

3Sum Unique {Leetcode: 15}

15. 3Sum

Medium 16260 1559 Add to List Share

Given an integer array `nums`, return all the triplets `[nums[i], nums[j], nums[k]]` such that `i != j`, `i != k`, and `j != k`, and `nums[i] + nums[j] + nums[k] == 0`.

Notice that the solution set must not contain duplicate triplets.

Example 1:

Input: `nums = [-1,0,1,2,-1,-4]`
Output: `[[-1,-1,2],[-1,0,1]]`

Return
3 triplets

-1, 0', 0'', 1, 2, -1, -4

{ -1, 0', 1 } This
is
{ -1, 0'', 1 } duplication
and it

is not allowed.
After sorting,
triplets should be unique.

Brute force:

```
for( ) {
```

```
    for( ) {
```

```
        for( ) {
```

 } } }

$$T() = O(N^3)$$

Optimization: 3 Pointer Approach; Normal Loop + Two

$p_1 \rightsquigarrow a^1 b^2 c^3 d^4 e \dots$

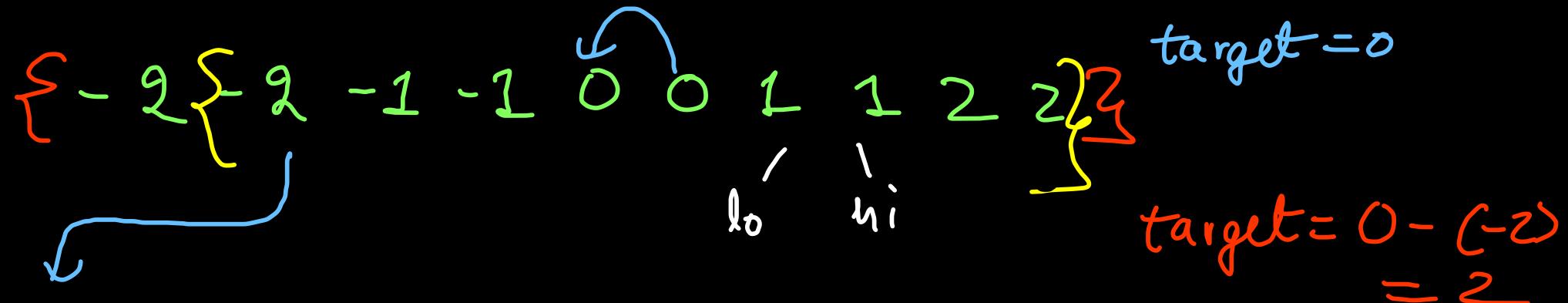
Pointer-

$$k = a + (y + z)$$

$$k = \underbrace{x}_{a} + y + z$$

$$\Rightarrow \Rightarrow \underbrace{y + z}_{\text{Target Sum pair}} - (k - a)$$

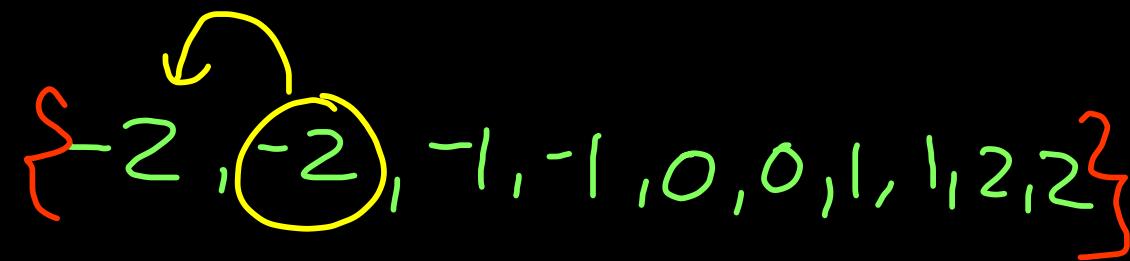
Target Sum pair (2 ptr)



In the two pointer loop condition that

$$\text{nums}[i-1] \neq \text{nums}[i]$$

should be applied to avoid
duplicacy.



$\text{nums}[i] \neq \text{nums}[i-1]$
condition should be applied here
as well.

```

public List<List<Integer>> twoSumUnique(int[] nums, int target, int lo, int hi) {
    //array will already be sorted
    List<List<Integer>> ans = new ArrayList<>();
    int start = lo;
    while(lo < hi) {
        List<Integer> smallAns = new ArrayList<>();
        if(lo > start && nums[lo - 1] == nums[lo]) {
            lo++;
            continue;
        }
        int sum = nums[lo] + nums[hi];
        if(sum == target) {
            smallAns.add(nums[lo]);
            smallAns.add(nums[hi]);
            lo++;
            hi--;
        } else if(sum < target) {
            lo++;
        } else {
            hi--;
        }
        if(smallAns.size() > 0) ans.add(smallAns);
    }
    return ans;
}

public List<List<Integer>> threeSum(int[] nums) {
    Arrays.sort(nums);
    List<List<Integer>> ans = new ArrayList<>();
    for(int i=0;i<nums.length;i++) {
        int target = 0 - nums[i];
        if(i>0 && nums[i-1] == nums[i]) continue;

        List<List<Integer>> targetSumPairs = twoSumUnique(nums,target,i+1,nums.length-1);
        for(List<Integer> tsp : targetSumPairs) {
            tsp.add(0,nums[i]);
            ans.add(tsp);
        }
    }
    return ans;
}

```

lu > start & not lo > 0

because

-1 {1 0 0 1 2}

3 Sum Code

{LC}

$$TC = O(N^2)$$

When I am starting 2 ptr loop for this

then I will skip this -1 because it is same as prev -1 however, this should have been included - So, check condn if $lo > start$ so that it does not skip 1st ele.

3 sum smaller (Lintcode)



3 pointers: Normal Loop + Two pointers

{ 2 sum smaller }

* Duplicate Triplets are allowed in this Ques.

Code for 3 Sum Smaller { Hint code }

```
public int twoSumSmaller(int[] nums, int target,int lo, int hi) {
    int ans = 0;
    while(lo < hi) {
        int sum = nums[lo]+nums[hi];
        if(sum < target) {
            ans += (hi-lo);
            System.out.println(nums[lo] + " " + nums[hi]);
            lo++;
        } else {
            hi--;
        }
    }
    return ans;
}

public int threeSumSmaller(int[] nums, int target) {
    // Write your code
    Arrays.sort(nums);

    int ans = 0;
    for(int i=0;i<nums.length;i++) {
        // if(i> 0 && nums[i-1] == nums[i]) continue;
        int numberOfPairs = twoSumSmaller(nums,target - nums[i],i+1,nums.length-1);
        ans += numberOfPairs;
    }

    return ans;
}
```

$$TC = O(N^2)$$

3 Sum Closest

3 pointer approach: Normal loop + 2 pointer closest

{closest sum
checking}

Duplicates may or may not be there. It does not matter in this question because we will not count/display triplets.

3 Sum Closest Code of Leetcode?

```
public int twoSumClosest(int[] nums,int target, int lo, int hi) {  
    int minDiff = Integer.MAX_VALUE;  
    int ans = 0;  
  
    while(lo < hi) {  
        int sum = nums[lo] + nums[hi];  
        if(sum == target) {  
            return target;  
        } else if(sum > target) {  
            int currDiff = sum - target;  
            if(currDiff < minDiff) {  
                minDiff = currDiff;  
                ans = sum;  
            }  
            hi--;  
        } else {  
            int currDiff = target - sum;  
            if(currDiff < minDiff) {  
                minDiff = currDiff;  
                ans = sum;  
            }  
            lo++;  
        }  
    }  
    return ans;  
}  
  
public int threeSumClosest(int[] nums, int target) {  
    Arrays.sort(nums);  
    int minDiff = Integer.MAX_VALUE;  
    int ans = 0;  
  
    for(int i=0;i<nums.length-2;i++) {  
        int closestPairSum = twoSumClosest(nums,target-nums[i],i+1,nums.length-1);  
        int currSum = closestPairSum + nums[i];  
        int currDiff = Math.abs(target - currSum);  
        if(currDiff < minDiff) {  
            minDiff = currDiff;  
            ans = currSum;  
        }  
    }  
    return ans;  
}
```

Count the Triplets $\{g, f, b\}$

$\{1, 2, 3, 4, 5\} \{6\}$

$$\# a + b + c = 0$$

$$\# a + b = c$$

$$\Rightarrow a + b - c = 0$$

$\{1, 2, 3, 4\} \{5, 6\}$

Important point is that we have to fix the third variable, not the first. If you fix a 2 pointer will be applied on difference i.e. $c - b$.

