Honu: Syntactic Extension for Algebraic Notation through Enforestation

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ABSTRACT

Honu is a new language that fuses traditional algebraic notation (e.g., infix binary operators) with Scheme-style language extensibility. A key element of Honu's design is an *enforestation* parsing step, which converts a flat stream of tokens into an S-expression-like tree, in addition to the initial "read" phase of parsing and interleaved with the "macro-expand" phase. We present the design of Honu, explain its parsing and macro-extension algorithm, and show example syntactic extensions.

Categories and Subject Descriptors

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Design, Languages

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Macros, infix syntax, hygiene

1. INTRODUCTION

An extensible programming language accommodates additions to the language without requiring those additions to be adopted by a standardization committee, approved by a core set of implementors, or imposed on all users of the language. Whether for domain-specific languages or improved general-purpose constructs, extensible languages offer the promise of accelerating language design, leading to clearer and more correct programs by narrowing the gap between an idea and its expression as a program.

As appealing as the idea sounds, only the Lisp family of languages has so far made extensibility work well enough to be widely embraced by its users. The line of work on extensible syntax runs from early Lisp days, through Scheme to better support composable macros [18], and through Racket to support language variants as radical as static types [13]. This success in the Lisp family of languages has been surprisingly difficult to replicate in non-parenthetical syntaxes, however.

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GPCE'12, September 26–27, 2012, Dresden, Germany. Copyright 2012 ACM 978-1-4503-1129-8/12/09 ...\$15.00. If language extensibility is not constrained to parentheses, then it seems natural to design an extension mechanism that accommodates as many grammar extensions as possible. SugarJ [10], for example, leverages SDF's [15] support for composable grammars to allow about as much flexibility as current parsing technology can manage. This flexibility opens the door to a range of grammar-composition problems, however. From a Lisp perspective, programmers may end up worrying about technical details of character-by-character parsing, instead of designing new expressive forms.

In this paper, we offer *Honu* as an example in the middle ground between the syntactic minimalism of Lisp and maximal grammatical freedom. Our immediate goal is to produce a syntax that is more natural for many programmers than Lisp notation—most notably, using infix notation for operators—but that is similarly easy for programmers to extend.

Honu adds a precedence-based parsing step to a Lisp-like parsing pipeline to support infix operators and syntax unconstrained by parentheses. Since the job of this step is to turn a relatively flat sequence of terms into a Lisp-like syntax tree, we call it *enforestation*. Enforestation is not merely a preprocessing of program text; it is integrated into the macro-expansion machinery so that it obeys and leverages binding information to support hygiene, macro-generating macros, and local macro binding—facilities that have proven important for building expressive and composable language extensions in Lisp, Scheme, and Racket.

2. HONU OVERVIEW

Honu's syntax is similar to other languages that use curly braces and infix syntax, such as C and Javascript. Honu's macro support is similar to Scheme's, but the macro system is tailored to syntactic extensions that continue the basic Honu style, including support for declaring new infix operators.

All examples covered in the rest of the paper occur in an environment where identifiers such as macro are bound as usual.

2.1 Honu Syntax

As an introduction to Honu syntax, the following Honu code declares a function to compute the roots of a quadratic equation.

```
function quadratic(a, b, c) {
  var discriminant = sqr(b) - 4 * a * c
  if (discriminant < 0) {
      []
  } else if (discriminant == 0) {
      [-b / (2 * a)]
  } else {
      [-b / (2 * a), b / (2 * a)]
  }
}</pre>
```

The function quadratic accepts three arguments and returns a list containing the roots of the formula, if any. Line 1 starts a function definition using function, which is similar to function in Javascript. Line 2 declares a lexically scoped variable named discriminant. Lines 4, 6, and 8 create lists containing zero, one, and two elements, respectively. Honu has no return form; instead, a function's result is the value of its last evaluated expression. In this case, lines 4, 6, and 8 are expressions that can produce the function's result.

As in Javascript, when function is used without a name, it creates a anonymous function. The declaration of quadratic in the example above is equivalent to

```
var quadratic = function(a, b, c) { .... }
```

Semicolons in Honu optionally delimit expressions. Typically, no semicolon is needed between expressions, because two expressions in a sequence usually do not parse as a single expression. Some expression sequences are ambiguous, however; for example, f(x)[y] could access either of the y element of the result of f applied to x, or it could be f applied to x followed by the creation of a list that contains y. In such ambiguous cases, Honu parses the sequence as a single expression, so a semicolon must be added if separate expressions are intended.

Curly braces create a block expression. Within a block, declarations can be mixed with expressions, as in the declaration of discriminant on line 2 of the example above. Declarations are treated the same as expressions by the parser up until the last step of parsing, in which case a declaration triggers a syntax error if it is not within a block or at the top level.

2.2 Honu Macros

The Honu macro form binds a $\langle name \rangle$ to a pattern-based macro:

```
macro \langle name \rangle ( \langle literals \rangle ) { \langle pattern \rangle } { \langle body \rangle }
```

The $\langle pattern \rangle$ part of a macro declaration consists of a mixture of concrete Honu syntax and variables that can bind to matching portions of a use of the macro. An identifier included in the $\langle literals \rangle$ set is treated as a syntactic literal in $\langle pattern \rangle$ instead of as a pattern variable, which means that a use of the macro must include the literal as it appears in the $\langle pattern \rangle$. The $\langle body \rangle$ of a macro declaration is an arbitrary Honu expression that computes a new syntactic form to replace the macro use. ¹

One simple use of macros is to remove boilerplate. For example, suppose we have a derivative function that computes the approximate derivative of a given function:

```
1 function derivative(f) {
2 function (pt) {
3     (f(pt + 0.001) - f(pt)) / 0.001
4 }
5 }
```

We can use derivative directly on an anonymous function:

```
1 var df = derivative(function (x) { x * x - 5 * x + 8 })
2 df(10) // 15.099
```

If this pattern is common, however, we might provide a D syntactic form so that the example can be written as

```
1 var df = D x, x * x - 5 * x + 8
2 df(10) // 15.099
```

As a macro, D can manipulate the given identifier and expression at the syntactic level, putting them together with function:

```
1 macro D(){ z:id, math:expression } {
2    syntax(derivative(function (z) { math }))
3  }
```

The pattern for the D macro is z:id, math:expression, which matches an identifier, then a comma, and finally an arbitrary expression. In the pattern, z and math are pattern variables, while id and expression are *syntax classes* [8]. Syntax classes play a role analogous to grammar productions, where macro declarations effectively extend expression. The syntax classes id and expression are predefined in Honu.

