



## Merge Sorted Arrays (with Extra Space)

$A_1 :$  2 4 5 7 8 ↓  $O(N)$

$A_2 :$  1 3 6 9 10 11 12  
↑ ↑ ↑ ↑  $O(M)$

$\text{ans} = 1 2 3 4 5 6 7 8 9 10 11 12$

$$TC = O(N+M)$$

$$SC = O(N+M)$$



## Code With Extra Space

```
class Solution {
    public void merge(int[] nums1, int m, int[] nums2, int n) {
        int[] c = new int[n + m];

        int i = 0;
        int j = 0;
        int k = 0;

        while(i < m && j < n) {
            if(nums1[i] < nums2[j]) {
                c[k++] = nums1[i++];
            } else {
                c[k++] = nums2[j++];
            }
        }

        while(i < m) {
            c[k++] = nums1[i++];
        }

        while(j < nums2.length) {
            c[k++] = nums2[j++];
        }

        for(int x=0;x<c.length;x++) {
            nums1[x] = c[x];
        }
    }
}
```

## Without Extra Space (Insertion Sort) {TC worse but space const.}

$a1[] = [1 \ 4 \ 7 \ 8 \ 10]$

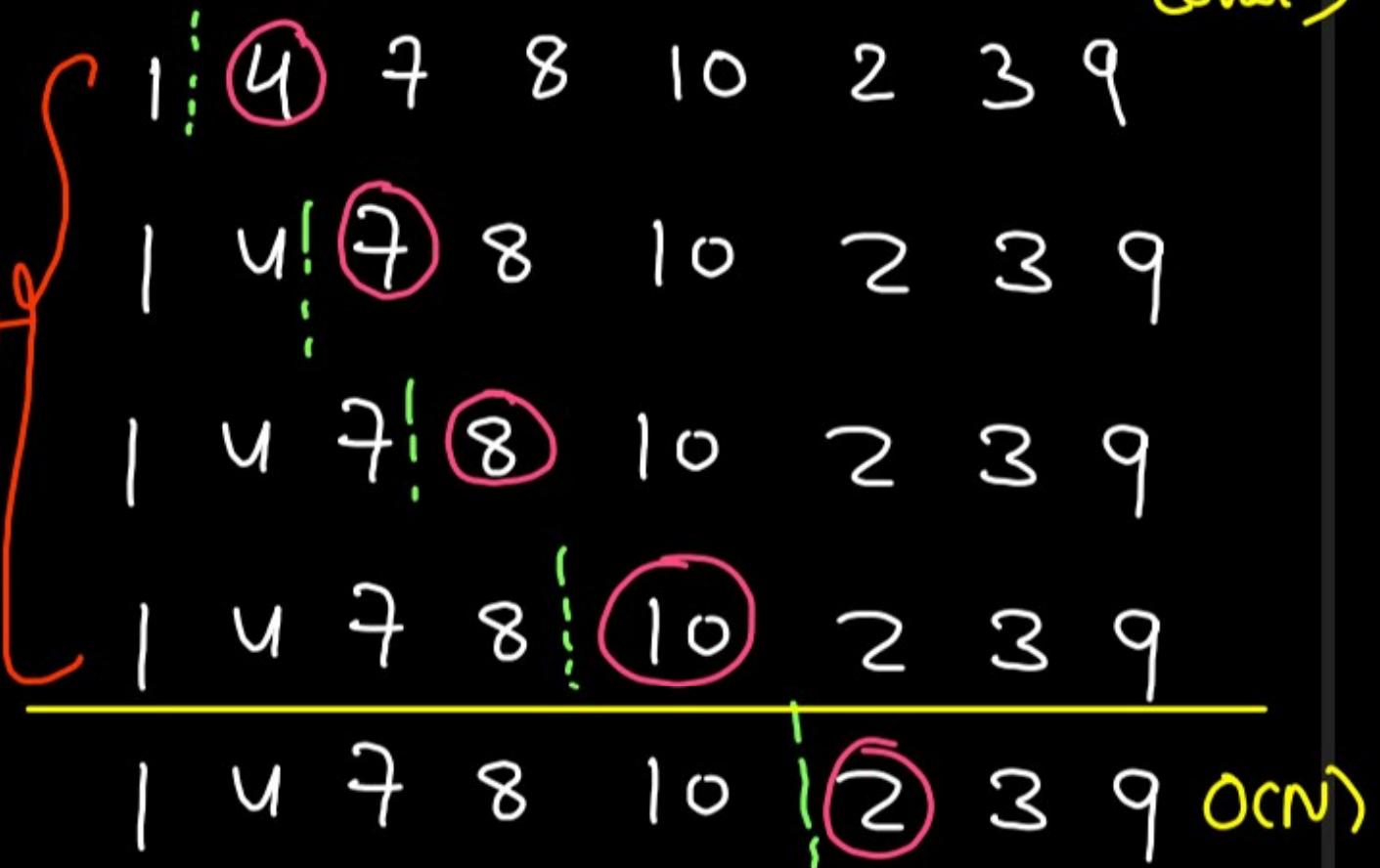
$a2[] = [2 \ 3 \ 9]$

$$TC = N + (N+1) + (N+2) + \dots + (N+M)$$

$$TC = N \times M + \left( \frac{M(M+1)}{2} \right)$$

$$TC = O(N \times M + M^2)$$

Redundant



1 2 3 4 7 8 9 10

1 2 4 7 8 10 3 9 0(N+1)  
1 2 3 4 7 8 10 9 0(N+2)



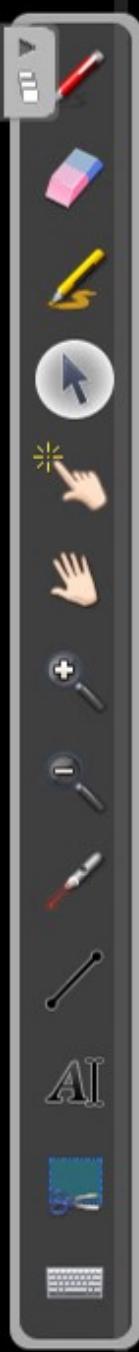
# Code for Insertion Sort Approach (constant space)

```
class Solution {

    private void swap(int[] arr, int i, int j) {
        int temp = arr[i];
        arr[i] = arr[j];
        arr[j] = temp;
    }

    public void merge(int[] nums1, int m, int[] nums2, int n) {
        for(int i=m; i<m+n; i++) {
            nums1[i] = nums2[i - m];
        }

        for(int i=m; i<m+n; i++) {
            for(int j=i; j>0; j--) {
                if(nums1[j] < nums1[j-1]) {
                    swap(nums1, j, j-1);
                } else {
                    break;
                }
            }
        }
    }
}
```



## Shell Sort (Learn this approach. No proof as why it works)

$$a_1[] = [1 \quad 4 \quad 7 \quad 8 \quad 10]$$

$$a_2[] = [2 \quad 3 \quad 9]$$

$$\text{gap sequence} = \frac{N+M}{2}, \frac{N+M}{4}, \frac{N+M}{8}, \dots$$

$$= \frac{8}{2}, \frac{8}{4}, \frac{8}{8}$$

① 4 7 8 10 2 3 9

gap = 4  
① 4 7 8 10 ② 3 9

1 2 ⑦ 8 10 4 ③ 9

1 2 3 ⑧ 10 4 7 9

1 2 3 8 10 4 7 9

① 2 ③ 8 10 4 7 9

1 ② 3 ⑧ 10 4 7 9

1 2 ③ 8 ⑩ 4 7 9

1 2 3 ⑧ 10 ④ 7 9

1 2 3 4 ⑩ 8 ⑦ 9

1 2 3 4 7 ⑧ 10 ⑨

↑ 2 3 4 7 8 10 9

1 2 3 4 7 8 9 10

↑ n+m-1

sorted comp

n+m-4 comparisons

n+m-2 comparisons



## Code using Shell Sort

```
class Solution {  
  
    public void swap(int[] nums, int i, int j) {  
        nums[i] = nums[i] ^ nums[j];  
        nums[j] = nums[i] ^ nums[j];  
        nums[i] = nums[i] ^ nums[j];  
    }  
  
    public void merge(int[] nums1, int m, int[] nums2, int n) {  
        for(int i=m; i<m+n; i++) {  
            nums1[i] = nums2[i-m];  
        }  
  
        for(int gap = (m + n + 1)/2; gap >= 1; gap = gap / 2) {  
            for(int i=0, j=i+gap; j<m+n; i++, j++) {  
                if(nums1[i] > nums1[j]) {  
                    swap(nums1, i, j);  
                }  
            }  
        }  
  
        for(int i=0, j=1; j<m+n; i++, j++) {  
            if(nums1[i] > nums1[j]) {  
                swap(nums1, i, j);  
            }  
        }  
    }  
}
```