Code for count the triplets.

```
int twoSum(int[] arr, int target, int lo, int hi) {  
    int ans = 0;  
  
    while(lo < hi) {  
        int sum = arr[lo] + arr[hi];  
        if(sum == target) {  
            lo++;  
            hi--;  
            ans++;  
        } else if(sum < target) {  
            lo++;  
        } else {  
            hi--;  
        }  
    }  
  
    return ans;  
}
```

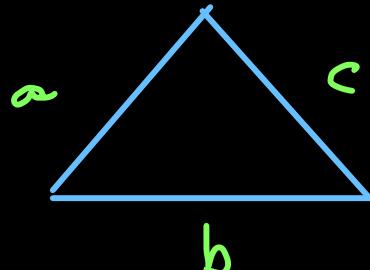
$O(N)$

```
int countTriplet(int arr[], int n) {  
    // code here  
    Arrays.sort(arr);  
    int ans = 0;  
    for(int i = n-1;i > 1;i--) {  
        int twoSumPairs = twoSum(arr,arr[i],0,i-1);  
        ans += twoSumPairs;  
    }  
  
    return ans;  
}
```

$O(N^2)$

Valid Triangle Number {LC: 611}

{ 1, 2, 3, 4, 5, 6 }



So, it is same as prev question. Instead of $a+b=c$ we have $a+b>c$.

$$\left\{ \begin{array}{l} a+b > c \\ b+c > a \\ a+c > b \end{array} \right\}$$

If the array $\{a, b, c\}$ is a sorted array, proving 1st will prove the rest 2 automatically.

$c = lo++$

$> hi--$
 $ans += hi - lo$

Valid Triangle Number ✓ SolC

```
public int twoSumGreater(int[] nums, int target,int lo, int hi) {  
    // write your code here  
    int ans = 0;  
    while(lo < hi) {  
        int sum = nums[lo] + nums[hi];  
        if(sum > target) {  
            ans += (hi-lo);  
            hi--;  
        } else {  
            lo++;  
        }  
    }  
  
    return ans;  
}  
}
```

```
public int triangleNumber(int[] nums) {  
    Arrays.sort(nums);  
    int ans = 0;  
  
    for(int i=nums.length-1;i>1;i--) {  
        ans += twoSumGreater(nums,nums[i],0,i-1);  
    }  
  
    return ans;  
}
```

Array 3 Pointers {Interview Bit}

A : [1, 4, 10]
 ^
 ; i

B : [2, 15, 20]
 ^
 j

C : [10, 12]
 ^
 k

{1, 2, 10}
 ^
 ; j
 ; k
 ; ⑨

$\max(\text{abs}(A[i] - B[j]), \text{abs}(B[j] - C[k]), \text{abs}(C[k] - A[i]))$

↓
minimize this term

*⁴ Algo: Keep incrementing the
min val ptr till anyone
array is finished.

Array & Pointers (IB) Code .

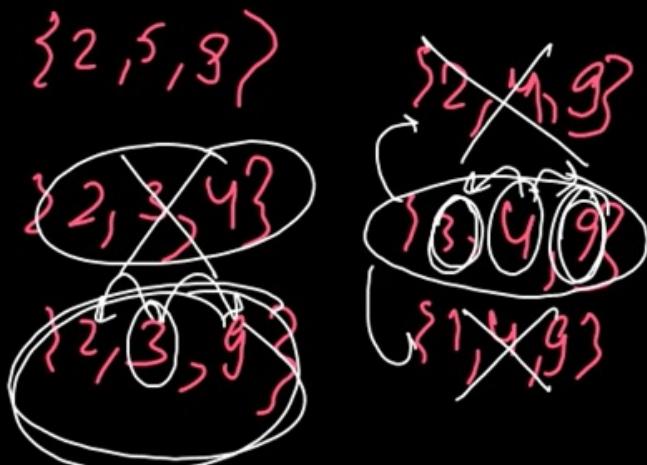
```
// DO NOT MODIFY THE ARGUMENTS WITH final PREFIX. IT IS READ ONLY
public int minimize(final int[] A, final int[] B, final int[] C) {
    int i = 0, j=0,k=0;
    int ans = Integer.MAX_VALUE;
    while(i<A.length && j<B.length && k<C.length) {
        int a = Math.abs(A[i] - B[j]), b = Math.abs(B[j] - C[k]),c = Math.abs(A[i] -C[k]);
        ans = Math.min(ans,Math.max(a,Math.max(b,c)));
        if(A[i] <= B[j] && A[i]<= C[k]) i++;
        else if(B[j] <= A[i] && B[j] <= C[k]) j++;
        else k++;
    }

    return ans;
}
```

Maximum Sum Triplet {IB}



[2, 5, 3, 1, 4, 9]



(i, j, k)

($i < j < k$)

($A[i] < A[j] < A[k]$)

$$A[i] + A[j] + A[k] = \underline{\underline{\text{max}}}$$

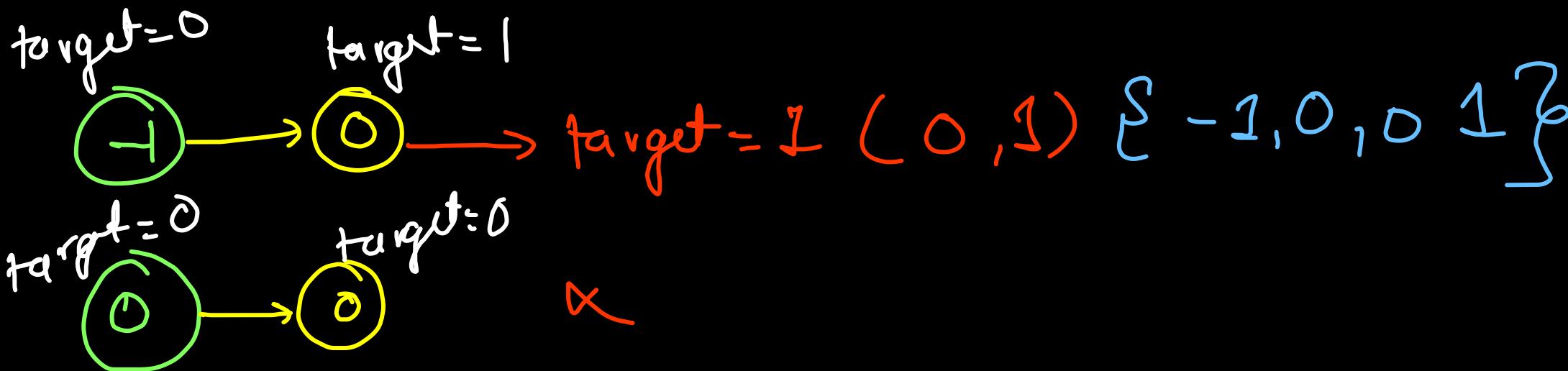
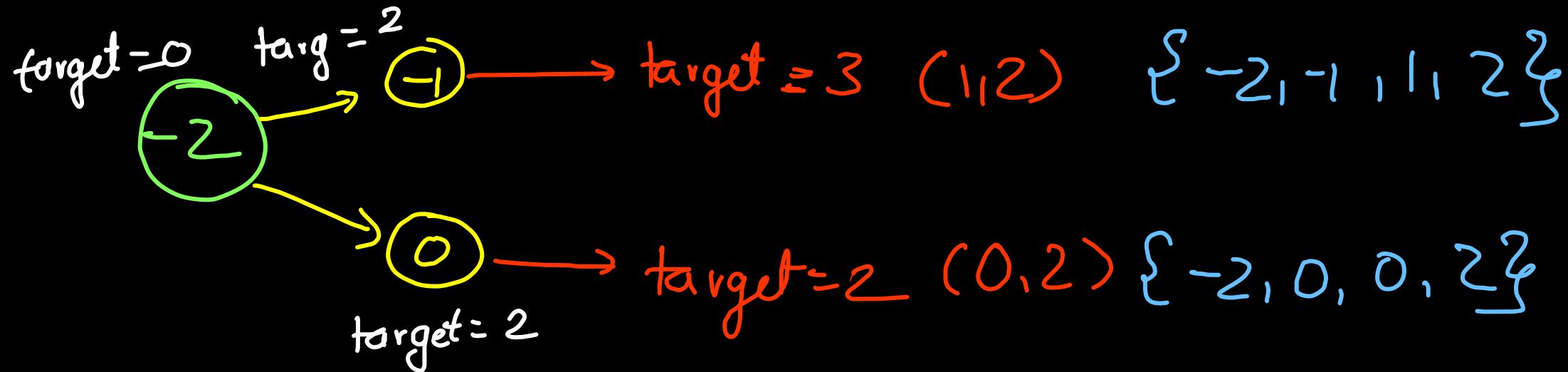
HINT →
left → Floor in left part
Fix the middle ele
right → $\underline{\underline{\text{max}}}$ in right part