Although the $\langle body \rangle$ of a macro declaration can be arbitrary Honu code, it is often simply a syntax form. A syntax form wraps a *template*, which is a mixture of concrete syntax and uses of pattern variables. The result of a syntax form is a *syntax object*, which is a first-class value that represents an expression. Pattern variables in syntax are replaced with matches from the macro use to generate the result syntax object.

The expansion of $\mathbb D$ is a call to derivative with an anonymous function. The macro could be written equivalently as

```
1  macro D(){ z:id, math:expression } {
2    syntax({
3         function f(z) { math }
4          derivative(f)
5         })
6  }
```

which makes D expand to a block expression that binds a local f and passes f to derivative. Like Scheme macros, Honu macros are hygienic, so the local binding f does not shadow any f that might be used by the expression matched to math.

The D example highlights another key feature of the Honu macro system. Since the pattern for math uses the expression syntax class, math can be matched to the entire expression x * x - 5 * x + 8 without requiring parentheses around the expression or around the use of D. Furthermore, when an expression is substituted into a template, its integrity is maintained in further parsing. For example, if the expression 1+1 was bound to the pattern variable e in e * 2, the resulting syntax object corresponds to (1 + 1) * 2, not 1 + (1 * 2).

Using expression not only makes D work right with infix operators, but it also makes it work with other macros. For example, we could define a parabola macro to generate parabolic formulas, and then we can use parabola with D:

The *\(\partition partor)* part of a macro declaration can use an ellipsis to match repetitions of a preceding sequence. The preceding sequence can be either a pattern variable or literal, or it can be multiple terms grouped by \$. For example, the following trace macro prints each term followed by evaluating the expression.

```
1 macro trace(){ expr ... } {
2    syntax($ printf("~a -> ~a\n", 'expr, expr) $ ...)
3 }
```

 $^{^{1}}$ The $\langle body \rangle$ of a macro is a compile-time expression, which is separated from the run-time phase in Honu in the same way as for Racket [12].

The ellipsis in the pattern causes the preceding expr to match a sequence of terms. In a template, expr must be followed by an ellipsis, either directly or as part of a group bracketed by \$ and followed by an ellipsis. In the case of trace, expr is inside a \$ group, which means that one printf call is generated for each expr.

All of our example macros so far immediately return a syntax template, but the full Honu language is available for a macro implementation. For example, an extended trace macro might statically compute an index for each of the expressions in its body and then use the index in the printed results:

```
macro ntrace(){ expr ... } {
var exprs = syntax_to_list(syntax(expr ...))
var indexes = generate_indices(exprs)
with_syntax (idx ...) = indexes {
syntax($ printf("~a -> ~a\n", idx, expr) $ ...)
}
```

In this example, syntax(expr ...) generates a syntax object that holds a list of expressions, one for each expr match, and the Honu syntax_to_list function takes a syntax object that holds a sequence of terms and generates a plain list of terms. A generate_indices helper function (not shown) takes a list and produces a list with the same number of elements but containing integers counting from 1. The with_syntax $\langle pattern \rangle = \langle expression \rangle$ form binds pattern variables in $\langle pattern \rangle$ by matching against the syntax objects produced by $\langle expression \rangle$, which in this case binds idx as a pattern variable for a sequence of numbers. In the body of the with_syntax form, the syntax template uses both expr and idx to generate the expansion result.

2.3 Defining Syntax Classes

The syntax classes id and expression are predefined, but programmers can introduce new syntax classes. For example, to match uses of a cond form like

```
cond
  x < 3: "less than 3"
  x == 3: "3"
  x > 3: "greater than 3"
```

we could start by describing the shape of an individual cond clause. The Honu pattern form binds a new syntax class:

```
pattern \langle name \rangle ( \langle literals \rangle ) { \langle pattern \rangle }
```

A pattern form is similar to a macro without an expansion $\langle body \rangle$. Pattern variables in $\langle pattern \rangle$ turn into sub-pattern names that extend a pattern variable whose class is $\langle name \rangle$.

For example, given the declaration of a cond_clause syntax class,

```
pattern cond_clause ()

check:expression : body:expression }
```

we can use cond_clause form pattern variables in the definition of a cond macro:

Since first has the syntax class cond_clause, then it matches an expression-colon-expression sequence. In the template of cond, first_check accesses the first of those expressions, since check is the name given to the first expression match in the definition of cond_clause. Similarly, first_body accesses the second expression within the first match. The same is true for rest, but since rest is followed in the macro pattern with an ellipsis, it corresponds to a sequence of matches, so that rest_check and rest_body must be under an ellipsis in the macro template.

Pattern variables that are declared without an explicit syntax class are given a default class that matches a raw term: an atomic syntactic element, or a set of elements that are explicitly grouped with parentheses, square brackets, or curly braces.

2.4 Honu Operators

In addition to defining new macros that are triggered through a prefix keyword, Honu allows programmers to declare new binary and unary operators. Binary operators are always infix, while unary operators are prefix, and an operator can have both binary and unary behaviors.

