

Implementation of Some Proposal for Spatiotemporal Representation Learning for Driving Behavior Analysis

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DECLARATION

We declare that this written submission represents our ideas in our own words and where others' ideas or words have been included, we have adequately cited and referenced the original sources. We also declare that we have adhered to all principles of academic honesty and integrity and have not misinterpreted or fabricated or falsified any ideas/ data / fact / source in our submission. We understand that any violation of the above will be a cause for disciplinary action by the Institute and can also evoke penal action from the sources which have thus not been properly cited or from whom proper permission has not been taken when needed.

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ABSTRACT

As the world is growing at a great pace, so are humans' dependencies on electronic gadgets and automobiles. Transportation has been one such field which has revolutionized and changed the life of millions. The major changes from walking in past to multi-featured vehicles in present sets our path to autonomous driving in future. As every major change comes with its pros and cons, so to ensure driving remains a safe activity, assessing a driver's behavior in different circumstances and providing improvement measures becomes a necessity.

Our project aims to achieve significant knowledge from various drives conducted in a variety of situations to analyze the driver's behavior. We are using a **Peer and Temporal Aware Representation Learning (PATRL)** based framework introduced in **Spatiotemporal Representation Learning for Driving Behavior Analysis: A Joint Perspective of Peer and Temporal Dependencies** by *Pengyang Wang, Xiaolin Li, Yu Zheng, Charu Aggarwal, Yanjie Fu* [6].

This framework is proposed for driving behavior analysis using GPS trajectory data. We first detect the driving operations and states of each driver from their GPS traces. Then, we derive a sequence of multi-view driving state transition graphs from the driving state sequences, in order to characterize a driver's driving behaviors that vary over time. In addition, we develop a peer and temporal-aware representation learning method to learn a sequence of time-varying yet relational vectorized representations from the driving state transition graphs.

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CHAPTER 1

LITERATURE SURVEY

As driving comprises of various speed and direction related operations, such as acceleration, deceleration, keeping constant speed, turning left, turning right, moving straight. By analyzing driving behaviors, we can try to provide driving assistance, enhance driving comforts, develop intelligent and resilient transportation systems, assessing driver's performances and enhance traffic safety.

Prior Studies

The studies conducted in this field till date can be categorized into:

(i) Descriptive Analysis, in which transportation experts define measurements (e.g., harsh or frequent acceleration/braking, sharp turn, acceleration before turn) based on transportation theory to describe driving behaviors. *Evaluating changes in driver behaviour: a risk profiling approach. Accident Analysis & Prevention*, by Adrian B Ellison et al. [1] used this methodology, firstly, the data is processed in such a way that the influence of the driver could be isolated. Secondly, a way to separate the effect of the financial and awareness components of the intervention is devised. Lastly, multilevel risk models are developed to evaluate the changes to driver behavior that occurred as a result of the intervention.

(ii) Predictive Analysis, in which researchers mine the patterns from driving data and apply machine learning models (e.g., SVM, naive Bayesian, etc.) to predict risky scores. *A bayesian network model for contextual versus noncontextual driving behavior assessment. Transportation Research Part C: Emerging Technologies* by Xiaoyu Zhu et al. [2] used this methodology, firstly, the concept of Bayesian Network is introduced and an overview of this method is provided. Secondly, the relevance of BN for the study is discussed. Lastly, the computation of this model is presented based on Monte Carlo Markov Chain (MCMC).

(iii) Causal Analysis, in which researchers identify the causal factors of driving behaviors and explain how these factors influence road safety [3].

Sarah M Simmons et al. used meta-analysis which is particularly useful in providing a clearer, more interpretable estimate of an effect, particularly when discordant findings are reported across studies, as is apparent within the field of naturalistic driving. Estimates of safety-critical event risk reported in naturalistic study reports appear to vary wildly at times.

