

Collaborative weighted multi-view feature extraction (CWMvFS)

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Chapter

1 Introduction

1.1 Multiview Learning

Multi-view learning is an emerging direction in machine learning which considers learning with multiple views to improve the generalization performance. Multi-view learning is also known as data fusion or data integration from multiple feature sets.

1.2 LCR

local collaborative representative (LCR) method is utilized to preserve the local correlation in between-view and within-view respectively. Furthermore, it realizes that less similar view pairs should share more consistency and complementary information

1.3 CWM_vFE

CWM_vFE preserves the local correlation in multi-view, including local correlation in both between-view and within-view, but also explores the differences in similarities between different view pairs. Experiments on four image data sets demonstrate that CWM_vFE has better performance than other related methods

Chapter 2

Mathematical Formulation

2.1 Formulation

Let us examine MCCA characterized by (8) and (9). First, MCCA only explores the correlations between different views, but neglects to explore the manifold structure of the single-view itself. Second, MCCA ignores the discriminant information between different view pairs, because it assigns the same weight to different view pairs. Thus, we propose a novel method CWMvFE for multi-view feature extraction with the data matrices (1). CWMvFE is based on locality collaborative representation and Jensen Shannon divergence. It not only considers locality correlation information in single-view and multi-view, but also explores similarity between any different view pairs. Thus corresponding to (8) and (9), our optimization problem of CWMvFE can be written as:

$$\min_{P_1, \dots, P_V} \sum_{\substack{A, B=1 \\ A \neq B}}^V \sum_{i=1}^N \|P_A^T(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A) - P_B^T(x_i^B - \tilde{X}_B^i s_{i,\cdot}^B)\|_2^2 JS(A \parallel B) \quad (19)$$

where the matrix $\tilde{X}_v^i = [x_{i,1}^v, \dots, x_{i,k}^v]$, $v = A, B$ is constructed by k -nearest neighborhood samples of x_i^v , and $s_{i,\cdot}^v$ is calculated by (14). $JS(A \parallel B)$ is weight value to measure the similarity between any view pairs, which is calculated by (18). CWMvFE embodies the ideal that less similar view pairs should share more complementary information with each other. The objective function can be expanded as:

$$\begin{aligned} & \sum_{\substack{A, B=1 \\ A \neq B}}^V \sum_{i=1}^N \|P_A^T(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A) - P_B^T(x_i^B - \tilde{X}_B^i s_{i,\cdot}^B)\|_2^2 JS(A \parallel B) \\ &= \sum_{\substack{A, B=1 \\ A \neq B}}^V \sum_{i=1}^N \left\{ \|P_A^T(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A)\|_2^2 + \|P_B^T(x_i^B - \tilde{X}_B^i s_{i,\cdot}^B)\|_2^2 \right. \\ & \quad \left. - 2P_A^T(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A)(x_i^B - \tilde{X}_B^i s_{i,\cdot}^B)^T P_B \right\} JS(A \parallel B) \\ &= 2 \sum_{\substack{A, B=1 \\ A \neq B}}^V \sum_{i=1}^N JS(A \parallel B) P_A^T(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A)(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A)^T P_A \\ & \quad - 2 \sum_{\substack{A, B=1 \\ A \neq B}}^V \sum_{i=1}^N JS(A \parallel B) P_A^T(x_i^A - \tilde{X}_A^i s_{i,\cdot}^A)(x_i^B - \tilde{X}_B^i s_{i,\cdot}^B)^T P_B \end{aligned}$$

$$\begin{aligned}
&= 2 \sum_{\substack{A, B=1 \\ A \neq B}}^V JS(A \parallel B) P_A^T \mathcal{X}_A \mathcal{X}_A^T P_A \\
&\quad - 2 \sum_{\substack{A, B=1 \\ A \neq B}}^V JS(A \parallel B) P_A^T \mathcal{X}_A \mathcal{X}_B^T P_B
\end{aligned} \tag{20}$$

where $\mathcal{X}_A = [x_1^A - \tilde{X}_A^1 s_{1,\cdot}^A, \dots, x_N^A - \tilde{X}_A^N s_{N,\cdot}^A]$ and $\mathcal{X}_B = [x_1^B - \tilde{X}_B^1 s_{1,\cdot}^B, \dots, x_N^B - \tilde{X}_B^N s_{N,\cdot}^B]$. Let us examine the last line in (20). It can be easily proven that the first term $\sum_{\substack{A, B=1 \\ A \neq B}}^V JS(A \parallel B) P_A^T \mathcal{X}_A \mathcal{X}_A^T P_A$ explores locality collaborative correlations from the single-view itself, which is similar to CRP (Lv et al., 2017; Huang et al., 2018a). And the second term $\sum_{\substack{A, B=1 \\ A \neq B}}^V JS(A \parallel B) P_A^T \mathcal{X}_A \mathcal{X}_B^T P_B$ is concerned with local canonical correlations information from multi-views. In order to get more generalized flexibility, a parameter $\gamma > 0$ is introduced to balance the above two terms. Thus, the final optimization problem of our CWMvFE is constructed as the following:

$$\begin{aligned}
&\max_{P_1, \dots, P_V} \text{tr} \left(\sum_{\substack{A, B=1 \\ A \neq B}}^V JS(A \parallel B) P_A^T \mathcal{X}_A \mathcal{X}_B^T P_B \right. \\
&\quad \left. - \gamma \sum_{\substack{A, B=1 \\ A \neq B}}^V JS(A \parallel B) P_A^T \mathcal{X}_A \mathcal{X}_A^T P_A \right) \\
&s.t. \quad P_A^T P_A = I, A = 1, \dots, V
\end{aligned} \tag{21}$$

where $I \in R^{d \times d}$ is identity matrix. $\gamma > 0$ is the parameter. The problem (21) is equivalent to the following generalized eigenvalue problem:

$$\begin{bmatrix}
-\gamma \mathcal{X}_1 \mathcal{X}_1^T \sum_{B=2}^V JS(1 \parallel B) & \mathcal{X}_1 \mathcal{X}_2^T JS(1 \parallel 2) & \dots & \mathcal{X}_1 \mathcal{X}_V^T JS(1 \parallel V) \\
\vdots & \vdots & \ddots & \vdots \\
\mathcal{X}_V \mathcal{X}_1^T JS(V \parallel 1) & \mathcal{X}_V \mathcal{X}_2^T JS(V \parallel 2) & \vdots & -\gamma \mathcal{X}_V \mathcal{X}_V^T \sum_{B=1}^{V-1} JS(V \parallel B)
\end{bmatrix}
\begin{bmatrix} P_1 \\ \vdots \\ P_V \end{bmatrix} = \lambda \begin{bmatrix} I & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \vdots & I \end{bmatrix} \begin{bmatrix} P_1 \\ \vdots \\ P_V \end{bmatrix} \tag{22}$$

The projection matrix $P_A = [p_1^A, \dots, p_d^A]$, $A = 1, \dots, V$, can be obtained by the eigenvectors associated with the d largest eigenvalues.

Chapter 3

Algorithm

Chapter 4

Documentation of API

4.1 Package organization

4.2 Methods

Chapter 5

Example 5.1

Example 1

```
from sklearn.cross_decomposition import CCA
X = [[0., 0., 1.], [1., 0., 0.], [2., 2., 2.], [3., 5., 4.]]
Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
cca = CCA(n_components=1)
cca.fit(X, Y)
X_c, Y_c = cca.transform(X, Y)
```

5.2 Example

1 ¶ ¶

Chapter 6

Learning Outcome

6.1 1 1

6.2 1 1

Appendix A

References

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