3 Swap using XOR

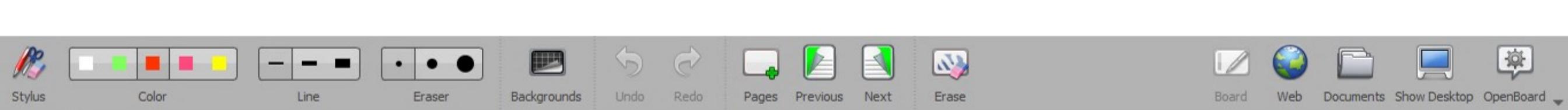
$$\begin{aligned}a &= a \wedge b \\b &= a \wedge b \\a &= a \wedge b\end{aligned}$$

More proper code



```
public void merge(int[] nums1, int m, int[] nums2, int n) {  
    for(int i = m; i < m+n; i++) {  
        nums1[i] = nums2[i - m];  
    }  
  
    for(double gap = (m + n) / 2.0; gap > 0; gap = gap/2.0){  
        int jStart = (int)Math.ceil(gap);  
        for(int i=0, j=jStart; j<m+n; i++, j++){  
            if(nums1[i] > nums1[j]){  
                swap(nums1, i, j);  
            }  
        }  
        if(jStart == 1) break;  
    }  
}
```

→ 1 Gap k liye chalana padega coz  
ho sakte hai and me gap 1 na acha ho.



```
public void merge(int[] nums1, int m, int[] nums2, int n) {  
    for(int i = m; i < m+n; i++){  
        nums1[i] = nums2[i - m];  
    }  
  
    for(double gap = (m + n) / 2.0; gap > 0; gap = gap/2.0){  
        int jStart = (int)Math.ceil(gap);  
        for(int i=0, j=jStart; j<m+n; i++, j++){  
            if(nums1[i] > nums1[j]){  
                swap(nums1, i, j);  
            }  
        }  
        if(jStart == 1) break;  
    }  
}
```

$$gap = \frac{N}{2} \quad N - \frac{N}{2}$$

$$\frac{N}{4} \quad N - \frac{N}{4}$$

$$\frac{N}{8} \quad N - \frac{N}{8}$$

$$TC = O(N \log_2 N - N \left\{ \frac{1}{2} + \frac{1}{4} + \dots \right\})$$

$$TC = O(N \log_2 N - 2^N)$$
$$\approx TC = O(N \log_2 N)$$

# Space Time trade-off in Merge Sorted Arrays Qs -

	Time	Space	
Two Ptr	$O(m+n)$	$O(m+n)$	
Insertion Sort	$O(N*M + M^2)$	$O(1)$	Constant Space
Shell Sort	$O((M+N) \log_2(M+N))$	$O(1)$	

# Merge Sort (with extra space) {In Place} & {Stable}

mergeSort (arr, 0, 7)

2 8 4 3 | 1 7 6 5

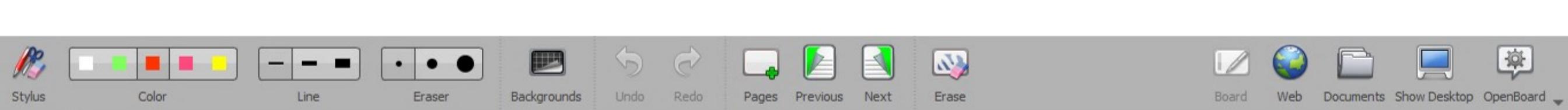


2 3 4 8 | 1 5 6 7

↓  
merge

⇒ Merge technique should be  
 $O(1)$  space technique

1 2 3 4 5 6 7 8



# Code for MergeSort (In-Place) with Extra Space-

```
public void mergeSort(int[] nums, int lo, int hi) {  
  
    if(lo >= hi) {  
        return;  
    }  
  
    int mid = (lo + hi) /2;  
    //sort the left part  
    mergeSort(nums,lo,mid);  
    //sort the right part  
    mergeSort(nums,mid + 1, hi);  
  
    //merge the sorted parts in place  
    merge(nums,lo,mid,mid+1,hi);  
}
```

```
public int[] sortArray(int[] nums) {  
    mergeSort(nums,0,nums.length-1);  
    return nums;  
}
```

```
public int[] sortArray(int[] nums) {  
    mergeSort(nums,0,nums.length-1);  
    return nums;  
}
```

## Time Complexity

$$T(n) = T(n/2) + T(n/2) + O\left(\frac{N}{2} + \frac{N}{2}\right)$$

merging       $x = \log_2 N$

$$T(n) = 2T(n/2) + O\left(\frac{N}{2} + \frac{N}{2}\right)$$

$$2T(n/2) = 2^2 T(n/4) + 2O\left(\frac{N}{4} + \frac{N}{4}\right)$$

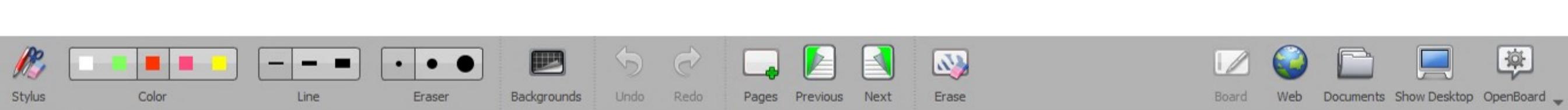
$$2^2 T(n/4) = 2^3 T(n/8) + 2O\left(\frac{N}{8} + \frac{N}{8}\right)$$

⋮

$$2^x T(1) = 2T(0) + O(1)$$

---


$$T(n) = O(N) + 2 * O\left(\frac{N}{2}\right) + 2^2 * O\left(\frac{N}{4}\right) + \dots + 2^x * O(1)$$



Time Complexity without Extra Space (Shell sort)

$$O(N \log_2 N)$$

# RL

$$T(n) = 2T(n/2) + O(N \log_2 N)$$



# Merge Sort is Stable

```

public void merge(int[] nums, int a1l, int a1h, int a2l, int a2h) {
    int size = (a1h-a1l+1) + (a2h-a2l+1);
    int[] res = new int[size];
    int i=a1l, j=a2l, k=0;

    while(i <= a1h && j<= a2h) {
        if(nums[i] <= nums[j]) {
            res[k++] = nums[i++];
        } else {
            res[k++] = nums[j++];
        }
    }

    while(i<= a1h) {
        res[k++] = nums[i++];
    }

    while(j<= a2h) {
        res[k++] = nums[j++];
    }

    for(int x=a1l;x<=a2h;x++) {
        nums[x] = res[x-a1l];
    }
}

```

stable coz of this line.



{ 1 <sup>a</sup> | <sup>b</sup> 2 3 <sup>x</sup> 3 <sup>y</sup> 4 <sup>a</sup> 4 <sup>b</sup> 5 }

## Quick Sort { Partition an Array }

$\downarrow$        $\downarrow$   
 4 5 9 6 4 2 8 1 6 9 3 6 4  
 4 2 1 5 9 6 5 9  
 3 4

$p_i^o = \text{left} - 1$

$\underline{4 4 2 1 3}$   $\textcircled{4}$   $\underline{8 6 6 9 5 6 9}$

$\leq \text{pivot}$

$> \text{pivot}$

$0 \text{ to } l-1 \rightarrow \leq \text{pivot}$

$l \text{ to } r-1 \rightarrow > \text{pivot}$

$r \text{ to } N \rightarrow \text{unexplored}$

```

if (arr[right] > pivot)
  right--
else {
  swap (arr[right], arr[left])
  left++
  right++
}
  
```

Variations

- -ve, +ve
- 0, 1
- even, non-even
- odd, even
- $\leq \text{pivot}, > \text{pivot}$

# DNF Sort / Sort 012 / Three Way Partitioning



# travel using j pointer

```
if (arr[j] == 0)
{
    swap(i, j);
    i++;
    j++;
}

else if (arr[j] == 1)
{
    j++;
}

else {
    swap(j, k);
    k--;
}
```

## Inversion Count {Count Inversion}

count the No of pairs  $(i, j)$  such that  $i < j$  and  $a[i] > a[j]$ .