Moreover, there are studies utilizing CAN data to quantify driving behaviors [4], [5]. CAN data may cause privacy issues which can be avoided by analyzing the ubiquitous GPS data. CAN data is more accurate to quantify driving operations, like speed and directions. It can record the vehicle status and can be read through specific facilities. However, since it needs equipments to read the data, the accessibility to CAN data may cause privacy issue that leads to the difficulty of collecting data. For example, many drivers are not willing to release CAN data to the insurance company. Unlike CAN data, due to the pervasiveness of GPS sensors (e.g., mobile phones), GPS data can be easily obtained from location-based apps (e.g., google maps, yelp) that are granted permission for collecting data by users themselves. On the other hand, there are many public GPS dataset on recording driver behaviors. All the personal information has been encrypted that there will be any privacy issues. In a nutshell, due to the easier availability and well protected personal information, GPS data remains the best alternative for the task of driving behavior analysis.

Thus, we are convinced to use GPS data for our task. It is highly promising to use high-resolution widely-available GPS trajectories with representation learning for the task of driving behavior analysis.

Challenges

Usage of high-resolution widely-available GPS trajectories and representation learning for driving behavior analysis, the following challenges rise:

- As the raw GPS data might not be suitable for classical or advanced mining algorithms, so it highly necessitates a novel method to transform GPS traces into an appropriate structure that can effectively characterize driving activities and corresponding spatio-temporal dynamics.
- The proposal of a new framework becomes essential which should take two major things into account. Peer-Dependencies, i.e., the similarity between two trajectories should convey similar behaviors of respective drivers. Temporal-Dependencies, i.e., the behavioral patterns of a driver from his past to present.
- The optimising strategy should be such that it minimizes the overall loss incorporated in the whole process of converting GPS data to mining ready form and mining itself.

CHAPTER 2

MODEL FRAMEWORK

Problem Statement

In our project, we implement the proposals made in a research paper titled Spatiotemporal Representation Learning for Driving Behavior Analysis: A Joint Perspective of Peer and Temporal Dependencies by *Pengyang Wang, Xiaolin Li, Yu Zheng, Charu Aggarwal, Yanjie Fu* [6]. Here they have stated high level statement of the problem as “capturing *driving behavior profiling* with GPS traces”. Formally, given a driver (a vehicle) and corresponding GPS trajectories, it is aimed to find a mapping function that takes the GPS trajectories as inputs, and outputs a sequence of time-varying yet relational vectorized representations in order to quantify the dynamics of the driver’s driving behavior. The said problem is formulated as a task of spatio-temporal representation learning. As per their proposal, first it is necessary to construct a sequence of driving state transition graphs from GPS trajectories, and then learn the latent representations of driving behavior from the graphs.

We present their definitions and proposals in this chapter.

Attributes Definition

- *Driving Operation*: Driving operations are defined as a set of activities and steps that a driver operates when driving a vehicle, according to the driver’s personal judgment, experience and skills. Since a moving object can be characterized by speed and direction, we similarly categorize driving operations into (i) speed-related operations (i.e., acceleration, deceleration, constant speed) and (ii) direction-related operations (i.e., turning left, turning right, moving straight). The driving operations can be detected from GPS traces [6].
- *Driving State*: A driving state concerns the way that a vehicle moves at a specific time point or in a small time window. In other words, a driving state of a vehicle contains both the speed status (i.e., acceleration, deceleration, constant speed) and the direction status (i.e., turning left, turning right, moving straight) of a vehicle [6]. For instance, a driving state example of a car can be <acceleration, moving straight>
- *State Transition Graphs*: The driving states of a vehicle usually changes over time. We propose to develop a driving state transition graph to summarize and characterize

such time-varying sequence. In a driving state transition graph, nodes denote driving states, and the weights of edges can be the probability of state changes or transition duration between two driving states [6].

TABLE 1: Summary of notations.

