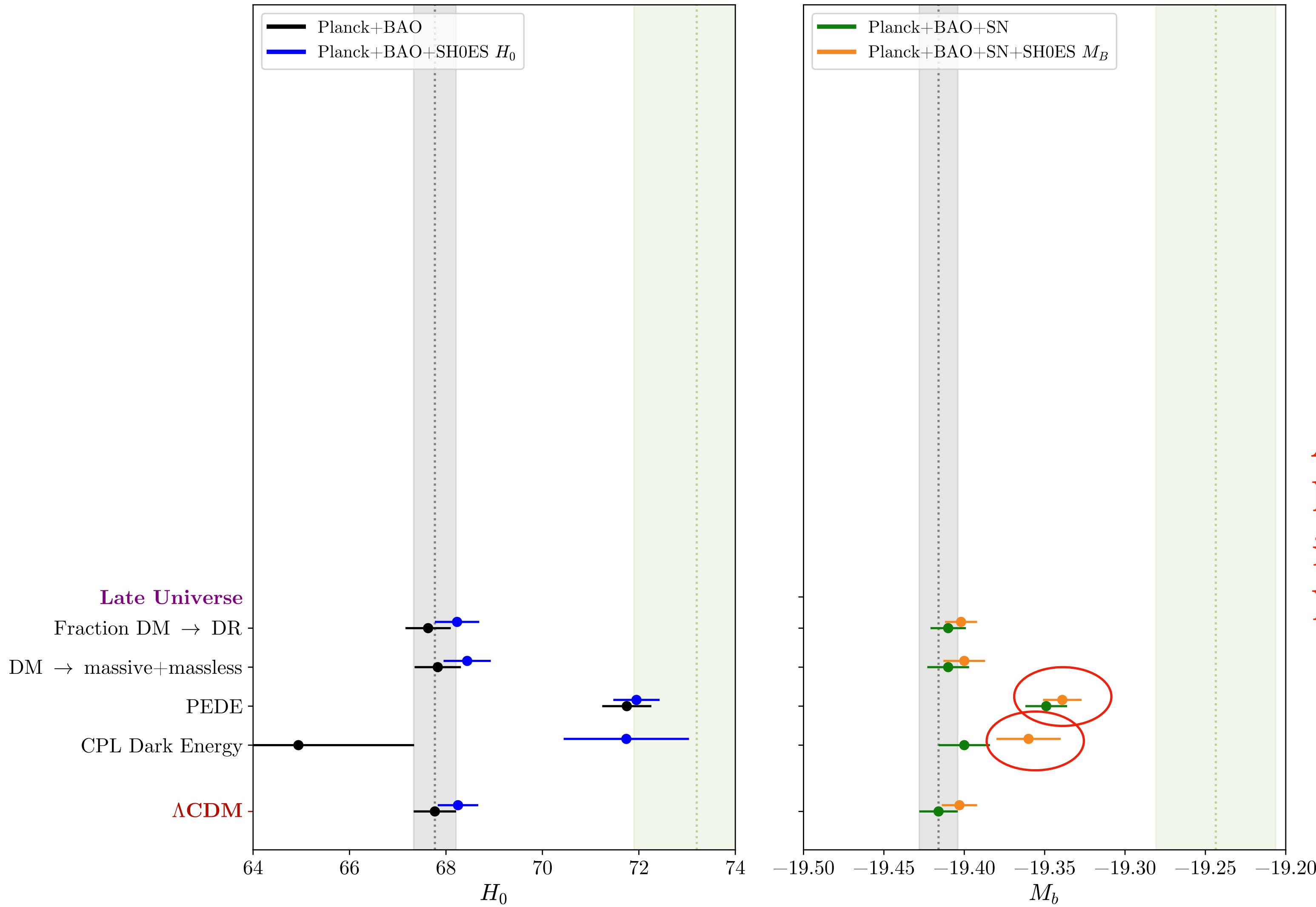
Finalists receive bronze, silver or  
golden medals if they satisfy one,  
two or three criteria, respectively



# Results of the contest



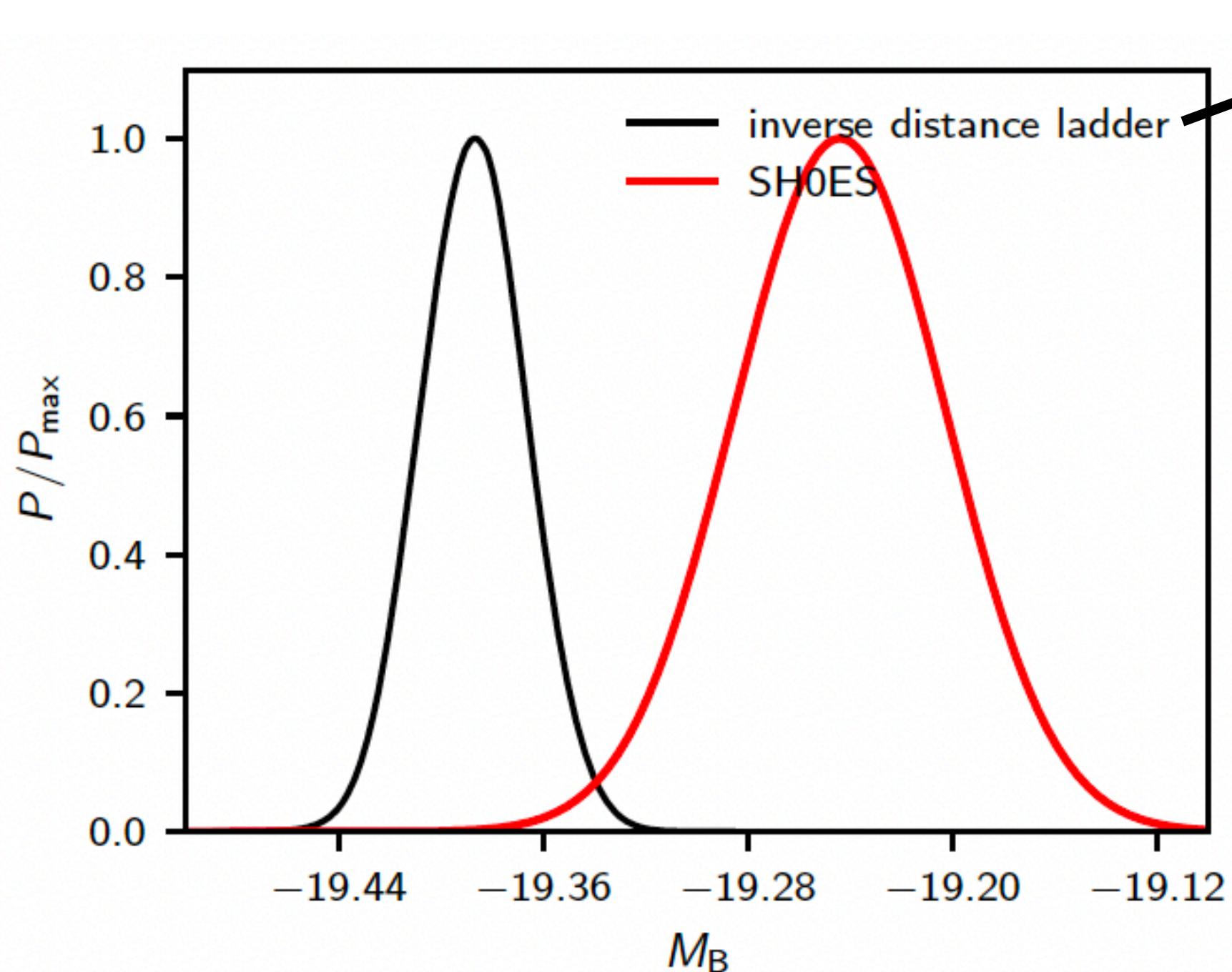
# Results of the contest



Adding  $M_b$  prior  
has a strong  
impact on  
late solutions!



# Late-time solutions are disfavoured by BAO+SNIA



Efstathiou 2103.08723

Given  $r_s$ , obtain  $D_A$  using BAO data

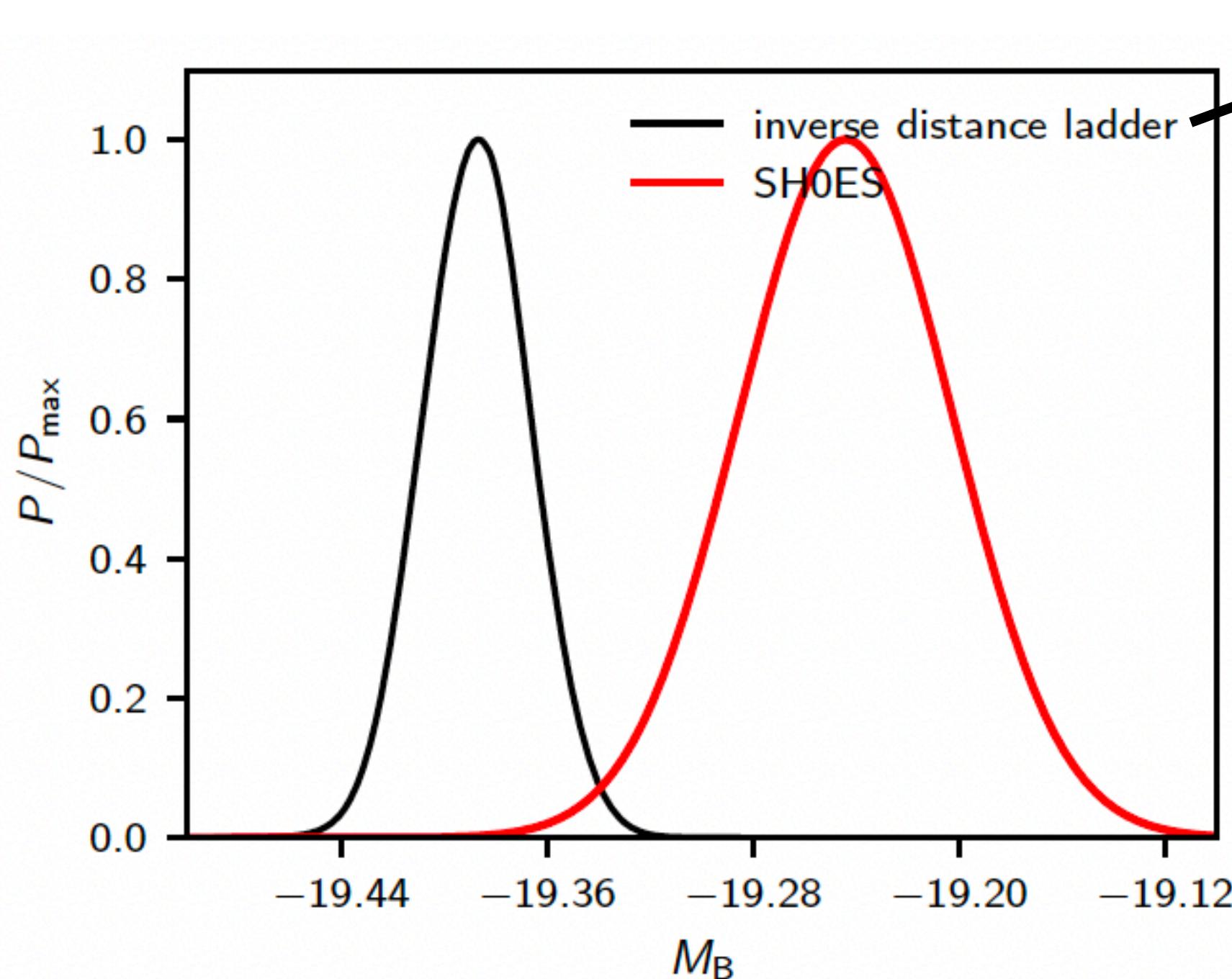
$$\theta_d(z)^\perp = \frac{r_s(z_{\text{drag}})}{D_A(z)}, \quad \theta_d(z)^\parallel = r_s(z_{\text{drag}})H(z)$$

$$D_L(z) = D_A(z)(1+z)^2$$

Obtain  $M_b$  from calibration const. of SNIA

$$m(z) = 5\log_{10}D_L(z) + \text{const}$$

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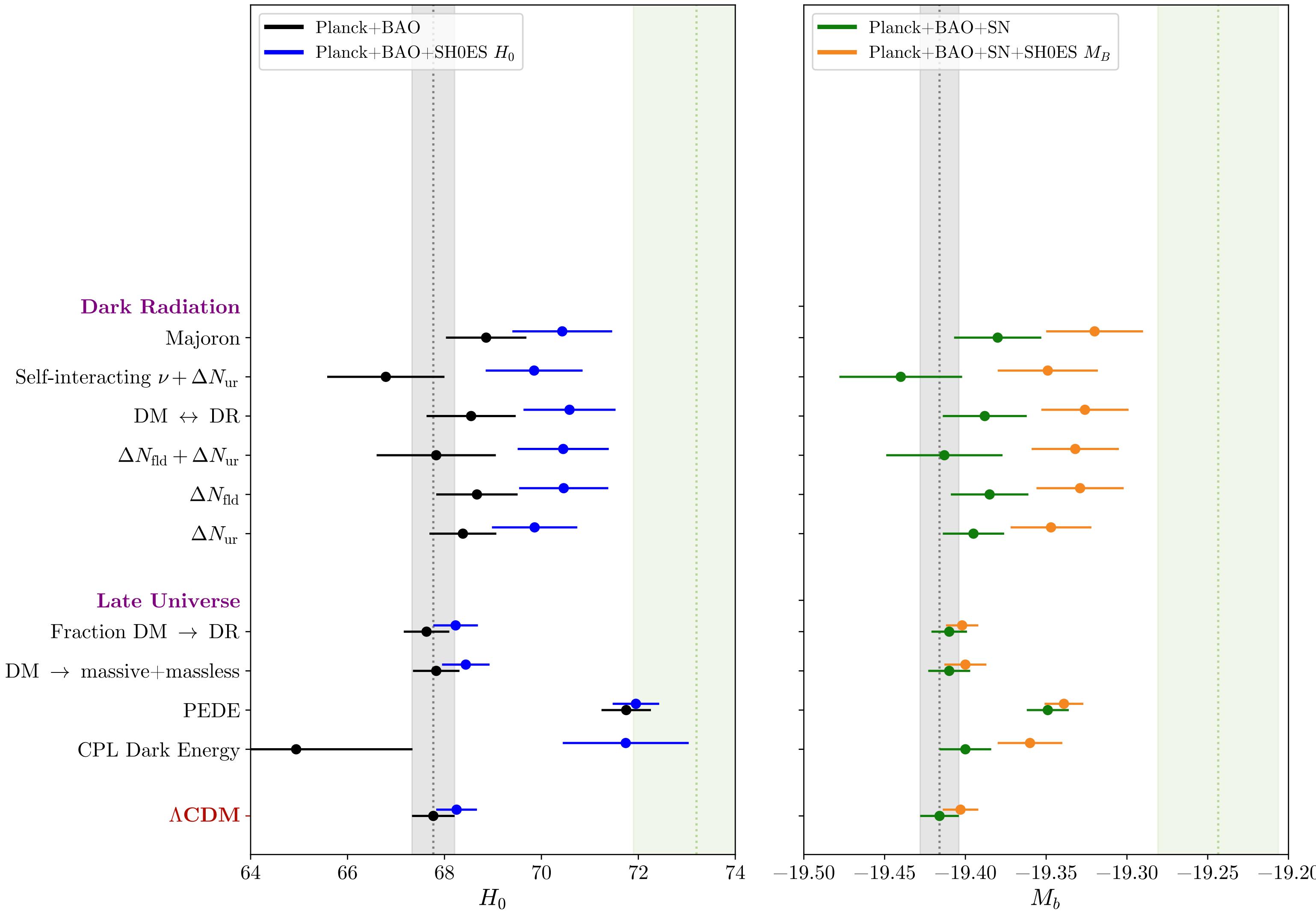
$$m(z) = 5\log_{10}D_L(z) + \text{const}$$

For  $r_s^{\Lambda\text{CDM}} = 147$  Mpc, inverse distance ladder disagrees with SH0ES

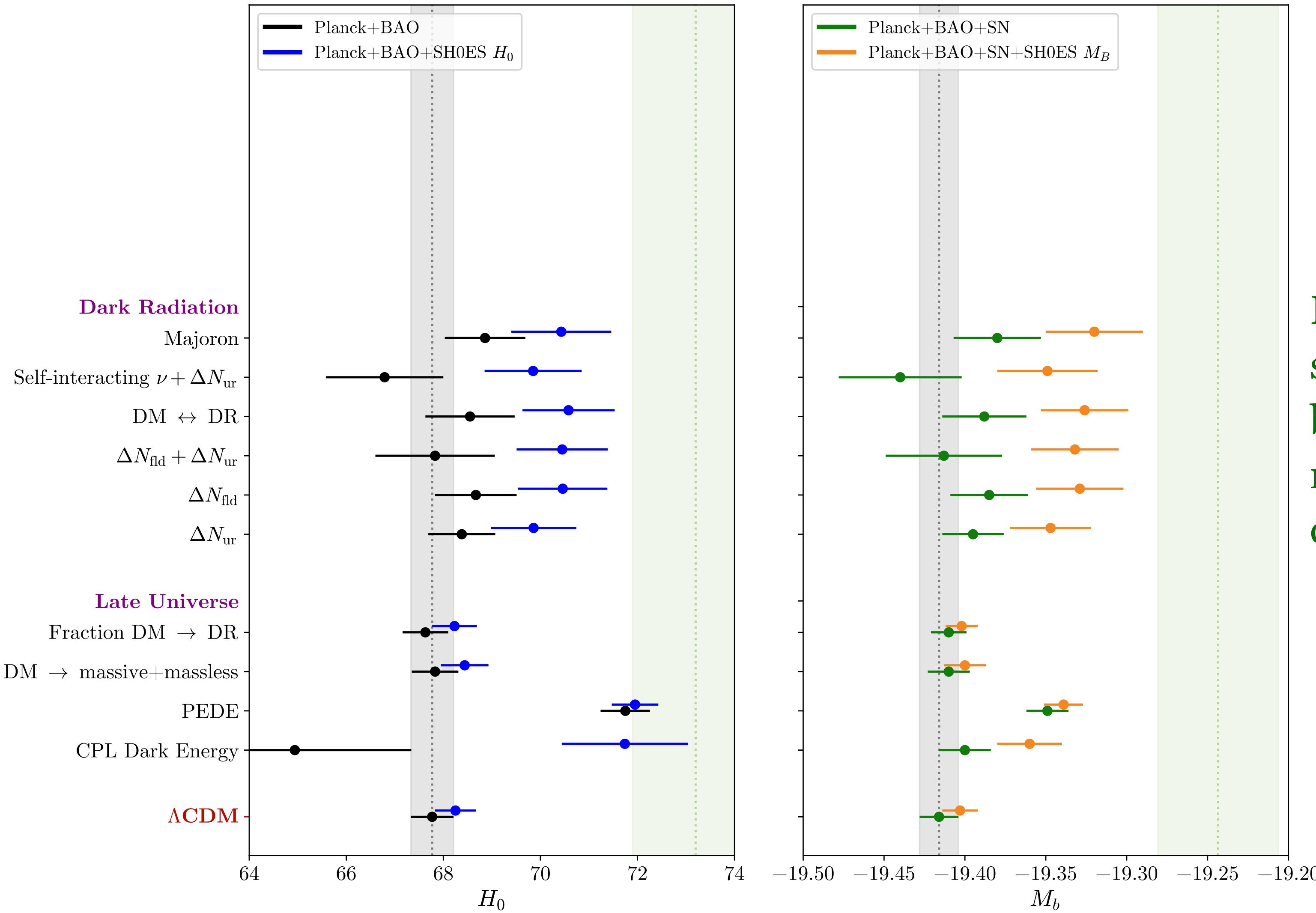
To make the two determinations agree, one is forced to reduce  $r_s$