Brute force:  $O(n^2)$

$(8, 5) (8, 3) (8, 4) (8, 1) (8, 6) (8, 2)$

$(5, 3) (5, 4) (5, 1) (5, 2)$

$(3, 1) (3, 2)$

$(4, 1) (4, 2)$

$(6, 2)$

Ans = 15

# The Ans is  
to return  
the count  
only-

There are various optimizations possible for this DS.

- Merge Sort ✓
- fenwick Tree
- Policy Based DS (ordered Set + Indexing)
- Self Balancing BST (Red Black Tree)

We are studying using MS.

0 1 2 3 4 5 6  
8 5 3 4 1 6 2

[5,8] [3,4]

if 1<sup>st</sup> ele of 1<sup>st</sup> array is > than  
1<sup>st</sup> ele of 2<sup>nd</sup> array, rest all ele of  
1<sup>st</sup> array will make pairs.

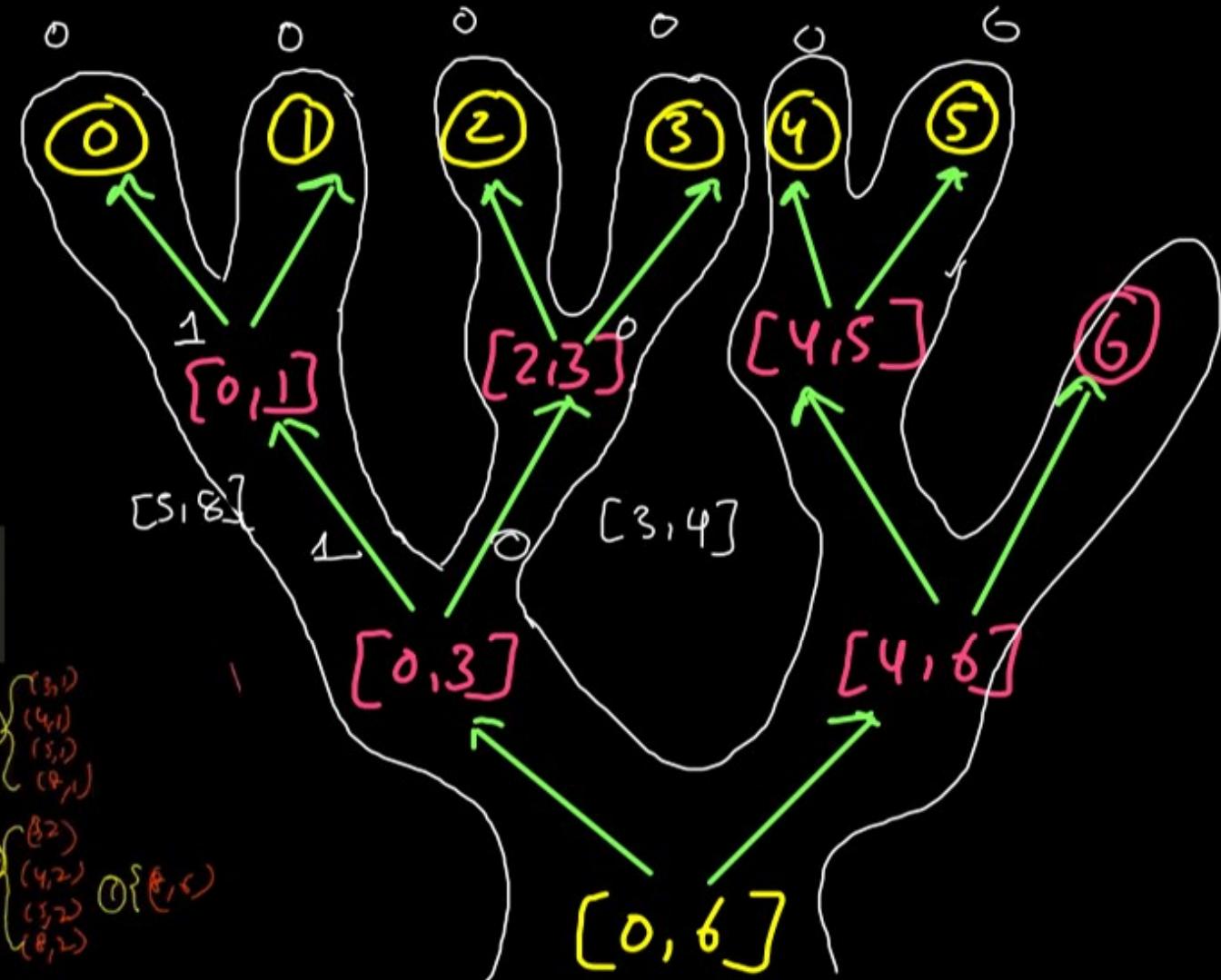
[5,3] [8,3] [5,4] [8,4]

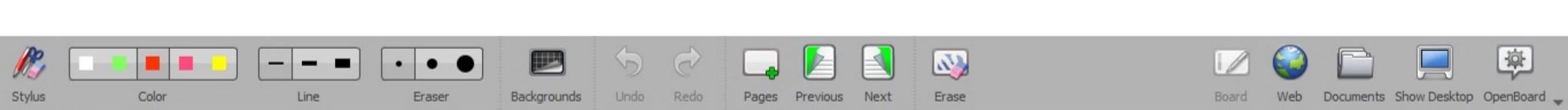
```
public void mergeSort(int[] nums, int lo, int hi) {
    if(lo >= hi) {
        return;
    }

    int mid = (lo + hi) / 2;
    //sort the left part
    mergeSort(nums, lo, mid);
    //sort the right part
    mergeSort(nums, mid + 1, hi);

    //merge the sorted parts in place
    merge(nums, lo, mid, mid+1, hi);
}
```

①(8,5)  
②(5,3)  
③(8,3)  
④(3,4)  
⑤(4,1)  
⑥(1,6)  
⑦(6,2)  
⑧(4,2)  
⑨(3,2)  
⑩(8,2)





# Code for Inversion Count

```
public static long mergeSort(long[] nums, int lo, int hi) {  
    if(lo >= hi) {  
        return 0l;  
    }  
  
    int mid = (lo + hi) / 2;  
    //sort the left part  
    long left = mergeSort(nums, lo, mid);  
    //sort the right part  
    long right = mergeSort(nums, mid + 1, hi);  
  
    //merge the sorted parts in place  
    long ans = merge(nums, lo, mid+1, hi);  
  
    return left + right + ans;  
}
```

```
static long inversionCount(long arr[], long N)  
{  
    return mergeSort(arr, 0, (int)N-1);  
}
```

```
public static long merge(long[] nums, int a1l, int a1h, int a2l, int a2h) {  
    int size = (int)(a1h-a1l+1) + (int)(a2h-a2l+1);  
    long[] res = new long[size];  
    int i=a1l, j=a2l, k=0;  
  
    long invCount = 0l;  
    while(i <= a1h && j <= a2h) {  
        if(nums[i] <= nums[j]) {  
            res[k++] = nums[i++];  
        } else {  
            res[k++] = nums[j++];  
            invCount += (a1h - i + 1l);  
        }  
    }  
  
    while(i <= a1h) {  
        res[k++] = nums[i++];  
    }  
  
    while(j <= a2h) {  
        res[k++] = nums[j++];  
    }  
  
    for(int x=a1l; x<=a2h; x++) {  
        nums[x] = res[x-a1l];  
    }  
  
    return invCount;  
}
```

→ 1<sup>st</sup> array k  
Save rem  
elements.