Symbol	Discription
ϕ_t	The latitude at time t
λ_t	The longitude at time t
G_i^τ	The driving behavior transition graph sequence of driver i at the time slot τ
\mathbf{x}_i^τ	The original original vector representation of G_i^τ
\mathbf{z}_i^τ	The learned representation for the driver i at the time slot τ
$(\mathbf{y}_i^o)^\tau$	The latent feature representations of the driver i at hidden layers o at the time τ in the encode process
$(\mathbf{y}_i^{\hat{o}})^\tau$	The latent feature representations of the driver i at hidden layers o at the time τ in the decode process
$\mathbf{W} \ \mathbf{b}$	Weights and biases in the encode process
$\hat{\mathbf{W}} \ \hat{\mathbf{b}}$	Weights and biases in the decode process process
$\mathcal{H}(\star)$	Loss function
A, B	The hyperparameters to control the weight of the representation learning loss and regression loss

To address the problem of consideration of both peer and temporal dependencies simultaneously, a framework called Peer and Temporal Aware Representation Learning Framework (PTARL) [6] is being used in this project. Raw GPS trajectories are converted into state transition graphs and are used with aforementioned framework which can learn a sequence of time-varying yet relational vectorized representations. PTARL framework consists of following essential steps:

1. **Construction of Multi-View Driving State Transition Graphs:** To obtain driving state sequence and then driving state transition graph from GPS trajectories, we first detect different speed and direction related operations for each driver and then identify driving states and obtain driving state sequence. Later, the driving state sequence is segmented into small subsequences with a fixed time window, and then it is converted into a driving state transition graph. For each driving state subsequence, we get a driving state transition graph and hence it can be used to characterize the time-varying driving behavior of a driver.
 - a. *Detection of speed-related operations:* Let $\Delta\phi_{1,2}$ be the difference of ϕ_1 and ϕ_2 , $\Delta\phi_{2,3}$ be the difference of ϕ_2 and ϕ_3 , $\Delta\lambda_{1,2}$ be the difference of λ_1 and λ_2 , $\Delta\lambda_{2,3}$ be the difference of λ_2 and λ_3 , and R be the radius of the earth. Then, the distance

$d_{1,2}$ between the two GPS points $\langle \phi_1, \lambda_1 \rangle$ and $\langle \phi_2, \lambda_2 \rangle$ is given by following equation:

$$2R \cdot \text{atan2} \left(\sqrt{\frac{\sin^2(\Delta\phi_{1,2})}{2} + \cos\phi_1 \cdot \cos\phi_2 \cdot \sin^2\left(\frac{\Delta\lambda_{1,2}}{2}\right)}, \sqrt{1 - \sin^2\left(\frac{\Delta\phi_{1,2}}{2}\right) - \cos\phi_1 \cdot \cos\phi_2 \cdot \sin^2\left(\frac{\Delta\lambda_{1,2}}{2}\right)} \right)$$

Similarly, the distance $d_{2,3}$ between the two GPS points $\langle \phi_2, \lambda_2 \rangle$ and $\langle \phi_3, \lambda_3 \rangle$ can also be calculated. Then, given the time stamps of the three GPS points, denoted by t_1 , t_2 and t_3 , the speed s_2 at t_2 is given by $s_2 = d_{1,2}/(t_2 - t_1)$, the speed s_3 at t_3 is given by $s_3 = d_{2,3}/(t_3 - t_2)$. For t_3 , if $s_3 > s_2$, the operation is detected as acceleration; if $s_3 < s_2$, the operation is deceleration; otherwise, the operation is “constant speed”. In practice, due to the noise caused by GPS devices, we introduce a losing boundary ϵ_s into the calculation. For t_3 , if $s_3 > s_2$ and $|s_3 - s_2| > \epsilon_s$, the operation is detected as acceleration; if $s_3 < s_2$ and $|s_3 - s_2| > \epsilon_s$, the operation is deceleration; otherwise, the operation is “constant speed”.

b. *Detection of direction-related operations:* To detect the direction-related operations, we calculate the bearing $\theta_{1,2}$ between the two GPS points $\langle \phi_1, \lambda_1 \rangle$ and $\langle \phi_2, \lambda_2 \rangle$ by the following equation:

$$\theta_{1,2} = \text{atan2} \left(\sin\Delta\lambda_{1,2} \cdot \cos\phi_2, \cos\phi_1 \cdot \sin\phi_2 - \sin\phi_1 \cdot \cos\phi_2 \cdot \cos\Delta\lambda_{1,2} \right)$$