**Ex:** Early Dark Energy or exotic neutrino interactions

# Results of the contest

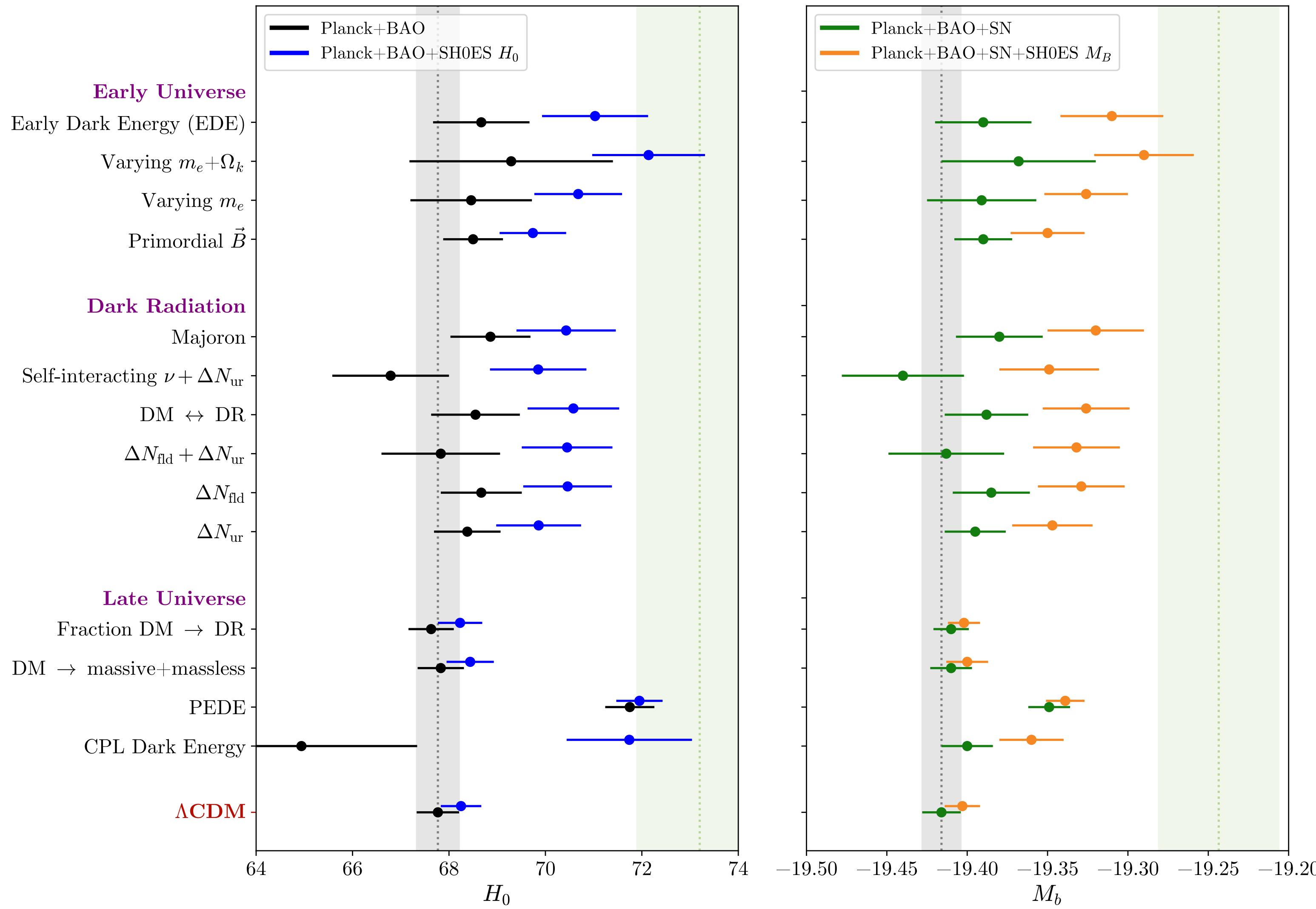


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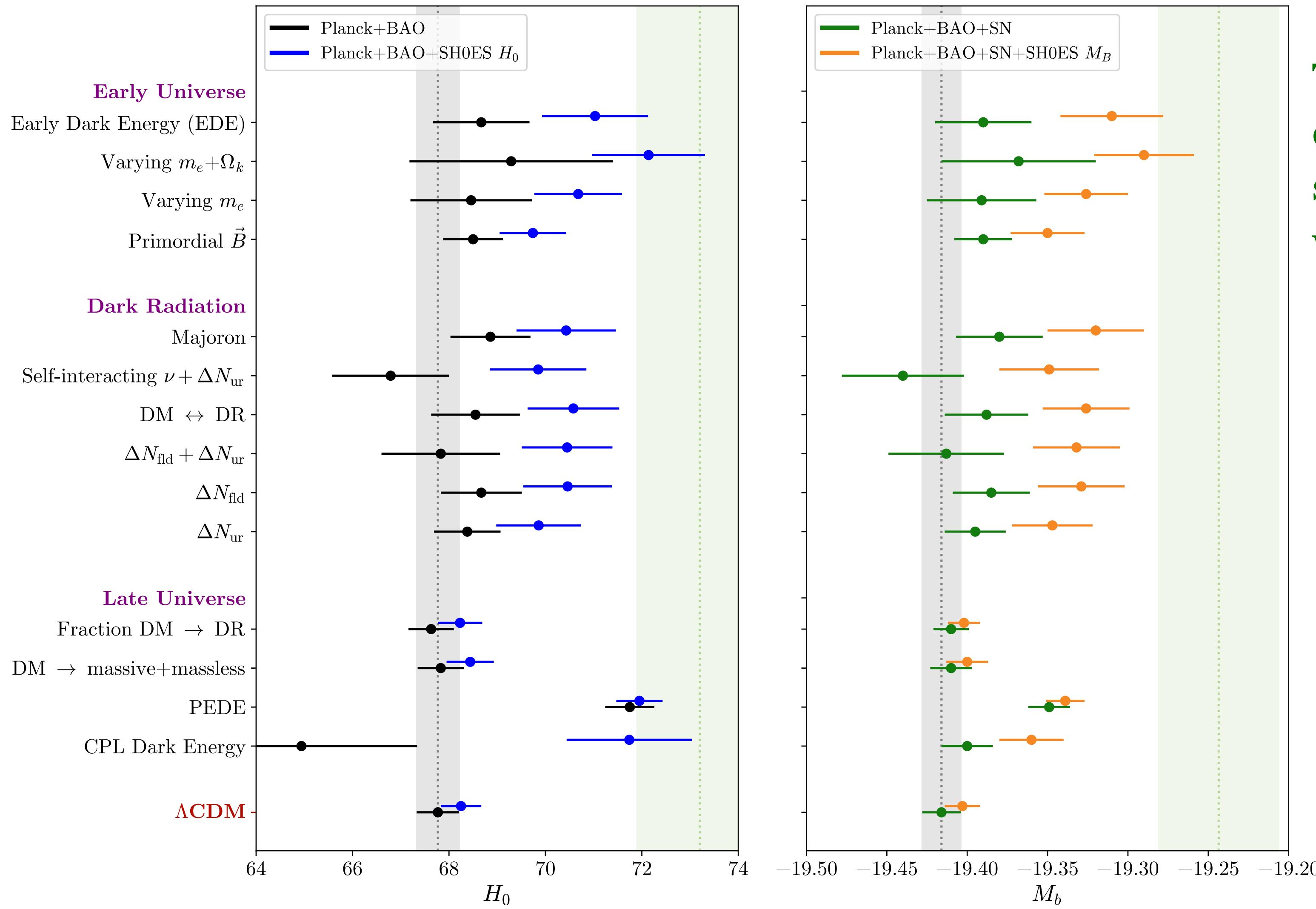


Dark radiation solutions work better, but remain very constrained

# Results of the contest



# Results of the contest



This is the category of solutions that work the best

# Results of the contest



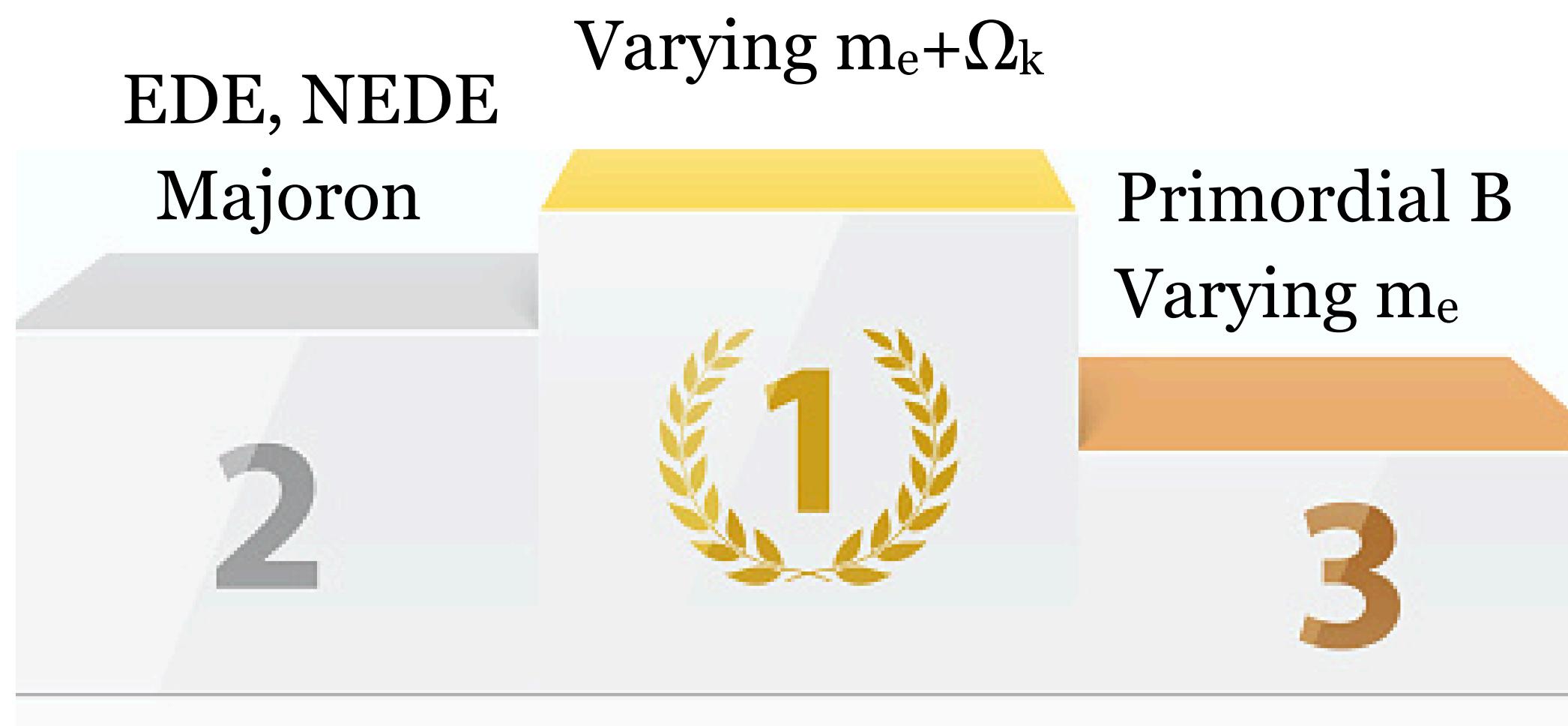
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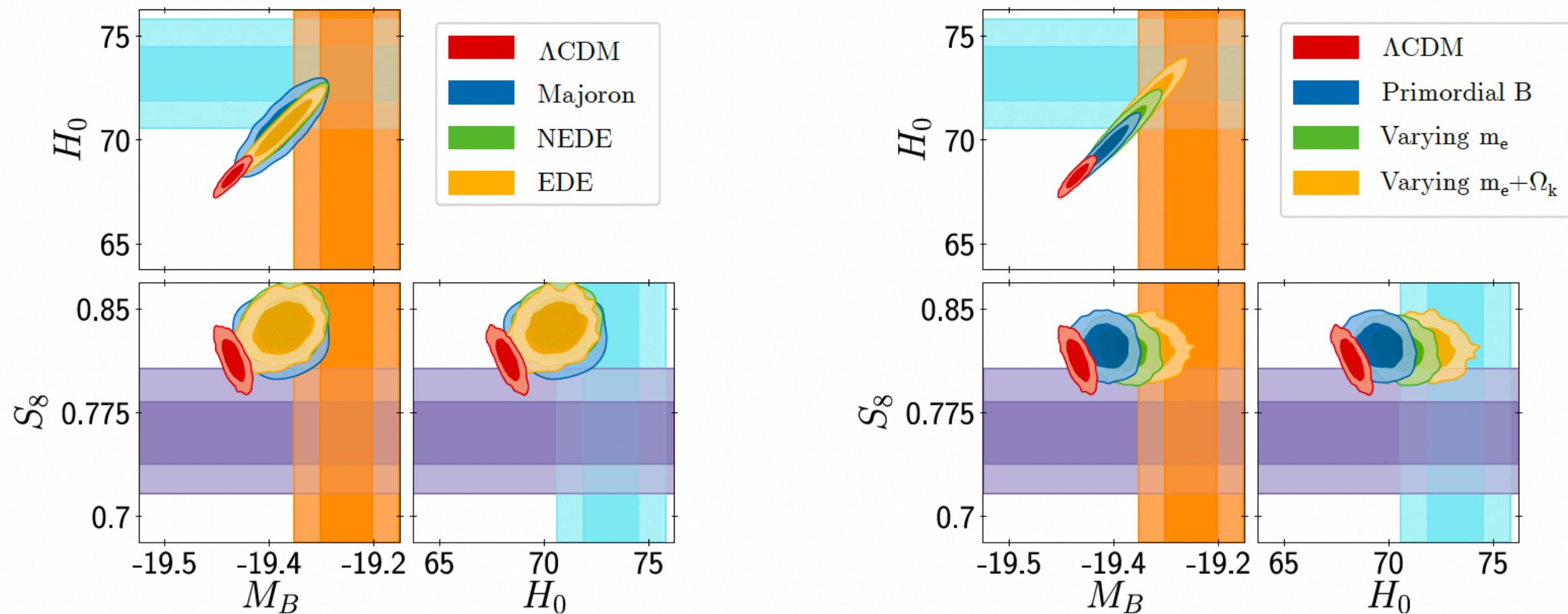


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Unfortunately, the most successful models are unable to explain the  $S_8$  tension

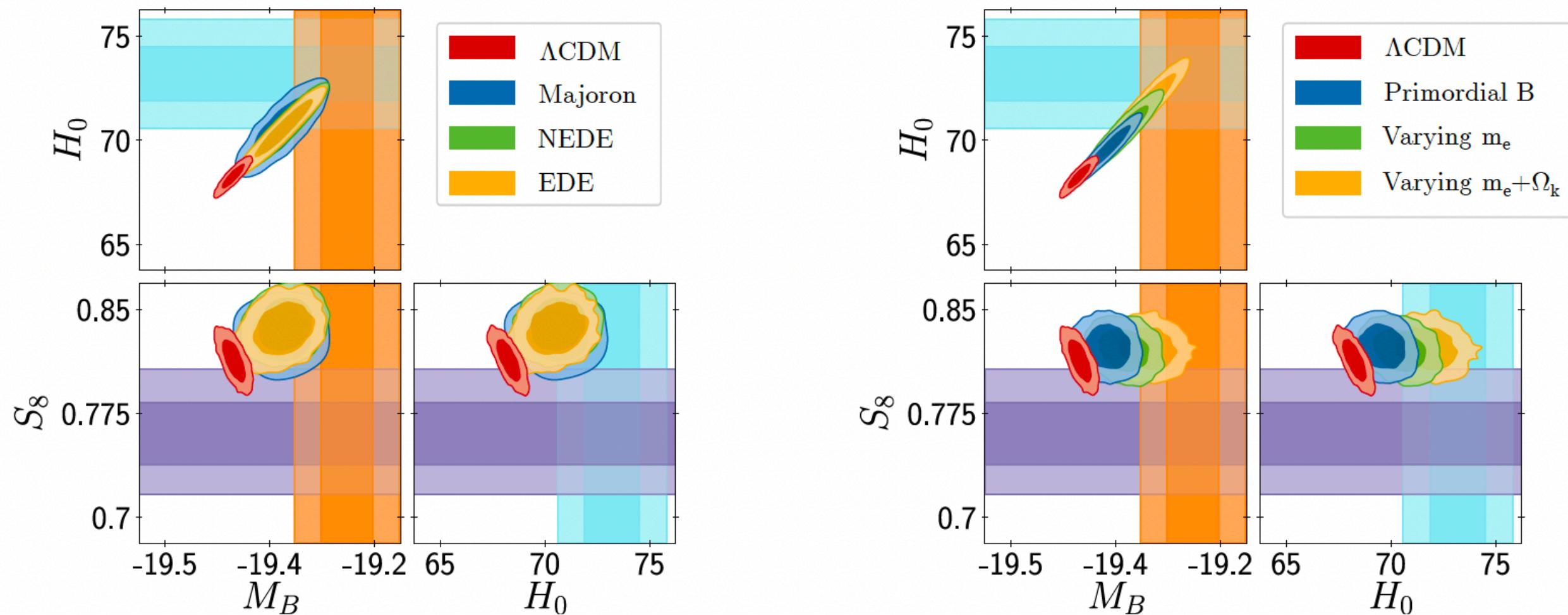


[Schöneberg, GFA, Pérez, Witte, Poulin, Lesgourgues 2107.10291](#)

Does this mean that adding **Large Scale Structure** data rules out the resolution of some of the winners (e.g. **Early Dark Energy**)?

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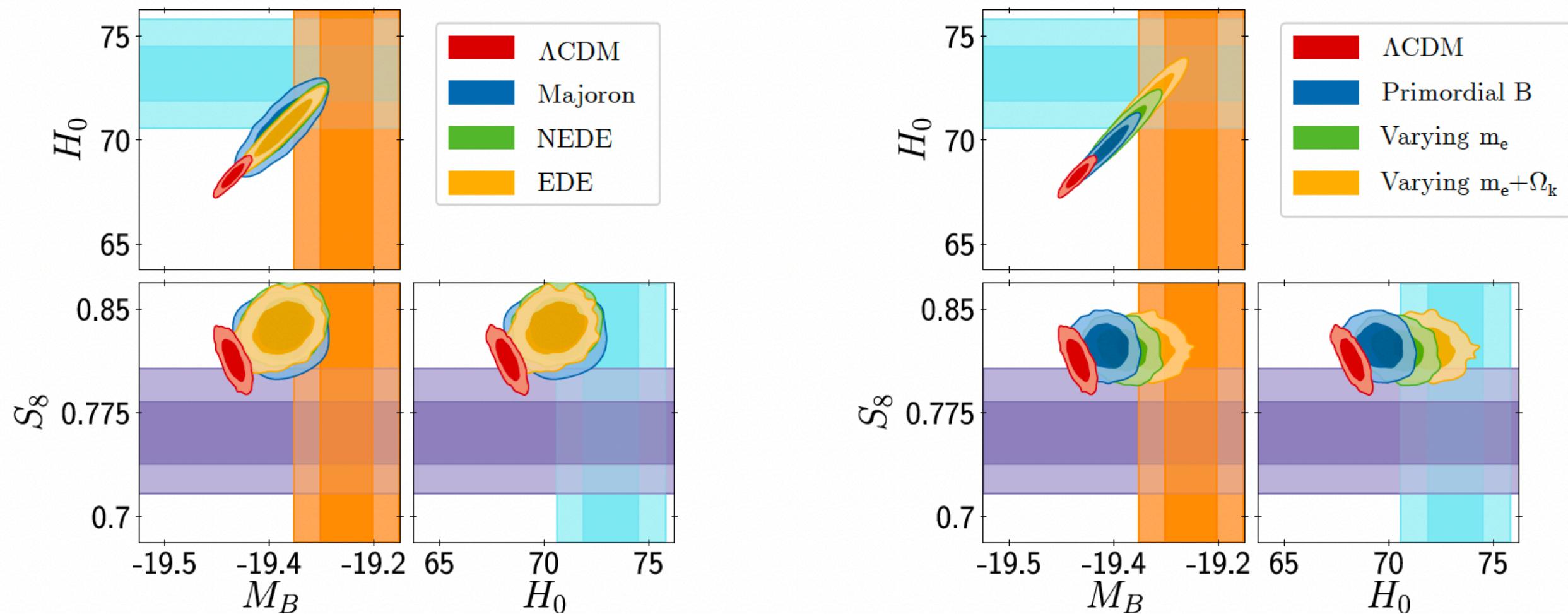
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The answer is no! [Murgia, GFA, Poulin 2107.10291](#)

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The answer is no! [Murgia, GFA, Poulin 2107.10291](#)

Is there any model that could explain the  $S_8$  anomaly?