The operator form declares a new operator:

```
operator \langle name \rangle \langle prec \rangle \langle assoc \rangle \langle binary transform \rangle \langle unary transform \rangle
```

The operator precedence $\langle prec \rangle$ is specified as a non-negative rational number, while the operator's associativity $\langle assoc \rangle$ is either left or right. The operator's $\langle binary\ transform \rangle$ is a function that is called during parsing when the operator is used in a binary position; the function receives two syntax objects for the operator's arguments, and it produces a syntax object for the operator application. Similarly, an operator's $\langle unary\ transform \rangle$ takes a single syntax object to produce an expression for the operator's unary application.

The binary_operator and unary_operator forms are short-hands for defining operators with only a $\langle binary\ transform \rangle$ or $\langle unary\ transform \rangle$, respectively:

```
binary_operator \langle name \rangle \langle prec \rangle \langle assoc \rangle \langle binary transform \rangle
unary_operator \langle name \rangle \langle prec \rangle \langle unary transform \rangle
```

A unary operator is almost the same as a macro that has a single expression subform. The only difference between a macro and a unary operator is that the operator has a precedence level, which can affect the way that expressions using the operator are parsed. A macro effectively has a precedence level of 0. Thus, if m is defined as a macro, then m 1 + 2 parses like m (1 + 2), while if m is a unary operator with a higher precedence than +, m 1 + 2 parses like (m 1) + 2. A unary operator makes a recursive call to parse with its precedence level but macros have no such requirement so unary operators cannot simply be transformed into macros.

As an example binary operator, we can define a raise operator that raises the value of the expression on the left-hand side to the value of the expression on the right-hand side:

```
binary_operator raise 10 left
function (left, right) {
    syntax(pow(left, right))
}
```

The precedence level of raise is 10, and it associates to the left.

Naturally, newly declared infix operators can appear in subexpressions for a macro use:

```
var d = D x, x raise 4 + x raise 2 - 3
```

We can define another infix operator for logarithms and compose it with the raise operator. Assume that make_log generates an expression that takes the logarithm of the left-hand side using the base of the right-hand side:

```
binary_operator lg 5 left make_log
x raise 4 lg 3 + x raise 2 lg 5 - 3
```

Since raise has higher precedence than 1g, and since both raise and 1g have a higher precedence than the built-in + operator, the parser groups the example expression as

```
((x \text{ raise 4}) \lg 3) + ((x \text{ raise 2}) \lg 5) - 3
```

As the raise and 1g examples illustrate, any identifier can be used as an operator. Honu does not distinguish between operator names and other identifiers, which means that raise can be an operator name and + can be a variable name. Furthermore, Honu has no reserved words and any binding—variable, operator, or syntactic form—can be shadowed. This flexible treatment of identifiers is enabled by the interleaving of parsing with binding resolution, as we discuss in the next section.

3. PARSING HONU

Honu parsing relies on three layers: a *reader* layer, an *enforestation* layer, and a *parsing* layer proper that drives enforestation, binding resolution, and macro expansion. The first and last layers are directly analogous to parsing layers in Lisp and Scheme, and so we describe Honu parsing in part by analogy to Scheme, but the middle layer is unique to Honu.

3.1 Grammar

A BNF grammar usually works well to describe the syntax of a language with a fixed syntax, such as Java. BNF is less helpful for a language like Scheme, whose syntax might be written as

```
 \langle expression \rangle ::= \langle literal \rangle \mid \langle identifier \rangle \\ \mid (\langle expression \rangle \langle expression \rangle^*) \\ \mid (lambda (\langle identifier \rangle^*) \langle expression \rangle^+) \\ \mid (lif \langle expression \rangle \langle expression \rangle \langle expression \rangle) \\ \mid ...
```

but such a grammar would be only a rough approximation. Because Scheme's set of syntactic forms is extensible via macros, the true grammar at the level of expressions is closer to

```
\langle expression \rangle ::= \langle literal \rangle | \langle identifier \rangle
| (\langle expression \rangle \langle expression \rangle^*)
| (\langle form\ identifier \rangle\ \langle term \rangle^*)
```

The (\langle expression \rangle \langle expression \rangle*) production captures the default case when the first term after a parenthesis is not an identifier that is bound to a syntactic term, in which case the expression is treated as a function call. Otherwise, the final (\langle form identifier \rangle \langle term \rangle*) production captures uses of lambda and if as well as macro-defined extensions. Putting a lambda or if production would be misleading, because the name lambda or if can be shadowed or redefined by an enclosing expression; an enclosing term might even rewrite a nested lambda or if away. In exchange for the loss of BNF and a different notion of parsing, Scheme programmers gain an especially expressive, extensible, and composable notation.

The syntax of Honu is defined in a Scheme-like way, but with more default structure than Scheme's minimal scaffolding. The grammar of Honu is roughly as follows:

```
⟨program⟩
                   ::=\langle sequence\rangle
⟨expression⟩
                         ⟨literal⟩ | ⟨identifier⟩
                         (unary operator) (expression)
                          (expression) (binary operator) (expression)
                         \langle expression \rangle (\langle comma-seq \rangle)
                         ( \( \langle expression \rangle \)
                         ⟨expression⟩ [ ⟨expression⟩ ]
                         [ (comma-sea) ]
                         [\langle expression \rangle : \langle expression \rangle = \langle expression \rangle ]
                         { \(\langle sequence \rangle \)}
                         ⟨form identifier⟩ ⟨term⟩*
                  := \langle expression \rangle [,] \langle comma-seq \rangle
⟨comma-seq⟩
                         (expression)
⟨sequence⟩
                  ::= \langle expression \rangle [;] \langle sequence \rangle
                         (expression)
```