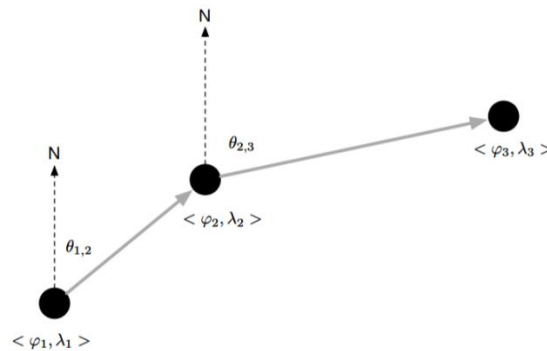
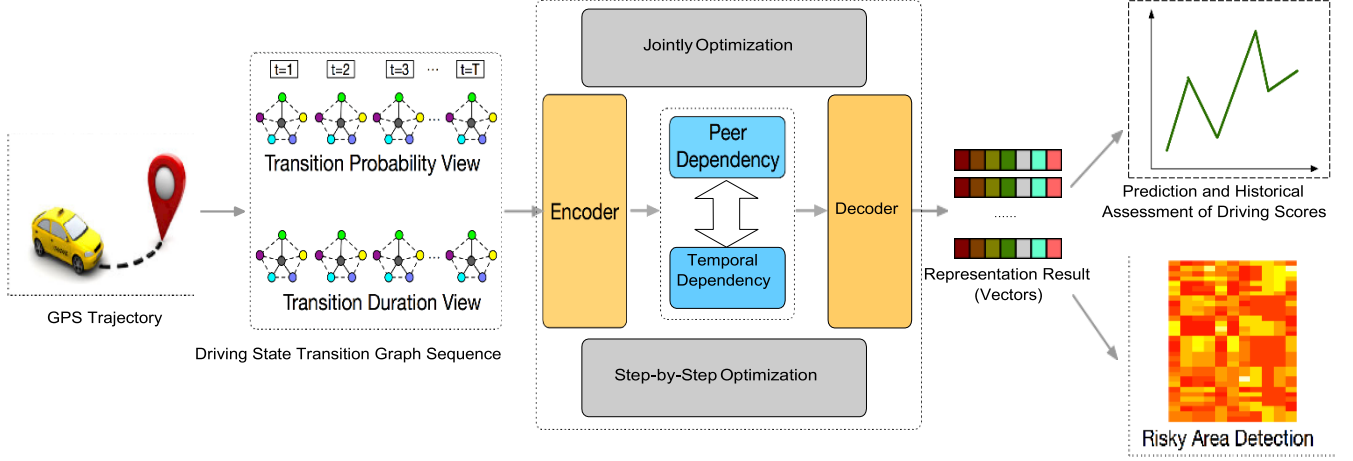


Fig. 2: An example for calculating directions.

Similarly, we can obtain the bearing $\theta_{2,3}$ between the two GPS points $\langle \phi_2, \lambda_2 \rangle$ and $\langle \phi_3, \lambda_3 \rangle$. Therefore, as shown in Figure2, at t_3 , if $\theta_{2,3} > \theta_{1,2}$, then the operation is “turning right”; if $\theta_{2,3} < \theta_{1,2}$, then the operation is “turning left”; otherwise, the operation is “moving straight”. In practice, we also introduce a

loosing boundary ϵ_d to estimate directions. At t_3 , if $\theta_{2,3} > \theta_{1,2}$ and $|\theta_3 - \theta_2| > \epsilon_d$, then the operation is “turning right”; if $\theta_{2,3} < \theta_{1,2}$ and $|\theta_3 - \theta_2| > \epsilon_d$, then the operation is “turning left”; otherwise, the operation is “moving straight”.



An overview of the proposed analytic framework

2. **Extraction of Driving State Sequences:** Based on the two speed-related operations and the three direction-related operations, we can define the following driving states as per the table:

TABLE 2: Driving states.