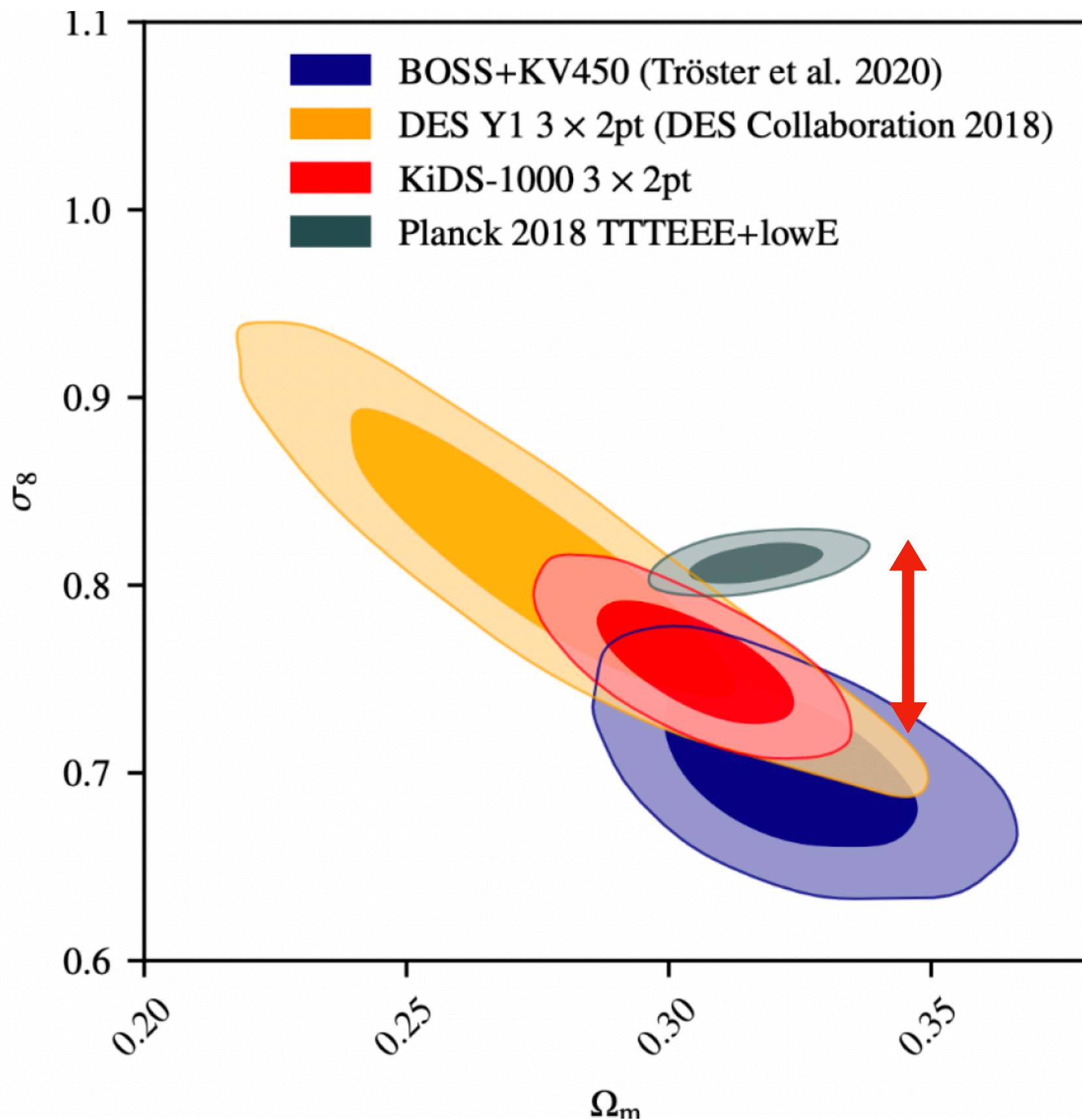
### **III. Explaining the $S_8$ tension with Decaying Dark Matter**

In collaboration with Riccardo Murgia, Vivian Poulin and Julien Lavalle

# What is needed to resolve the $S_8$ tension?

Di Valentino++ 2008.11285

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3}$$



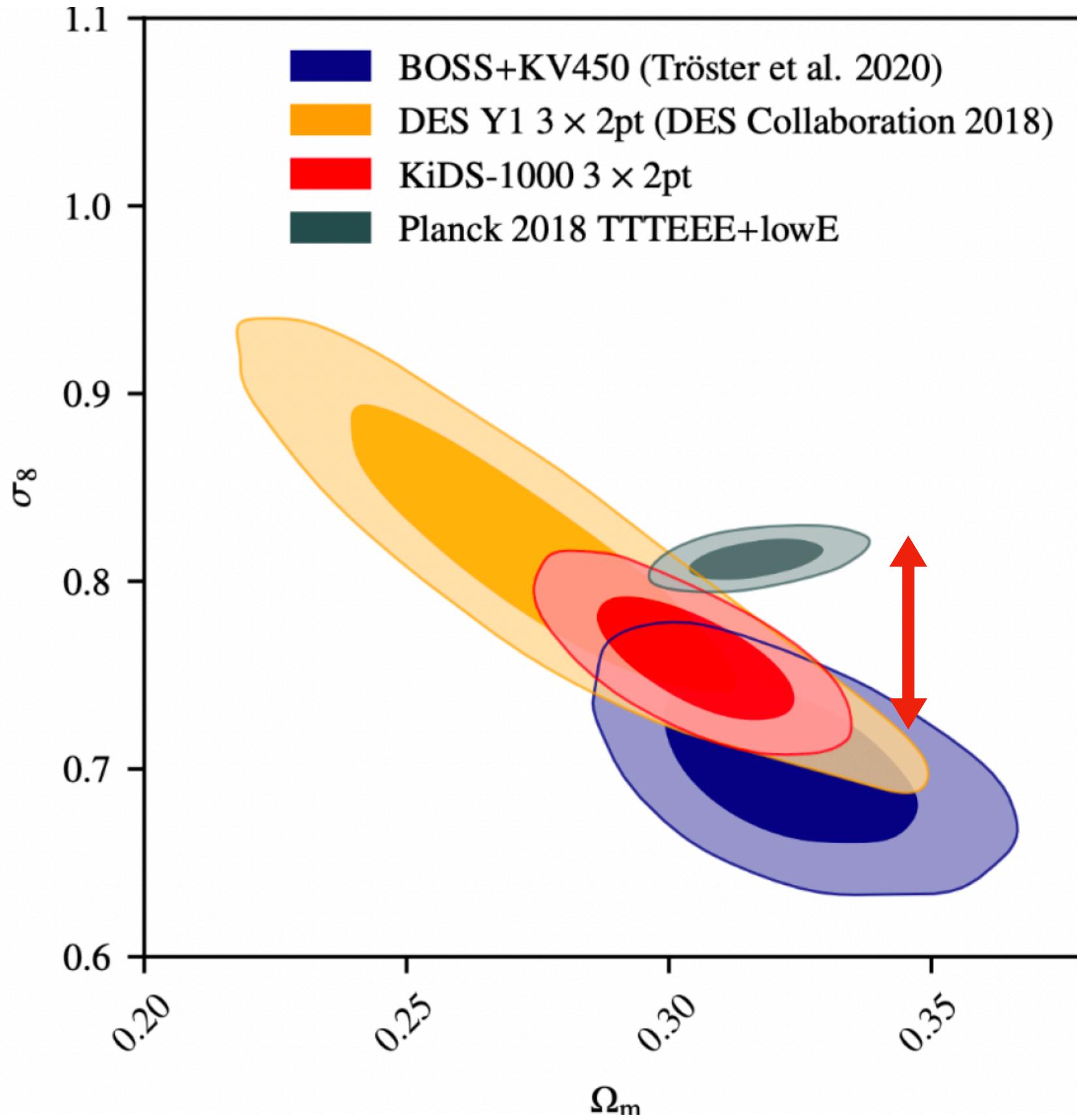
$\Omega_m$  should be left unchanged

$$\sigma_8 = \int P_m(k, z=0) W_R^2(k) d\ln k$$

# What is needed to resolve the $S_8$ tension?

Di Valentino++ 2008.11285

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3}$$



Ex: Warm Dark Matter

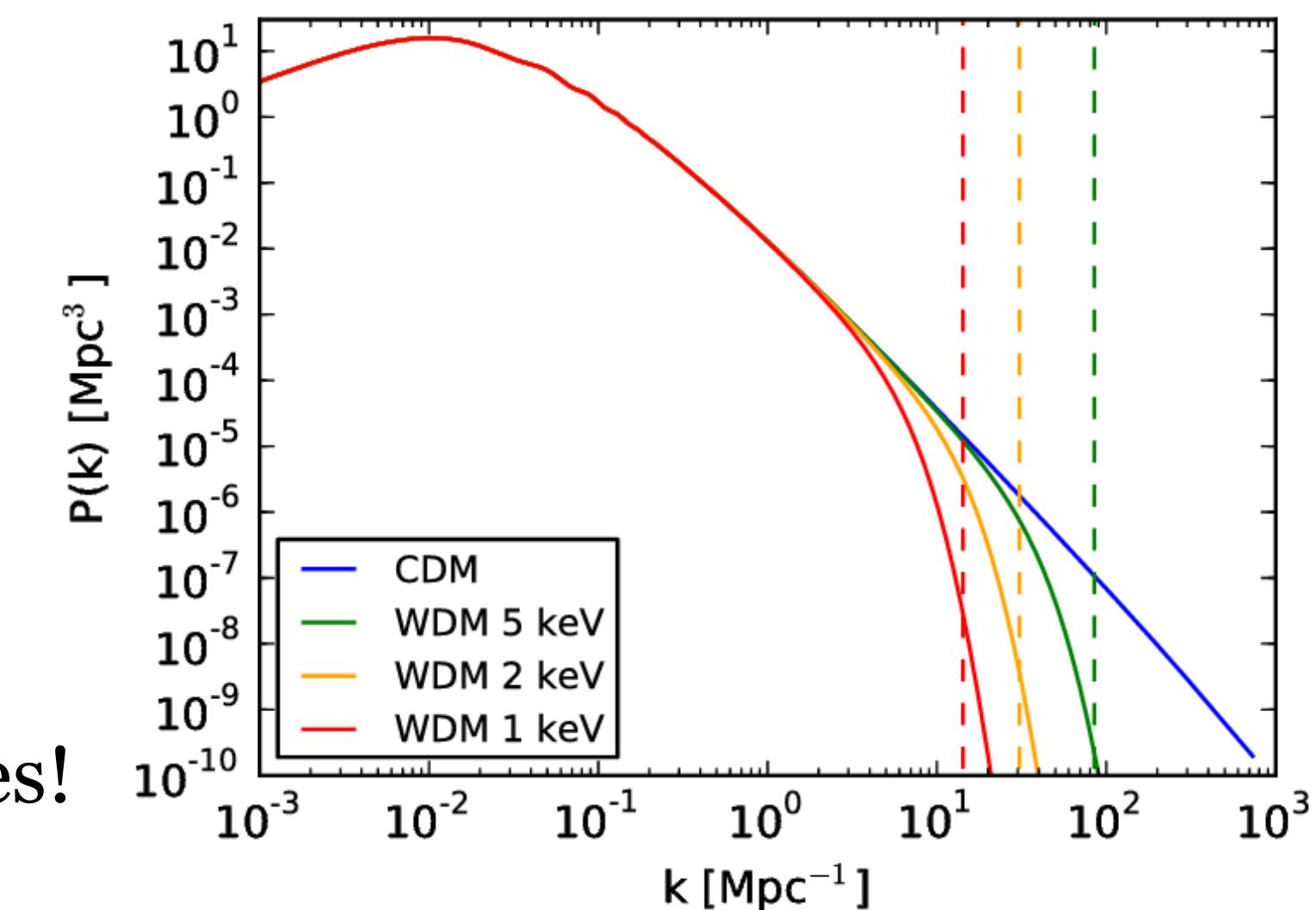
Very constrained by many probes!

$\Omega_m$  should be left unchanged

$$\sigma_8 = \int P_m(k, z=0) W_R^2(k) dk$$

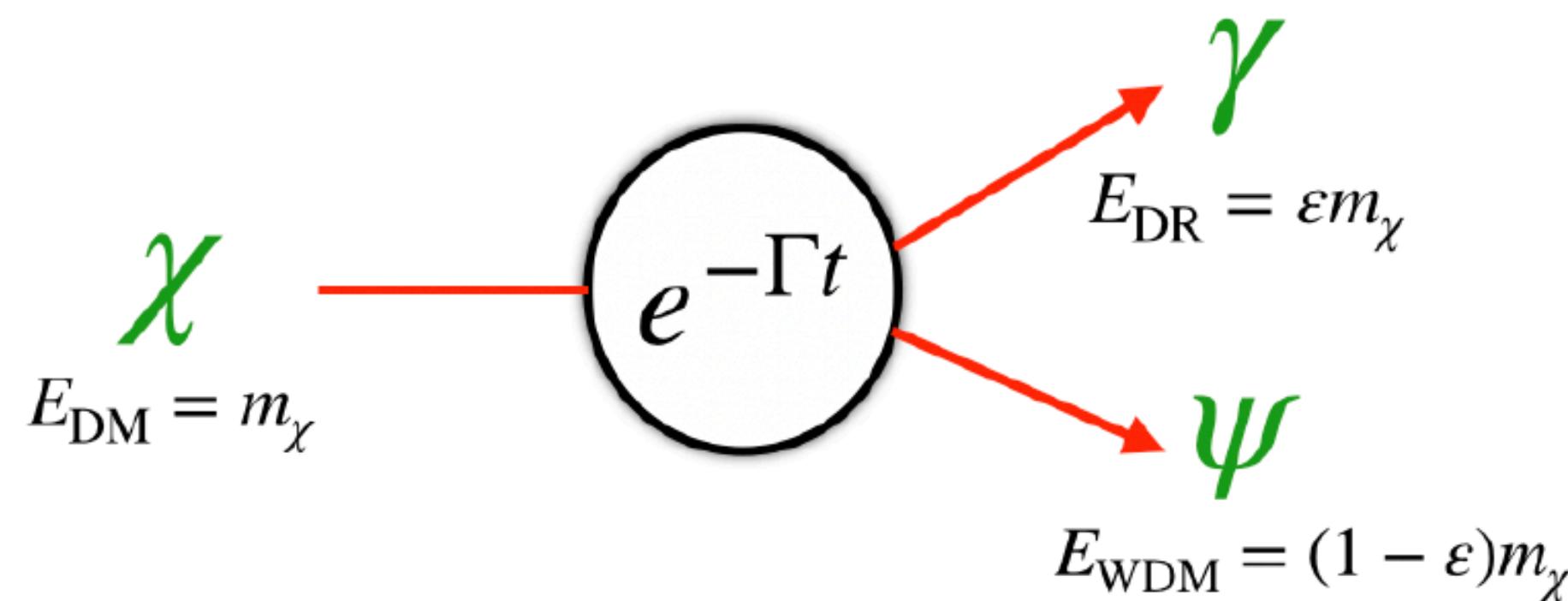


Need to **suppress power** at scales  $k \sim 0.1 - 1 h/\text{Mpc}$



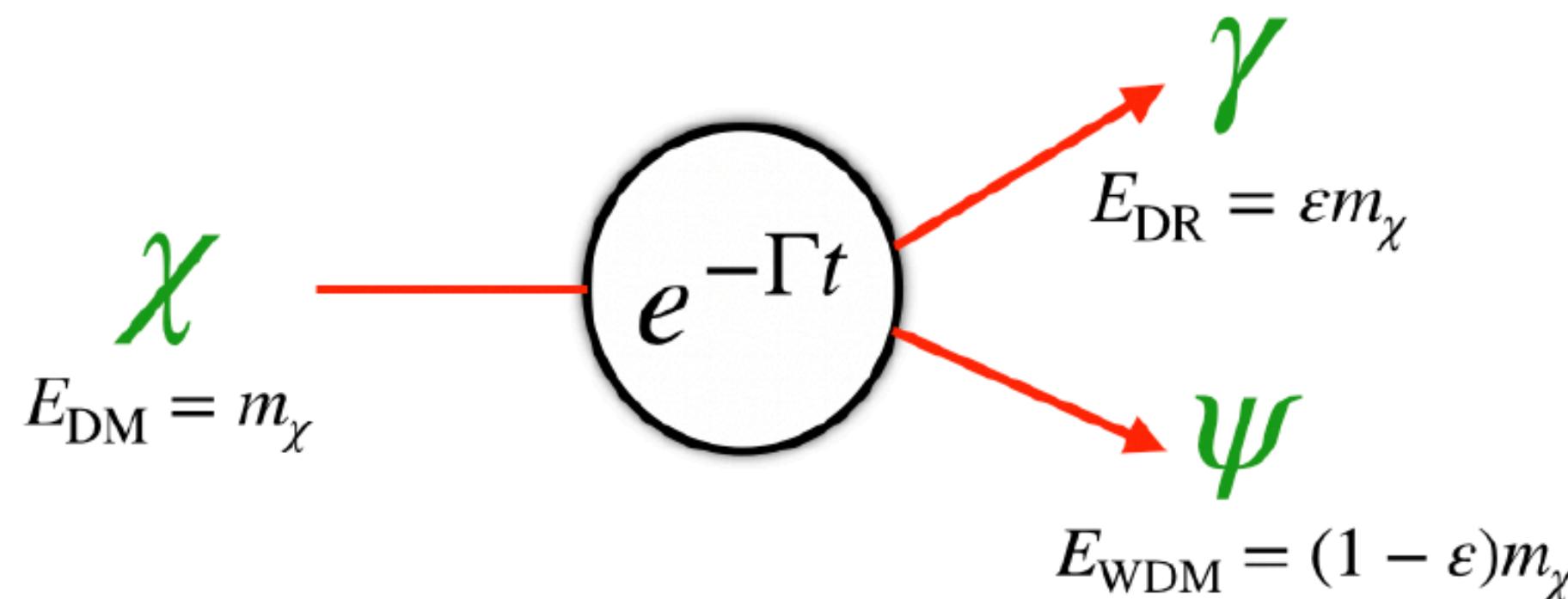
# 2-body Dark Matter decay

We explore DM decays to massless (**Dark Radiation**) and massive (**Warm Dark Matter**) particles,  $\chi(\text{DM}) \rightarrow \gamma(\text{DR}) + \psi(\text{WDM})$



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The model is fully specified by:

$$\{\Gamma, \varepsilon\} \text{ where } \varepsilon = \frac{1}{2} \left( 1 - \frac{m_\psi^2}{m_\chi^2} \right) \begin{cases} = 0 \text{ for } \Lambda\text{CDM} \\ = 1/2 \text{ for } \text{DM} \rightarrow \text{DR} \end{cases}$$

# 2-body Dark Matter decay

Aoyama++ 1402.2972



Full treatment of perts.