This grammar reflects a mid-point between Scheme-style syntax and traditional infix syntax:

- Prefix unary and infix binary operations are supported through the extensible \(\lambda unary operator \rangle \) and \(\lambda binary operator \rangle \) productions.
- The \(\langle expression\rangle\) (\(\langle comma-seq\rangle\)) production plays the same role as Scheme's default function-call production, but in traditional algebraic form.
- The (\(\langle expression \rangle \)) production performs the traditional role
 of parenthesizing an expression to prevent surrounding operators with higher precedences from grouping with the constituent parts of the expression.
- The \(\lambda expression \rangle \) [\(\lambda expression \rangle \)] production provides a default interpretation of property or array access.
- The [\(\chicomma-seq \rangle \)] production provides a default interpretation of square brackets without a preceding expression as a list creation mechanism.
- The [\(\langle expression \rangle : \langle expression \rangle = \langle expression \rangle]\) production provides a default interpretation of square brackets with : and = as a list comprehension.
- The { \(\sequence\)\) } production starts a new sequence of expressions that evaluates to the last expression in the block.
- Finally, the \(\form\) identifier\(\rangle\) \(\text{term}\)\(\rangle\)* production allows extensibility of the expression grammar.

In the same way that Scheme's default function-call interpretation of parentheses does not prevent parentheses from having other meanings in a syntactic form, Honu's default interpretation of parentheses, square brackets, curly braces, and semi-colons does not prevent their use in different ways within a new syntactic form.

3.2 Reading

The Scheme grammar relies on an initial parsing pass by a *reader* to form $\langle term \rangle$ s. The Scheme reader plays a role similar to token analysis for a language with a static grammar, in that it distinguishes numbers, identifiers, string, commas, parentheses, comments, etc. Instead of a linear sequence of tokens, however, the reader produces a tree of values by matching parentheses. Values between a pair of matching parentheses are grouped as a single term within the enclosing term. In Honu, square brackets and curly braces are distinguished from parentheses, but they similarly matched.

Ignoring the fine details of parsing numbers, strings, identifiers, and the like, the grammar recognized by the Honu reader is

```
enforest(atom\ term_{rest}\ ...,\ combine,\ prec,\ stack)
                                                                                                                     = enforest((literal: atom) term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                      = enforest((id: identifier_binding) term_rest ..., combine, prec, stack)
enforest(identifier term<sub>rest</sub> ..., combine, prec, stack)
where (var: identifier_{binding}) = lookup(identifier)
enforest(identifier term<sub>rest</sub> ..., combine, prec, [(combine<sub>stack</sub>, prec<sub>stack</sub>) stack])
                                                                                                                      = enforest(transformer(term_rest ...), combine_stack, prec_stack, stack)
where \langle macro: transformer \rangle = lookup(identifier)
enforest(tree-term<sub>first</sub> identifier term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                     = enforest(term_rest ..., function(t){\din: identifier, tree-term_first, t\},
                                                                                                                                      precoperator, [(combine, prec) stack])
where \langle binop: prec_{operator}, assoc \rangle = lookup(identifier), prec_{operator} >_{assoc} prec
enforest(tree-term<sub>first</sub> identifier term<sub>rest</sub> ..., combine, prec, [(combine<sub>stack</sub>, prec<sub>stack</sub>) stack]) = enforest(combine(tree-term<sub>first</sub>) identifier term<sub>rest</sub> ...,
                                                                                                                                      combine<sub>stack</sub>, prec<sub>stack</sub>, stack)
where \langle binop: prec_{operator}, assoc \rangle = lookup(identifier), prec_{operator} <_{assoc} prec
enforest(identifier term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                      = enforest(term_{rest} ..., function(t){combine(\langle un: identifier, t \rangle)}, prec_{operator}, stack)
where \langle unop: prec_{operator} \rangle = lookup(identifier)
enforest((term<sub>inside</sub> ...) term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                      = enforest(tree-term<sub>inside</sub> term<sub>rest</sub> ..., combine, prec, stack)
where (tree-term_{inside}, \varepsilon) = enforest(term_{inside}, ..., identity, 0, [])
enforest(tree-term (term<sub>arg</sub> ...) term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                      = enforest(\langle call: tree-term, tree-term_{arg}, ... \rangle term_{rest} ..., combine, prec, stack)
where (tree-term_{arg}, \varepsilon) ... = enforest(term_{arg}, identity, 0, []) ...
enforest(tree-term [term ...] term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                      = enforest(\langle arrayref: tree-term, tree-term_lookup\rangle term_rest ...,
                                                                                                                                      combine, prec, stack)
where (tree-term_{lookup}, \epsilon) = enforest(term ..., identity, 0, [])
enforest([term ...] term<sub>rest</sub> ..., combine, prec, stack)
                                                                                                                      = enforest(\langle list: term, ...\rangle term_{rest} ..., combine, prec, stack)
                                                                                                                      = enforest(\langle block: term, ...\rangle term_{rest} ..., combine, prec, stack)
enforest({term ...} term<sub>rest</sub> ..., combine, prec, stack)
enforest(tree-term term<sub>rest</sub> ..., combine, prec, [])
                                                                                                                     = (combine(tree-term), term<sub>rest</sub> ...)
                                                                                                                      = enforest(combine(tree-term) term_{rest} ..., combine_{stack}, prec_{stack}, stack)
enforest(tree-term\ term_{rest}\ ...,\ combine,\ prec,\ [(combine_{stack},\ prec_{stack})\ stack])
```

Figure 1: Enforestation

make(1, 2, 3)

the reader produces a sequence of two $\langle term \rangle$ s: one for make, and another for the parentheses. The latter contains five nested $\langle term \rangle$ s: 1, a comma, 2, a comma, and 3.