4 Sum { Leetcode }

Brute force; 4 nested loops $O(n^4)$

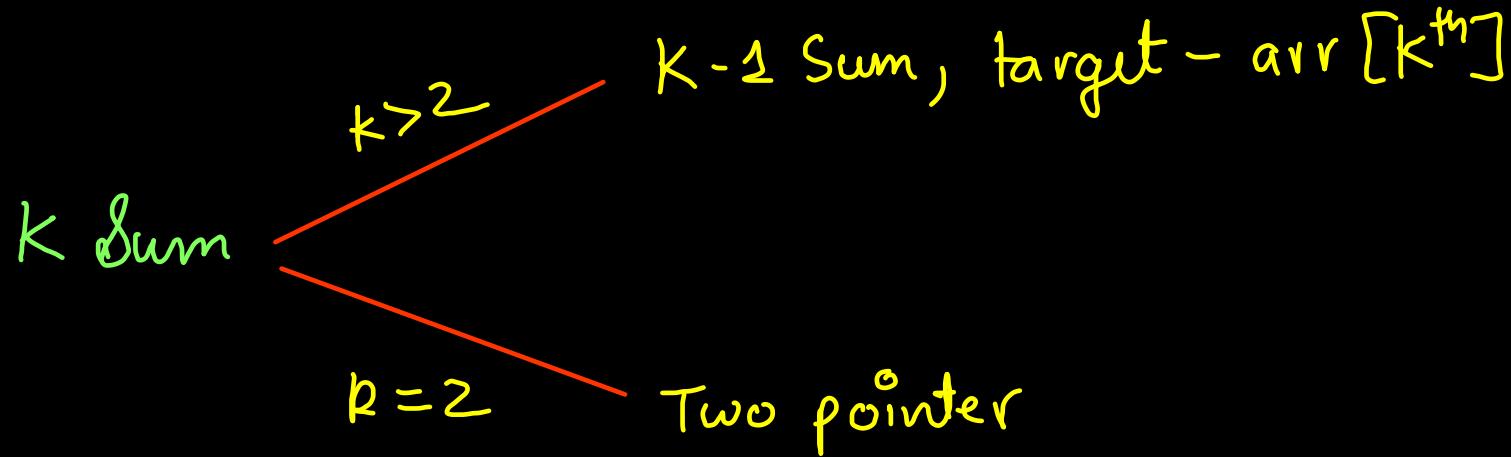
Optimised ; Nested Loop + 2 Pointer Approach

{ -2, 1, 0, 0, 1, 2 } }

$$\{-2, -1, 0, 0, 1, 2\}$$


K Sum

Recurrence Relation



$O(n^{k-1})$

$$O(k \text{Sum}) = \begin{cases} O((k-1) \text{Sum} * N) & k > 2 \\ O(n) & k = 2 \end{cases}$$

K Sum (4 Sum Leetcode)

```
public List<List<Integer>> kSum(int[] nums, int start,int target,int k) {  
    if(k == 2) {  
        return twoSumUnique(nums,target,start);  
    }  
  
    List<List<Integer>> res = new ArrayList<>();  
    for(int i=start; i<= nums.length-k;i++) {  
        if(i>start && nums[i] == nums[i-1]) continue;  
        List<List<Integer>> subRes = kSum(nums,i+1,target-nums[i],k-1);  
        for(List<Integer> sub : subRes) {  
            sub.add(0,nums[i]);  
            res.add(sub);  
        }  
    }  
  
    return res;  
}  
  
public List<List<Integer>> fourSum(int[] nums, int target) {  
    Arrays.sort(nums);  
    return kSum(nums,0,target,4);  
}
```

4 Sum II {LeetCode}

Instead of giving a single array & finding quadruplets equal to the target sum, we are given 4 arrays this time - and we have to make quadruplets from them.

→ Approach 1 : Same as array 3 pointers question

(4 pointer
Approach)

- ① Sort all arrays:
- ② Take 4 pointers i,j,k,l
- ③ keep updating the smallest ptr till 1 array is completed



This approach won't work. Many pairs will be skipped.

Approach-2

A $\{1, 2, 2\}$

} Pairs (AB)

B $\{-2, -2, -1\}$

C $\{-1, -1, 2\}$

D $\{0, 1, 2\}$

$$a + b + c + d = 0$$

HM <sum, AL <Pair>>

↳ all pairs of
that sum

-1 $(1, -2)$

0 $(1, -1)(2, -2)$

1 $(2, -1)$

-1 $(-1, 0)$

0 $(-1, -1)$

1 $(-1, 2)$

2 $(2, 0)$

3 $(2, 1)$

4 $(2, 2)$

Worst case:
 $O(n^4)$

$\{1, -2, -1, 2\}$

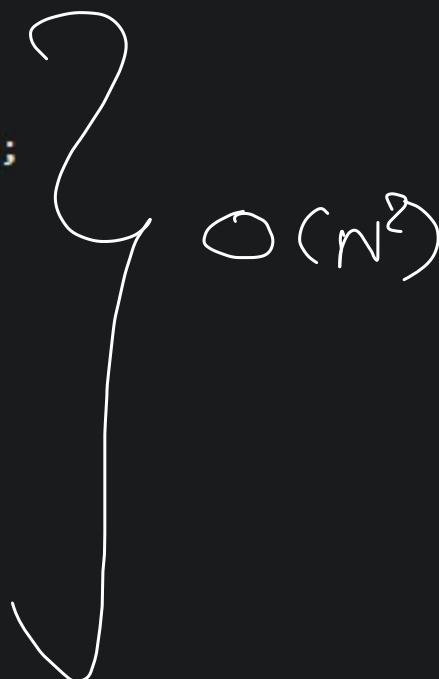
$\{2, -1, -1, 2\}$

Code for 4 Sum II {leetcode}

```
class Solution {
    public int fourSumCount(int[] nums1, int[] nums2, int[] nums3, int[] nums4) {
        HashMap<Integer, Integer> AB = new HashMap<>();
        //store the sum of pair vs count
        for(int val1: nums1)
            for(int val2: nums2)
                AB.put(val1 + val2, AB.getOrDefault(val1 + val2, 0) + 1);

        int count = 0;
        for(int val3: nums3) {
            for(int val4: nums4) {
                int target = -val3 - val4;
                count += AB.getOrDefault(target, 0);
            }
        }

        return count;
    }
}
```