No parameter scan

Vattis++ 1903.06220



Resolution to  $H_0$  tension ?

Haridasu&Viel 2004.07709



SNIa+BAO rule out solution

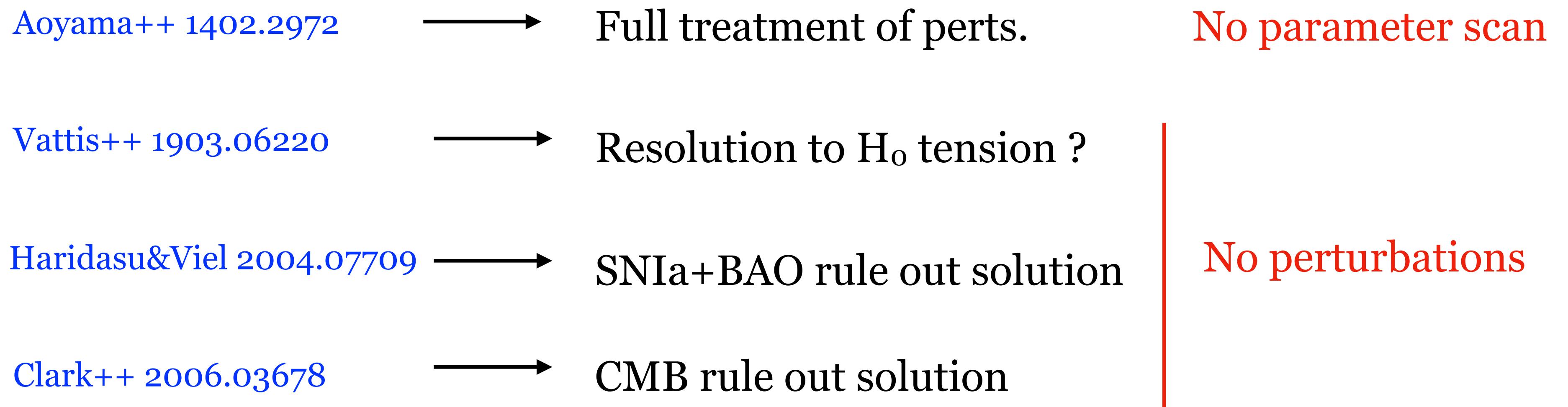
No perturbations

Clark++ 2006.03678



CMB rule out solution

# 2-body Dark Matter decay



**Our goal:** Perform parameter scan by including full treatment of linear perts, in order to assess the impact on the  $S_8$  tension

→ Track  $\delta_i$ ,  $\theta_i$  and  $\sigma_i$  for  $i = \text{dm, dr, wdm}$

# Evolution of perturbations: fluid equations

New fluid eqs.\*, based on previous approximation for massive neutrinos

Lesgourgues & Tram, 1104.2935

$$\dot{\delta}_{\text{wdm}} = -3aH(c_{\text{syn}}^2 - w)\delta_{\text{wdm}} - (1 + w) \left( \theta_{\text{wdm}} + \frac{\dot{h}}{2} \right) + a\Gamma(1 - \varepsilon) \frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}} (\delta_{\text{dm}} - \delta_{\text{wdm}})$$

$$\dot{\theta}_{\text{wdm}} = -aH(1 - 3c_a^2)\theta_{\text{wdm}} + \frac{c_{\text{syn}}^2}{1 + w} k^2 \delta_{\text{wdm}} - k^2 \sigma_{\text{wdm}} - a\Gamma(1 - \varepsilon) \frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}} \frac{1 + c_a^2}{1 + w} \theta_{\text{wdm}}$$

\*Implemented in modified version of public Boltzmann solver CLASS

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where

$$c_a^2(\tau) = w\left(5 - \frac{p_{\text{wdm}}}{P_{\text{wdm}}} - \frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}}\frac{\Gamma}{3wH}\frac{\varepsilon^2}{1-\varepsilon}\right)\left[3(1+w) - \frac{\bar{\rho}_{\text{dm}}}{\bar{\rho}_{\text{wdm}}}\frac{\Gamma}{H}(1-\varepsilon)\right]^{-1}$$

and

$$c_{\text{syn}}^2(k, \tau) = c_a^2(\tau)[1 + (1-2\varepsilon)T(k/k_{\text{fs}})]$$

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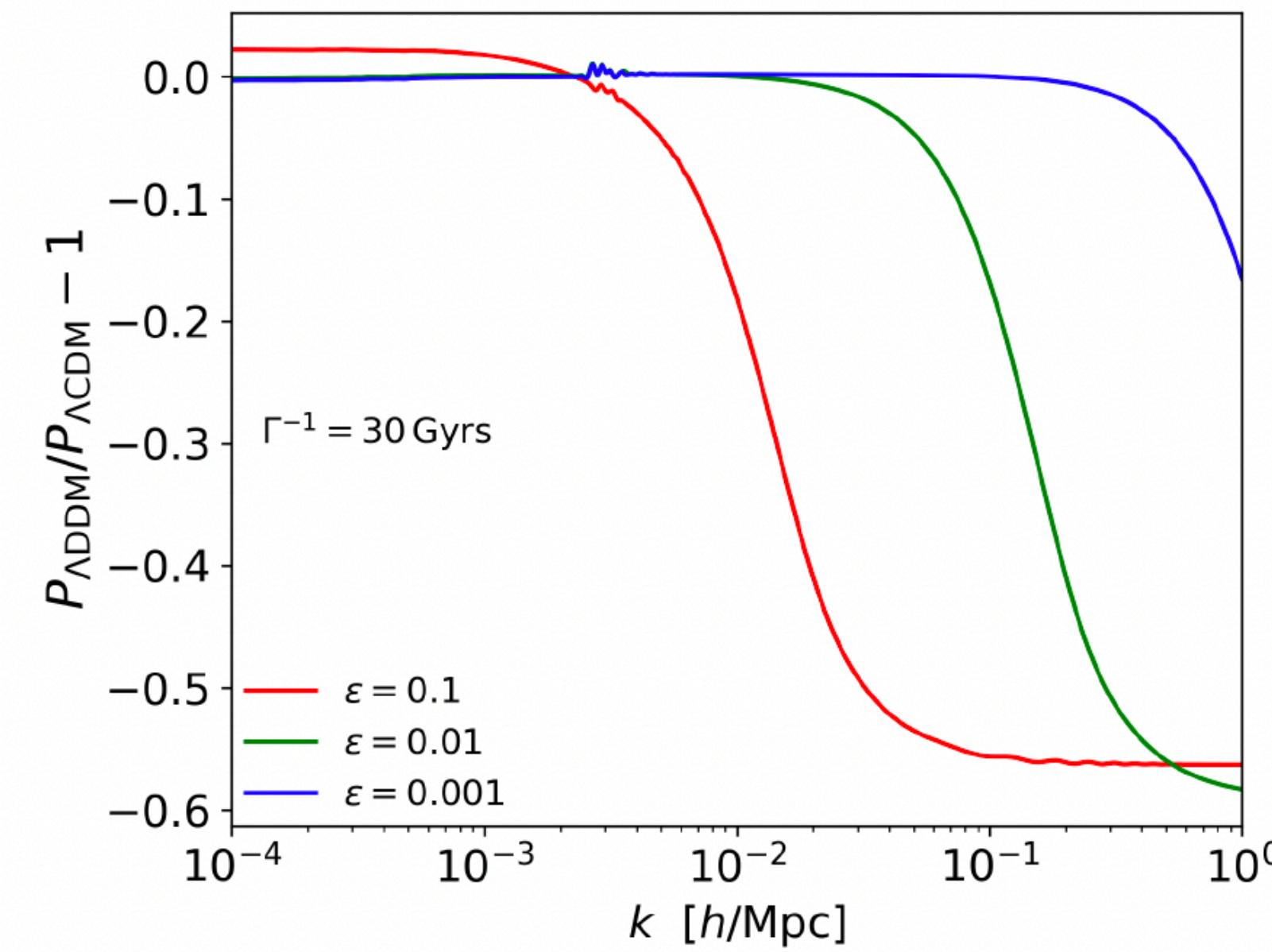
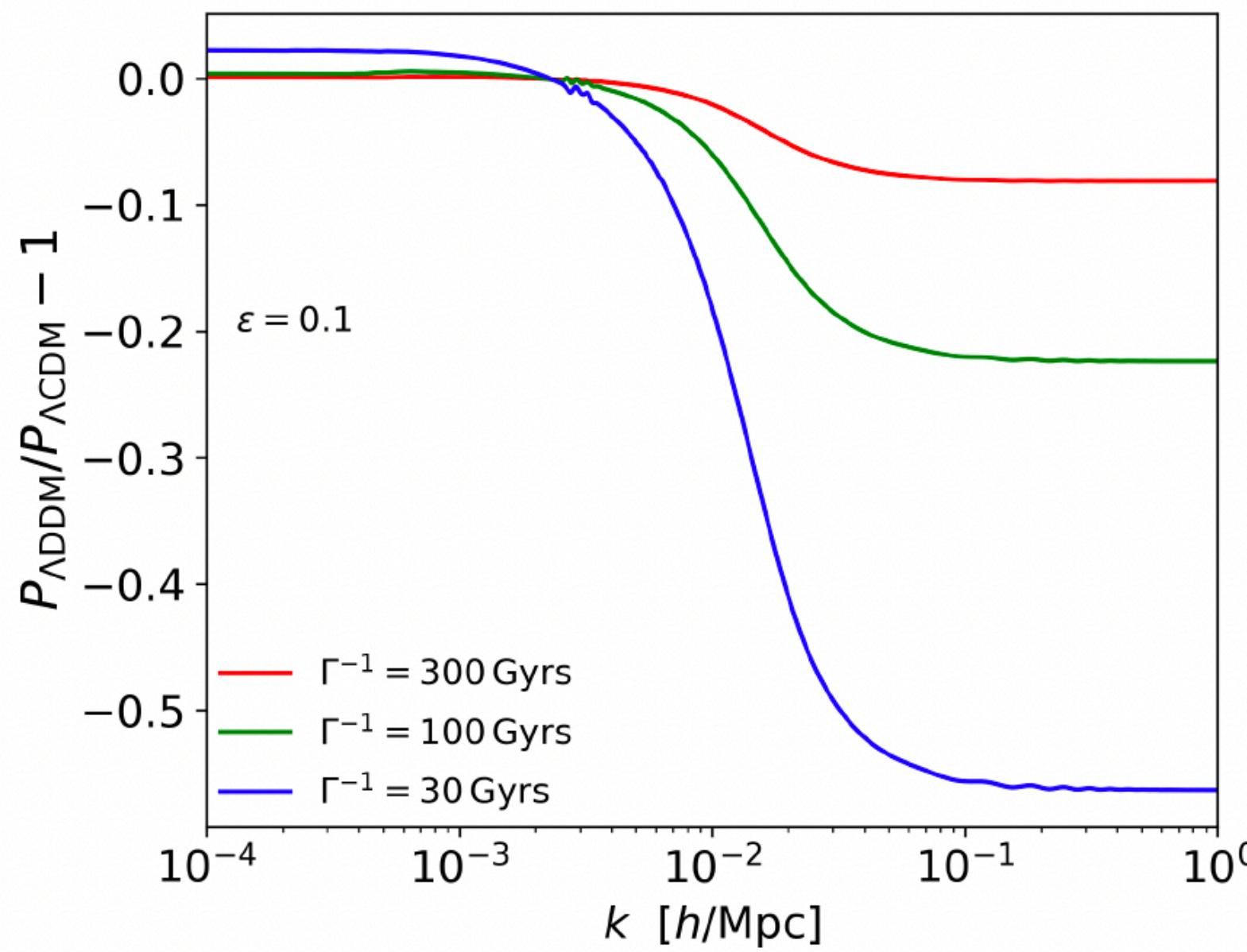
$$c_{\text{syn}}^2(k, \tau) = c_a^2(\tau)[1 + (1-2\varepsilon)T(k/k_{\text{fs}})]$$

**CPU time reduced from  $\sim 1$  day to  $\sim 1$  minute!**

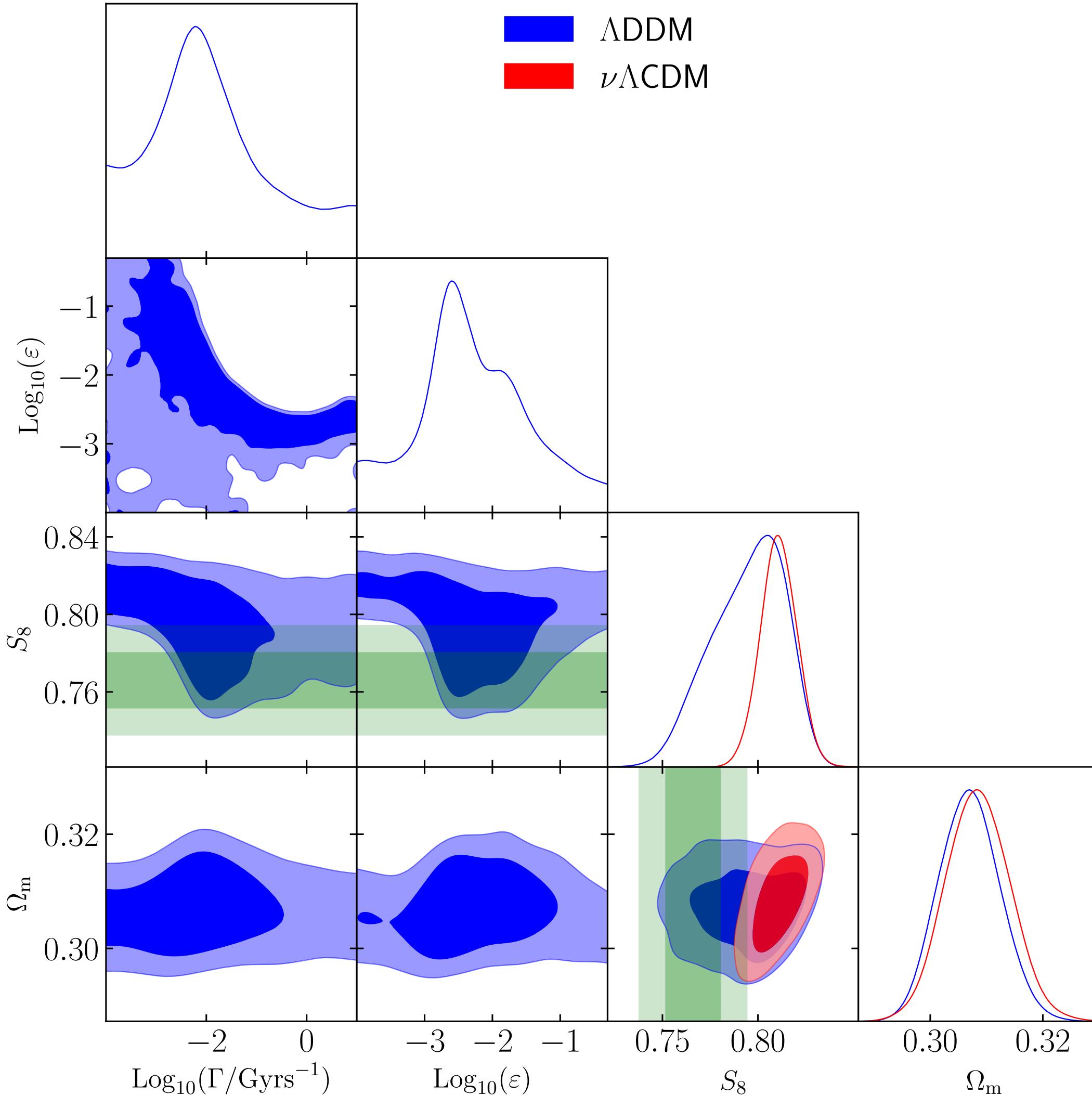
\*Implemented in modified version of public Boltzmann solver CLASS

# Impact of decaying DM on the matter spectrum

The WDM daughter leads to a power suppression in  $P_m(k)$  at small scales  $k > k_{fs}$ , where  $k_{fs} \sim aH/c_a$

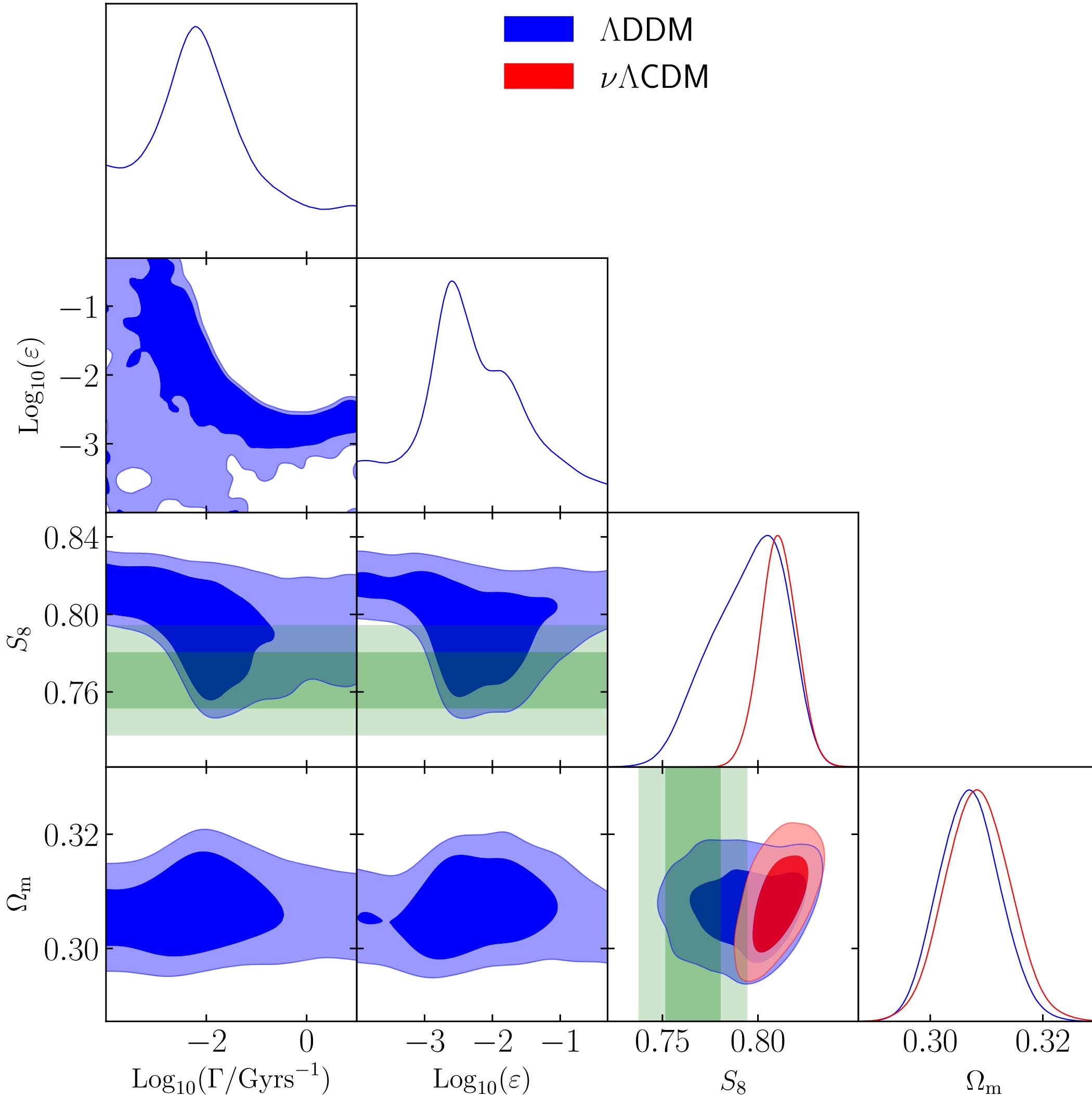


# Resolution to the $S_8$ tension



- MCMC analysis using Planck+BAO+SNIa+prior on  $S_8$  from KIDS+BOSS+2dfLenS

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- MCMC analysis using Planck+BAO+SNIa+prior on  $S_8$  from KIDS+BOSS+2dfLenS
- Reconstructed  $S_8$  values are in excellent agreement with WL data!

