

```

add (Val) {  $\Theta(1)$ 
  → if (isFull()) {
    → return ERROR
  }
  A[tail] = Val
  ← tail ++
}

```

3	40
2	72
1	50
0	20

head = 1 tail = ~~0~~ ~~1~~ ~~2~~ ~~3~~ 4

```

delete() {  $\Theta(1)$ 
  → if (isEmpty()) {
    → return ERROR
  }
  answer = A[head]
  head ++
}

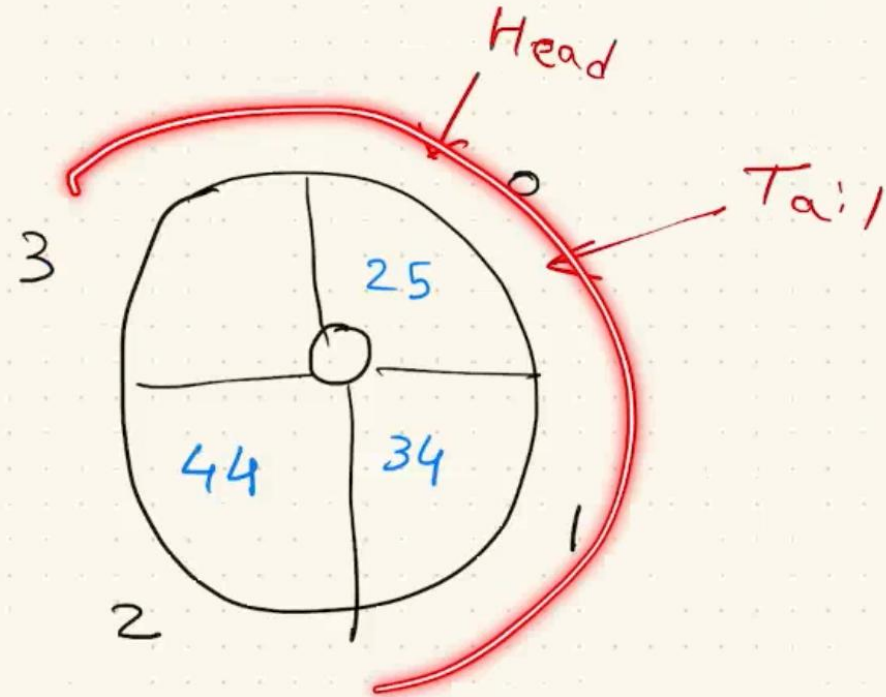
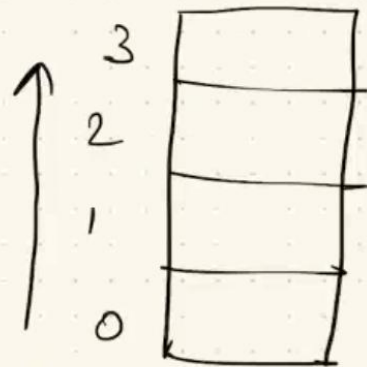
```

```

createNew (4)
add (20)
add (50)
add (72)
add (40)
delete() → 20
add (49)

```

Circular Queue



Data: Array A, integer head, integer tail

```
createNew(capacity) {
  → A.createNew(capacity + 1)
  head = 0
  tail = 0
}
```

$\Theta(1)$

```
isEmpty() {
  → if (head == tail) {
    → return TRUE
  }
  return FALSE
}
```

$\Theta(1)$

```
add(val) {
   $\Theta(1)$  → if (val == capacity) {
    → return 0
  }
  → return (val + 1)
}

isFull() {
  → if (head == add(tail)) {
     $\Theta(1)$  → return TRUE
  }
  return FALSE
}
```



x

01 Introduction

x

05 ADT

□



```
add ( val ) {  
    ↘  
    if ( isFull ( ) ) {  
        ↘  
        return ERROR  
    }  
    A [ tail ] = val  
    tail = cAdd1 ( tail )  
    ↙  
}
```

$\Theta(1)$

```
delete ( ) {  
    ↘  
    if ( isEmpty ( ) ) {  
        ↘  
        return ERROR  
    }  
    answer = A [ head ]  
    head = cAdd1 ( head )  
    return answer  
    ↙  
}
```