$O(N^2)$

4 Sum Leetcode {HashMap Approach} {4 Sum-II Appr}

```
public List<List<Integer>> fourSum(int[] nums, int target) {
    //sum against all the pairs with that sum
    HashMap<Integer,List<List<Integer>>> AB = new HashMap<>();

    int n = nums.length;
    //we have to store the indices of the pair and not the values to check for duplicates later
    for(int i=0;i<n;i++) {
        for(int j=i+1;j<n;j++) {
            int sum = nums[i] + nums[j];
            List<Integer> pair = new ArrayList<>();
            pair.add(i);pair.add(j);
            if(AB.containsKey(sum) == false) {
                List<List<Integer>> temp = new ArrayList<>();
                AB.put(sum,temp);
            }
            AB.get(sum).add(pair);
        }
    }

    HashSet<List<Integer>> hs = new HashSet<>(); //to check for uniqueness

    for(int p=0;p<n;p++) {
        for(int q=p+1;q<n;q++) {
            int remTarget = target - nums[p] - nums[q];
            if(AB.containsKey(remTarget) == false) {
                continue;
            }
            for(List<Integer> pair : AB.get(remTarget)) {
                if(p != pair.get(0) && p!= pair.get(1) && q!=pair.get(0) && q!=pair.get(1)) {
                    List<Integer> quad = new ArrayList<>();
                    quad.add(nums[p]);
                    quad.add(nums[q]);
                    quad.add(nums[pair.get(0)]);
                    quad.add(nums[pair.get(1)]);
                    Collections.sort(quad);
                    hs.add(quad);
                }
            }
        }
    }

    List<List<Integer>> res = new ArrayList<>();
    for(List<Integer> quad: hs) {
        res.add(quad);
    }

    return res;
}
```

This code gives
TLE on Leetcode
because Wc is
 $O(n^4)$ & the
test cases are
strict.

Count Tuples Product SLC Tuples with same product

1726. Tuple with Same Product

Medium 385 17 Add to List Share

Given an array `nums` of **distinct** positive integers, return the number of tuples (a, b, c, d) such that $a * b = c * d$ where $a, b, c, \text{ and } d$ are elements of `nums`, and $a \neq b \neq c \neq d$.

No of quadruplets * 8

- $\{2, 3, 4, 6\}$
- (2,6) (3,4)
- ① (2,3) (2,6) (4,3)
- ② (2,4) (2,6) (3,4)
- ③ (2,6) { $\times 8$ } (6,2) (3,4)
- ④ (3,4) (6,2) (4,3)
- ⑤ (3,6) (3,4) (2,6)
- ⑥ (4,6) (3,4) (6,2)
- (4,3) (2,6) (4,3) (6,2)

Count Tuples Code

```
class Solution {
    public int tupleSameProduct(int[] nums) {
        HashMap<Integer, Integer> AB = new HashMap<>();

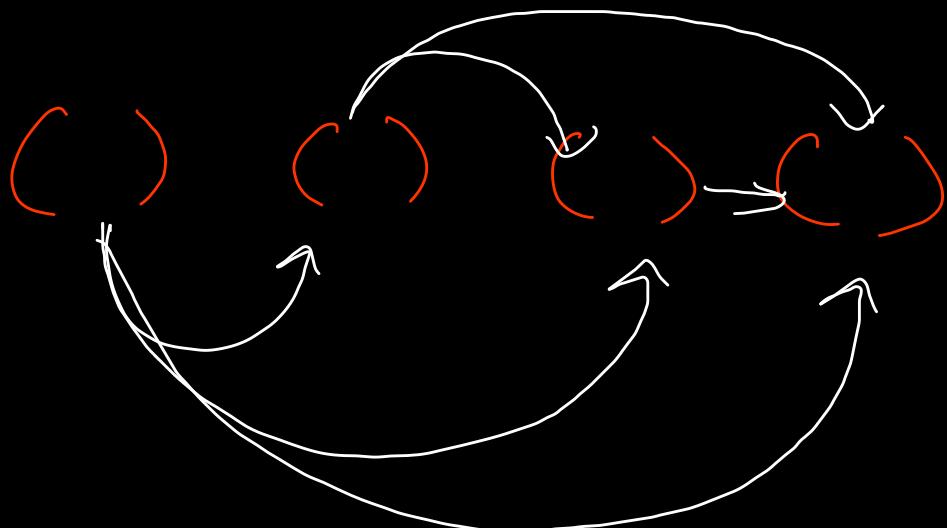
        for(int i=0;i<nums.length;i++) {
            for(int j=i+1;j<nums.length;j++) {
                AB.put(nums[i] * nums[j], AB.getOrDefault(nums[i] * nums[j],0) + 1);
            }
        }

        int count = 0;
        for(Integer key: AB.keySet()) {
            int val = AB.get(key);
            count = count + (val*(val-1))/2;
        }

        return count * 8;
    }
}
```

What is $\text{val} * (\text{val} - 1) / 2$ in Count Tuples?

Let us say we have 4 pairs with product k
Now quadruplets can be formed in the following way.



This is exactly how
a nested loop works
i.e. $\frac{n(n-1)}{2}$ So,
 $\text{val} * (\text{val} - 1) / 2$

Difference Pair

{ 1, 2, 3, 10, 11 }

↑
lo

↑
hi

target = 8

$$\text{arr}[p2] - \text{arr}[p1] = 8$$

decreasing
higher val

increasing
lower val



hence 2ptr in 2 opp dirs \Rightarrow
should not be applied in diff pair

this means the
Same -

$$\{1, 2, 3, 10, 11\} \quad a[p_2] - a[p_1] = 1 \uparrow$$

\uparrow
 b^1

$$\{1, 2, 3, 10, 11\} \quad a[p_2] - a[p_1] = 3 - 1 = 2 \uparrow$$

\uparrow
 b^1

$$\{1, 2, 3, 10, 11\} \quad a[p_2] - a[p_1] = 10 - 1 = 9 \downarrow$$

\uparrow
 p^1

$$\{1, 2, 3, 10, 11\} \quad a[p_2] - a[p_1] = \text{target}$$

$\downarrow b^1 \quad \downarrow b^2$

$\{1, 2, 3, 10, 11\}$

target = -20

2-1 = $(1) \downarrow$

2-2 = $(0) \downarrow$

2-3 = $(-1) \downarrow$

2-10 = $(-8) \downarrow$

2-11 = $(-9) \downarrow$

*+ p_1 can also reach
arr.length before p_2 .

also target = 0

$ptr1 = ptr2$
 $ptr1++$
pair found

$ptr1 = ptr2 + 2$
 $ptr2++$
or $ptr1++$

```
/*
public int[] twoSum7(int[] nums, int target) {
    // write your code here
    int left = 0;
    int right= 1;

    while(left < nums.length && right<nums.length) {
        if(left == right) {
            if(target < 0) {
                left++;
            } else {
                right++;
            }
        }

        if(nums[right] - nums[left] == target) {
            int min = Math.min(nums[left],nums[right]);
            int max = Math.max(nums[left],nums[right]);
            return new int[]{min,max};
        } else if(nums[right] - nums[left] < target) {
            right++;
        } else {
            left++;
        }
    }

    return null;
}
```