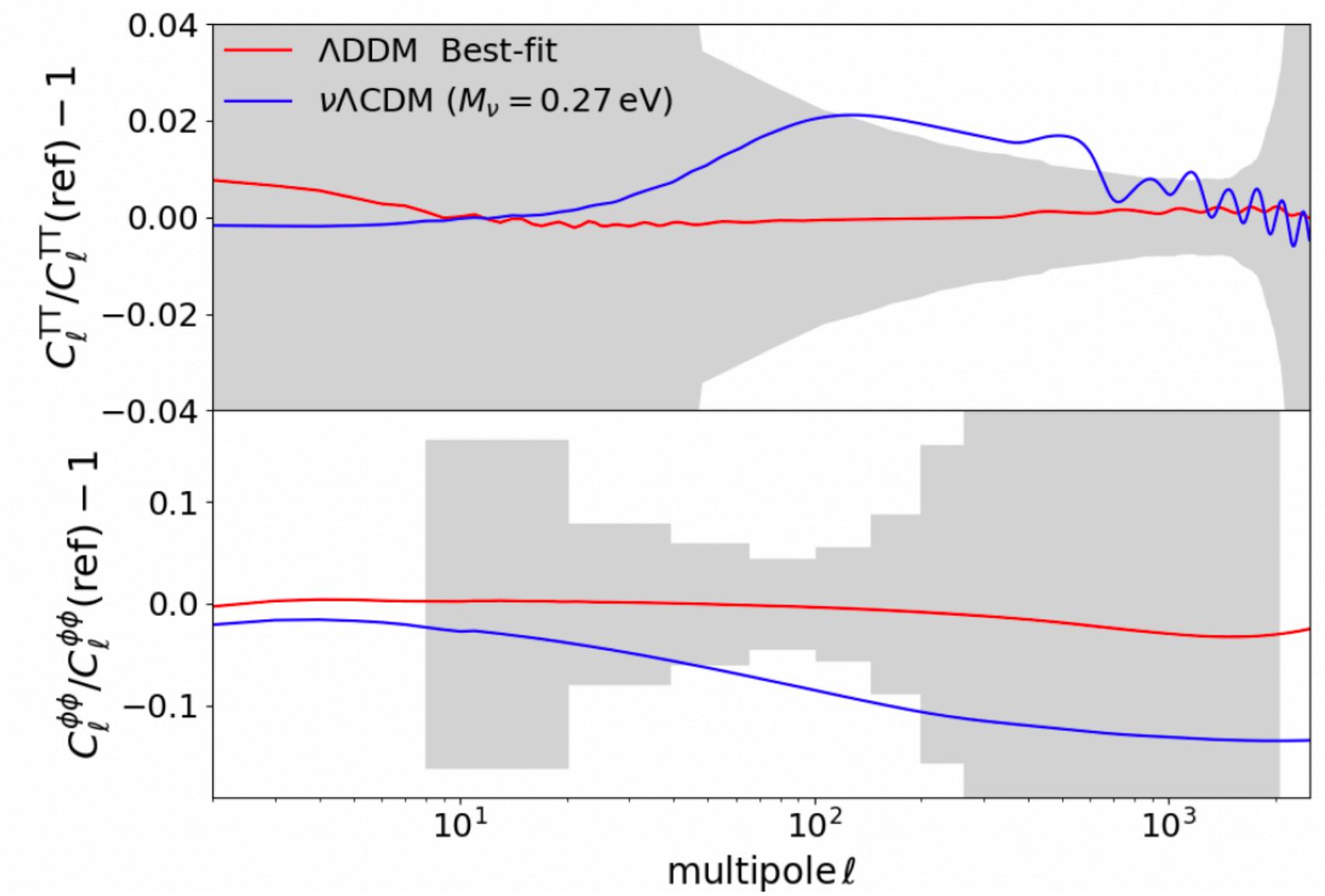
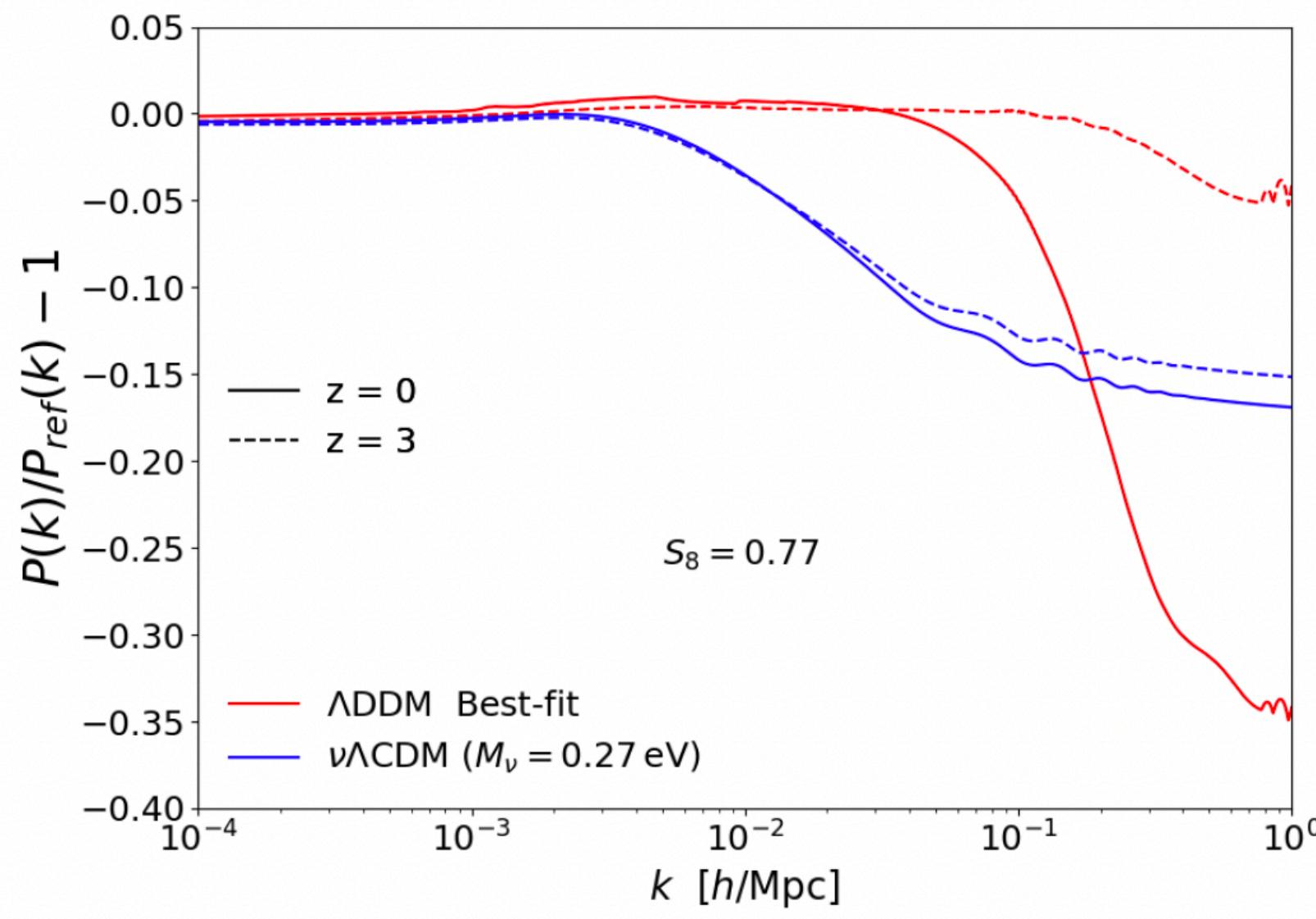
	$\nu\Lambda$ CDM	$\Lambda$ ADD M
$\chi^2_{\text{CMB}}$	1015.9	1015.2
$\chi^2_{S_8}$	5.64	0.002

$$\rightarrow \Delta\chi^2_{\min} \simeq -5.5$$

$$\Gamma^{-1} \simeq 55 (\varepsilon/0.007)^{1.4} \text{ Gyr}$$

# Why does the 2-body DM decay work better than massive neutrinos?

The 2-body decay gives a better fit thanks to the **time-dependence of the power suppression** and the cut-off scale



# Interesting implications

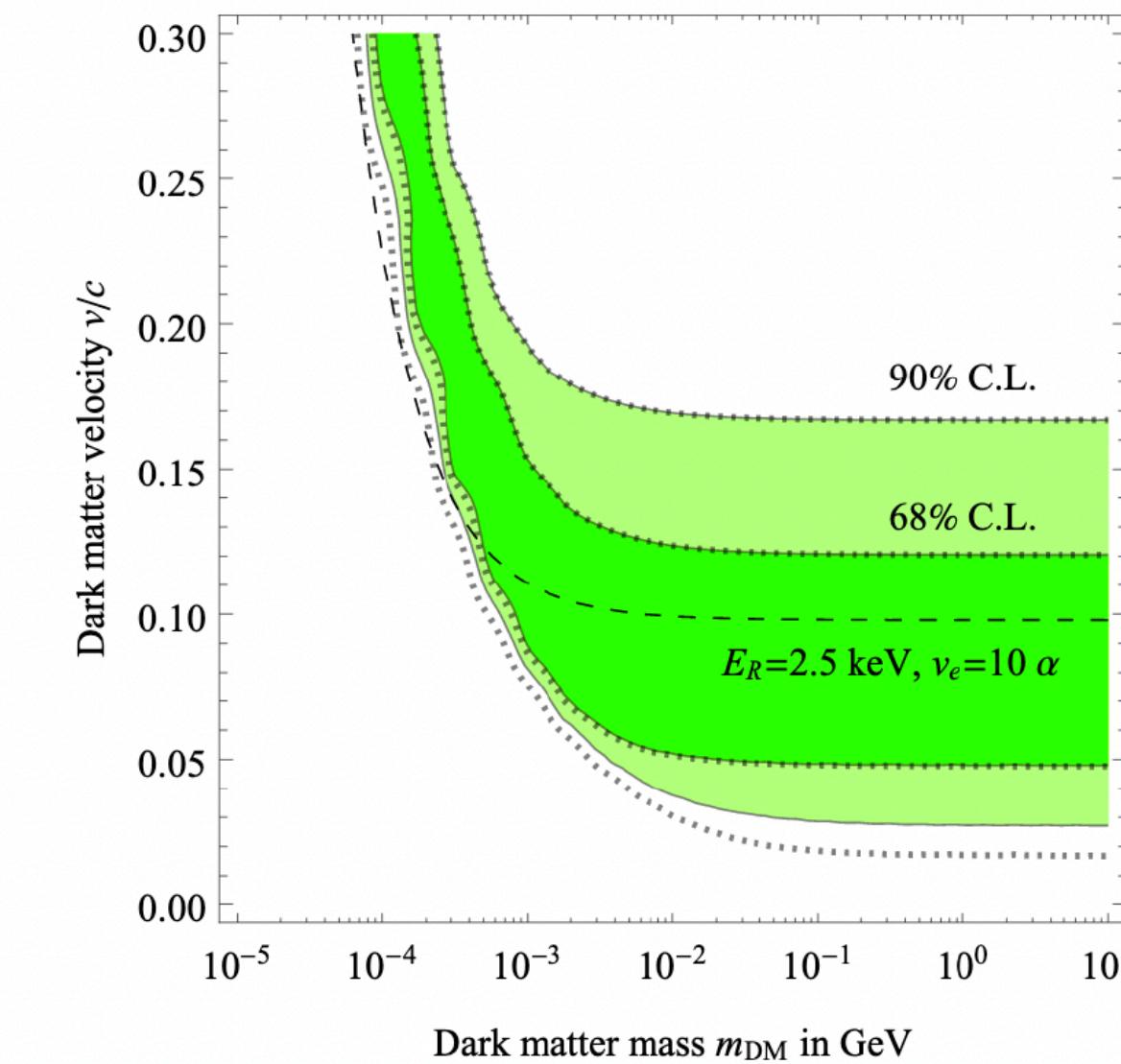
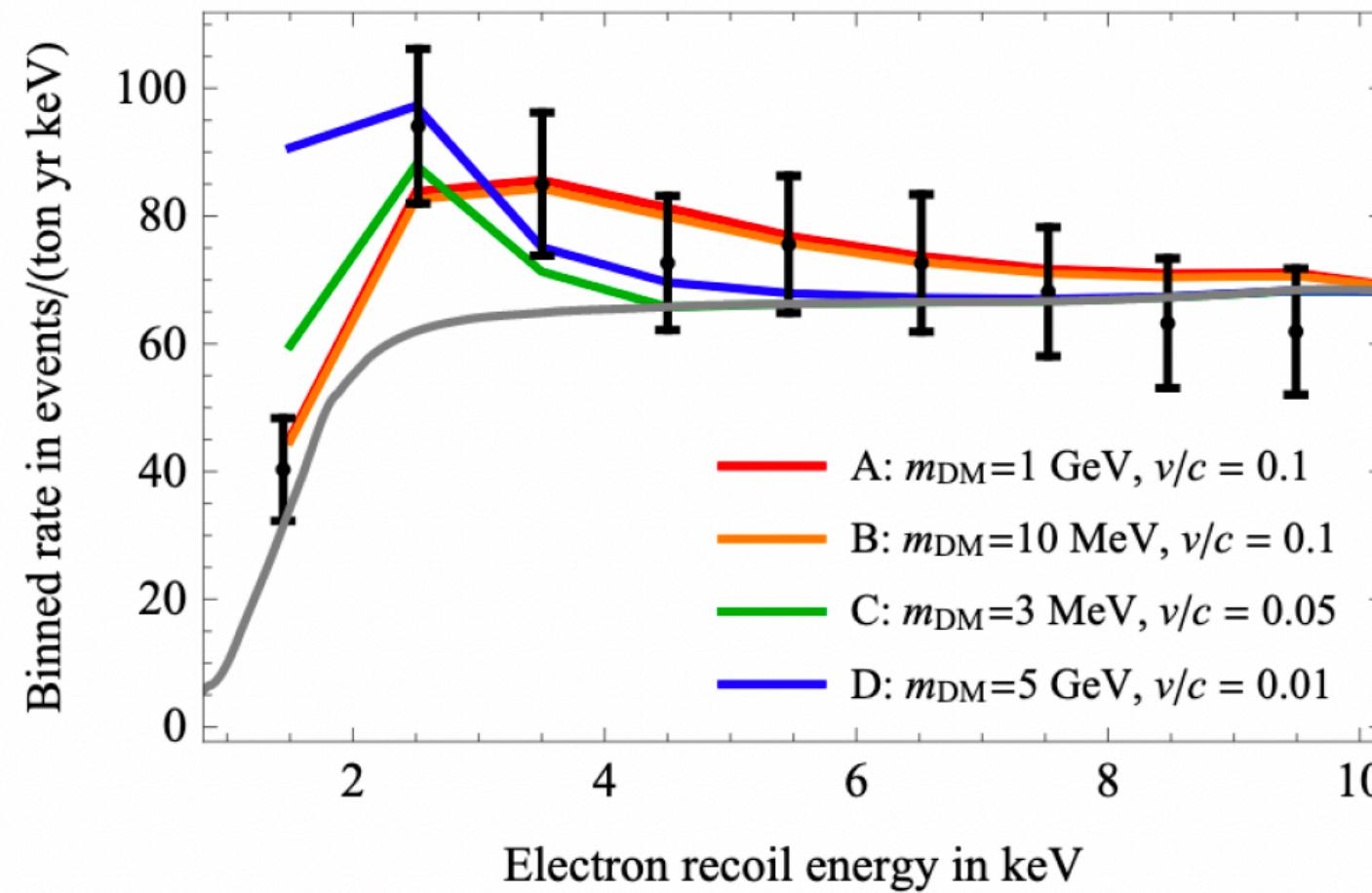
- Model building: Why  $\varepsilon \ll 1/2$ , i.e.  $m_{\text{wdm}} \sim m_{\text{dm}}$  ?  
Ex : Supergravity [Choi&Yanagida 2104.02958](#)

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- **Small-scale crisis of  $\Lambda$ CDM:** Reduction in the abundance of subhalos and their concentrations [Wang++ 1406.0527](#)

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- **Small-scale crisis of  $\Lambda$ CDM:** Reduction in the abundance of subhalos and their concentrations Wang++ [1406.0527](#)
- **Xenon-1T excess:** It could be explained by a fast DM component, such as the WDM, with  $v/c \simeq \varepsilon$  Kannike++ [2006.10735](#)



# Conclusions

- $\Lambda$ CDM provides a remarkable fit to many observations, but there exists a  $4\text{-}5\sigma$   **$H_0$  tension** and a  $2\text{-}3\sigma$   **$S_8$  tension**. These tensions offer an interesting **window** to the yet unknown **dark sector**.