(1)	acceleration while turning right
(2)	acceleration while turning left
(3)	acceleration while straightforward
(4)	deceleration while turning right
(5)	deceleration while turning left
(6)	deceleration while straightforward
(7)	constant speed while turning right
(8)	constant speed while turning left
(9)	constant speed while straightforward

With the above definitions, we can identify the driving state of a driver at each time stamp. In other words, each trajectory is associated with a driving state sequence, which is denoted by $\{(ID, t_n, S_n)\}_{n=1}^N$, where ID is the identity of the driver, N is the size of the driving state sequence, t_n is the n^{th} time stamp, and S_n is the driving state at t_n .

3. **Peer and Temporal-Aware Representation Learning:** There are peer and temporal dependencies among driving behavior. Therefore, in this project, we model the representation of driving behavior based on the following intuitions.
- Intuition 1: *Structural Reservation*: After reducing driving behavior into graphs, we need a representation learning based method to transform graphs into vectors in a latent feature space for automated quantification and profiling. Consequently, the method should be able to project graphs into lower-dimensional vectors while reserving corresponding characteristics and structures.
 - Intuition 2: *Peer Dependency*: If two drivers exhibit similar driving habits, and the vehicle operation patterns of two corresponding trajectories are similar, then the driving state transition graphs of these two trajectories share a lot in terms of structures and characteristics. As a result, the learned representations of driving behavior should be close to each other. Consequently, the method should be able to model the graph-graph peer dependency in representation learning.
 - Intuition 3: *Temporal Dependency*: The driving operations of the current time slot have autocorrelation with previous driving states. For example, if a driver decelerates while straightforward at t , and if $\Delta(t, t+1)$ is small enough, then he is likely to accelerate at $t + 1$. Consequently, the method should be able to model the current-past temporal dependency in representation learning.
4. **Base Model:** We utilize the deep Auto-Encoder model [8] as our base model. The motivation of using Auto-Encoder is that we aim to model the structural information of the driving state transition graph. Auto-Encoder shows the good performance of modeling structural information [9]. In addition, previous studies [10], [11] show that autoencoder is effective in modeling human mobility data, which fits the scenario in our work.

Auto-Encoder is an unsupervised neural network model, which projects the instances in original feature representations into a lower-dimensional feature space via a series of non-linear mappings. The Auto-Encoder model involves two steps: encode and decode. The encode part projects the original feature vector to the objective feature space, while the decode step recovers the latent feature representation to a reconstruction space. In the auto-encoder model, we need to ensure that the original feature representation of instances should be as similar to the reconstructed feature representation as possible. Formally, let x_i be the original feature representation of the i^{th}

driver, and y^1, y^2, \dots, y^o be the latent feature representations of the driver at hidden layers 1, 2, \dots , o in the encode step respectively, the encoding result in the objective lower-dimension feature space can be represented as $z_i \in \mathbb{R}^d$ with dimension d . Formally, the relationship between these vector variables is denoted by:

$$\begin{cases} y_i^1 &= \sigma(W^1 x_i + b^1), \\ y_i^k &= \sigma(W^k y_i^{k-1} + b^k), \quad \forall k \in \{2, 3, 4, \dots, o\}, \\ z_i &= \sigma(W^{o+1} y_i^o + b^{o+1}). \end{cases} \quad (3)$$

Meanwhile, in the decode step, the input will be the latent feature vector z_i (i.e., the output of the encode step), and the final output will be the reconstructed vector \hat{X}_i . The latent feature vectors at each hidden layers can be represented as $\hat{y}_i^o, \hat{y}_i^{o-1}, \hat{y}_i^{o-2}, \dots, \hat{y}_i^1$. The relationship between these vector variables is denoted by:

$$\begin{cases} \hat{y}_i^o &= \sigma(\bar{W}^{o+1} z_i + \bar{b}^{o+1}), \\ \hat{y}_i^{k-1} &= \sigma(\bar{W}^k y_i^k + \bar{b}^k), \quad \forall k \in \{2, 3, 4, \dots, o\}, \\ \hat{x}_i &= \sigma(\bar{W}^1 \hat{y}_i^1 + \bar{b}^1). \end{cases} \quad (4)$$

where W s and b s are the weight matrices and bias terms to be learned in the model. The objective of the auto-encoder model is to minimize the loss between the original feature vector x and the reconstructed feature vector \hat{x} . Formally, the loss function is

$$\mathbb{H}_c(G^T) = \sum_{u_i \in \mathcal{U}} \sum_{u_j \in \mathcal{U}, u_i \neq u_j} S_{i,j}^T \cdot \|Z_i^T - Z_j^T\|_2^2$$

where u_i denotes the i^{th} driver and \mathcal{U} denotes the driver set.