Code for Difference Pair

$$TC = O(N)$$

Count Diff Pairs {Unique} } {LC : S32}

if $\text{diff} < \text{target} \Rightarrow \text{right}++;$

$\text{diff} > \text{target} \Rightarrow \text{left}++;$

$\text{diff} = \text{target} \Rightarrow \underbrace{\text{left}}_{\text{++}}$

because we will check $a[\text{left}] = a[\underline{\text{left}+1}]$
for duplicates -

Count Diff Pairs {Unique}

```
public int diffPair(int[] nums, int target) {
    int left = 0, right = 1;
    int count = 0;
    while(left < nums.length && right < nums.length) {

        if(left > 0 && nums[left] == nums[left-1]) {
            left++; continue;
        }

        if(left == right) {
            right++; continue;
        }

        int diff = nums[right] - nums[left];
        if(diff == target) {
            left++;
            count++;
        } else if(diff < target) {
            right++;
        } else {
            left++;
        }
    }

    return count;
}

public int findPairs(int[] nums, int k) {
    Arrays.sort(nums);
    return diffPair(nums, k);
}
```

Count All Diff Pairs {LC : 2006}

2006 {All}

{1, 2, 2, 1}
0 1 2 3

1 → ②
2 → ②

target = ①
 $2 \times 2 = 4$

1	2
0	1
0	2
2	1
1	3
2	1
2	3

① Approach: Store each element and its frequency in a HashMap & multiply its freq with its comp's freq & add it to the total no of pairs.

Count All Diff Pairs {LC : 2006}

2006 {All}

{1, 2, 2, 1}
0 1 2 3

1 → ②
2 → ②

target = ①
 $2 \times 2 = 4$

1	2
0	1
0	2
2	1
1	3
2	1
2	3

① Approach: Store each element and its frequency in a HashMap & multiply its freq with its comp's freq & add it to the total no of pairs.

Count All Diff Pairs

```
public int countKDifference(int[] nums, int k) {  
    HashMap<Integer, Integer> fmap = new HashMap<>();  
  
    for(int i=0;i<nums.length;i++) {  
        fmap.put(nums[i],fmap.getOrDefault(nums[i],0) + 1);  
    }  
  
    int count = 0;  
    for(int key: fmap.keySet()) {  
        int freq = fmap.get(key);  
  
        if(k == 0) {  
            count = (k * (k - 1)) / 2;  
        } else {  
            int compFreq = fmap.getOrDefault(k + key,0);  
            count = count + freq * compFreq;  
        }  
    }  
  
    return count;  
}
```

Maximum Width Ramp

$$(2, 0) \Rightarrow 2$$

$$(5, 1) \Rightarrow 4$$

$$(9, 3) \Rightarrow 6$$

⁰ 20	¹ 14	² 38	³ 10	⁴ 9	⁵ 27	⁶ 12	⁷ 20	⁸ 18	⁹ 14
--------------------	--------------------	--------------------	--------------------	-------------------	--------------------	--------------------	--------------------	--------------------	--------------------

38 38 28 27 27 27 20 20 18 14 \Rightarrow Suffix Array
 \downarrow

while ($a[j] > a[i]$) $j++$

$$(j^0 - 1, i^0)$$

j^0 is at a pos where
 $a[j^0] < a[i^0]$

Code for Max Width Ramp.

```
class Solution {
    public int maxWidthRamp(int[] nums) {
        int [] suffix = new int[nums.length];

        int max = Integer.MIN_VALUE;

        for(int i=nums.length-1;i>=0;i--) {
            max = Math.max(nums[i],max);
            suffix[i] = max;
        }

        int i = 0;
        int j = 0;

        int maxDiff = Integer.MIN_VALUE;
        while(i < nums.length && j < nums.length) {

            while(j< nums.length && nums[i] <= suffix[j]) j++;
            int currDiff = (j-1)-i;
            maxDiff = Math.max(maxDiff,currDiff);
            i++;
        }

        return maxDiff;
    }
}
```

Static Sliding Window {Max sum subarray of size k}

fixed sized window

$$\begin{array}{cccc} 100 & 200 & 300 & 400 \\ 0 & 1 & 2 & 3 \\ & \text{---} \\ 300 & 300 - 100 + 300 & 500 - 200 \\ & = 500 & + 400 \\ & & = 700 \end{array} \quad k = 2$$

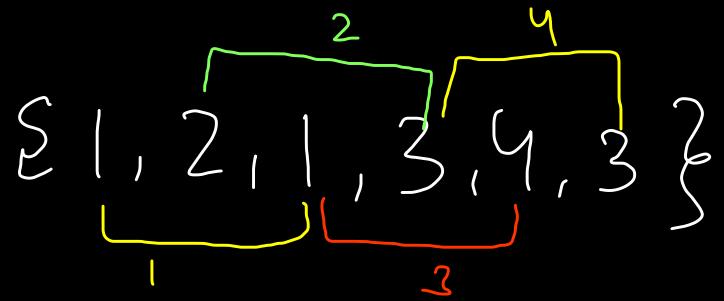
if Take a window of size 2.
when sliding it forward,
remove the last ele of
prev window & add the
new element to the sum.

Code for Maximum Sum Subarray .

```
static int maximumSumSubarray(int K, ArrayList<Integer> Arr,int N){  
    // code here  
    if(K > N) return 0;  
  
    int sum = 0;  
    for(int i=0;i<K;i++) {  
        sum += Arr.get(i);  
    }  
  
    int maxSum = sum;  
    for(int i=1;i<=N-K;i++) {  
        sum = sum - Arr.get(i-1) + Arr.get(i+K-1);  
        maxSum = Math.max(maxSum,sum);  
    }  
  
    return maxSum;  
}
```

} $\mathcal{O}(N)$ Time
} $\mathcal{O}(1)$ Space

Distinct Numbers in Window ∈ FIB



① $\{1-2\} \quad s=2$

④ $\{3-2\} \quad s=2$

② $\{2-1\} \quad s=3$

Total No of
Windows

③ $\{1-1\} \quad s=3$

$= N-k+1$

Windows

→ Take a HashMap for each window (freq Map). The size of the HashMap will be the no of unique elems in that

Code for distinct Nums in a window .

```
public class Solution {
    public int[] dNums(int[] A, int B) {
        HashMap<Integer, Integer> hm = new HashMap<>();
        int N = A.length;
        int K = B;

        for(int i=0;i<K;i++) {
            hm.put(A[i],hm.getOrDefault(A[i],0) + 1);
        }

        int[] ans = new int[N-K+1];
        ans[0] = hm.size();

        for(int i=1;i<=N-K;i++) {
            int oFreq = hm.get(A[i-1]);
            if(oFreq == 1) {
                hm.remove(A[i-1]);
            } else {
                hm.put(A[i-1],oFreq-1);
            }
            hm.put(A[i+K-1], hm.getOrDefault(A[i+K-1],0) + 1);
            ans[i] = hm.size();
        }

        return ans;
    }
}
```

Minimum Swaps & K Together

Minimum swaps and K together ↗

Medium Accuracy: 47.98% Submissions: 52092

Points: 4

Given an array **arr** of **n** positive integers and a number **k**. One can apply a swap operation on the array any number of times, i.e choose any two index **i** and **j** (**i < j**) and swap **arr[i]**, **arr[j]**. Find the **minimum** number of swaps required to bring all the numbers less than or equal to **k** together, i.e. make them a contiguous subarray.

$$k = 6$$

2 9 8 7 3 9 4 5 7 8 1

- ① Count total no of elems less than or equal to **k**. This will be our window size -
 $= 5$ in this case

- ② Slide the fixed size window and every time count the no of elems less than equal to **K** in that window. The no of swaps req these will be Size of window - that count -