In both Scheme and Honu, the parser consumes a $\langle term \rangle$ representation as produced by the reader, and it expands macros in the process of parsing $\langle term \rangle$ s into $\langle expression \rangle$ s. The $\langle term \rangle$ s used during parsing need not have originated from the program source text, however; macros that are triggered during parsing can synthesize new $\langle term \rangle$ s out of symbols, lists, and other literal values. The ease of synthesizing $\langle term \rangle$ representations—and the fact that they are merely $\langle term \rangle$ s and not fully parsed ASTs—is key to the ease of syntactic extension in Scheme and Honu.

3.3 Enforestation

To handle infix syntax, the Honu parser relies on an *enforestation* phase that converts a relatively flat sequence of $\langle term \rangle$ s into a more Scheme-like tree of nested expressions. Enforestation handles operator precedence and the relatively delimiter-free nature of Honu syntax, and it is macro-extensible. After a layer of enforestation, Scheme-like macro expansion takes over to handle binding, scope, and cooperation among syntactic forms. Enforestation and expansion are interleaved, which allows the enforestation process to be sensitive to bindings.

Enforestation extracts a sequence of terms produced by the reader to create a *tree term*, which is ultimately produced by a primitive syntactic form or one of the default productions of $\langle expression \rangle$,

such as the function-call or list-comprehension production. Thus, the set of $\langle tree\ term \rangle$ s effectively extends the $\langle term \rangle$ grammar although $\langle tree\ term \rangle$ s are never produced by the reader:

```
\langle term \rangle ::= ...
| \langle tree \ term \rangle
```

Enforestation is driven by an enforest function that extracts the first expression from an input stream of $\langle term \rangle$ s. The enforest function incorporates aspects of the precedence parsing algorithm by Pratt [20] to keep track of infix operator parsing and precedence. Specifically, enforest has the following contract:

```
enforest : \langle term \rangle^* (\langle tree\ term \rangle \rightarrow \langle tree\ term \rangle) \langle prec \rangle \langle stack \rangle \rightarrow (\langle tree\ term \rangle, \langle term \rangle^*)
```

The arguments to enforest are as follows:

- *input* a list of $\langle term \rangle$ s for the input stream;
- combine a function that takes a \(\langle tree \text{term} \rangle\) for an expression and produces the result \(\langle tree \text{term} \rangle\); this argument is initially the identity function, but operator parsing leads to \(\chi \text{combine}\) functions that close over operator transformers;
- precedence an integer representing the precedence of the pending operator combination combine, which determines whether combine is used before or after any further binary operators that are discovered; this argument starts at 0, which means that the initial combine is delayed until all operators are handled.
- *stack* a stack of pairs containing a combine function and precedence level. Operators with a higher precedence level than the current precedence level push the current combine and precedence level on the stack. Conversely, operators with a lower precedence level pop the stack.

In addition, enforest is implicitly closed over a mapping from identifiers to macros, operators, primitive syntactic forms, and declared variables. The result of enforest is a tuple that pairs a tree term representing an $\langle expression \rangle$ with the remainder terms of the input stream.

The rules of enforestation are given in figure 1. If the first term is not a tree term or a special form then it is first converted into a tree term. Special forms include macros, operators, function calls, and bracketed sequences.

As an example, with the input

```
1+2*3-f(10)
```

enforestation starts with the entire sequence of terms, the identity function, a precedence of zero, and an empty stack:

```
enforest(1 + 2 * 3 - f (10), identity, 0, [])
```

The first term, an integer, is converted to a literal tree term, and then enforest recurs for the rest of the terms. We show a tree term in angle brackets:

```
enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enforest(enfor
```

Since the input stream now starts with a tree term, enforest checks the second element of the stream, which is a binary operator with precedence 1. Enforestation therefore continues with a new *combine* function that takes a tree term for the operator's right-hand side and builds a tree term for the binary operation while the old combine function and precedence level are pushed onto the stack:

```
enforest(2 * 3 - f (10), combine1, 1, [(identity, 0)])
  where combine1(t) = <bin: +, <li>teral: 1>, t>
```

The first term of the new stream starts with 2, which is converted to a literal tree term:

The leading tree term is again followed by a binary operator, this time with precedence 2. Since the precedence of the new operator is higher than the current precedence, a new *combine* function builds a binary-operation tree term for * while the *combine1* function and its precedence level are pushed onto the stack:

The current input sequence once again begins with a literal:

The binary operator - has precedence 1, which is less than the current precedence. The current *combine* function is therefore applied to teral: 3>, and the result becomes the new tree term at the start of the input. We abbreviate this new tree term:

Parsing continues by popping the combine function and precedence level from the stack. Since the precedence of – is the same as the current precedence and is left associative the *combine1* function is applied to the first tree term and another level of the stack is popped:

```
enforest(<expr: 1+2*3> - f (10), identity, 0, [])
```

The – operator is handled similarly to + at the start of parsing. The new *combine* function will create a subtraction expression from the current tree term at the start of the input and its argument:

```
enforest( f (10), combine3, 1, [(identity, 0)])
  where combine3(t) = <bin: -, exp<1+2*3>, t>
```

Assuming that f is bound as a variable, the current stream is enforested as a function-call tree term. In the process, a recursive call enforest(10, identity, 0, empty) immediately produces literal: 10> for the argument sequence, so that the non-nested enforest continues as

Since the input stream now contains only a tree term, it is passed to the current *combine* function, producing the result tree term:

```
<bin: -, <expr: 1+2*3>, <call: <id: f>, teral: 10>>>
```

Finally, the input stream is exhuasted so the identity combination function is popped from the stack and immediately applied to the tree term.