# Reverse Pairs (Leetcode Hard : 493)

$i < j, a[i] > 2 * a[j]$

0 1 2 3 4 5 6  
40 25 19 12 9 6 2

$[12, 19, 25, 40]$      $[2, 6, 9]$   
 ↗ ↑              ↗ ↗ ↑  
 $\{4, 12, 18\}$

$[12, 2] [19, 2] [25, 2] [40, 2]$

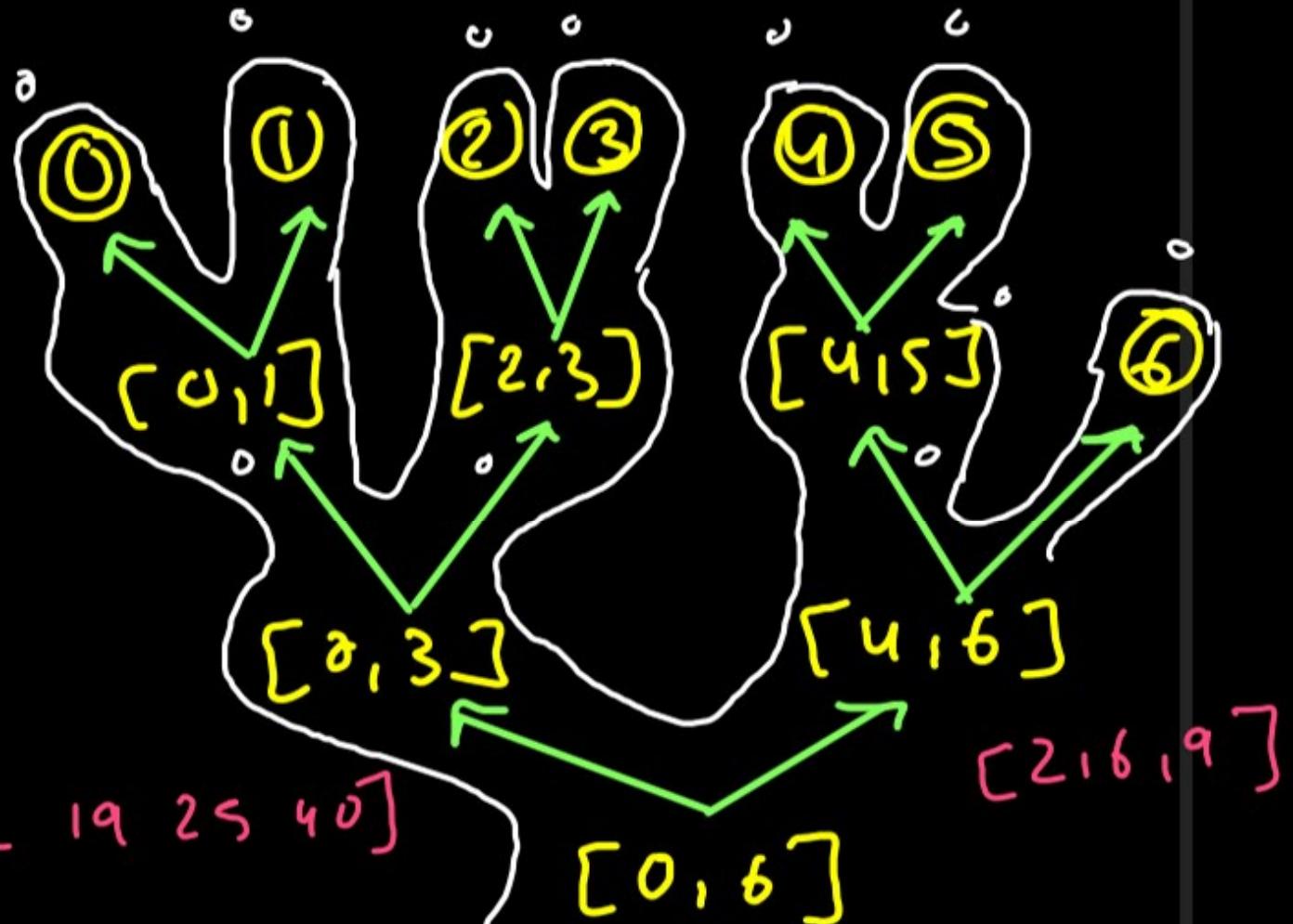
$[19, 6] [25, 6] [40, 6]$

$[19, 9] [25, 9] [40, 9]$

$[12, 19, 25, 40]$

$[0, 6]$

$[2, 6, 9]$



Why should we merge & count the reverse pairs separately?

⇒ If we do merging and counting simultaneously:

$\{25, 40\}$        $\{12, 19\}$       [12]

$\uparrow \longrightarrow +2 (25, 12) (40, 12)$

$\{25, 40\}$        $\{12, 19\}$       [12, 19]  
No pair added However  $\{40, 19\}$

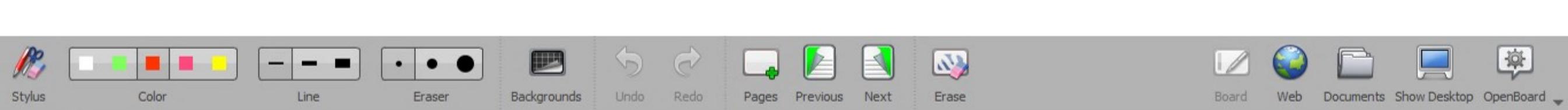
Now only merging will occur

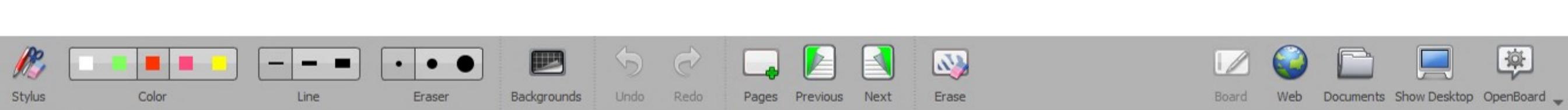
$\{25, 40\}$       [12, 19, 25, 40]

Because while merging  
we only see  $a[i] > a[j]$   
& not  $a[i] > 2 * a[j]$

}

$\rightarrow (40, 19)$  pair  
was missed





## Count Winning Streaks (N^2 approach)

TC:  $O(N^2)$  | count subarrays with more 1s than 0s } { Premium }

0 1 2 3 4 5 6 7  
{ 0, 1, 1, 0, 1, 0, 1, 0 }

```
public static int winningStreak(int[] arr){  
    int ans = 0;  
  
    for(int st=0;st<arr.length;st++) {  
        int countOf0s = 0, countOf1s = 0;  
        for(int end=st;end < arr.length;end++) {  
            if(arr[end] == 0) {  
                countOf0s++;  
            } else {  
                countOf1s++;  
            }  
  
            if(countOf1s > countOf0s) {  
                ans++;  
            }  
        }  
    }  
    return ans;  
}
```

}  $O(N^2)$  approach  
Gives TLE

0 1 2 3 4 5 6 7  
{ 0, [1, 1, 0], 1, 1, 1, 1, 0 }

ls > Os  
↓ ↓  
+1 -1

[ -1, [0, 1, 0] ] , 1, 2, 3, 1, 2 ] → prefix sum

In the original array, jaha jaha valid subarrays

hai, humare array me w subarray ka first ile aur  
w ka (end + 1) index inversion count banaoenge.



$$x \leq l, l < 0, l \geq y$$

$\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$   
 $-1$        $-1$        $1$        $-1$

$(-2)$

$$IS > OS$$

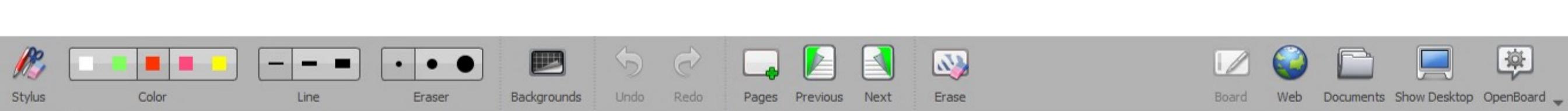
$\downarrow$        $\downarrow$   
 $-1$        $+1$

$$IS > OS$$

-ve

$$y - x < 0$$

$$y < x$$
$$x > y$$



Minimum Swaps to Sort (Swapping only adjacent elems)  
(MinSwaps II)