Code for Min Swaps & K Together.

```
// Function for finding maximum and value pair
public static int minSwap (int arr[], int n, int k) {
    //Complete the function
    int count = 0;
    for(int i=0;i<n;i++) {
        if(arr[i] <= k) count++;
    }

    int currNoOfEle = 0;
    for(int i=0;i<count;i++) {
        if(arr[i] <= k) currNoOfEle++;
    }

    int ans = count - currNoOfEle;

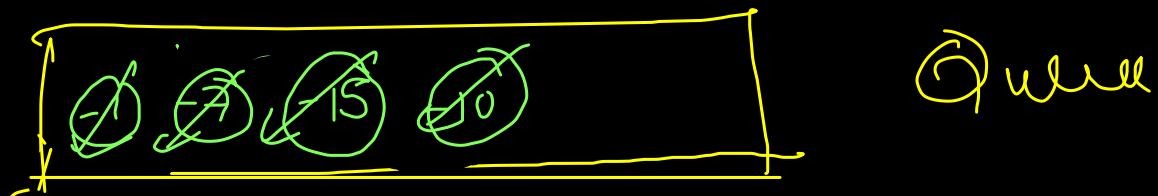
    for(int i=1;i<=n-count;i++) {
        if(arr[i-1] <= k) currNoOfEle--;
        if(arr[i + count -1] <= k) currNoOfEle++;
        int currAns = count - currNoOfEle;
        ans = Math.min(ans,currAns);
    }

    return ans;
}
```

$O(N)$

first Negative Integer in Every Window of Size k {Gf67}

$$\{ 12, -1, -7, 8, -15, -10 \} \left[\begin{matrix} 6 & 7 & 8 & 9 \\ 30, 16, 28, 40 \end{matrix} \right] \text{window} = 4$$



-1, -1, -7, -15, -15, -10, 0

Code

```
public long[] printFirstNegativeInteger(long A[], int N, int K)
{
    Queue<Integer> que = new ArrayDeque<>();
    for(int i=0;i<K;i++) {
        if(A[i] < 0) que.add(i);
    }

    long[] ans = new long[N-K+1];
    ans[0] = que.size() > 0 ? A[que.peek()] : 0;

    for(int i=1;i<=N-K;i++) {
        if(A[i-1] < 0) que.remove();
        if(A[i+K-1] < 0) que.add(i+K-1);
        if(que.size() == 0) ans[i] = 0;
        else ans[i] = A[que.peek()];
    }

    return ans;
}
```

$O(N)$

Permutation in String. SLCQ

{
Anagram
Permutations} in String

$a \rightarrow 1$ $b \rightarrow 1$ $c \rightarrow 1$ $d \rightarrow 1$

"a | b c c | a a b d | d a c b b c a d"

$a \rightarrow 1$ $b \rightarrow 1$ $c \rightarrow 1$
"abcd" or

"abcc"	"bccaa"	"ccao"	"caab"	"aabd"	"abdd"
$a \rightarrow 1$	$a \rightarrow 1$	$a \rightarrow 2$	$a \rightarrow 2$	$a \rightarrow 2$	$a \rightarrow 1$
$b \rightarrow 1$	$b \rightarrow 1$	$c \rightarrow 2$	$c \rightarrow 1$	$d \rightarrow 1$	$b \rightarrow 1$
$c \rightarrow 2$	$c \rightarrow 2$		$b \rightarrow 1$	$b \rightarrow 1$	$d \rightarrow 2$

"bdda"
 $b \rightarrow 1$ $d \rightarrow 2$ $a \rightarrow 1$

"dabc"
 $a \rightarrow 1$ $c \rightarrow 1$
 $c \rightarrow 1$ $d \rightarrow 1$

{
bacd
bcda
cabd
...
}

Code for Permutation in a String {LC 567}

```
public boolean areEqual(int[] a, int [] b) {
    for(int i=0;i<26;i++) {
        if(a[i] != b[i]) return false;
    }
    return true;
}

public boolean checkInclusion(String s1, String s2) {
    int[] reqFreq = new int[26];
    int windowSize = s1.length();

    for(int i=0;i<s1.length();i++)
        reqFreq[s1.charAt(i) - 'a']++;

    int []currFreq = new int[26];
    for(int i=0;i<s2.length();i++) {
        currFreq[s2.charAt(i)- 'a']++;

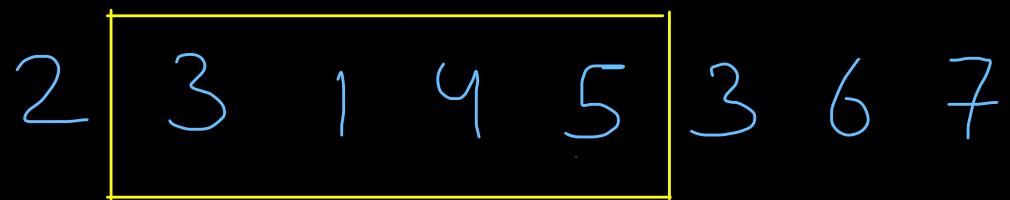
        if(i >= windowSize) {
            currFreq[s2.charAt(i - windowSize) - 'a']--;
        }

        if(areEqual(reqFreq,currFreq) == true) {
            return true;
        }
    }

    return false;
}
```

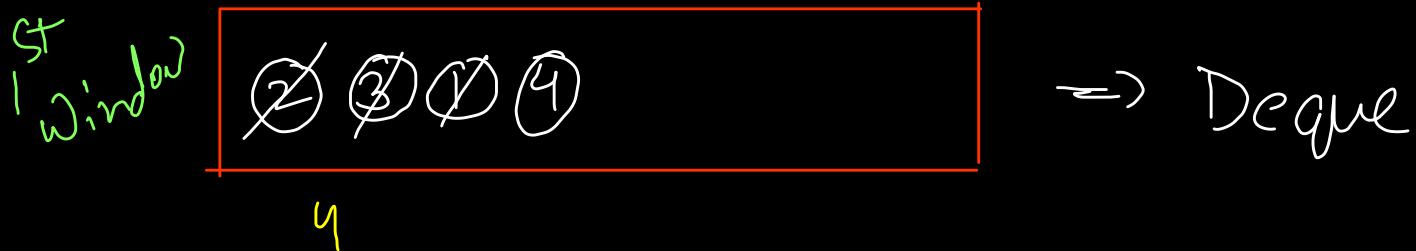
$O(26 * N)$

Sliding Window Maximum



window = 4

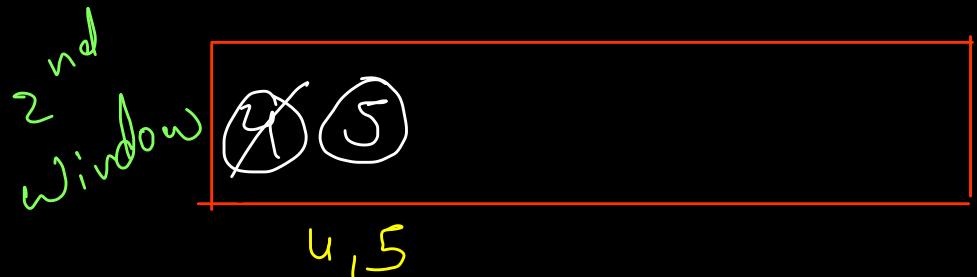
4 5 5 6 7



+ peekhe se

blop korvana

hai unsabko



jo humse chote
hai jab hum insert
no rahi hai.

2 3 1 4 5 3 6 7

3rd
window
~~4~~ 5 3
4, 5, 5

5th
window
~~4~~ 5 ~~3~~ ~~6~~ 7
4, 5, 5, 6, 7

4th
window
~~4~~ ~~5~~ ~~3~~ 6
4, 5, 5, 6

remove first → out of window
remove last → val < add val
add last → always
dequeue ↗ chronological order
 ↘ decreasing order

Code for Sliding Window Maximum

```
ass Solution {
    public int[] maxSlidingWindow(int[] nums, int k) {
        int[] res = new int[nums.length - k + 1];
        Deque<Integer> q = new ArrayDeque<>();

        int window = 0;
        for(int i=0;i<nums.length;i++) {
            if(q.size() > 0 && q.getFirst() <= i-k) {
                q.removeFirst();
            }
            while(q.size() > 0 && nums[q.getLast()] < nums[i]) {
                q.removeLast();
            }

            q.addLast(i);
            if(i >= k - 1) {
                res[window++] = nums[q.getFirst()];
            }
        }

        return res;
    }
}
```

$O(N)$

Dynamic Window {Max Consecutive Ones : LC 485}

485. Max Consecutive Ones

Easy 2383 394 Add to List Share

Given a binary array `nums`, return the maximum number of consecutive 1's in the array.

