Count triplets with sum smaller than X

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Medium Accuracy: 49.96% Submissions: 25677 Points: 4

Given an array arr[] of distinct integers of size N and a value sum, the task is to find the count of triplets (i, j, k), having (i<j<k) with the sum of (arr[i] + arr[j] + arr[k]) smaller than the given value sum.

Example 1:

Input: N = 4, sum = 2 arr[] = {-2, 0, 1, 3}

Output: 2

Explanation: Below are triplets with sum less than 2 (-2, 0, 1) and (-2, 0, 3).

Example 2:

Input: N = 5, sum = 12 arr[] = {5, 1, 3, 4, 7}

Output: 4

Explanation: Below are triplets with sum less than 12 (1, 3, 4), (1, 3, 5),

(1, 3, 7) and (1, 4, 5).

Your Task:

This is a function problem. You don't need to take any input, as it is already accomplished by the driver code. You just need to complete the function countTriplets() that take array arr[], integer N and integer sum as parameters and returns the count of triplets.

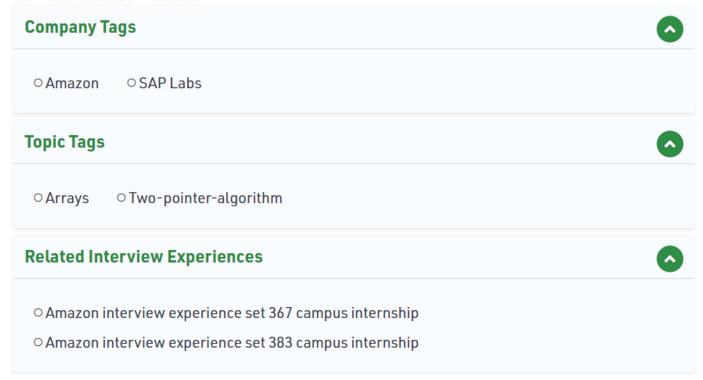
From < https://practice.geeksforgeeks.org/problems/count-triplets-with-sum-smaller-than-x5549/1>

Expected Time Complexity: $O(N^2)$. **Expected Auxiliary Space:** O(1).

Constraints:

 $3 \le N \le 10^3$ -10³ \le arr[i] \le 10³

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Given an array of distinct integers and a sum value. Find count of triplets with sum smaller than given sum value. The expected Time Complexity is $O(n_2)$.

Examples:

```
Input : arr[] = {-2, 0, 1, 3}
sum = 2.

Output : 2

Explanation : Below are triplets with sum less than 2
(-2, 0, 1) and (-2, 0, 3)

Input : arr[] = {5, 1, 3, 4, 7}
sum = 12.
Output : 4
```

```
Explanation: Below are triplets with sum less than 12 (1, 3, 4), (1, 3, 5), (1, 3, 7) and (1, 4, 5)
```

A **Simple Solution** is to run three loops to consider all triplets one by one. For every triplet, compare the sums and increment count if the triplet sum is smaller than the given sum.

From https://practice.geeksforgeeks.org/problems/count-triplets-with-sum-smaller-than-x5549/1#>

```
// A Simple Java program to count triplets with sum smaller
// than a given value
class Test
    static int arr[] = new int[]{5, 1, 3, 4, 7};
    static int countTriplets(int n, int sum)
        // Initialize result
        int ans = 0;
        // Fix the first element as A[i]
        for (int i = 0; i < n-2; i++)
        {
           // Fix the second element as A[j]
           for (int j = i+1; j < n-1; j++)
                // Now look for the third number
               for (int k = j+1; k < n; k++)
                    if (arr[i] + arr[j] + arr[k] < sum)</pre>
                        ans++;
           }
        return ans;
    }
    // Driver method to test the above function
    public static void main(String[] args)
    {
        int sum = 12;
        System.out.println(countTriplets(arr.length, sum));
    }
}
```

The time complexity of the above solution is $O(n_3)$. An **Efficient Solution** can count triplets in $O(n_2)$ by sorting the array first, and then using method 1 of this post in a loop.

```
1) Sort the input array in increasing order.
2) Initialize result as 0.
3) Run a loop from i = 0 to n-2. An iteration of this loop finds all
triplets with arr[i] as first element.
a) Initialize other two elements as corner elements of subarray
arr[i+1..n-1], i.e., j = i+1 and k = n-1
b) Move j and k toward each other until they meet, i.e., while (j < k),
(i) If arr[i] + arr[j] + arr[k] >= sum
then k--
// Else for current i and j, there can (k-j) possible third elements
// that satisfy the constraint.
(ii) Else Do ans += (k - j) followed by j++
Below is the implementation of the above idea.
From <a href="https://practice.geeksforgeeks.org/problems/count-triplets-with-sum-smaller-than-x5549/1#">https://practice.geeksforgeeks.org/problems/count-triplets-with-sum-smaller-than-x5549/1#>
// A Simple Java program to count triplets with sum smaller
// than a given value
import java.util.*;
import java.io.*;
public class countTriplet {
    public static long countTriplets(long arr[], int n, int sum) {
         Arrays.sort(arr);
         int count=0;
       System.out.println(Arrays.toString(arr));
         for (int i = 0; i < arr.length-2; i++) {</pre>
             System.out.println(" current i: "+i);
             int start =i+1;
             int end=n-1;
             while(start<end)</pre>
                  long currentSum=arr[start]+arr[end]+arr[i];
```

if (currentSum<sum)</pre>

```
{
                    count+=end-start;
                    start++;
                }
                else
                {
                    end--;
            }
        }
        return count;
    }
    public static void main(String[] args) throws IOException {
        BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
        String lineOne[] = br.readLine().trim().split("\\s");
        int n = Integer.parseInt(lineOne[0]);
        int k = Integer.parseInt(lineOne[1]);
        String[] lineTwo = br.readLine().trim().split("\\s");
        long arr[] = new long[n];
        for (int i = 0; i < arr.length; i++) {</pre>
            arr[i] = Long.parseLong(lineTwo[i]);
        System.out.println("Arr : " + Arrays.toString(arr));
        int sum = k;
        long ans = countTriplets(arr, n, sum);
        System.out.println(" ANs :" + ans);
    }
}
```