

# EXPERIMENT 8

**Objective:** Implementation of Edmonds-Karp algorithm to find maximum flow.

## Brief Theory:

The Edmonds-Karp algorithm is an implementation of the **Ford-Fulkerson method** for computing the **maximum flow** in a flow network. It uses **Breadth-First Search (BFS)** to find augmenting paths, ensuring the shortest path (in terms of the number of edges) is selected in each iteration.

## Key Concepts:

1. Flow Network: A directed graph where each edge has a capacity and a flow.
2. Residual Graph: Tracks the available capacity for each edge after considering the current flow.
3. Augmenting Path: A path in the residual graph from the source to the sink where additional flow can be pushed.

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**Algorithm 1** FORDFULKERSON( $G$ )

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```
1:  $f \leftarrow 0$ ;  $G_f \leftarrow G$ 
2: while  $G_f$  contains an  $s - t$  path  $P$  do
3:   Let  $P$  be one such path.
4:   Augment  $f$  using  $P$ .
5:   Update  $G_f$ 
6: end while
7: return  $f$ 
```

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**Algorithm 2** EDMONDSKARP( $G$ )

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```
1:  $f \leftarrow 0$ ;  $G_f \leftarrow G$ 
2: while  $G_f$  contains an  $s - t$  path  $P$  do
3:   Let  $P$  be an  $s - t$  path in  $G_f$  with the minimum number of edges.
4:   Augment  $f$  using  $P$ .
5:   Update  $G_f$ 
6: end while
7: return  $f$ 
```

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## Task:

- 1) Write a program to perform BFS on a graph and find the shortest path (in terms of the number of edges) from the source to the sink.
- 2) Implement a function to calculate the bottleneck capacity along a given path and update the flow in the residual graph.
- 3) Combine BFS and flow augmentation to implement the Edmonds-Karp algorithm and compute the maximum flow in a flow network.
- 4) Implement Ford-Fulkerson using DFS. Compare it with Edmonds-Karp in terms of execution time.

**Apparatus and components required:** Computer with C or C++ Compiler and Linux/Windows platform.

**Experimental/numerical procedure:** Coding, compilation, editing, run and debugging.