$\Theta(1)$

Implement ADT 1 using ADT 2

P

R

Stack

Queue

Queue

Stack

↳ implemented using Queue

P

R

operation P_1 →

operations over R

⋮

⋮

operation P_n →

Operations over R

Queue using Stack

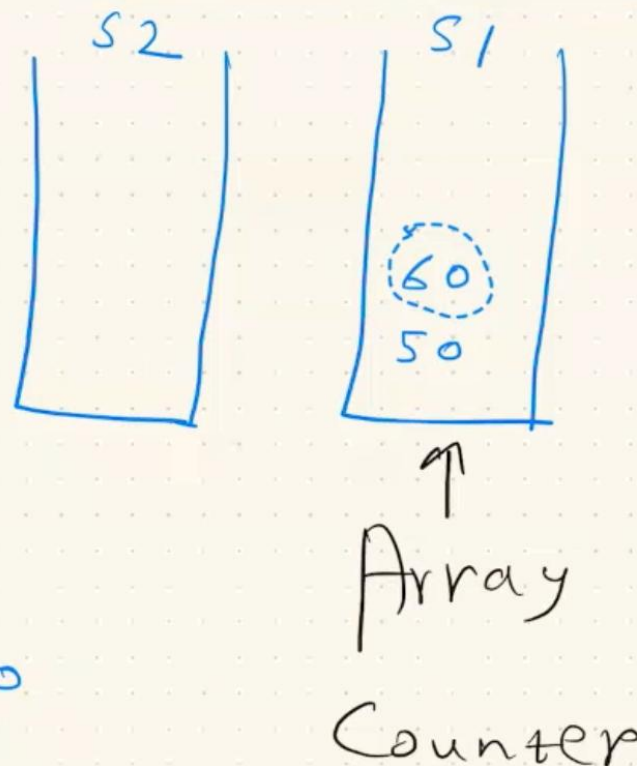
createNewQueue →

is Empty

is Full

add → Push on to S1

delete → empty S1 and push it on S2
answer = pop from S2
empty S2 and push it on S1



Queue using Stack

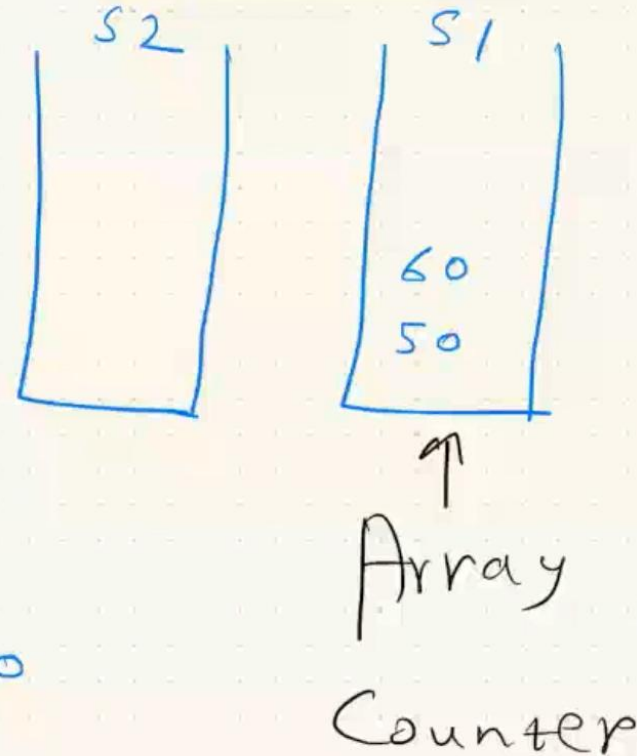
createNewQueue \rightarrow create S_1 and S_2

isEmpty \rightarrow $S_1.isEmpty()$

isFull \rightarrow $S_1.isFull()$ 20

add \rightarrow push on to S_1

delete \rightarrow empty S_1 and push it on S_2
answer = pop from S_2
empty S_2 and push it on S_1



```
createNew (capacity) {  
    S1.createNew (capacity)  
    S2.createNew (capacity)  
}
```

 $\Theta(1)$

```
isEmpty () {  
    ↘ return (S1.isEmpty ())  
    ↙  
}
```

 $\Theta(1)$

```
isFull () {  
    ↘ return (S1.isFull ())  
    ↙  
}
```

 $\Theta(1)$

```
add (val) {  
    ↗ result = S1.push (val)  
    ↘ return (result)  
}
```

True / False

Success / Failure


```
delete () {
```

```
    S1.emptyStack (S2)  $\Theta(n)$ 
```

```
    answer = S2.pop()
```

```
    S2.emptyStack (S1)
```

```
    ← return (answer)
```

```
Stack :: emptyStack (Stack Target) {
```

```
    ↓ while (!(isEmpty())) {
```

```
        ↓ Target.push (pop())
```

```
    } ←
```

$\Theta(n)$

Stack using Queue

Data: Queue Q1, Queue Q2

createNew \rightarrow Q1.createNew, Q2.createNew

isEmpty \rightarrow Q1.isEmpty

isFull \rightarrow Q1.isFull

push \rightarrow Q1.add

pop \rightarrow Q1.transferAllButLast(Q2)

answer = Q1.delete

Q2.transferAll(Q1)