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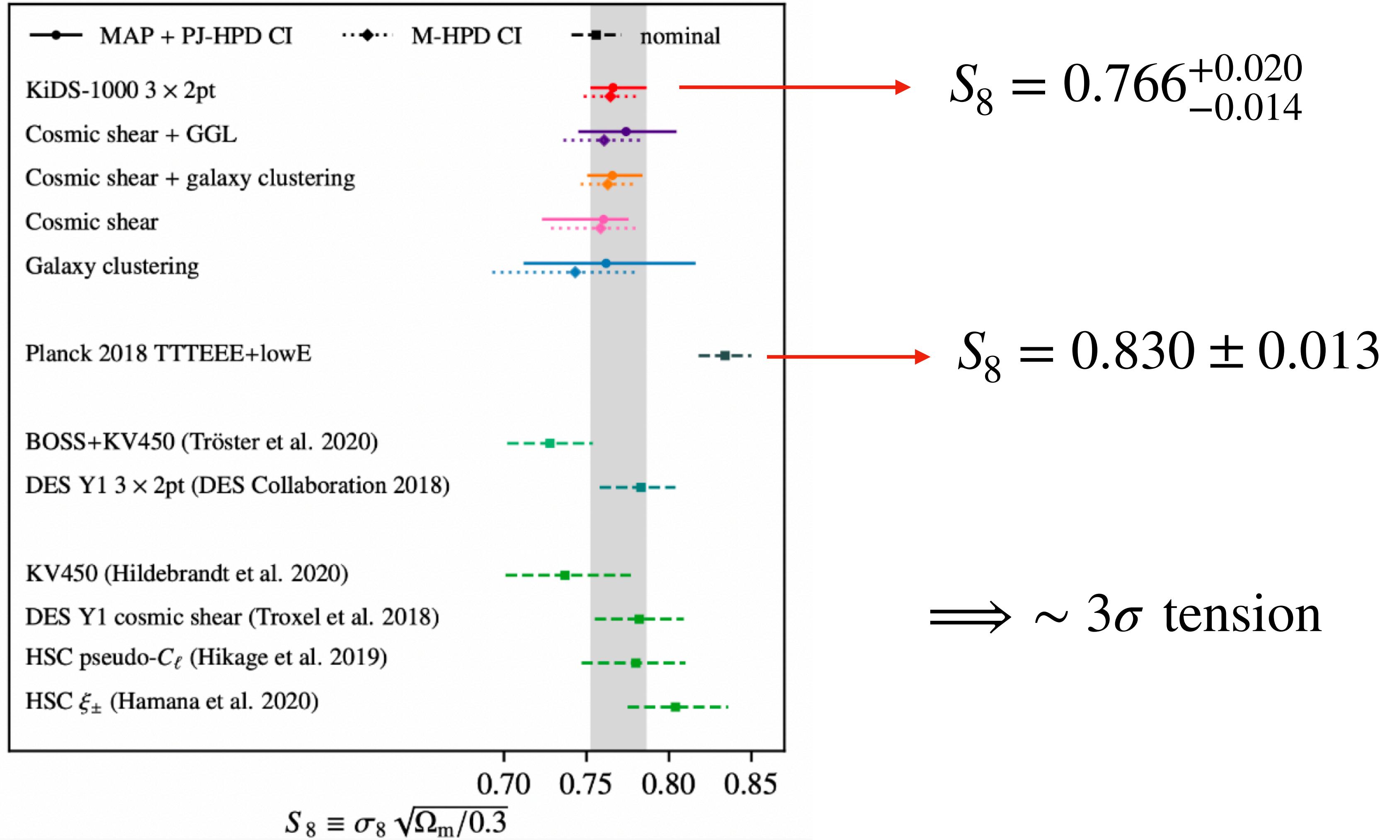
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**We might be on the verge of the discovery of a rich dark sector!**

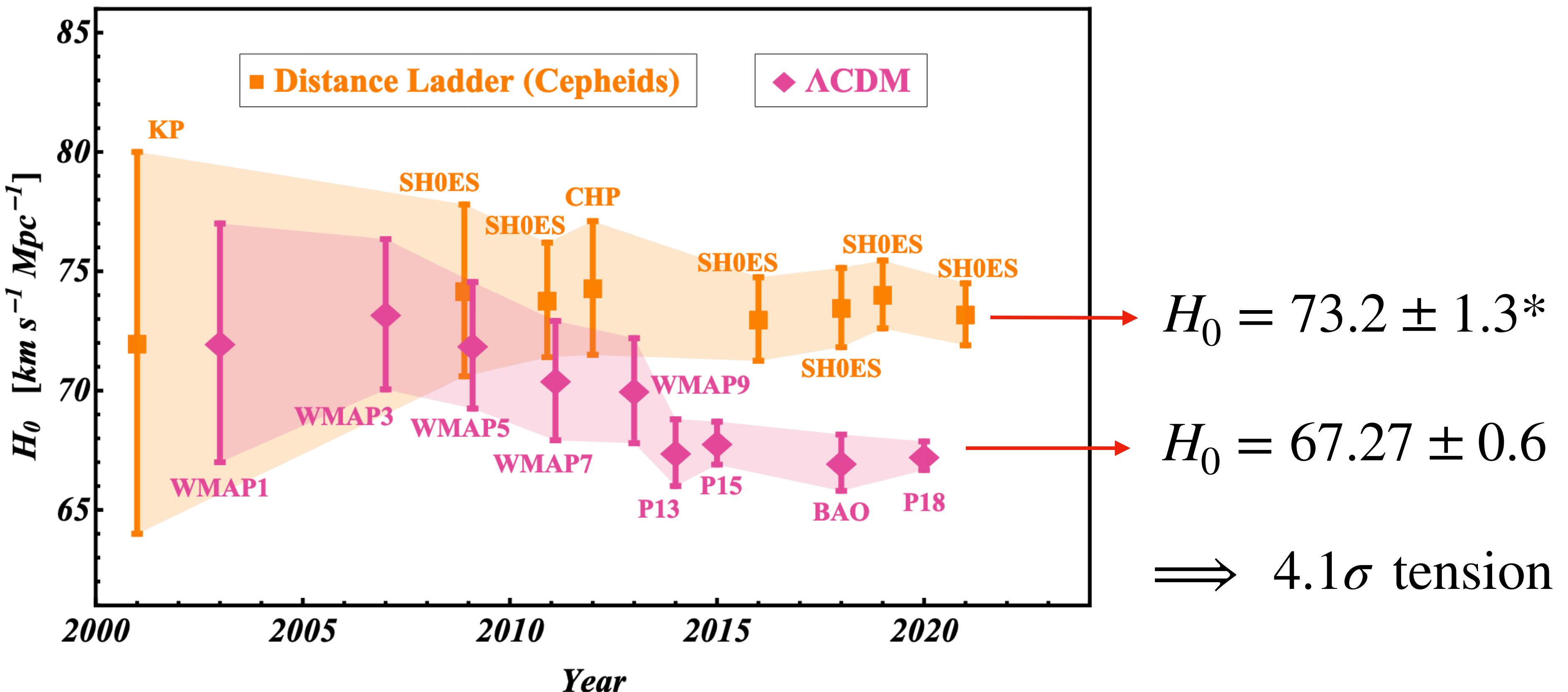
## **BACK-UP SLIDES**

# The $S_8$ tension



# The $H_0$ tension

Predominantly driven by the Planck and SHoES collaborations



Perivolaropoulos&Skara 2105.05208

\*Units of km/s/Mpc are always assumed

# $H_0$ Olympics: testing against other datasets

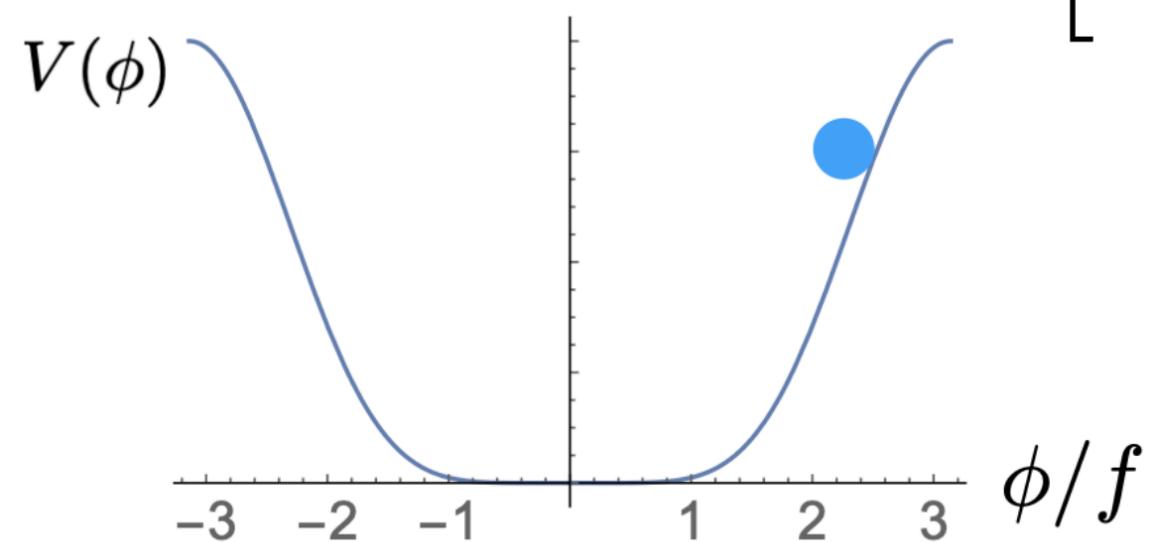
**Role of Planck data:** We replaced Planck by WMAP+ACT and BBN+BAO

→ No significant changes (*notable exceptions are EDE and NEDE*)

**Adding extra datasets:** We included data from Cosmic Chronometers, Redshift-Space-Distortions and BAO Ly- $\alpha$ .

→ No huge impact, but decreases performance of finalist models

# Early Dark Energy



$$V(\phi) \propto \left[1 - \cos\left(\frac{\phi}{f}\right)\right]^n$$

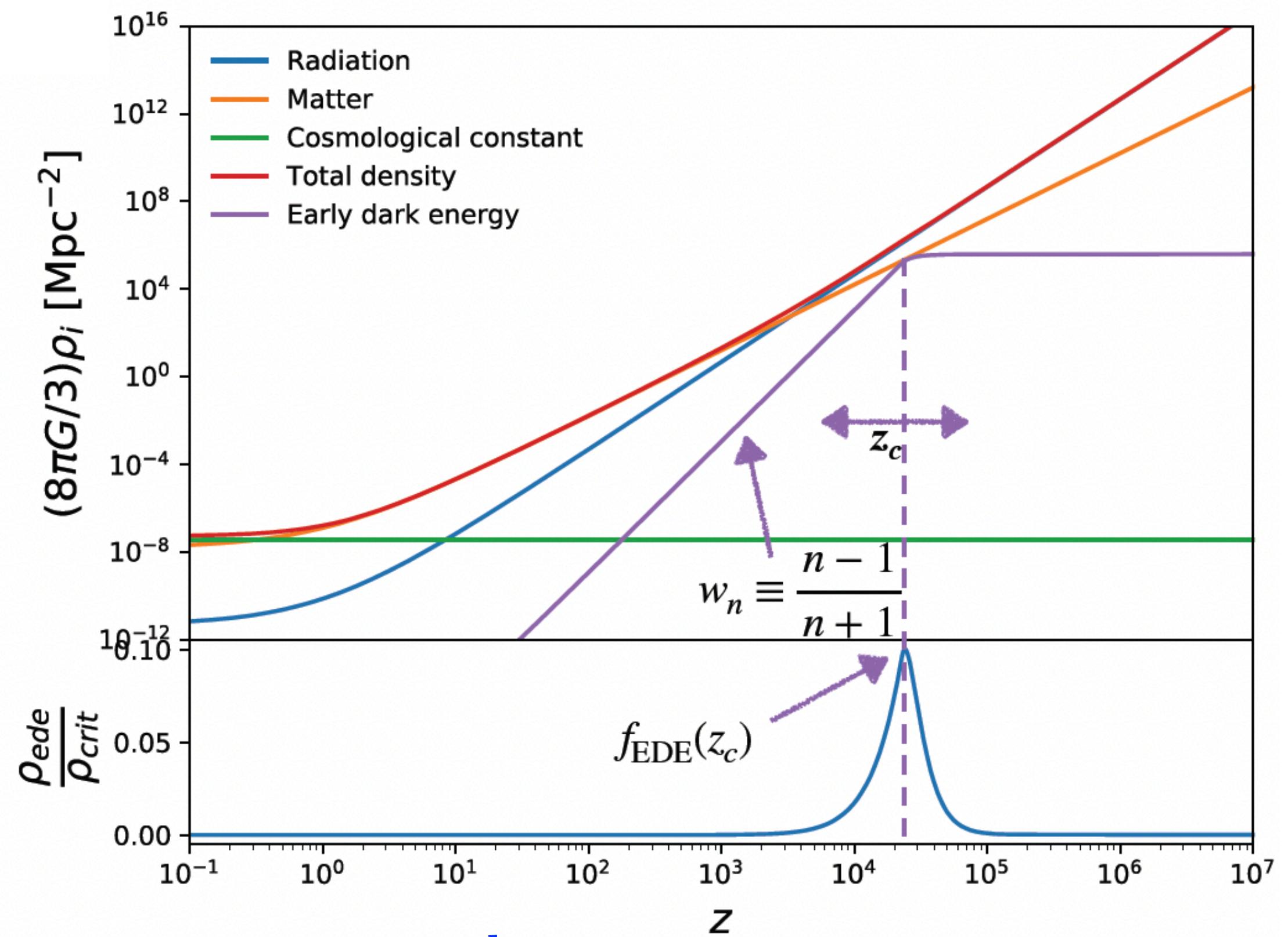
Scalar field initially frozen, then dilutes away equal or faster than radiation

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

+ perturbed linear eqs.

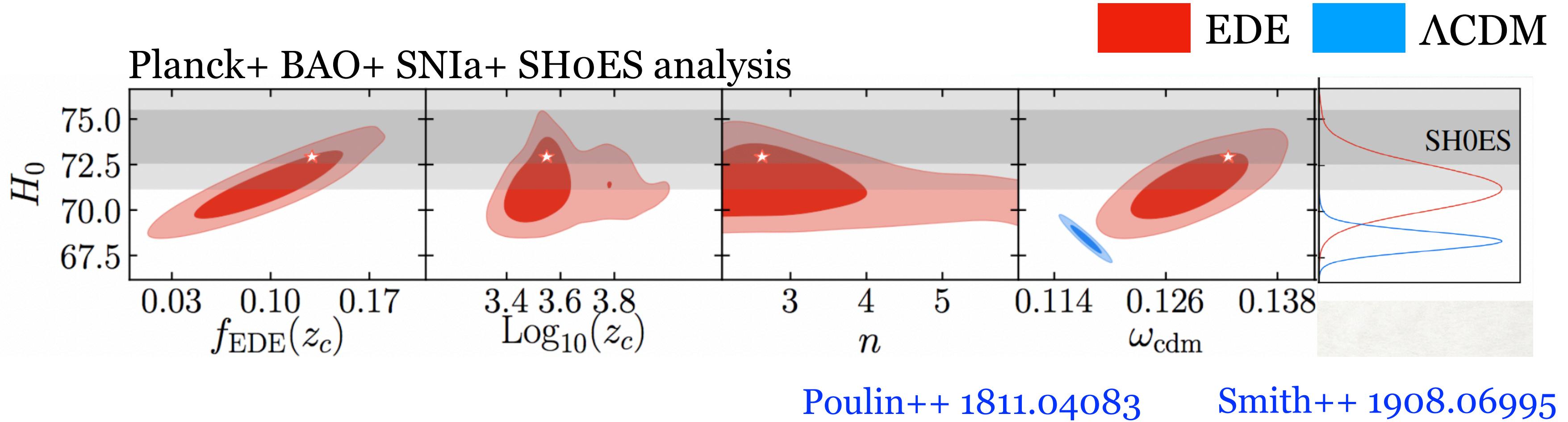
The model is fully specified by

$$\{f_{\text{EDE}}(z_c), z_c, n, \phi_i\}$$



# Early Dark Energy

Early Dark Energy can resolve the  $H_0$  tension if  $f_{\text{EDE}}(z_c) \sim 10\%$  for  $z_c \sim z_{\text{eq}}$



Some caveats

## 1. Very fine tuned?

→ Proposed connexions of EDE with neutrino sector and present DE  
Sakstein++ 1911.11760      Freese++ 2102.13655

## 2. Increased value of $\omega_{\text{cdm}} = \Omega_{\text{cdm}} h^2$ , exacerbates $S_8$ tension

Jedamzik++ 2010.04158.

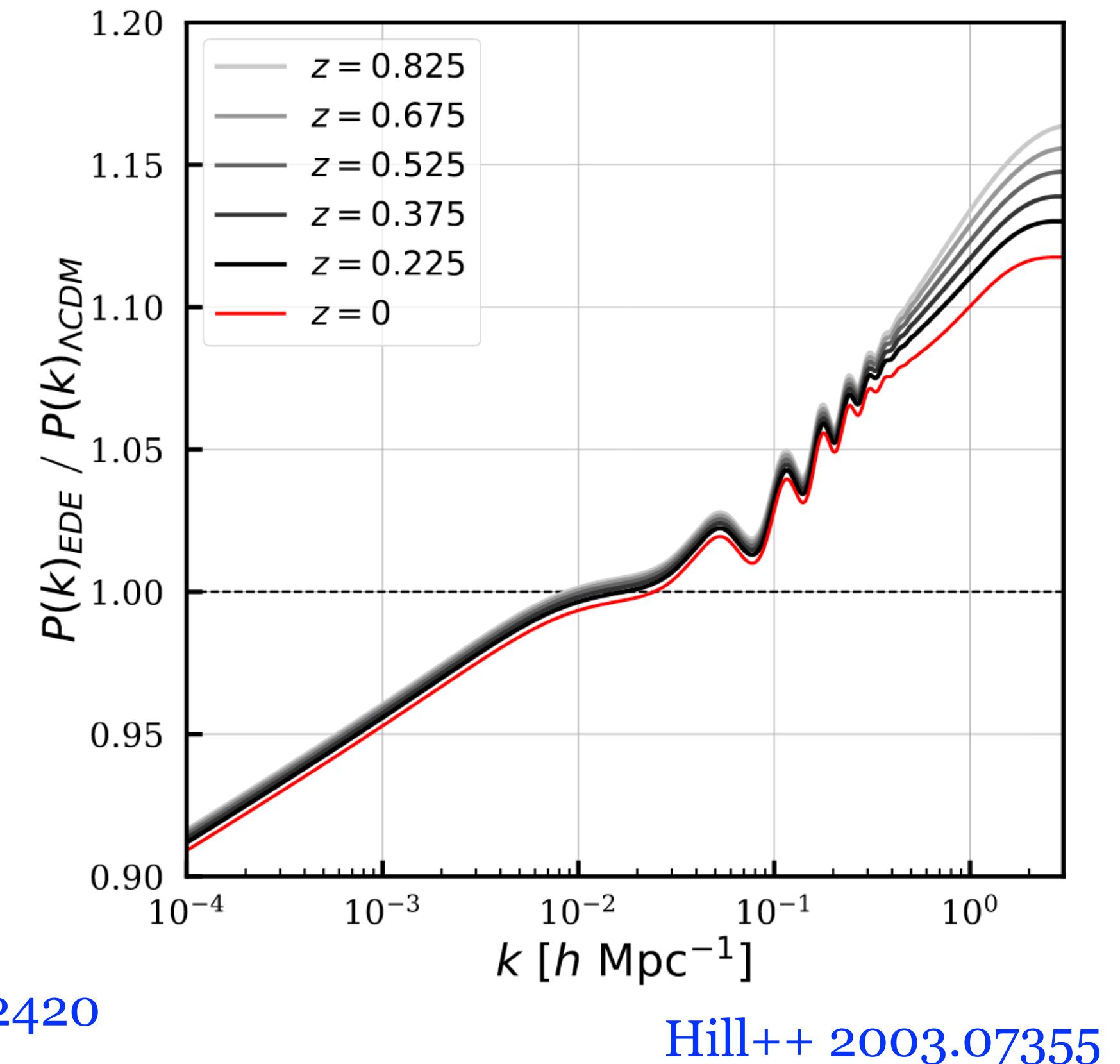
# Is EDE solution ruled out?

