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Assignment 1

AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

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Question 13.2.12:

1) Problem Statement

A die is tossed thrice. Find the probability of getting an odd number at least once.

Solution

Given:

We are given that the die is tossed thrice.

Need to find:

Probability of getting an odd number at least once in the three trials.

Solving steps:

Let X be a random variable defined as the number of odd number occurrences in three trials. Possible values of random variable X are;

$$X = \{0, 1, 2, 3\} \tag{1}$$

Required values of X are;

$$X = \{1, 2, 3\} \tag{2}$$

which correspond to at least one odd number. Probability of an observation being odd is;

$$p = \frac{3}{6} = \frac{1}{2} \tag{3}$$

We know that;

$$\Pr(X = i) = {}^{n} C_{i} \times p^{i} \times (1 - p)^{(n-i)}$$
 (4)

where
$$n = 3$$
 and $i \in \{0, 1, 2, 3\}$ (5)

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On solving;

$$\Pr(X = 1) = {}^{3}C_{1} \times \left(\frac{1}{2}\right)^{1} \times \left(\frac{1}{2}\right)^{(3-1)}$$
 (6)

$$\Pr(X = 1) = \frac{3}{8} \tag{7}$$

$$\Pr(X = 2) = {}^{3}C_{2} \times \left(\frac{1}{2}\right)^{2} \times \left(\frac{1}{2}\right)^{(3-2)}$$
 (8)

$$\Pr(X=2) = \frac{3}{8} \tag{9}$$

$$\Pr(X = 3) = {}^{3}C_{3} \times \left(\frac{1}{2}\right)^{3} \times \left(\frac{1}{2}\right)^{(3-3)}$$
 (10)

$$\Pr(X=3) = \frac{1}{8} \tag{11}$$

Required probability of at least one odd observation is equivalent to sum of Pr(X = 1), Pr(X = 2) and Pr(X = 3). Therefore, probability of at least one odd (1) observation is;

$$\therefore \Pr(At \ least \ one \ odd) = \frac{7}{8} = 0.875 \tag{12}$$

Conclusion

The probability of getting an odd number at least once is 0.875 as also calculated using the python code. [1]

REFERENCES

 $[1] \ https://github.com/Gunethra/AI1110_2023/tree/master/code.$