### Minimum Swaps to Sort

Medium Accuracy: 50.0% Submissions: 89710 Points: 4

Given an array of  $n$  distinct elements. Find the minimum number of swaps required to sort the array in strictly increasing order.

$$\{ 8, 5, 3, 4, 1, 6, 2 \}$$
$$\{ 1, 2, 3, 4, 5, 6, \textcircled{8} \}$$

So, if I want to take 8 to the last pos, I need to swap 8 with all the elements that are greater than 8 and are to its right. (Inversion count for 8)

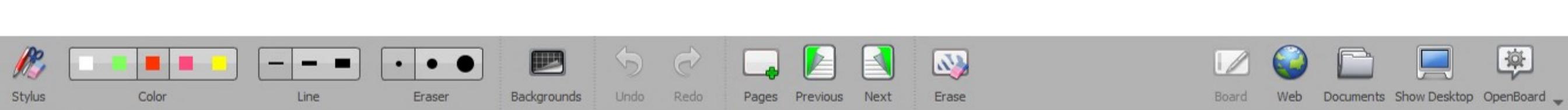


{ 8, 5, 3, 4, 1, 6, 2 }

↓ After 8 reaches correct position

{ (5, 3, 4, 1, 6, 2) 8 }

Ans for 5 is in remaining array. This means that the ans for 5 does not concern 8. This implies (in original array) that  $i < j$  { for  $a[i] > a[j]$  } .



bubble sort -  
min adjacent swaps to sort  
↓  
inversion count

```
public static int merge(int[] nums, int a1l, int a1h, int a2l, int a2h) {  
    int size = (int)(a1h-a1l+1) + (int)(a2h-a2l+1);  
    int[] res = new int[size];  
    int i=a1l, j=a2l, k=0;  
  
    int invCount = 0;  
    while(i <= a1h && j <= a2h) {  
        if(nums[i] <= nums[j]) {  
            res[k++] = nums[i++];  
        } else {  
            res[k++] = nums[j++];  
            invCount += (a1h - i + 1);  
        }  
    }  
  
    while(i <= a1h) {  
        res[k++] = nums[i++];  
    }  
  
    while(j <= a2h) {  
        res[k++] = nums[j++];  
    }  
  
    for(int x=a1l;x<=a2h;x++) {  
        nums[x] = res[x-a1l];  
    }  
  
    return invCount;  
}
```

```
public static int mergeSort(int[] nums, int lo, int hi) {  
  
    if(lo >= hi) {  
        return 0;  
    }  
  
    int mid = (lo + hi) / 2;  
    //sort the left part  
    int left = mergeSort(nums, lo, mid);  
    //sort the right part  
    int right = mergeSort(nums, mid + 1, hi);  
  
    //merge the sorted parts in place  
    int ans = merge(nums, lo, mid, mid+1, hi);  
  
    return left + right + ans;  
}
```

```
int countSwaps(int nums[], int n) {  
    // code here  
    return mergeSort(nums, 0, n-1);  
}
```

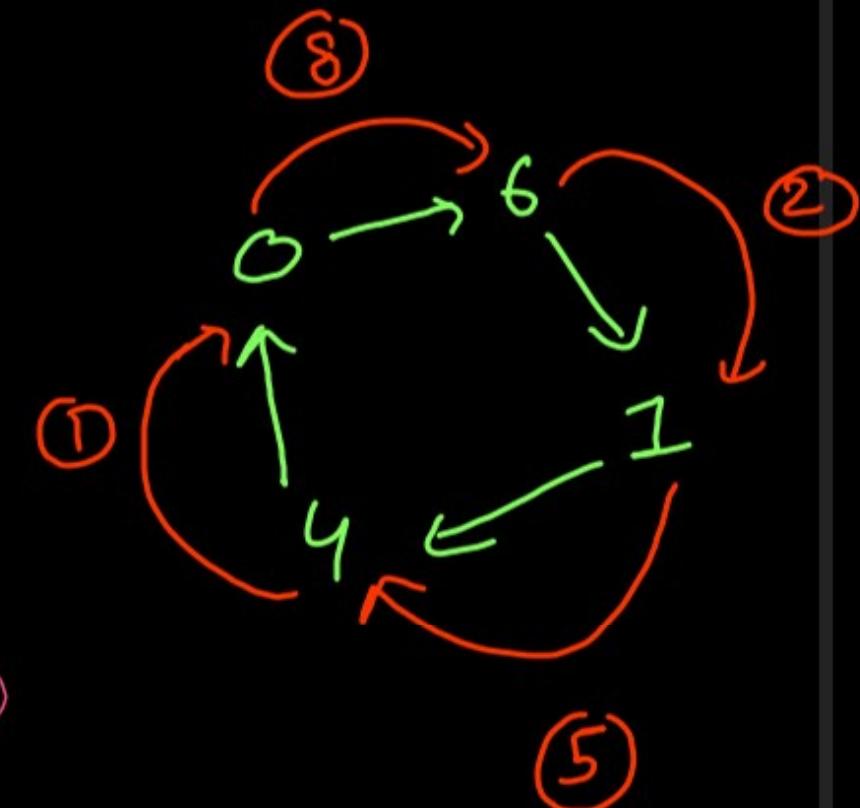


# Minimum Swaps to Sort - I

$\{8, 5, 3, 4, 1, 6, 2\}$

$\{1, 2, 3, 4, 5, 6, 8\}$

	src	dest
8	(8, 6)	
5	(1, 4)	
3	(2, 2)	
4	(3, 3)	
1	(4, 0)	
6	(5, 5)	
2	(6, 1)	

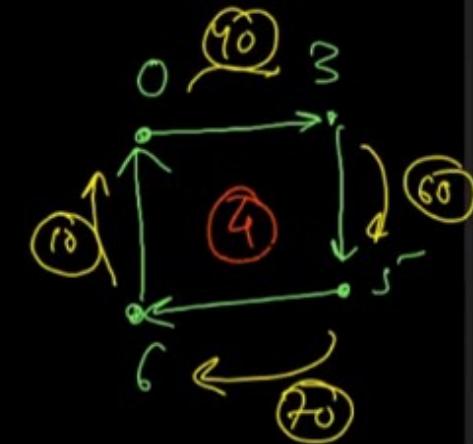
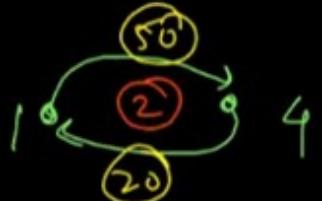


Min Swaps = 4

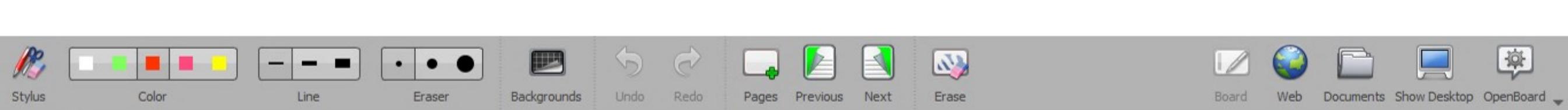
Multiple Cycles are also possible - (Add all cycles length for ans)

40	50	30	60	20	70	10	80
0	1	2	3	4	5	6	7
10	20	30	40	50	60	70	80

$\textcircled{40} \rightarrow \textcircled{3}$     $\textcircled{60} \rightarrow \textcircled{5}$     $\textcircled{10} \rightarrow \textcircled{0}$   
 $\textcircled{50} \rightarrow \textcircled{4}$     $\textcircled{20} \rightarrow \textcircled{1}$     $\textcircled{80} \rightarrow \textcircled{7}$   
 $\textcircled{30} \rightarrow \textcircled{2}$     $\textcircled{40} \rightarrow \textcircled{6}$



One node cannot be a part of 2 cycles as one node will always have only one incoming & one outgoing edge - (Except self loops)



```
public static class Pair implements Comparable<Pair>{
    int ele;
    int idx;

    Pair(int ele, int idx) {
        this.ele = ele;
        this.idx = idx;
    }

    public int compareTo(Pair other) {
        return this.ele - other.ele;
    }

    public int cycleSize(List<Pair> list, int start, boolean[] vis) {
        int res = 0;
        int j = start;

        while(vis[j] == false) {
            vis[j] = true;
            j = list.get(j).idx;
            res++;
        }

        return res - 1;
    }
}
```

```
// FUNCTION TO FIND THE MINIMUM NUMBER OF SWAPS NEEDED
// TO SORT AN ARRAY BY CYCLICALLY SHIFTING ELEMENTS

public int minSwaps(int nums[])
{
    int n = nums.length;
    List<Pair> list = new ArrayList<>();

    for(int i=0;i<n;i++) {
        Pair p = new Pair(nums[i],i);
        list.add(p);
    }

    Collections.sort(list);
    boolean[] vis = new boolean[n];
    int res = 0;
    for(int i=0;i<n;i++) {
        if(vis[i] == false)
            res += cycleSize(list,i,vis);
    }

    return res;
}
```

## Count Sort (Without Stability)

9 6 3 5 3 4 3 9 6 4 6 5 8 2 9  
 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

① 1<sup>st</sup> iteration → find Max & Min.