EDE solution **increases** power at small  $k$   
*(with a corresponding increase in  $S_8$  ),*  
rising mild tension with Large Scale  
Structure (LSS) data

When LSS data is added to analysis, EDE  
detection is **reduced** from  $3\sigma$  to  $2\sigma$

In addition, EDE is **not detected** from  
Planck data alone

D'amico++ 2006.12420  
Ivanov++ 2006.11235



Hill++ 2003.07355

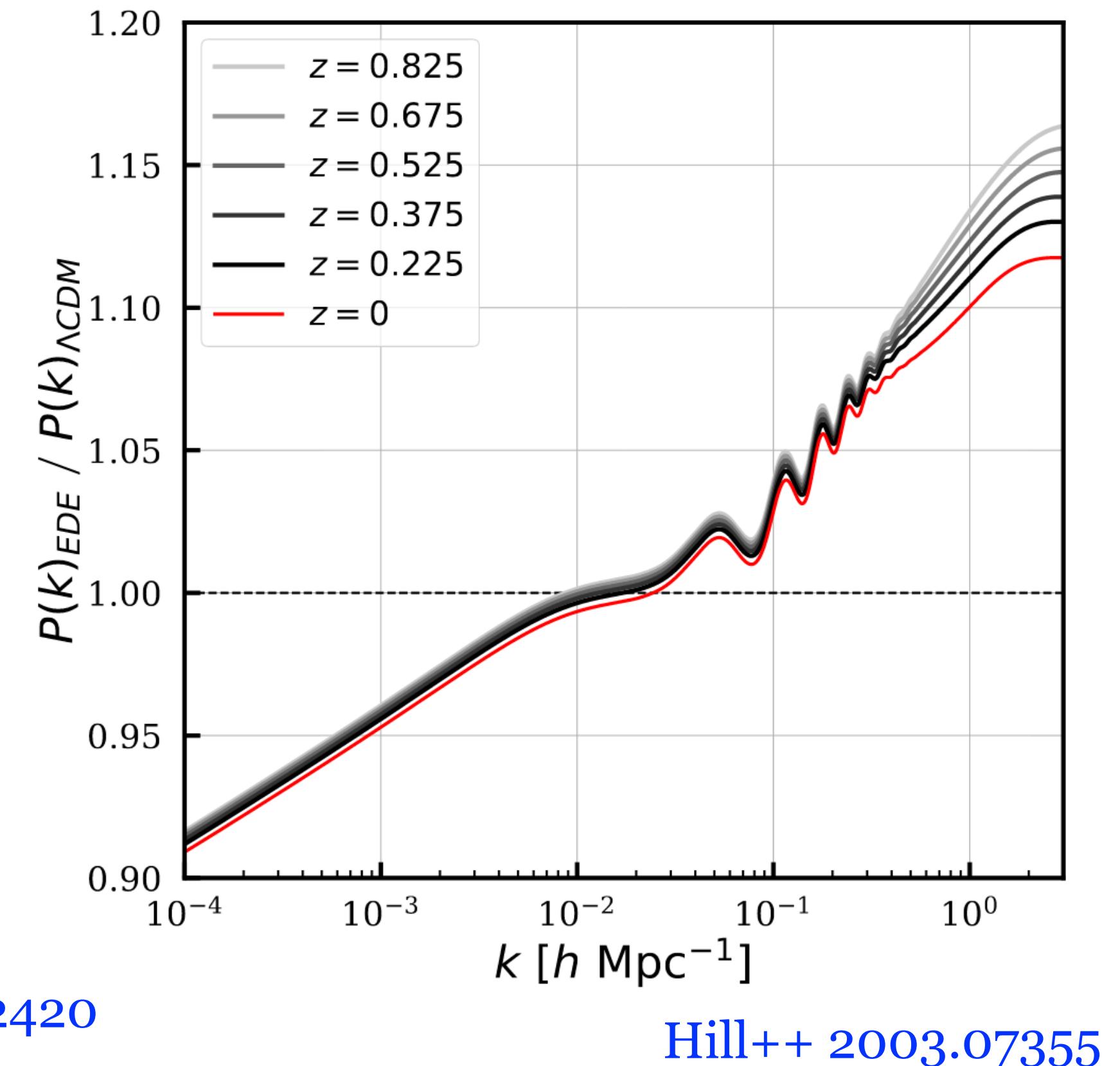
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D'amico++ 2006.12420  
Ivanov++ 2006.11235



Hill++ 2003.07355

# Answer: no, EDE solution is still robust

## 1. Why EDE is not detected from Planck alone?

---

Strong  $\chi^2$  degeneracy in Planck between  $\Lambda$ CDM and EDE :

Once  $f_{\text{EDE}} \rightarrow 0$ , parameters  $z_c$  and  $\phi_i$  become irrelevant, so posteriors are naturally weighted towards  $\Lambda$ CDM

To avoid this Bayesian volume effect, consider a  
**1 parameter model (1pEDE)** : Fix  $z_c$  and  $\phi_i$  and let  $f_{\text{EDE}}$  free to vary

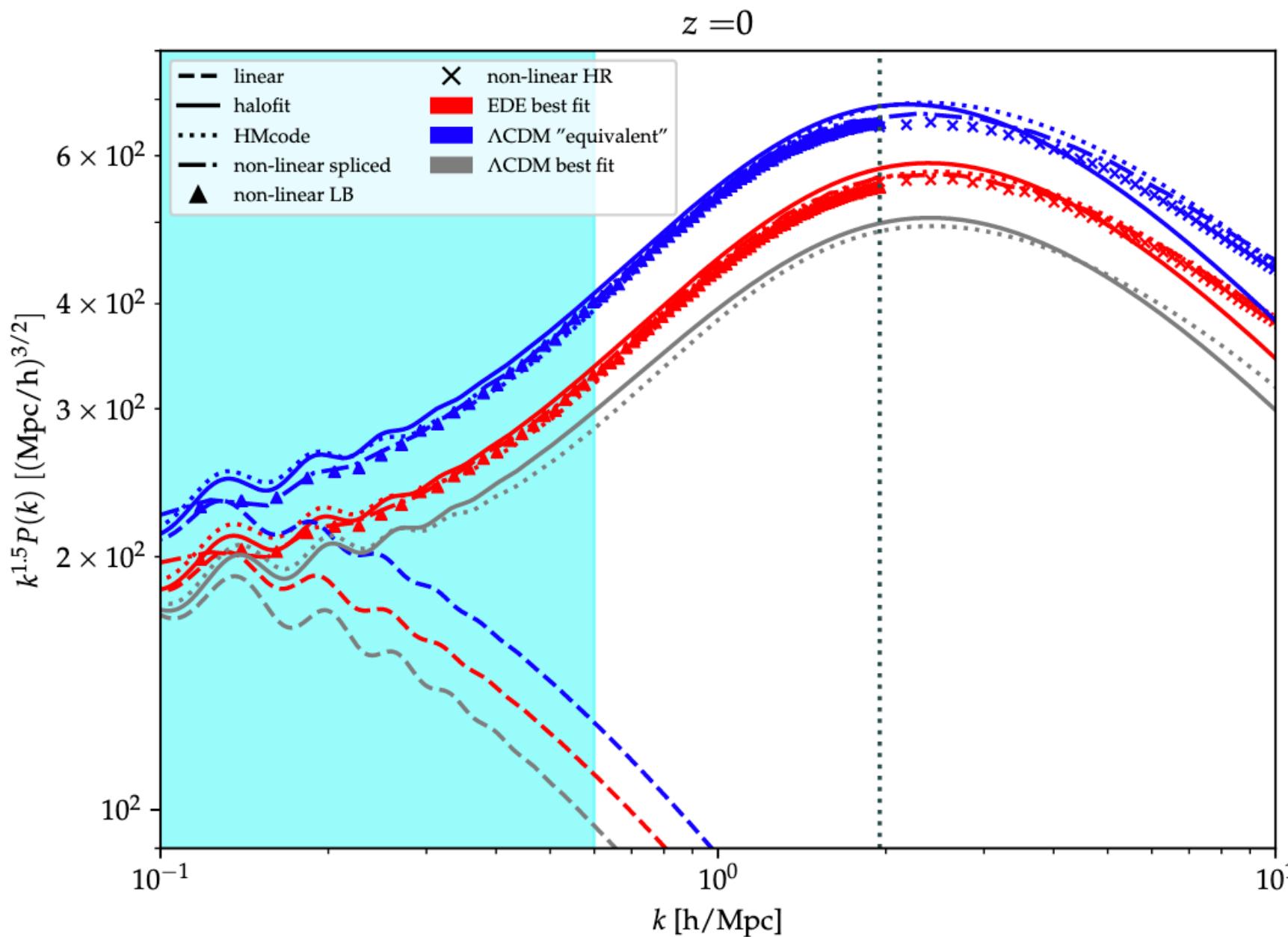
Within 1pEDE, we get a  $2\sigma$  detection of EDE from *Planck data alone*

$$f_{\text{EDE}} = 0.08 \pm 0.04$$

$$H_0 = 70 \pm 1.5 \text{ km/s/Mpc}$$

# Answer: no, EDE solution is still robust

## 2. Is LSS data constraining enough to rule out EDE?



Important cross-check:

EDE non-linear  $P(k)$  from standard semi-analytical algorithms agrees well with results from N-body simulations

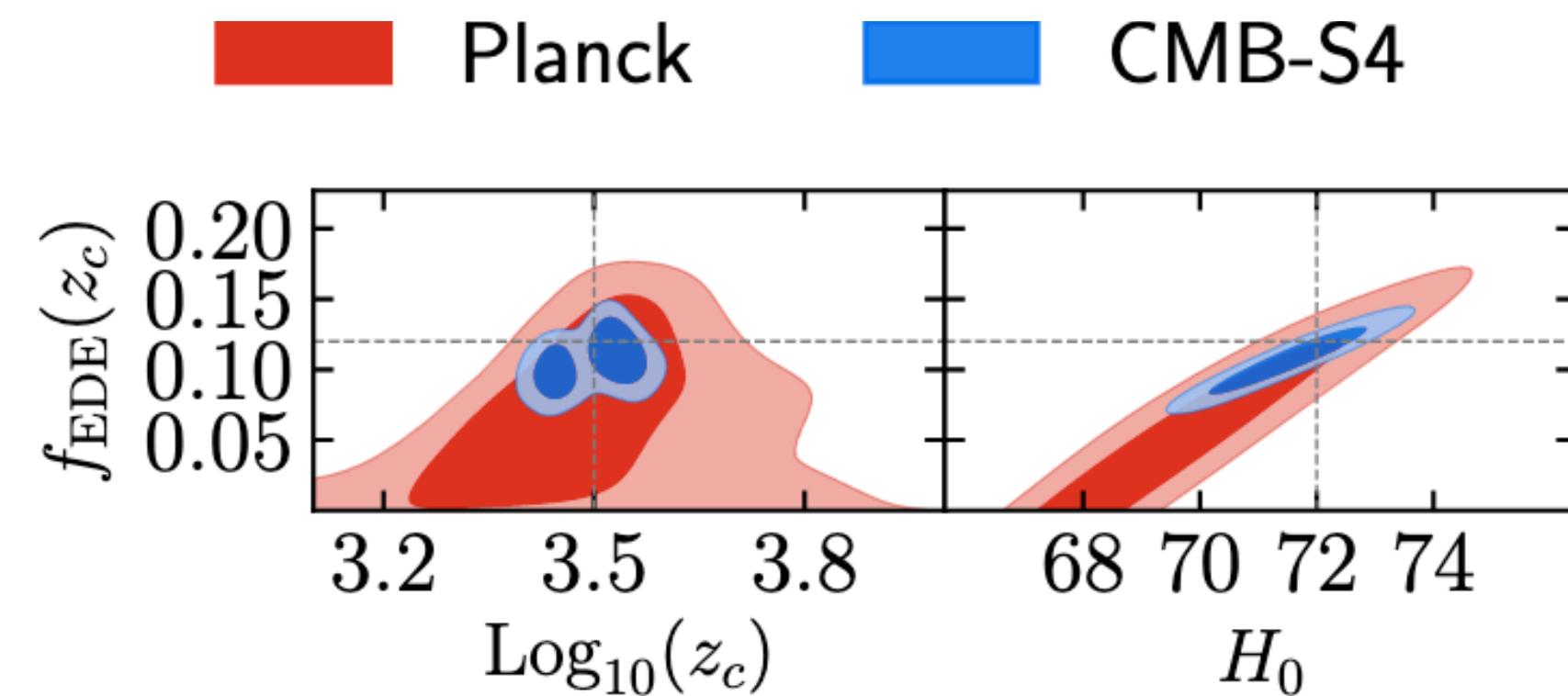
1pEDE tested against Planck+BAO+SNIa+SHoEs and WL data from KiDS/Viking+DES:  
S<sub>8</sub> tension persists, but fit is not significantly degraded wrt  $\Lambda\text{CDM}$ , and solution to the H<sub>0</sub> tension survives

$$f_{\text{EDE}} = 0.09^{+0.03}_{-0.02}$$

$$H_0 = 71.3 \pm 0.9 \text{ km/s/Mpc}$$

# Prospects for Early Dark Energy

Future CMB experiments (i.e. CMB-S4) will be able to unambiguously detect EDE



[Smith++ 1908.06995](#)

Other current CMB experiments like ACT are already showing a  $3\sigma$  detection of EDE!

[Hill++ 2109.04451](#)

[Poulin++ 2109.06229](#)

# Decaying dark matter

- Dark matter (DM) is assumed to be perfectly **stable** in  $\Lambda$ CDM

*Can we test this hypothesis?*

- DM Decays to SM particles  $\longrightarrow$  **very constrained**

From **e.m. impact** on CMB :  $\Gamma^{-1} \gtrsim 10^8$  Gyr    [Poulin++ 1610.10051](#)

- DM decays to **massless** Dark Radiation  $\longrightarrow$  **less constrained**,  
but more **model-independent**

From **grav. impact** on CMB :  $\Gamma^{-1} \gtrsim 10^2$  Gyr    [Audren++ 1407.2418](#)  
[Poulin++ 1606.02073](#)

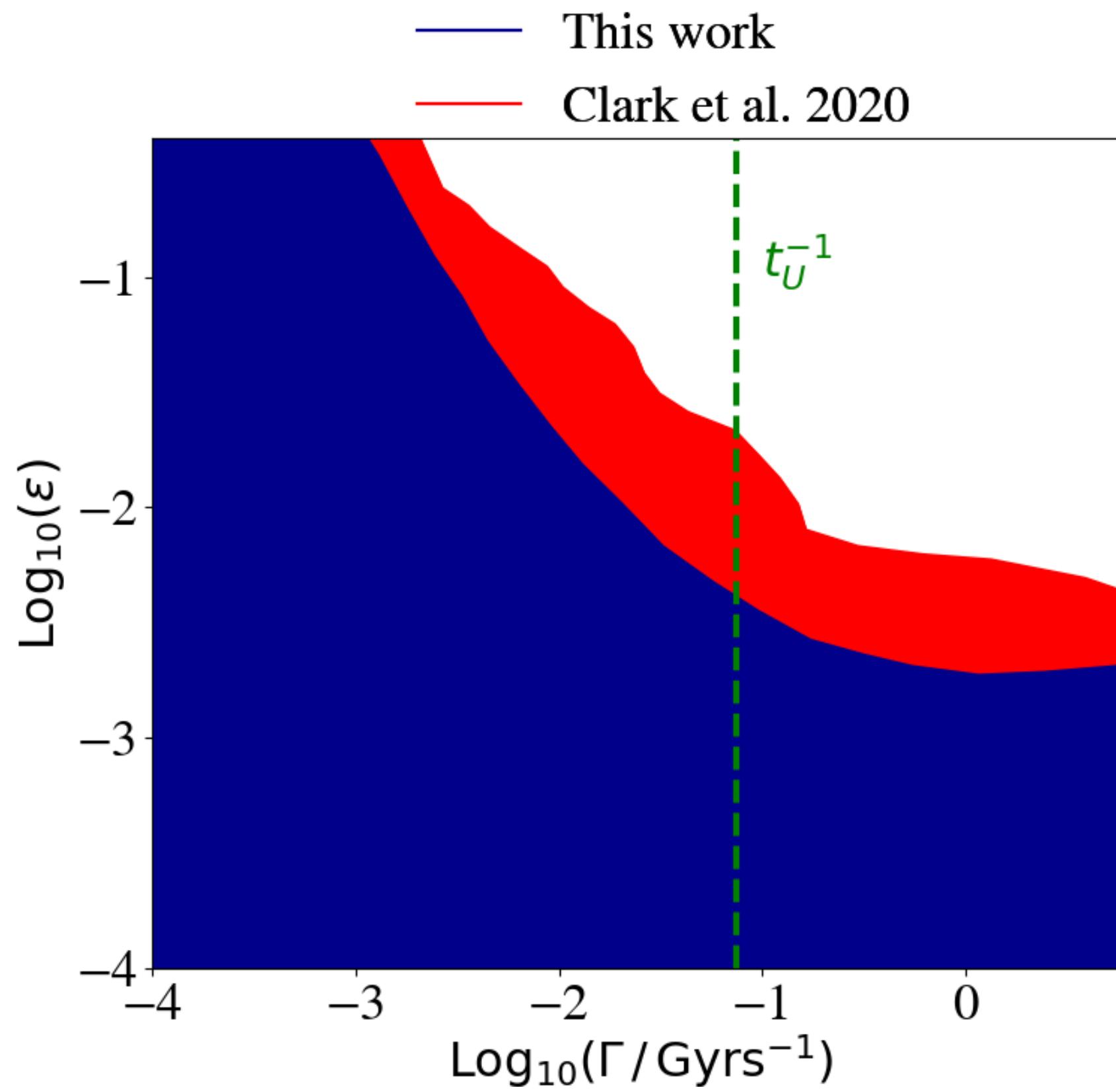
- What about massive products?

# Evolution of perturbations: full treatment

- Effects on  $P_m(k)$  and  $C_\ell$ ? Track **linear perts.** for the particles species involved in the decay:  $\delta_i$ ,  $\theta_i$  and  $\sigma_i$  for  $i = dm, dr, wdm$
- Boltzmann hierarchy of eqs. Dictate the evolution of the **p.s.d. multipoles**  $\Delta f_\ell(q, k, \tau)$ 
  - ◆ DM and DR treatments are **easy**, momentum d.o.f. are integrated out
  - ◆ For WDM, one needs to follow the evolution of the full p.s.d. Computationally expensive  $\longrightarrow \mathcal{O}(10^8)$  ODEs to solve!