{ 1, 1, 0, 1, 1, 1 }
↓

$c = \emptyset \times \emptyset \times \emptyset$

$mc = \emptyset \times \emptyset \times \emptyset$

```
public int findMaxConsecutiveOnes(int[] nums) {
    int count = 0;
    int maxCount = 0;

    int i = 0;
    while(i < nums.length) {
        count = 0;
        while(i < nums.length && nums[i] == 1) {
            count++; i++;
        }
        maxCount = Math.max(count, maxCount);
        i++;
    }

    return maxCount;
}
```

Maximum Consecutive Ones - II {LC: 1004}

$\text{arr} = [0, 0, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1]$

r
 \downarrow
 l

$k = 3$

ans $\in \{X, X, X, X, X, X\}$

left \rightarrow exclude

right \rightarrow include

$$\maxLen = (r - l + 1)$$

10

11

Code for Max Consecutive Ones - III

```
public int longestOnes(int[] nums, int k) {
    int maxLen = 0, countOfZeroes = 0, left = 0;

    for(int right=0;right<nums.length;right++) {
        if(nums[right] == 0) {
            countOfZeroes++;
        }

        //make subarray valid by excluding left elements
        while(countOfZeroes > k) {
            if(nums[left] == 0) countOfZeroes--;
            left++;
        }

        maxLen = Math.max(maxLen,right - left + 1);
    }

    return maxLen;
}
```

Minimum Window Substring {LC Hand}

pattern
 ab b c d c

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
d	b	a	e	c	b	b	a	b	d	c	g	a	f	b	d	d	c	a	b	g	b	a

l r

"dbaecbb₁₁a₁₁bdc" \Rightarrow bbabdc a-1

"bbab**d**caaf**b**ddc" b-2

d-1 < 1 < 3 < 2

b-1 < 3 < 4 minLen = 6 11
 a-1 < 1 < 3 < 2 < 1 < 3 10
 c-1 < 2 < 3 < 2 < 4 9
 e-1 < 3 < 4 < 3 < 4 8
 g-1 < 2 < 1

d-1 g-1

Count = # of matching char

2 3 4
 3 4 3
 3 4 3 4

```
public String minimumWindowString(String s, String t) {
    if (t.equals("") == true || s.equals("") == true
        || s.length() < t.length())
        return "";
    HashMap<Character, Integer> req = new HashMap<>();
    for (int i = 0; i < t.length(); i++) {
        char ch = t.charAt(i);
        req.put(ch, req.getOrDefault(ch, 0) + 1);
    }
    HashMap<Character, Integer> curr = new HashMap<>();
    int matchCount = 0, l = 0;
    int idx = 0, len = Integer.MAX_VALUE;
```

(1)

```
for (int r = 0; r < s.length(); r++) {
    char ch = s.charAt(r);
    int freq = curr.getOrDefault(ch, 0) + 1;
    curr.put(ch, freq);

    if (freq == req.getOrDefault(ch, 0)) {
        matchCount++;
    }

    while (matchCount >= req.size()) {
        if (matchCount >= req.size() && r - l < len) {
            idx = l;
            len = r - l + 1;
        }

        char chl = s.charAt(l);
        int freql = curr.get(chl) - 1;
        curr.put(chl, freql);

        if (freql + 1 == req.getOrDefault(chl, 0)) {
            matchCount--;
        }
        l++;
    }
}

if (len == Integer.MAX_VALUE)
    return "";
return s.substring(idx, idx + len);
```

(2)

Largest Substring Without Repeating Characters {LC: 3}

"(Q3) Leetcode)
"Longest Substring without repeating characters"
longer → Valid → Include
invalid → Exclude

A handwritten note "right" is at the top left. Below it, a piano keyboard diagram shows the white keys from A to G. Above each key, there is a small red mark: a vertical line for A, a diagonal line for B, an X for C, another diagonal line for D, another vertical line for E, an X for F, and a horizontal line for G. Below the keyboard, the word "right" is written again, followed by a series of red marks: a vertical line, an X, an X, an X, an X, an X, and an upward-pointing arrow.

man = ♂ / ♀ ↗ ↘ ↙ ↖

Hashmap

a → X Ø X Ø
b → X Ø X Ø
c → X Ø X Ø
d → 1
e → 1

Code for Longest Substring Without Repeating Chars.

```
public int lengthOfLongestSubstring(String s) {  
    int left = 0, maxLen = 0;  
    HashMap<Character, Integer> freq = new HashMap<>();  
    for(int right=0;right < s.length(); right++) {  
        char ch = s.charAt(right);  
        freq.put(ch, freq.getOrDefault(ch, 0) + 1);  
  
        while(freq.get(ch) > 1) {  
            char chl = s.charAt(left);  
            freq.put(chl, freq.get(chl)-1);  
            left++;  
        }  
  
        maxLen = Math.max(maxLen, right-left + 1);  
    }  
  
    return maxLen;  
}
```

Count Substring Without Repeating Character

a b b a c b c d l a d b d b b d c b
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17
l

count = (r - l + 1) maxlen = 0 \leq 4

a - t \neq s \neq x o

d - k x s \neq x p l

b - x z a r y z x \neq x z x z s x z

c - x z z o l

Code for Count Substring w/o Repeating character

```
public static int solution(String s) {  
    // write your code here  
    int left = 0, count = 0;  
    HashMap<Character, Integer> freq = new HashMap<>();  
    for(int right=0;right < s.length(); right++) {  
        char ch = s.charAt(right);  
        freq.put(ch,freq.getOrDefault(ch,0) + 1);  
  
        while(freq.get(ch) > 1) {  
            char chl = s.charAt(left);  
            freq.put(chl,freq.get(chl)-1);  
            left++;  
        }  
        count += (right - left + 1);  
    }  
    return count;  
}
```

Longest } SubString with atmost K Unique Characters
count }

d d a c b b a c c d e d a c e b b $k=3$
d 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18
(atmost
3 unique
chars allowed)

a → 1 2 1 0 1 0

maxlen = 6

b → 1 2 1 0 1 1

count = 1 2 1 0 1 3

c → 1 2 3 2 1 0 1

1 2 2 2

d → 1 2 1 0 1 2 1 0

2 8 3 5 3 9 4 3
4 8 5 2 5 8 6 1 6 5

e → 1 6 1

* Previous que are same
with $k=1$

```

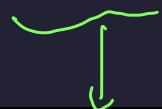
public static int solution(String str, int k) {
    // write your code here
    HashMap<Character, Integer> fmap = new HashMap<>();
    int maxLen = 0, left = 0;

    for(int right=0; right < str.length(); right++) {
        char ch = str.charAt(right);
        fmap.put(ch, fmap.getOrDefault(ch, 0) + 1);

        while(fmap.size() > k) {
            char chl = str.charAt(left);
            int oFreq = fmap.get(chl);
            if(oFreq == 1) fmap.remove(chl);
            else fmap.put(chl, oFreq - 1);
            left++;
        }

        maxLen = Math.max(maxLen, right - left + 1);
    }
    return maxLen;
}