0	1	2	3	4	5	6	7
1	X23X2X2X2	X23X23X23	X23X23X23	X23X23X23	X23X23X23	X23X23X23	X23X23X23

2 3 1 5 6 7 8 9

0	1	2	3	4	5	6	7
1	3	2	2	3	0	1	3

2 3 1 5 6 7 8 9

2 3 3 3 4 4 5 5 6 6 6 8 9 9 9

3<sup>rd</sup> iteration

$$TC = O(N)$$

$$SC = O(\max - \min + 1)$$



## Bucket Sort

① Characters → Sorting a String

lower case



26 buckets

Uppercase



52 buckets

All ASCII characters



256 buckets

② Maths →  $(0, 100)$

③ Values corresponding to index: N elements & values are  
1 to N or 0 to N-1

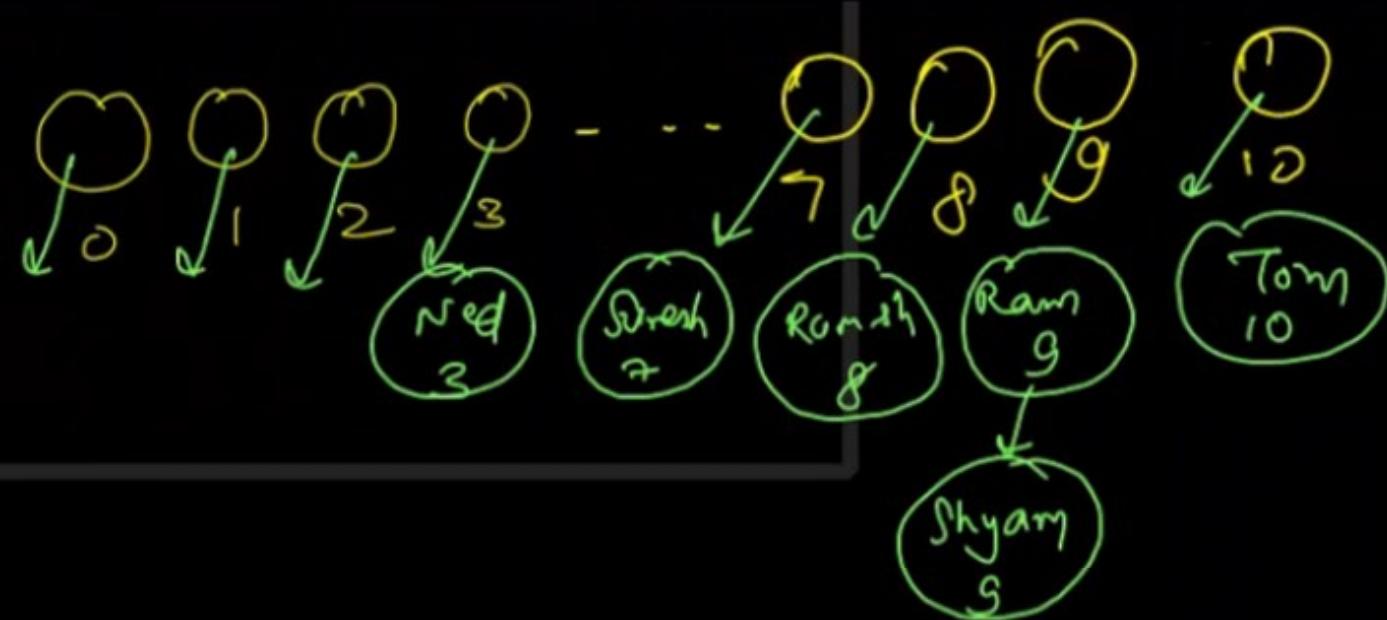
HashMap kind of chaining. This is Stable.

② Marks → (0, 100)

Ram → 9  
Ramesh → 8  
Shyam → 9  
Suresh → 7

Sorting objects based

Tom → 10  
Ned →



No. of buckets = no of distinct elements

Total space = No of buckets +  $\mathcal{O}(N)$  → No of elements  
 if  $N$  is  $\approx$  greater than No of buckets.  $SC = \mathcal{O}(n)$



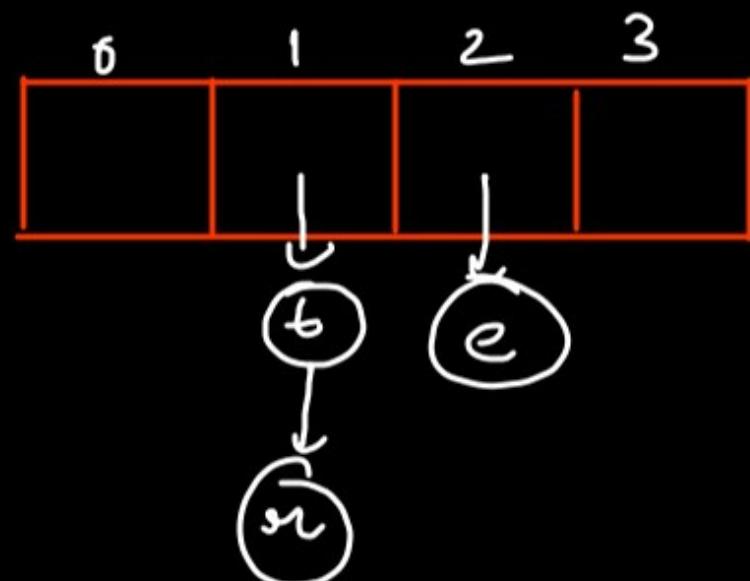
Java  
Tim Sort → intSort ↗ C++  
Merge Sort  $\Rightarrow N > 16$   
Array size { fixed = 16 }  $\rightarrow$  range  $N \leq 16$  ↗ insertion sort

### 451. Sort Characters By Frequency

Medium    4156    181    Add to List    Share

Given a string `s`, sort it in **decreasing order** based on the **frequency** of the characters. The **frequency** of a character is the number of times it appears in the string.

Return the sorted string. If there are multiple answers, return any of them.



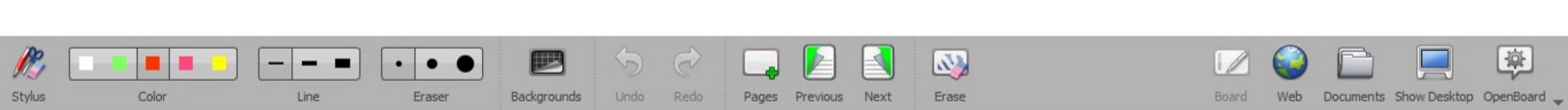
tree

↓

make an array of size `s.length() + 1`  
as max freq of a character can be  
`s.length() & min(0).`

Now traverse each bucket  
But traverse this array of  
buckets in reverse order as  
we want max freq 1st.