# General constraints on the 2-body DM decay

Planck+BAO+SNIa analysis

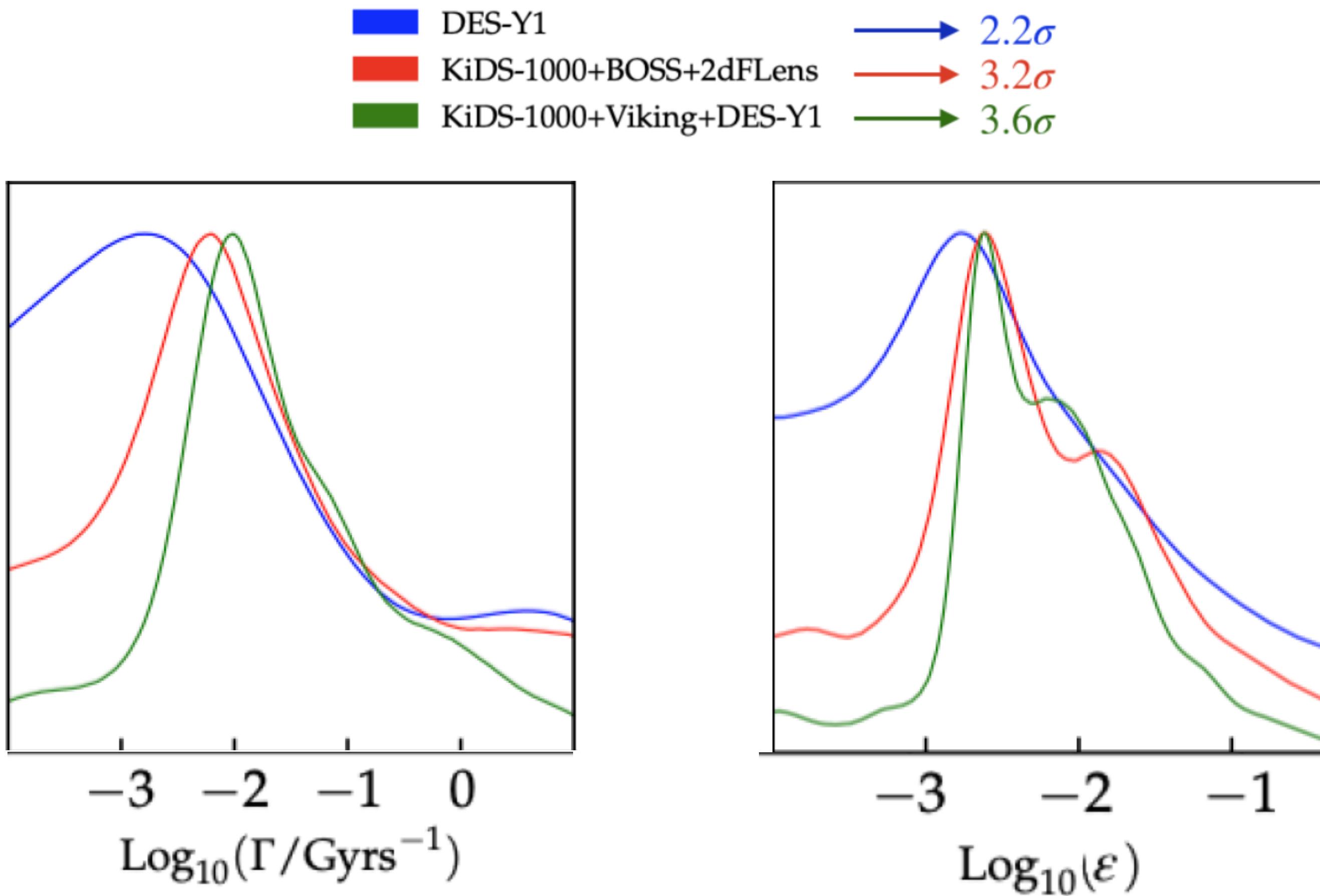


Strong negative correlation  
between  $\epsilon$  and  $\Gamma$

Constraints up to 1 order of  
magnitude stronger than  
previous literature

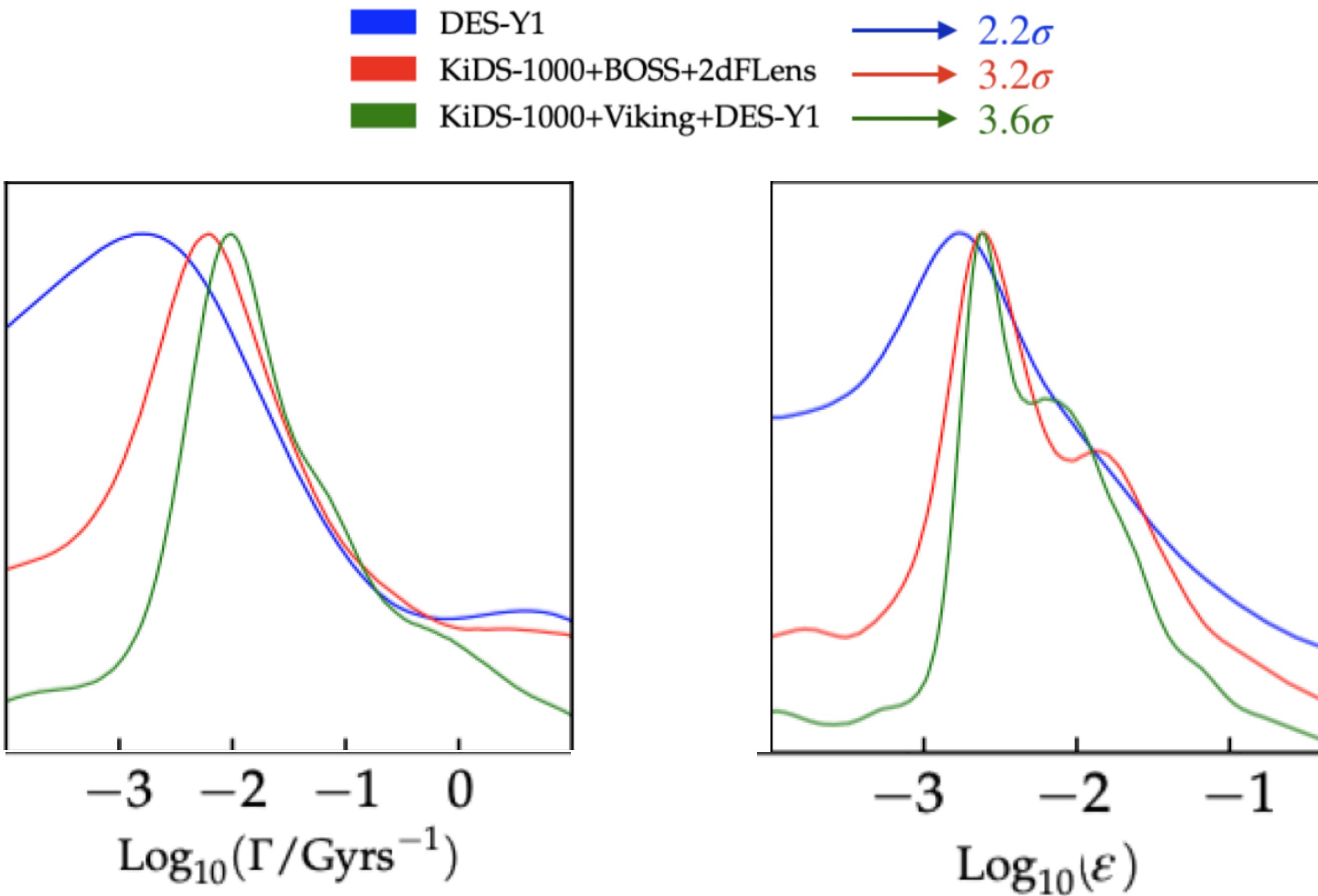
# Resolution to the $S_8$ tension

The level of detection depends on the level of tension with  $\Lambda$ CDM



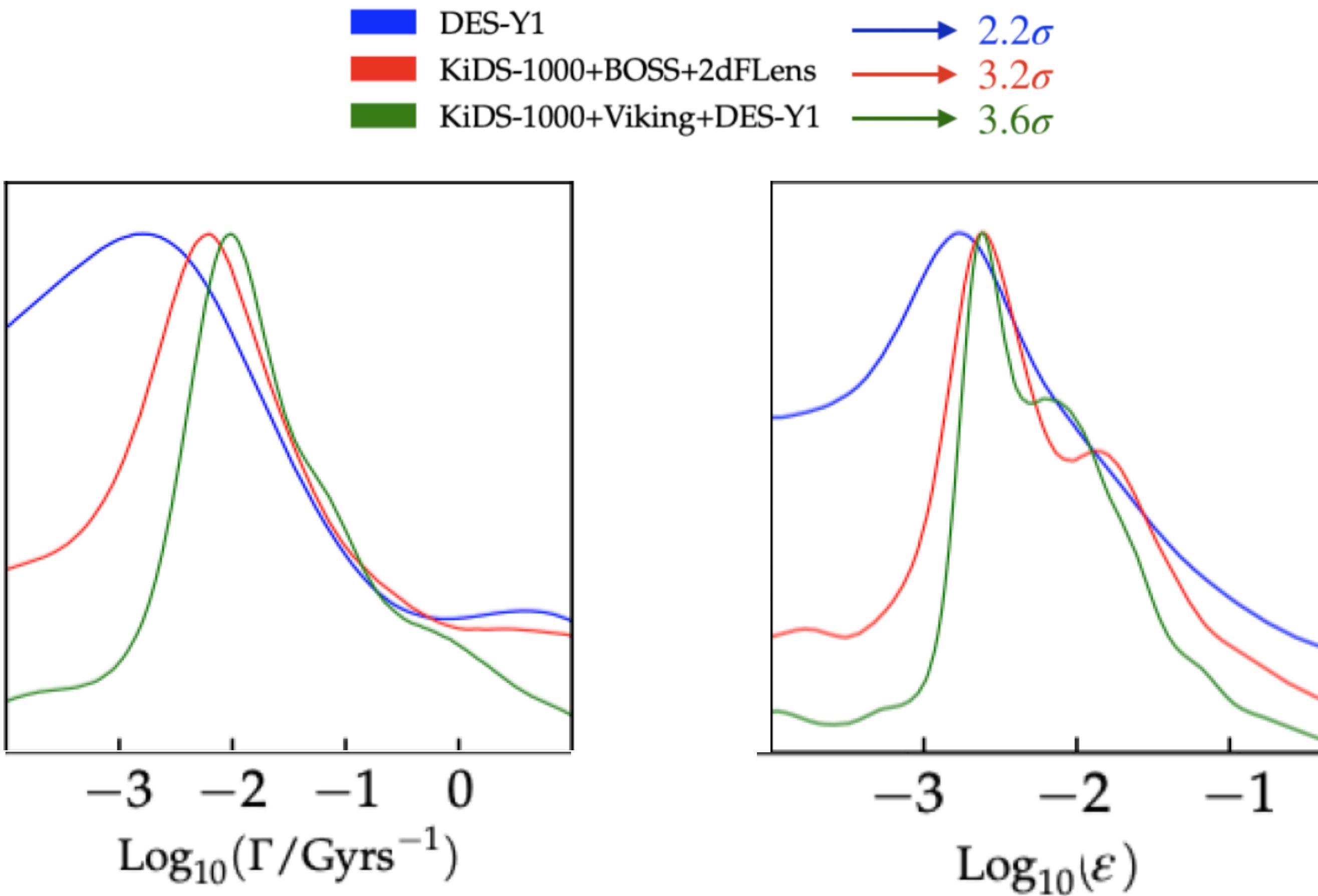
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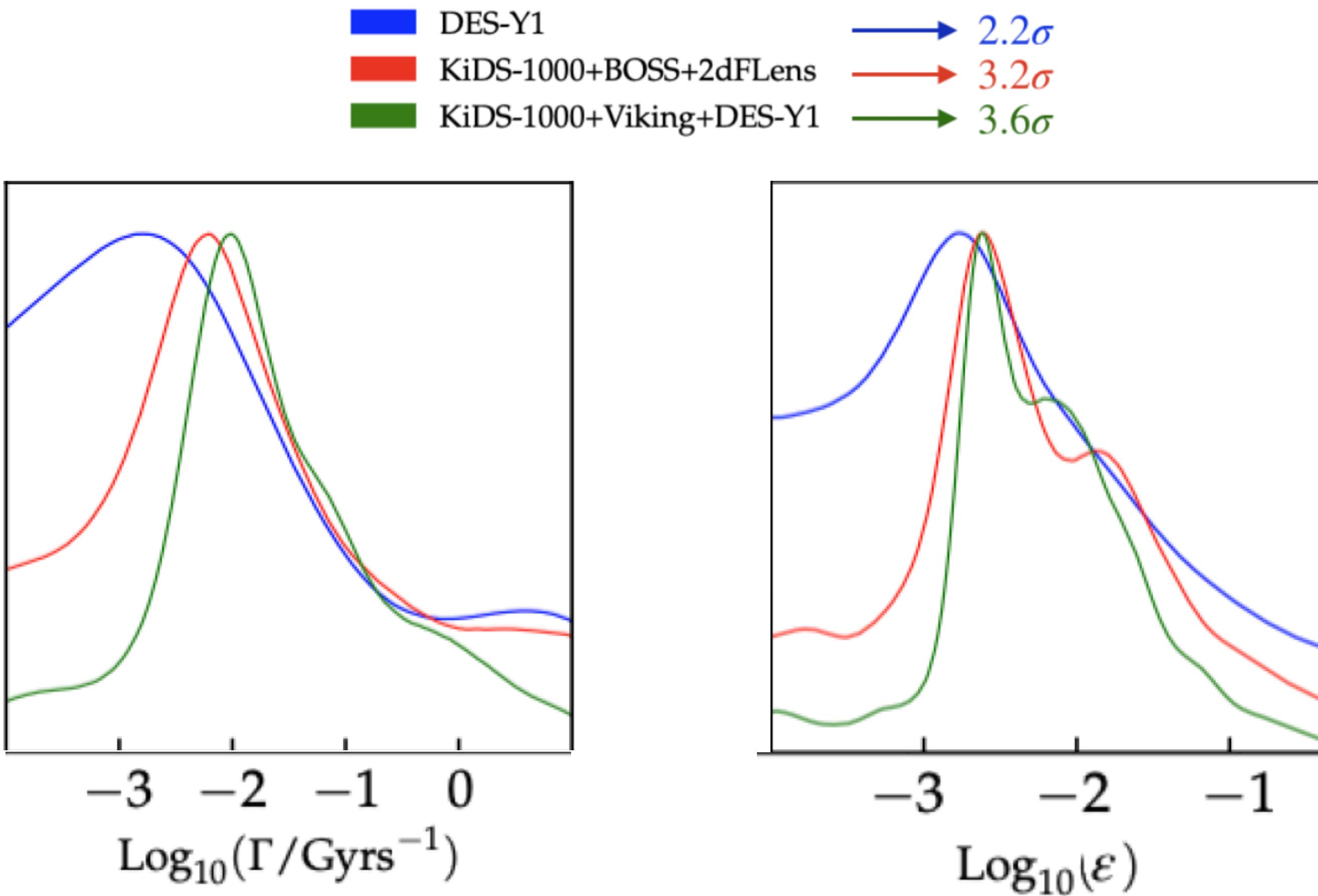
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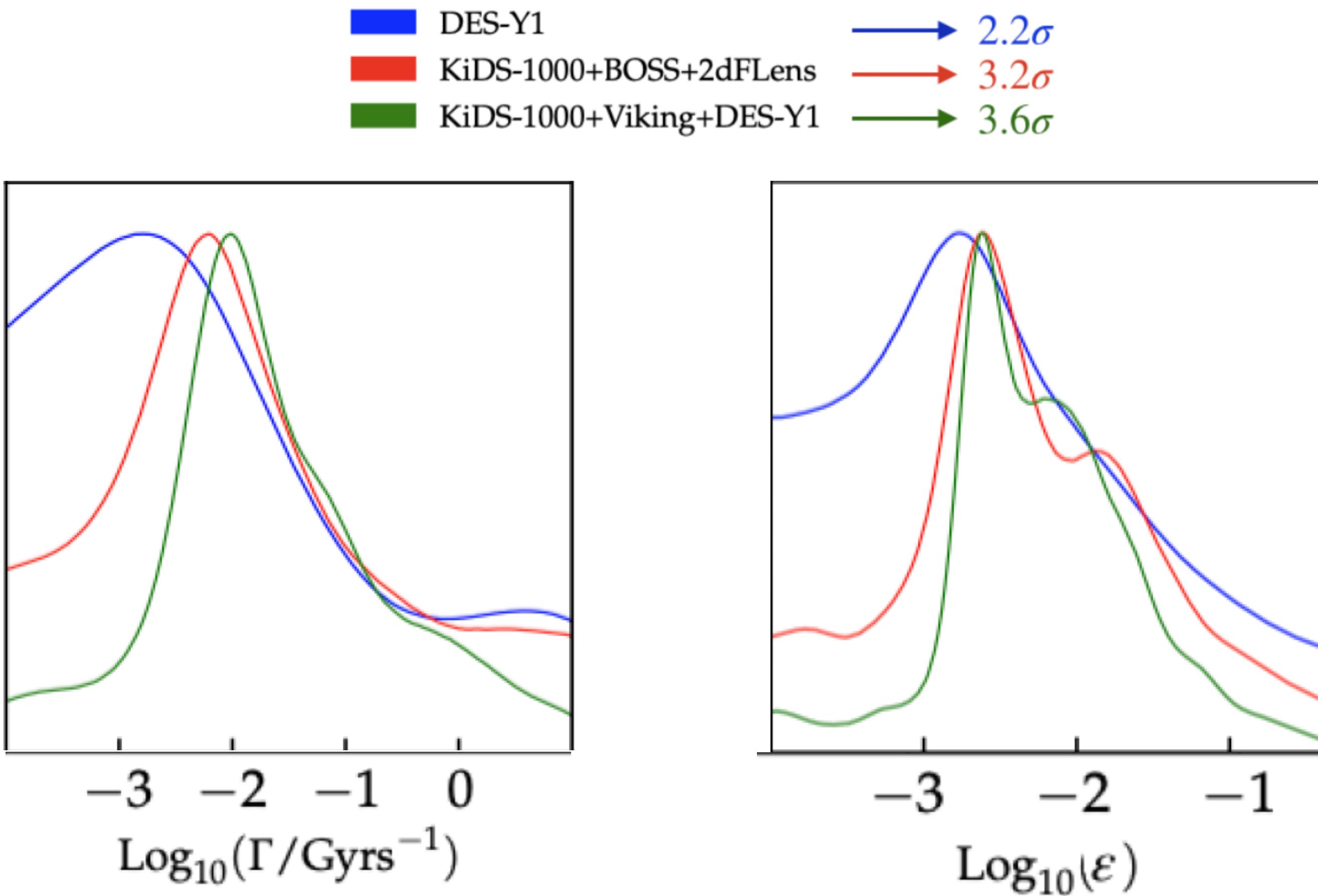
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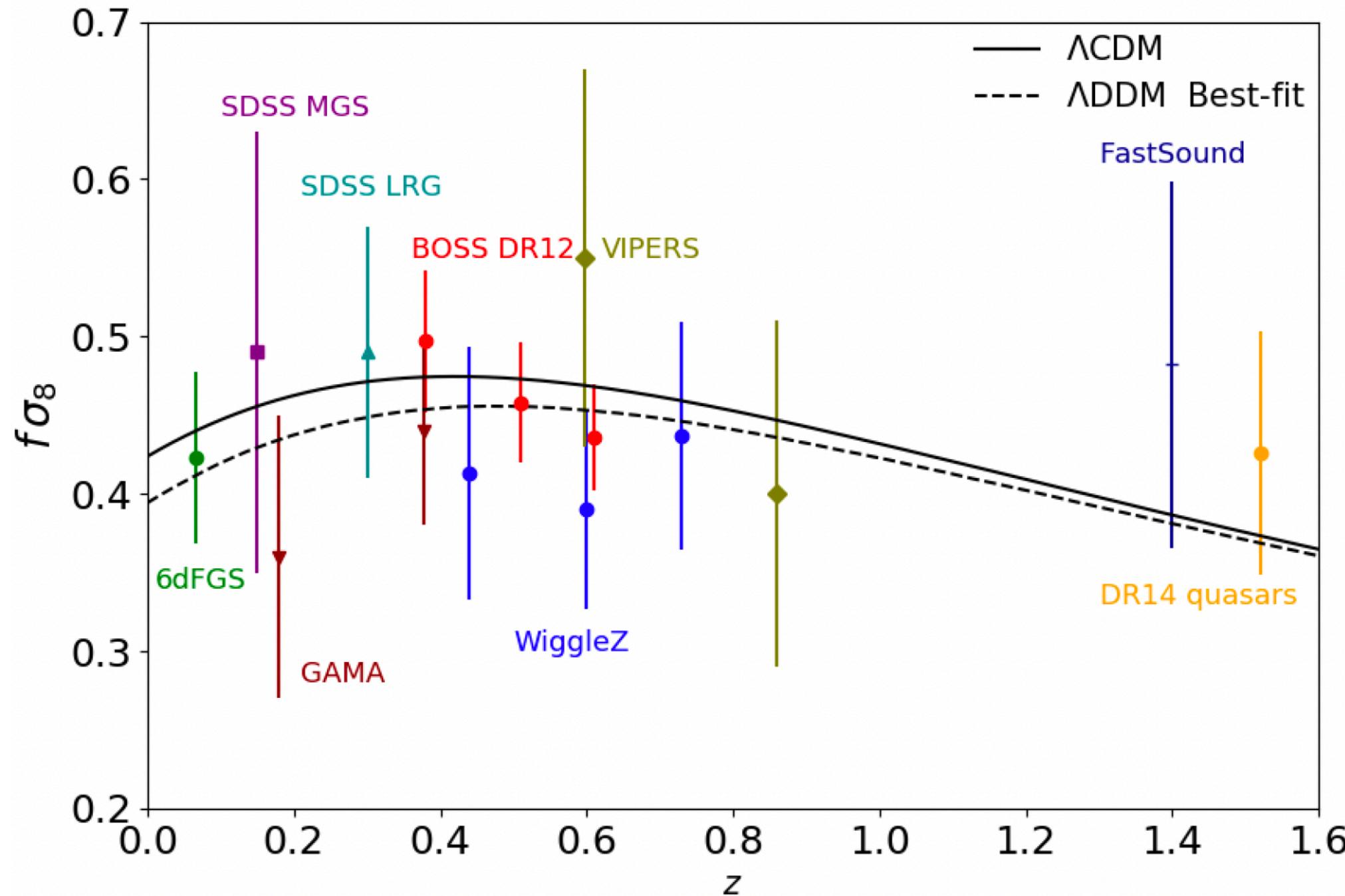


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# Prospects for the 2-body DM decay



Accurate measurements of  $f\sigma_8$  at  $0 \lesssim z \lesssim 1$  will further test the 2-body decay

**Next goal:** Predict non-linear matter power spectrum  
(using either N-body simulations or EFT of LSS)