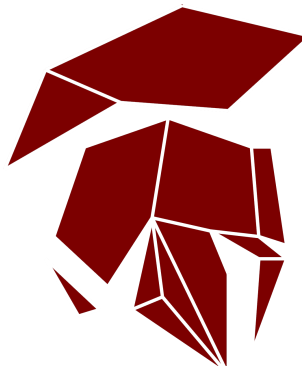


Individual Tiebreakers (Division A)

Gunn Math Competition 2025



Instructions and Basic Format

- This round contains 3 short-answer questions to be solved in 15 minutes, by you. Each problem is worth more points than all previous points, but by no significant amount, so be mindful of where you spend your time. All answers must be expressed in simplest form unless specified otherwise. Only answers written inside the boxes on the answer sheet will be considered for grading.
- **NO CALCULATORS (or abaci).** Protractors, rulers, and compasses are permitted. Do not cheat in any way. When caught, you will be blacklisted from the competition and will not be able to participate for the rest of the day.
- Carry out any reasonable calculations. For instance, you should evaluate $\frac{1}{2} + \frac{1}{3}$, but you do not need to evaluate large powers such as 7^8 .
- Write rational numbers in lowest terms. Decimals are also acceptable, provided they are exact. You may use constants such as π , e , $\sin 10^\circ$, and $\ln 2$ in your answers.
- Move all square factors outside radicals. For example, write $3\sqrt{7}$ instead of $\sqrt{63}$.
- Denominators do *not* need to be rationalized. Both $\frac{\sqrt{2}}{2}$ and $\frac{1}{\sqrt{2}}$ are acceptable.
- Do not express an answer using a repeated sum or product.

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Problems

1. Compute the following:

$$\sum_{k=1}^{\infty} \arctan \left(\frac{1}{k^2 + k + 1} \right).$$

2. Find the number of all possible distinct positive integer values of $2025 \left(\frac{\text{lcm}(x,y)}{x+y} \right)$.

3. Let ABC with $\angle BAC \geq 120^\circ$ be inscribed in a circle with radius 34 and center O . Let E be the intersection between (\overline{ABC}) and the altitude from A onto BC , and let F be the point on (\overline{ABC}) such that EF is parallel to BC . Given that AOC is equilateral and $\cos \angle BCF = \frac{8}{17}$, the area of triangle BEF can be expressed as $a\sqrt{b} - c$, where a, b, c are positive integers and b is square-free. Find $a + b + c$.