# Assignment 2

**AI1110**: Probability and Random Variables
Indian Institute of Techonology, Hyderabad

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**10.15.1.12** A game of chance consists of spinning an arrow which comes to rest pointing at one of the numbers 1, 2, 3, 4, 5, 6, 7, 8 (see Fig. 4), and these are equally likely outcomes. What is the probability that it will point at:

(i) 8?
(ii) an odd number?
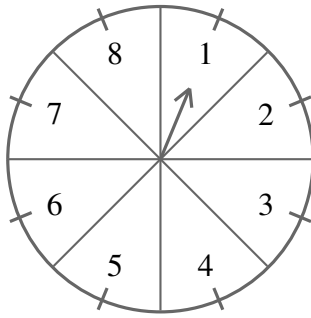(iii) a number greater than 2?
(iv) a number less than 9?

Fig. 4. Spinner



Fig. 4. Plot of Probability Mass Function

**Solution:** Let X be a random variable defined as the value given by the pointer. The distribution is unform since all the outcomes are equally likely.

$$\therefore \Pr(X = i) = \frac{1}{8} \tag{1}$$

Let $F_X(i)$ be the Cumulative distribution function(CDF) such that;

$$F_X(i) = P(X \leq i) \tag{2}$$

$$= \begin{cases} 0, & i \leq 0 \\ \frac{i}{8} & 1 \leq i \leq 8 \\ 1, & i \geq 9 \end{cases} \tag{3}$$
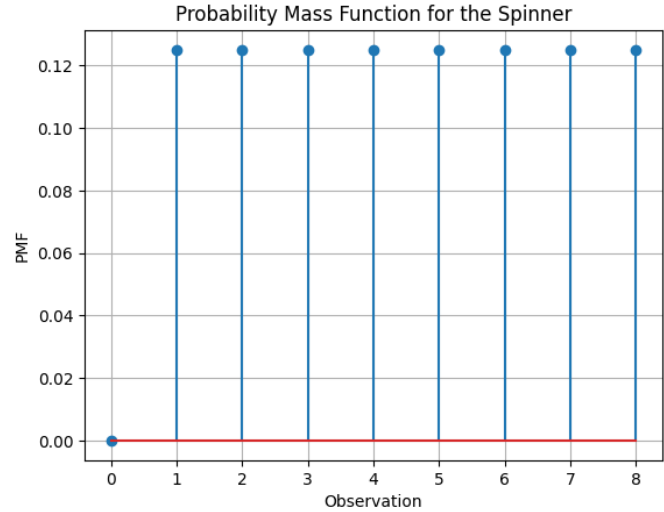
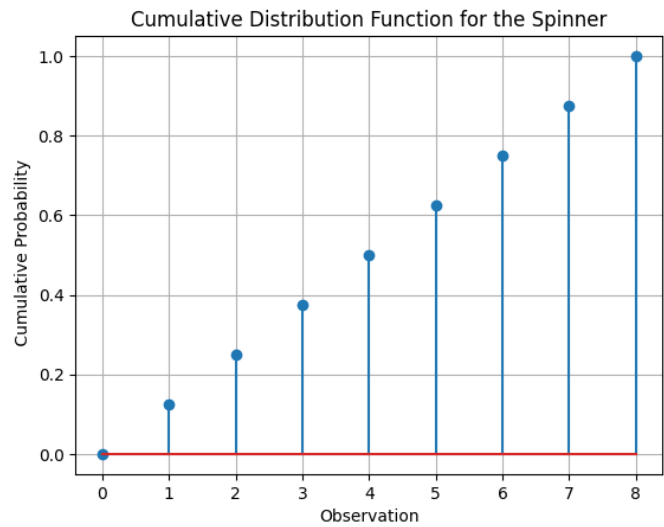See python code for PMF and CDF plots: [1]



Fig. 4. Plot of Cumulative Distribution Function

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(i) For i = 8, required probability is equivalent to;

$$\Pr(X = 8) = \frac{1}{8} \tag{4}$$
$$= 0.125 \tag{5}$$

(ii) For i being odd, required probability is equivalent to;

$$\Pr(X = \{1, 3, 5, 7\}) = \frac{4}{8} \tag{6}$$
$$= 0.5 \tag{7}$$

(iii) For i greater than 2, required probability is equivalent to;

$$\Pr(X > 2) = 1 - \Pr(X \leq 2) \tag{8}$$
$$= 1 - (F_X(2) - F_X(0)) \tag{9}$$
$$= \frac{6}{8} = 0.75 \tag{10}$$

(iv) For i less than 9, required probability is equivalent to;

$$\Pr(1 \leq X < 9) = F_X(8) - F_X(0) \tag{11}$$
$$= \frac{8}{8} = 1 \tag{12}$$

See simulation using python: [2]

### REFERENCES

[1] https://github.com/Gunethra/AI1110_2023/blob/master/
Assignment_2/code/pmf.py
https://github.com/Gunethra/AI1110_2023/tree/master/
Assignment_2/code/cdf.py.
[2] https://github.com/Gunethra/AI1110_2023/blob/master/
Assignment_2/code/code.py.