3.4 Macros and Patterns

From the perspective of enforest, a macro is a function that consumes a list of terms, but Honu programmers normally do not implement macros at this low level. Instead, Honu programmers write pattern-based macros using the macro form that (as noted in section 2.2) has the shape

```
macro \langle name \rangle ( \langle literals \rangle ) { \langle pattern \rangle } { \langle body \rangle }
```

The macro form generates a low-level macro that returns a new sequence of terms and any unconsumed terms from its input. The $\langle pattern \rangle$ is compiled to a matching and destructuring function on an input sequence of terms. This generated matching function automatically partitions the sequence into the terms that are consumed by the macro and the leftover terms that follow the pattern match.

Literal identifiers and delimiters in $\langle pattern \rangle$ are matched to equivalent elements in the input sequence. A parenthesized sequence in $\langle pattern \rangle$ corresponds to matching a single parenthesized term whose subterms match the parenthesized pattern sequence, and so on. A pattern variable associated to a syntax class corresponds to calling a function associated with the syntax class to extract a match from the sequence plus the remainder of the sequence.

For example, the macro

expands to the low-level macro function

```
function(terms) {
  var x = first(terms)
  var [a_stx, after_a] = get_expression(rest(terms))
  check_equal(",", first(after_a))
  var [b_stx, after_b] = get_expression(rest(after_a))
  check_equal(",", first(after_b))
  var [c_stx, after_c] = get_expression(rest(after_b))
  // return new term plus remaining terms:
  [with_syntax a = a_stx, b = b_stx, c = c_stx {
      syntax(a * x * x + b * x + c)
    }, after_c]
}
```

The get_expression function associated to the expression syntax class is simply a call back into enforest:

```
function get_expression(terms) {
  enforest(terms, identity, 0)
}
```

New syntax classes declared with pattern associate the syntax class name with a function that similarly takes a term sequence and separates a matching part from the remainder, packaging the match so that its elements can be extracted by a use of the syntax class. In other words, the matching function associated with a syntax class is similar to the low-level implementation of a macro.

3.5 Parsing

Honu parsing repeatedly applies enforest on a top-level sequence of $\langle term \rangle$ s, detecting and registering bindings along the way. For example, a macro declaration that appears at the top level must register a macro before later $\langle term \rangle$ s are enforested, since the macro may be used within those later $\langle term \rangle$ s.

Besides the simple case of registering a macro definition before its use, parsing must also handle mutually recursive definitions, such as mutually recursive functions. Mutual recursion is handled by delaying the parsing of curly-bracketed blocks (such as function bodies) until all of the declarations in the enclosing scope have been registered, which requires two passes through a given scope level. Multiple-pass parsing of declarations and expressions has been worked out in detail for macro expansion in Scheme [25] and Racket [13], and Honu parsing uses the same approach.

Honu not only delays parsing of blocks until the enclosing layer of scope is resolved, it even delays the enforestation of block contents. As a result, a macro can be defined after a function in which the macro is used. Along the same lines, a macro can be defined within a block, limiting the scope of the macro to the block and allowing the macro to expand to other identifiers that are bound within the block.

Flexible ordering and placement of macro bindings is crucial to the implementation of certain kinds of language extensions [13]. For example, consider a cfun form that supports macros with contracts:

```
cfun quadratic(num a, num b, num c) : listof num { .... }
```

The cfun form can provide precise blame tracking [11] by binding quadratic to a macro that passes information about the call site to the raw quadratic function. That is, the cfun macro expands to a combination of function and macro declarations. As long as macro declarations are allowed with the same placement and ordering rules as function declarations, then cfun can be used freely as a replacement for function.

The contract of the Honu parse function is

```
parse : \langle term \rangle^* \langle bindings \rangle \rightarrow \langle AST \rangle^*
```

That is, parse takes a sequence of $\langle term \rangle$ s and produces a sequence of $\langle AST \rangle$ records that can be interpreted. Initially, parse is called with an empty mapping for its $\langle bindings \rangle$ argument, but nested uses of parse receive a mapping that reflects all lexically enclosing bindings.

Since parse requires two passes on its input, it is implemented in terms of a function for each pass, parse1 and parse2:

```
parse1 : \langle term \rangle^* \langle bindings \rangle \rightarrow (\langle tree\ term \rangle^*, \langle bindings \rangle)
parse2 : \langle tree\ term \rangle^* \langle bindings \rangle \rightarrow \langle AST \rangle^*
```

The parse1 pass determines bindings for a scope, while parse2 completes parsing of the scope using all of the bindings discovered by parse1.

Details of the parsing algorithm can be found in the appendix.

3.5.1 Parsing Example

As an example, consider the following sequence:

```
macro info(at){ x:id, math:expression
    at point:expression } {
    syntax({
        var f = function(x) { math }
            printf("at ~a dx ~a\n", f(point))
        })
}
info x, x*x+2*x-1 at 12
```

Initially, this program corresponds to a sequence of $\langle terms \rangle$ starting with macro, info, and (at). The first parsing step is to enforest one form, and enforestation defers to the primitive macro, which consumes the next four terms. The program after the first enforestation is roughly as follows, where we represent a tree term in angle brackets as before:

```
<macro declaration: info, ...>
info x, x*x+2*x-1 at 12
```

The macro-declaration tree term from enforest causes parse1 to register the info macro in its *bindings*, then parse1 continues with enforest starting with the info identifier. The info identifier is bound as a macro, and the macro's pattern triggers the following actions:

- it consumes the next x as an identifier;
- it consumes the comma as a literal;
- it starts enforesting the remaining terms, which succeeds with a tree term for x*x+2*x-1;
- it consumes at as a literal;
- starts enforesting the remaining terms as an expression, again, which succeeds with the tree term 11teral: 12>.

