

- \* Principle: When the set  $S$  consists of numbers and is finite, the value of a number belonging to  $S$  cannot be decreased infinitely often, always to a distinct number belonging to  $S$ .

Examples presented in class on using the principle of infinite descent<sup>1</sup>:

- $\sqrt{2}$  is irrational.
- For a positive integer  $k$ ,  $\sqrt{k}$  is irrational if it is not an integer.
- No integral solutions to  $a^2 + b^2 = 3(s^2 + t^2)$ , other than the trivial solution  $a = b = s = t = 0$ .
- *Sylvester-Gallai theorem*: If there are  $n$  ( $n \geq 3$ ) points on the plane such that not all on a line, then there exists a line passing through exactly two of these points.

---

<sup>1</sup>Prepared by R. Inkulu, Dept of CSE, <http://www.iitg.ac.in/rinkulu/>