**eetr** ⇒ Ans.



```
class Solution {
    public String frequencySort(String s) {
        HashMap<Character, Integer> freq = new HashMap<>();

        for(int i=0;i<s.length();i++) {
            char ch = s.charAt(i);
            int oFreq = freq.getOrDefault(ch,0);
            freq.put(ch, oFreq + 1);
        }

        ArrayList<Character>[] buckets = new ArrayList[s.length() + 1];
        for(int i=0;i<buckets.length;i++) {
            buckets[i] = new ArrayList<>();
        }

        for(Character ch : freq.keySet()) {
            int val = freq.get(ch);
            buckets[val].add(ch);
        }

        StringBuilder sb = new StringBuilder("");
        for(int b=buckets.length-1;b>=0;b--) {
            for(Character ch : buckets[b]) {
                for(int f=0;f<b;f++) {
                    sb.append(ch);
                }
            }
        }

        return sb.toString();
    }
}
```

1636. Sort Array by Increasing Frequency

Easy    1400    55    Add to List    Share

Given an array of integers `nums`, sort the array in **increasing** order based on the frequency of the values. If multiple values have the same frequency, sort them in **decreasing** order.

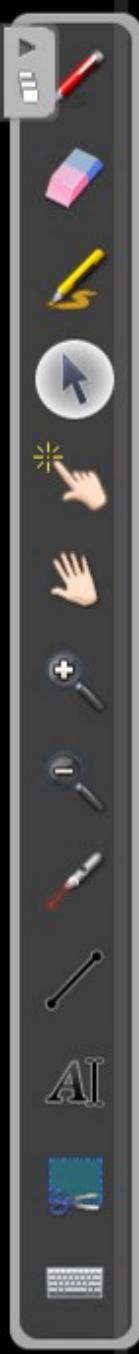
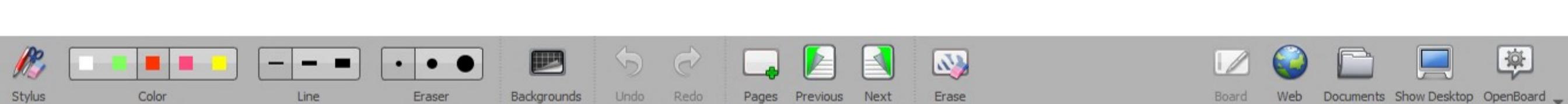
Return the *sorted array*.

# Same as prev ques- Just,  
the buckets will point to  
a TreeSet instead of  
ArrayList because of this  
reason.

TreeSet (Java)

Ordered set (C++)

↳ Self Balancing BST



```
public int[] frequencySort(int[] nums) {
    HashMap<Integer, Integer> freq = new HashMap<>();
    for(int i=0;i<nums.length;i++) {
        int oFreq = freq.getOrDefault(nums[i],0);
        freq.put(nums[i],oFreq + 1);
    }

    TreeSet<Integer>[] buckets = new TreeSet[nums.length + 1];
    for(int i=0;i<buckets.length;i++) {
        buckets[i] = new TreeSet<>();
    }

    for(Integer x : freq.keySet()) {
        int freqVal = freq.get(x);
        buckets[freqVal].add(x); //x will be added in ordered manner itself
    }

    int[] res = new int[nums.length];
    int idx = 0;

    for(int b=0;b<buckets.length;b++) {
        for(Integer x : buckets[b].descendingSet()) {
            for(int f=0;f<b;f++) {
                res[idx++] = x;
            }
        }
    }

    return res;
}
```

WC TC :  $O(N \log_2 N)$

BC TC :  $O(N)$

# Top K Elements {LC: 347}

## 347. Top K Frequent Elements

Medium    9285    374    Add to List    Share

Given an integer array `nums` and an integer `k`, return the `k` most frequent elements. You may return the answer in **any order**.

{ 0 1 2 3 4 5 6 7 8  
{ 1, 1, 1, 2, 2, 2, 3, 4, 6 }



freq, Map

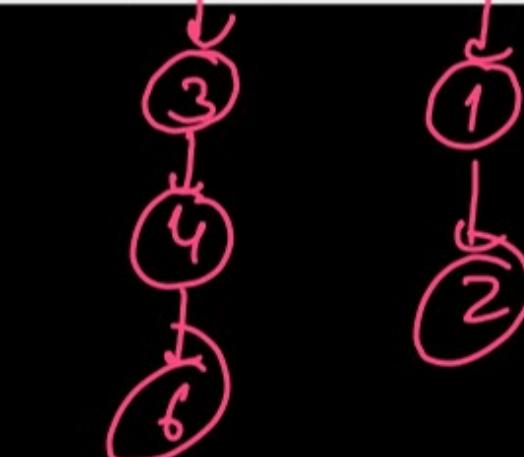
1 - 3

2 - 3

3 - 1

4 - 1

6 - 1





```
class Solution {
    public int[] topKFrequent(int[] nums, int k) {
        HashMap<Integer, Integer> freq = new HashMap<>();

        for(int i=0;i<nums.length;i++) {
            int oFreq = freq.getOrDefault(nums[i], 0);
            freq.put(nums[i], oFreq + 1);
        }

        ArrayList<Integer>[] buckets = new ArrayList[nums.length + 1];

        for(int i=0;i<buckets.length;i++) {
            buckets[i] = new ArrayList<>();
        }

        for(Integer ele : freq.keySet()) {
            int valFreq = freq.get(ele);
            buckets[valFreq].add(ele);
        }

        int[] res = new int[k];
        int idx = 0;
        for(int i=buckets.length-1;i>=0;i--) {

            if(k == 0) break;

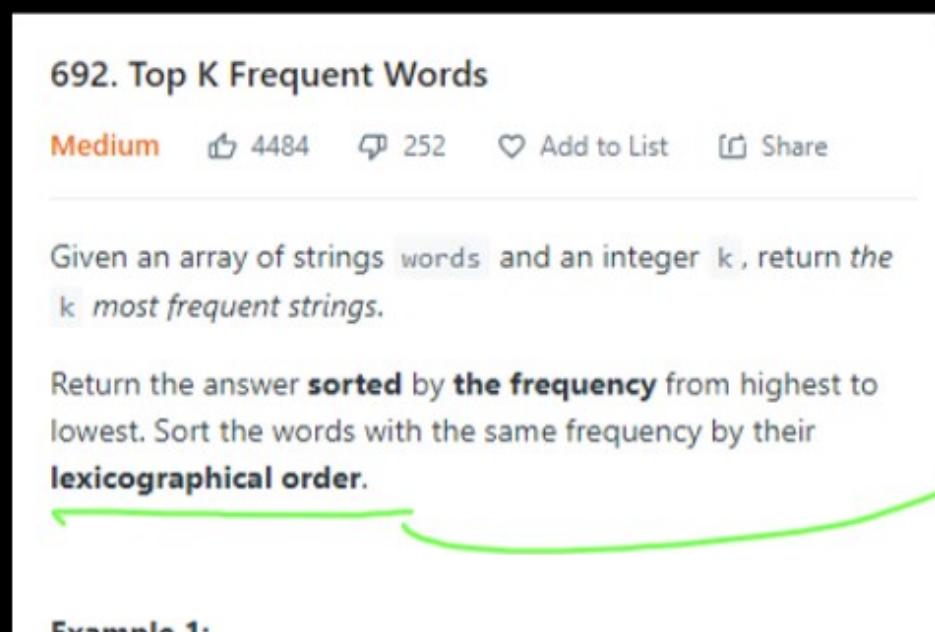
            for(int ele : buckets[i]) {
                res[idx++] = ele;
                k--;
                if(k == 0) break;
            }
        }

        return res;
    }
}
```

$T = O(N)$

A large, hand-drawn red checkmark is drawn on the right side of the screen, pointing towards the handwritten time complexity analysis. It consists of a vertical line with a curved hook at the bottom and a circular loop at the top.

# Top k Words (LC: 692)



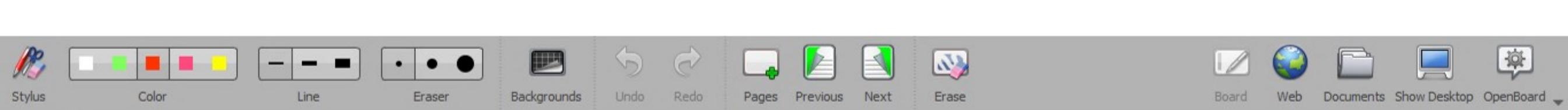
692. Top K Frequent Words  
Medium    4484    252    Add to List    Share

Given an array of strings words and an integer k, return the k most frequent strings.