CHAPTER 3

EXPERIMENTAL RESULTS

In this chapter, we aim to present our implementation details of the proposals made in a research paper titled Spatiotemporal Representation Learning for Driving Behavior Analysis: A Joint Perspective of Peer and Temporal Dependencies by *Pengyang Wang, Xiaolin Li, Yu Zheng, Charu Aggarwal, Yanjie Fu* [6]

Data Preprocessing:

Before using trajectory data, we need to deal with a number of issues, such as *noise-filtering*, *segmentation* [7]. The goal of noise filtering is to remove from a trajectory some noise points that may be caused by the poor signal of location positioning systems (e.g., when traveling in a city canyon). Trajectory segmentation divides a trajectory into fragments by time interval, spatial shape, or semantic meanings, for a further process like clustering and classification.

TABLE 3: Statistics of the experimental data.

Properties	Statistics
Number of drivers	10,357
Time range	Feb.2 - Feb.8
Sampling Interval	117 Seconds
Sampling Distance	623 Meters
Total Trajectories	15 Million
Total Distance	9 million KM
Records are within a time window	83 in Average
City	Beijing

Data Description:

Table 3 shows the statistics of our real-world data sets T-Drive trajectory dataset [12], [13]. This dataset contains the GPS trajectories of 10,357 taxis during the period of Feb. 2 to Feb. 8, 2008 within Beijing. The total number of points in this dataset is about 15 million and the total distance of the trajectories reaches to 9 million kilometers. The average sampling interval is about 177 seconds with a distance of about 623 meters. Each GPS point contains the information of corresponding driver ID, latitude, longitude, and time stamp.

Experimental Setup:

We run our programs on python 3.6 on x64 machine and standard plotting packages with 8GB RAM, 1.8 Ghz i7 CPU. Majority of the work implemented was using the pandas data frame.

Results:

The formulation of problem statement has been done along with the study required for the implementation. Dataset for the implementation is collected and will be used to complete the implementation task. As our implementation is not yet completed, hence results are not submitted.

Future Scope:

Implementation of the proposed idea of PTARL framework opens up the possibility of improvements in terms of better efficiency and more accurate results. Moreover, the idea can thus be tested using a variety of algorithms and the overall loss can even be optimized.

CHAPTER 4

CONCLUSION

Driving behavior analysis can be very useful in assessing driver performances, improving traffic safety, and development of an intelligent and resilient transportation systems. In this project, we have tried to implement the proposals made in a research paper titled Spatiotemporal Representation Learning for Driving Behavior Analysis: A Joint Perspective of Peer and Temporal Dependencies by *Pengyang Wang, Xiaolin Li, Yu Zheng, Charu Aggarwal, Yanjie Fu* [6]

The ideas help to investigate driving behavior analysis from the perspective of representation learning. We used the formulation of problem of driving behavior profiling and scoring as a task of spatial and temporal embedding and labelling with driving state transition graphs. We used the studies of large-scale driving behavior data, and identified the peer and temporal dependencies.

To improve the performance of automated behavior profiling, we used an analytic framework that jointly modelled the peer and temporal dependencies, discussed in this paper [6]. Specifically, we used the idea to first construct multi-view driving state transition graphs from GPS traces to characterize driving behavior. Besides, the idea of gated recurrent unit is also incorporated to model both the graph-graph peer dependency and integrate graph-graph peer penalties to capture the current-past temporal dependency in two optimization strategies, i.e.(i) jointly optimization and (ii) step-by-step optimization. The empirical experiments on real-world data demonstrated the effectiveness of spatio-temporal representation learning for profiling driving behavior.

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