Having collected matches for the macro's pattern variables, the info macro's body is evaluated to produce the expansion, so that the overall sequence becomes

```
{
  var f = function(x) { <expr: x*x+2*x-1> }
  printf("at ~a dx ~a\n", f(<literal: 12>))
}
```

Macro expansion of info did not produce a tree term, so enforest recurs. At this point, the default production for curly braces takes effect, so that the content of the curly braces is preserved in a block tree term. The block is detected as the enforest result by parse1, which simply preserves it in the result tree term list. No further terms remain, so parse1 completes with a single tree term for the block.

The parse2 function receives the block, and it recursively parses the block. That is, parse is called to process the sequence

```
var f = function(x) { <expr: x*x+2*x-1> } printf("at \sima dx \sima\n", f(<literal: 12>))
```

The first term, var, is bound to the primitive declaration form, which consumes f as an identifier, = as a literal, and then enforests the remaining terms as an expression.

The remaining terms begin with function, which is is the primitive syntactic form for functions. The primitive function form consumes the entire expression to produce a tree term representing a function. This tree term is produced as the enforestation that var demanded, so that var can produce a tree term representing the declaration of f. The block body is therefore to the point

When parse1 receives this function-declaration tree term, it registers f as a variable. Then parse1 applies enforest on the terms starting with printf, which triggers the default function-call production since printf is bound as a variable. The function-call production causes enforestation of the arguments "at \sim a dx \sim a\n" and f(<literal: 12>) to a literal string and function-call tree term, respectively. The result of parse1 is a sequence of two tree terms:

The parse2 phase at this level forces enforestation and parsing of the function body, which completes immediately, since the body is already a tree term. Parsing similarly produces an AST for the body in short order, which is folded into a AST for the function declaration. Finally, the function-call tree term is parsed into nested function-call ASTs.

3.5.2 Parsing as Expansion

For completeness, we have described Honu parsing as a standalone and Honu-specific process. In fact, the Honu parser implementation leverages the existing macro-expansion machinery of Racket. For example, the Honu program

```
#lang honu
```

is converted via the Honu reader to

```
#lang racket
(honu-block 1 + 2)
```

The honu-block macro is implemented in terms of enforest:

```
(define-syntax (honu-block stx)
  (define terms (cdr (syntax->list stx)))
  (define-values (form rest) (enforest terms identity 0))
  (if (empty? rest)
      form
      #'(begin #,form (honu-block . #,rest))))
```

where #' and #, are forms of quasiquote and unquote lifted to the realm of lexically scoped S-expressions.

The strategy of treating enforest's first result as a Racket form works because enforest represents each tree term as a Racket S-expression. The tree term for a Honu var declaration is a Racket define form, function call and operator applications are represented as Racket function calls, and so on.

Expanding honu-block to another honu-block to handle further terms corresponds to the parse1 recursion in the stand-alone description of Honu parsing. Delaying enforestation and parsing to parse2 corresponds to using honu-block within a tree term; for example, the enforestation of

```
function(x) { D y, y*x }
is
  (lambda (x) (honu-block D y |, | y * x))
```

When such a function appears in the right-hand side of a Racket-level declaration, Racket delays expansion of the function body until all declarations in the same scope are processed, which allows a macro definition of D to work even if it appears after the function.

Honu macro and pattern forms turn into Racket define-syntax forms, which introduce expansion-time bindings. The enforest function and pattern compilation can look up macro and syntax-class bindings using Racket's facilities for accessing the expansion-time environment [13].

Besides providing an easy way to implement Honu parsing, building on Racket's macro expander means that the more general facilities of the expander can be made available to Honu programmers. In particular, Racket's compile-time reflection operations can be exposed to Honu macros, so that Honu macros can cooperate in the same ways as Racket macros to implement pattern matchers, class systems, type systems, and more.

4. RELATED WORK

C++ templates are most successful language-extension mechanism outside of the Lisp tradition. Like Honu macros, C++ templates allow only constrained extensions of the language, since template invocations have a particular syntactic shape. Honu macros are more flexible than C++ templates, allowing extensions to the language that have the same look as built-in forms. In addition, because Honu macros can be written in Honu instead of using only pattern-matching constructs, complex extensions are easier to write and can give better syntax-error messages than in C++'s template language. C++'s support for operator overloading allows an indirect implementation of infix syntactic forms, but Honu allows more flexibility for infix operators, and Honu does not require an a priori distinction between operator names and other identifiers.

Honu macro definitions integrate with the parser without having to specify grammar-related details. Related systems, such as SugarJ [10], Xoc [7], and Polyglot [19] require the user to specify which grammar productions to extend, which can be an additional burden for the programmer. Xoc and SugarJ use a GLR [27] parser that enables them to extend the the class of tokens, which allows a natural embedding of domain-specific languages. Ometa [28] and Xtc [14] are similar in that they allow the user to extend how the raw characters are consumed, but they do not provide a macro system. Honu does not contain a mechanism for extending its lexical analysis of the raw input stream because Honu implicitly relies on guarantees from the reader about the structure of the program to perform macro expansion.

Composability of macros is tightly correlated with the parsing strategy. Honu macros are highly composable because they are limited to forms that start with an identifier bound to a macro or be in operator position. Other systems that try to allow more general forms expose underlying parsing details when adding extensions. Systems based on LL, such as the one devised by Cardelli and Matthes [6], and LALR, such as Maya [4], have fundamental limits to the combinations of grammar extensions. PEG based systems are closed under union but force an ordering of productions which may be difficult to reason about.

Some macro systems resort to AST constructors for macro expansions instead of templates based on concrete syntax. Maya fits the AST-constructor category. Template Haskell [16], SugarJ, and the Java Syntax Extender [3] include support for working with concrete syntax, but they also expose a set of abstract syntax tree constructors for more complex transformations. Camlp4 [9] is a preprocessor for Ocaml programs that can output concrete Ocaml syntax, but it cannot output syntax understood by a separate preprocessor, so syntax extensions are limited to a single level. MS2 [29]

incorporates Lisp's quasiquote mechanism as a templating system for C, but MS2 does not include facilities to expand syntax that correspond to infix syntax or any other complex scheme.