Return the answer sorted by the frequency from highest to lowest. Sort the words with the same frequency by their lexicographical order.

Example 1:

Same as prev ques. But use TreeSet instead of LinkedList  
to maintain lexicographical order



```
class Solution {
    public List<String> topKFrequent(String[] words, int k) {
        HashMap<String, Integer> freq = new HashMap<>();

        for(String str : words) {
            int oFreq = freq.getOrDefault(str, 0);
            freq.put(str, oFreq + 1);
        }

        TreeSet<String>[] buckets = new TreeSet[words.length + 1];

        for(int i=0;i<buckets.length;i++) {
            buckets[i] = new TreeSet<>();
        }

        for(String word : freq.keySet()) {
            int valFreq = freq.get(word);
            buckets[valFreq].add(word);
        }

        List<String> res = new ArrayList<>();

        for(int i=buckets.length-1;i>=0;i--) {
            if(k == 0) break;

            for(String word : buckets[i]) {
                res.add(word);
                k--;
            }

            if(k == 0) break;
        }

        return res;
    }
}
```

$O(n)$  TC

# Coordinate Compression.

## Convert an array to reduced form

Medium Accuracy: 69.45% Submissions: 4206 Points: 4

Given an array with **N** distinct elements, convert the given array to a reduced form where all elements are in range from **0** to **N-1**. The order of elements is same, i.e., **0** is placed in place of smallest element, **1** is placed for second smallest element, ... **N-1** is placed for largest element.

$\{1^0, 4^0, 2^2\}$

$\{10^0, 40^1, 20^2\}$

$\{10^0, 20^1, 40^2\}$  ↴ Soft

0 2 1

Count sort was also  
Coordinate compression

0	1	2	3	4	5	6	7
1	X23	X2	X2	123	1	X23	
2	3	1	5	6	7	8	9
1	1	2	1	1	1	1	1
0	1	2	2	4	5	6	7

2 ko value 0

3 ko value 1

& soon

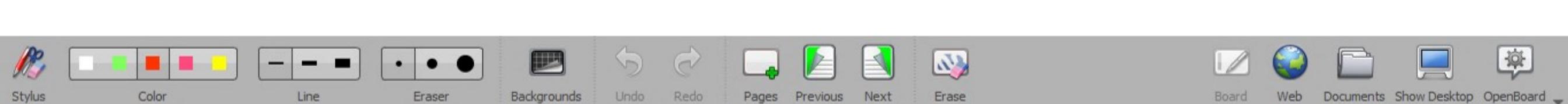
# Coordinate compression can be used in many questions.

Volume factors

$$\left\{ \begin{array}{l} 10^9 \times 7, \quad 10^9, \quad 10^8, \quad 10^6, \quad 10^7 \\ \downarrow \uparrow \quad \downarrow \uparrow \quad \downarrow \uparrow \quad \downarrow \uparrow \quad \downarrow \uparrow \\ 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \end{array} \right.$$

0 1 2 3 4 5

Example



Code for  
Coordinate Compression

```
static class Pair implements Comparable<Pair>{
    int ele;
    int idx;

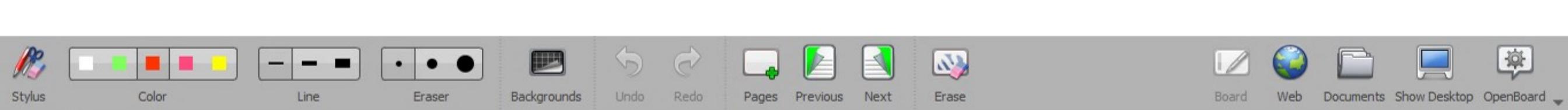
    Pair(int ele, int idx) {
        this.ele = ele;
        this.idx = idx;
    }

    public int compareTo(Pair other) {
        return (this.ele - other.ele);
    }
}

void convert(int[] arr, int n) {
    // code here
    Pair[] nums = new Pair[n];
    for(int i=0;i<nums.length;i++) {
        Pair p = new Pair(arr[i],i);
        nums[i] = p;
    }

    Arrays.sort(nums);

    for(int i=0;i<nums.length;i++) {
        arr[nums[i].idx] = i;
    }
}
```



## 164. Maximum Gap

Hard    2127    287    Add to List    Share

Given an integer array `nums`, return the *maximum difference between two successive elements in its sorted form*. If the array contains less than two elements, return `0`.

You must write an algorithm that runs in linear time and uses linear extra space.

Radix

Sort



```
class Solution {  
    // Radix Sort karna hai  
    // Yaani har digit pe count sort  
    // Since integer me max 10 digits honge  
    // TC -> O(10 * N)  
    // SC -> O(N)  
  
    void countSort(int[] nums,int exp) {  
        int n = nums.length;  
        int[] output = new int[n];  
        int[] count = new int[10];  
  
        for(int i=0;i<n;i++)  
            count[(nums[i]/ exp) % 10]++;  
  
        for(int i=1;i<10;i++) {  
            count[i] += count[i-1];  
        }  
  
        for(int i=n-1;i>=0;i--) {  
            output[count[(nums[i] / exp) % 10] - 1] = nums[i];  
            count[(nums[i] / exp) % 10]--;  
        }  
  
        for(int i=0;i<n;i++)  
            nums[i] = output[i];  
    }  
}
```

```
public int maximumGap(int[] nums) {  
    if(nums.length <= 1) return 0;  
  
    //Radix Sort  
    int n = nums.length;  
    int max = Integer.MIN_VALUE;  
    for(int i=0;i<nums.length;i++) {  
        max = Math.max(max,nums[i]);  
    }  
  
    for(int exp=1;max/exp > 0; exp*= 10) {  
        countSort(nums,exp);  
    }  
  
    int res = 0;  
    for(int i=0;i<n-1;i++) {  
        res = Math.max(res,nums[i+1] - nums[i]);  
    }  
  
    return res;  
}
```



# H-Index

## 274. H-Index

Medium    1239    1857    Add to List    Share

Given an array of integers `citations` where `citations[i]` is the number of citations a researcher received for their  $i^{\text{th}}$  paper, return compute the researcher's **h-index**.

According to the definition of h-index on Wikipedia: A scientist has an index  $h$  if  $h$  of their  $n$  papers have at least  $h$  citations each, and the other  $n - h$  papers have no more than  $h$  citations each.

If there are several possible values for  $h$ , the maximum one is taken as the **h-index**.

$\{3, 0, 6, 1, 5\}$   
 $\downarrow \text{Sort}$   
 $\{0, 1, 1, 3, 5, 6\}$   
 $\downarrow$   
 kam se  
 kam 0 papers with value  $\geq 0$  are  
 $\downarrow$   
 $\text{Highest such value}$   
 $\downarrow$   
 kam se  
 kam 5 papers with value  $\geq 5$

There are not at least 5 papers with value  $\geq 5$ .

{1, 3, 4, 5, 7, 9, 10, 11}

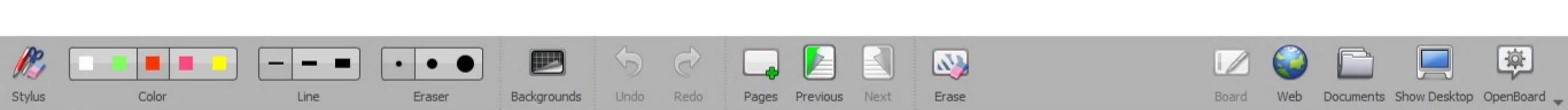
0	1	2	3	4	5	6	7	8	>8
0	1		1	1	1		1		3

→ freq

0	1	2	3	4	5	6	7	8	>8
8	8	7	7	6	5	4	4	3	3

← suffix array

any = 5



```
class Solution {
    public int hIndex(int[] citations) {
        int[] buckets = new int[citations.length + 2];

        for(int citation : citations) {
            if(citation > citations.length) {
                buckets[buckets.length-1]++;
            } else {
                buckets[citation]++;
            }
        }

        for(int i=buckets.length-2;i>=0;i--) {
            buckets[i] += buckets[i + 1];
            if(buckets[i] >= i) return i;
        }

        return 0;
    }
}
```

TC:  $O(z^n)$