```



maxLength

Max Len
is updated when we
have $\leq K$ unique
characters

```

public static int solution(String str, int k) {
    // write your code here
    HashMap<Character, Integer> fmap = new HashMap<>();
    int count = 0, left = 0;

    for(int right=0; right < str.length(); right++) {
        char ch = str.charAt(right);
        fmap.put(ch, fmap.getOrDefault(ch, 0) + 1);

        while(fmap.size() > k) {
            char chl = str.charAt(left);
            int oFreq = fmap.get(chl);
            if(oFreq == 1) fmap.remove(chl);
            else fmap.put(chl, oFreq - 1);
            left++;
        }

        count += (right - left + 1);
    }
    return count;
}

```

Count

longest
count

Exactly K unique characters

We have to update maxlen when we have exactly K unique characters.

```
public int longestkSubstr(String str, int k) {
    // code here
    HashMap<Character, Integer> fmap = new HashMap<>();
    int maxlen = 0, left = 0;

    for(int right=0; right < str.length(); right++) {
        char ch = str.charAt(right);
        fmap.put(ch, fmap.getOrDefault(ch, 0) + 1);

        while(fmap.size() > k) {
            char chl = str.charAt(left);
            int oFreq = fmap.get(chl);
            if(oFreq == 1) fmap.remove(chl);
            else fmap.put(chl, oFreq - 1);
            left++;
        }

        if(fmap.size() == k) maxlen = Math.max(maxlen, right - left + 1);
    }
    if(maxlen == 0) return -1;
    return maxlen;
}
```

⇒ Longest K Unique
Chars Substring
(GfG)

Count Exact K Unique SubArra^y with K diff Integers {LC: 992}

d d a c b b a c c d e d a c e b b
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

\Rightarrow count += (right - left + 1) will not work as it gives answer for atmost K

\Rightarrow count++; will not work as we can have more than 1 substring

\Rightarrow So, we will use the formula

Exactly K = Almost(K) - Almost(K-1)

Code for Subarrays with K Diff Integers.

```
class Solution {
    public int subarraysWithAtmostKDistinct(int[] nums, int k) {
        HashMap<Integer, Integer> fmap = new HashMap<>();
        int count = 0, left = 0;

        for(int right=0;right < nums.length;right++) {
            int ch = nums[right];
            fmap.put(ch,fmap.getOrDefault(ch,0) + 1);

            while(fmap.size() > k) {
                int chl = nums[left];
                int oFreq = fmap.get(chl);
                if(oFreq == 1) fmap.remove(chl);
                else fmap.put(chl,oFreq - 1);
                left++;
            }

            count += (right - left + 1);
        }
        return count;
    }
    public int subarraysWithKDistinct(int[] nums, int k) {
        return subarraysWithAtmostKDistinct(nums,k) - subarraysWithAtmostKDistinct(nums,k-1);
    }
}
```

Count K Odds { LC Count No of Nice Subarrays }
{ Return the count of those subarrays that have exactly K odd elems }

$$\text{Count of exactly } K \text{ odds} = \text{Count of} \begin{matrix} \\ \text{Atmost } K \\ \text{odds} \end{matrix} - \text{Count of} \begin{matrix} \\ \text{Atmost } K-1 \\ \text{odds} \end{matrix}$$

Do not Insert Even nos.

Count No of Nice Subarrays {LC 1248}

```
public int numberOfSubarraysWithAtmost(int[] nums, int k) {
    int left = 0, ans = 0, odd = 0;

    for(int right = 0; right<nums.length;right++) {
        if(nums[right] % 2 == 1) odd++;

        while(odd > k) {
            if(nums[left] % 2 == 1) {
                odd--;
            }

            left++;
        }

        ans += (right - left + 1);
    }

    return ans;
}

public int numberOfSubarrays(int[] nums, int k) {
    return numberOfSubarraysWithAtmost(nums,k) - numberOfSubarraysWithAtmost(nums,k-1);
}
```

Longest Repeating Character Replacement {LC424}

d d a c b b a c c d e d a c e b b
l r

Dry run for

char 'A'

K = 3

O(26N) # Apply 2 pointers 26

times.

maxLen = Ø \nearrow 2 \nearrow 4 \nearrow 5 \Rightarrow maxLen = 5 for 'A'

no of Chs changed = Ø \nearrow 2 \nearrow 3 \nearrow 4 \nearrow 5 \nearrow 3 \nearrow 2 \nearrow 1

Z Y Z M B X Y Z Y K B Y Z Y 3

Code for Longest Repeating Character Replacement.

```
public int helper(String nums, int k, char ch) {  
    int maxLen = 0, replacement = 0, left = 0;  
  
    for(int right = 0;right < nums.length();right++) {  
        if(nums.charAt(right) != ch) replacement++;  
  
        while(replacement > k) {  
            if(nums.charAt(left) != ch) replacement--;  
            left++;  
        }  
  
        maxLen = Math.max(maxLen, (right - left + 1));  
    }  
  
    return maxLen;  
}  
  
public int characterReplacement(String s, int k) {  
    int ans = 0;  
    for(int i=0;i<26;i++) {  
        ans = Math.max(ans, helper(s,k,(char)(i+'A')));  
    }  
    return ans;  
}
```

Minimum Size Subarray Sum { LC : 209 }

Smallest subarray with sum \geq target
or
 \downarrow

2 3 1 2 4 3
 \uparrow
 l

Sum = ~~2 3 6 8 6~~ ~~10~~ ~~7~~
6 9

minLen = ~~4~~ ~~3~~ 2

right ++ \Rightarrow Invalid
subarray
(sum < target)
left ++ \rightarrow smallest valid subarray.

Code for Minimum Size Subarray Sum

```
public int minSubArrayLen(int k, int[] nums) {
    int left = 0, minLen = Integer.MAX_VALUE, sum = 0;

    for(int right=0;right<nums.length;right++) {
        sum += nums[right];

        while(sum >= k) {
            minLen = Math.min(minLen,right -left + 1);
            sum = sum- nums[left];
            left++;
        }
    }

    if(minLen == Integer.MAX_VALUE) return 0;
    return minLen;
}
```

Maximum Sum SubArray $\leq K$ } GfG Max sum of
Subarray less than or equal to K

Variation of Kadane's Algo?

target = 7
or

2 8 6 4 10 2 6 ↓ valid

↑
l 6 2 6 right ++

sum < target

Sum = 2 10 8 6 10 4

invalid

maxSum = 2 6

left ++ sum > target

Code

```
long findMaxSubarraySum(long arr[], int N,int X)
{
    // Your code goes here
    int left = 0;
    long maxSum = 0, sum = 0;

    for(int right = 0;right<N;right++) {
        sum += arr[right];

        while(sum > X) {
            sum -= arr[left];
            left++;
        }

        maxSum = Math.max(maxSum,sum);
    }

    return maxSum;
}
```

Subarray Product less than K {Leetcode}

{10, 5, 2, 6, 3, 1} \downarrow or
l \uparrow \downarrow Product = 100

count = 0 ~~125815~~

product = 10 ~~50~~ 100 ~~100~~

~~180~~ 36

right++ \rightarrow Product $< k$

left++ \rightarrow Product $\geq k$

Code

```
>>> SOLUTION 3
public int numSubarrayProductLessThanK(int[] nums, int k) {
    int left = 0;
    int count = 0;
    int product = 1;

    for(int right=0;right<nums.length;right++) {
        product = product * nums[right];

        while(left < nums.length && product >= k) {
            product = product/nums[left];
            left++;
        }

        count += (right - left + 1);
    }

    if(count < 0) return 0;
    return count;
}
```

Number of Subarrays with Bounded Maximum

$\downarrow r^{\text{right}}$

3	9	4	12	2	1	6	9
0	1	2	3	4	5	6	7

\uparrow
 left

invalid \rightarrow Inclusion

valid \rightarrow Exclusion

count of subarrays with max in range [3, 8]

subarrays =

count of subarrays with max > 2 - with max greater than 8