Honu macros have the full power of the language to implement a macro transformation. Systems that only allow term rewriting, such as R5RS Scheme [17], Dylan [24], Arai and Wakita [1] and Fortress [21], can express many simple macros, but they are cumbersome to use for complex transformations.

ZL [2] is like Honu in that it relies on Lisp-like read and parsing phases, it generalizes those to non-parenthesiz-ed syntax, and its macros are expressed with arbitrary ZL code. Compared to Honu, macros in ZL are more limited in the forms they can accept, due to decisions made early on in the read phase. Specifically, arbitrary expressions cannot appears as subforms unless they are first parenthesized. ZL supports more flexible extensions by allowing additions to its initial parsing phase, which is similar to reader extension in Lisp or parsing extensions in SugarJ, while Honu allows more flexibility within the macro level.

Stratego [15] supports macro-like implementations of languages as separate from the problem of parsing. Systems built with Stratego can use SDF for parsing, and then separate Stratego transformations process the resulting AST. Transformations in Stratego are written in a language specific to the Stratego system and different from the source language being transformed, unlike Honu or other macro languages.

Many systems implement some form of modularity for syntactic extension. Both SDF and Xoc [7] provide a way to compose modules which define grammar extensions. These systems have their own set of semantics that are different from the source language being extended. Honu uses its natural lexical semantics to control the scope of macros. Macros can be imported into modules and shadowed at any time thus macros do not impose a fundamental change into reasoning about a program.

Multi-stage allows programs to generate and optimize code at run-time for specific sets of data. Mython [22], MetaOcaml [5], LMS [23] are frameworks that provide methods to optimize expressions by analyzing a representation of the source code. A similar technique can be achieved in Honu by wrapping expressions with a macro that analyzes its arguments and plays the role of a compiler by rewriting the expression to a semantically equivalent expression. Typed Racket [26] implements compile-time optimizations using the Racket macro system.

5. CONCLUSION

Honu is a syntactically extensible language that builds on Lispstyle extensibility while supporting infix operators and other syntactic forms that are unconstrained by parentheses. Although Honu syntax is more flexible than parenthesized syntax, Honu continues a tradition of trading expressiveness for syntactic simplicity in that Honu accommodates only syntactic extensions that fit certain conventions. More generally, we suggest that a language has its own syntactic style, and successful extensions leverage that consistency rather than subverting it.

Syntactic consistency is especially clear in Lisp-style languages, but many other languages have their own conventions that can be exploited and preserved by extensions to the language. Java, Javascript and other curly-brace languages consistently delimit sub-expressions with parenthesis, braces, and brackets. A Honu-style parser would work well in those languages, at least for expressions. Languages with complex grammars, such as Java or Ruby, would likely require incorporating the precedence parser with an LR-based parser. In the worst case, the parser can add support for macros without requiring changes to deal with infix operators.

Composability is a key feature of the Honu macro system. The token-level consistency that is imposed by the reader layer, the extensible $\langle expression \rangle$ grammar production, and the hygienic treatment of identifiers together allow programmers to implement macros that compose naturally. Furthermore, user-defined forms are like built-in forms in that they have no special identifiers or other markers to distinguish them. Macros in Honu thus offer the promise of a smooth path from building simple syntactic abstractions to whole new languages.

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Appendix

The parse1 function takes input as the $\langle term \rangle$ sequence and bindings as the bindings found so far. If input is empty, then parse1 returns with an empty tree term sequence and the given bindings. Otherwise, parse1 applies enforest to input, the identity function, and zero; more precisely, parse1 applies an instance of enforest that is closed over bindings. The result from enforest is form, which is a tree term, and rest, which is the remainder of input that was not consumed to generate form. Expansion continues based on case analysis of form:

- If form is a var declaration of identifier, then a variable mapping for identifier is added to bindings, and parse1 recurs with rest; when the recursive call returns, form is added to (the first part of) the recursion's result.
- If form is a macro or pattern declaration of identifier, then the macro or syntax class's low-level implementation is created and added to bindings as the binding of identifier. Generation of the low-level implementation may consult bindings to extract the implementations of previously declared syntax classes. The parse1 function then recurs with rest and the new bindings.
 - If parse1 was called for the expansion of a module body, then an interpretable variant of *form* is preserved in case the macro is exported. Otherwise, *form* is no longer needed, since the macro or syntax-class implementation is recorded in the result *bindings*.
- If form is an expression, parse1 recurs with rest and unchanged bindings; when the recursive call returns, form is added to (the first part of) the recursion's result.

The results from parse1 are passed on to parse2. The parse2 function maps each *form* in its input tree term to an AST:

- If form is a var declaration, the right-hand side of the declaration is parsed through a recursive call to parse2. The result is packaged into a variable-declaration AST node.
- If form is a function expression, the body is enforested and
 parsed by calling back to parse, passing along parse2's
 \(\begin{aligned} \begin{aligned} \begin{aligned} \begin{aligned} \delta \begin{aligned} \delta \delt
- If *form* is a block expression, then parse is called for the block body in the same way as for a function body (but without argument variables), and the resulting ASTs are packaged into a single sequence AST node.
- If form is an identifier, then it must refer to a variable, since macro references are resolved by enforest. The identifier is compiled to a variable-reference AST.
- If form is a literal, then a literal AST node is produced.
- Otherwise, form is a compound expression, such as a functioncall expression. Subexpressions are parsed by recursively calling parse2, and the resulting ASTs are combined into a suitable compound AST.