

ML-475 Final Project: Face Masking Recognition

A monitoring strategy based on machine learning algorithm in the COVID-19 era Instructed by: Aggelos K Katsaggelos

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YouTube Access: https://youtu.be/r6gWZx 7GY4

GitHub Access: https://github.com/GuoJiaqi-1020/EE-475-ML-Final-Project

Project

December 6, 2021

1 EE475 Group Project : Machine Learning Based Face Mask Recognition

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As the COVID-19 has brought great disaster to human beings, personal protection has become particularly important. For the purpose of controlling the spread of the epidemic, every one of us has the obligation and responsibility to wear masks. The objective of our project is to proposed a system that can monitor people's mask wearing status (Correct, Incorrect and No mask). In our project, we reduce the dimension of input data space by using pre-processing methods: convert into gray image, Histogram of Oriented Gradients algorithm and Canny edge detector algorithm. We firstly implement linear model from scratch, then implement SVM, Decision Tree and Random Forest using scikit learn library.

```
[]: import numpy as np
  import matplotlib.pyplot as plt
  import sklearn.svm as svm
  import sklearn.tree as tree
  import sklearn.ensemble as ensemble
  from sklearn.pipeline import make_pipeline
  from sklearn.preprocessing import StandardScaler
  from sklearn.model_selection import train_test_split
  from sklearn import metrics
  from lib_fun import *
  from skimage.feature import hog
```

```
[]: # Load the original face mask data with pixel of 20*20, 50*50 and 100*100
# We visulaize these image of Correct, Incorrect and No mask with each
→resolution.

data20, labels20 = load('../Data/Pixel20/')
data50, labels50 = load('../Data/Pixel50/')
data100, labels100 = load('../Data/Pixel100/')
VisualizeRGB(data20, data50, data100)
```

```
X shape: (4559, 20, 20, 3), Y shape: (4559,)
X shape: (4559, 50, 50, 3), Y shape: (4559,)
X shape: (4559, 100, 100, 3), Y shape: (4559,)
```



















[]: # In order to reduce the input dimension and keep critical information, well → transfer the RGB image to gray image

data20 gray = RGBtoGray(data20) data50_gray = RGBtoGray(data50) data100_gray = RGBtoGray(data100)

VisualizeGray(data20_gray, data50_gray, data100_gray)



















[]: # Using Histogram of Oriented Gradients to extract features from RGB image # Compute 8 direction in each 2*2 pixel

data20_hog = RGBtoHOG(data20) data50 hog = RGBtoHOG(data50) data100_hog = RGBtoHOG(data100)

VisualizeGray(data20_hog, data50_hog, data100_hog)



















[]: # Using Canny edge detector to extract features from gray image

data20_edge = GRAYtoEDGE(data20_gray, sigma=1) data50_edge = GRAYtoEDGE(data50_gray, sigma=3) data100_edge = GRAYtoEDGE(data100_gray, sigma=5) VisualizeGray(data20_edge, data50_edge, data100_edge)



















```
[]: # Training process using different model. Split the data into training: test = 4:1.

# Flatten the image as the input data of model

def train_model(model, data, labels):
    x = Flatten(data)
    x_train, x_test , y_train, y_test = train_test_split(x, labels, test_size = 0.2, random_state=1)
    clf = make_pipeline( StandardScaler(), model)
    clf.fit(x_train, y_train)
    pred = clf.predict(x_test)
    print('accuracy: ', metrics.accuracy_score(y_test, pred))
    confusion = metrics.confusion_matrix(y_test, pred)
    return confusion
```

Firstly We implement one vs rest SVM model. SVM maps training examples to points in space so as to maximise the width of the gap between the two categories. New examples are then mapped into that same space and predicted to belong to a category based on which side of the gap they fall. As we are using a soft margin SVM, we set the penalty term C as 1. A low C makes the decision surface smooth, while a high C aims at classifying all training examples correctly. And we are using a kernel function to map the input features to a higher dimension space. In this experiment, we compare the linear, polynomial and rbf kernel. We choose gray and hog data as out training data in this experiment.

```
[]: # SVM with linear kernel, using gray images as data.

confusion20 = train_model(svm.SVC(C=1, kernel='linear', cache_size=4000),

data20_gray, labels20)

confusion50 = train_model(svm.SVC(C=1, kernel='linear', cache_size=4000),

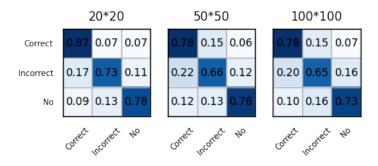
data50_gray, labels50)

confusion100 = train_model(svm.SVC(C=1, kernel='linear', cache_size=4000),

data100_gray, labels100)

plot_confusion_matrix([confusion20, confusion50, confusion100])
```

accuracy: 0.7905701754385965 accuracy: 0.7324561403508771 accuracy: 0.7214912280701754



It is not difficult to find that with the increase of image size, the accuracy of our model even decreases, which is very counterintuitive.

```
[]: # SVM with linear kernel, using hog images as data.

confusion20 = train_model(svm.SVC(C=1, kernel='linear', cache_size=4000),

data20_hog, labels20)

confusion50 = train_model(svm.SVC(C=1, kernel='linear', cache_size=4000),

data50_hog, labels50)

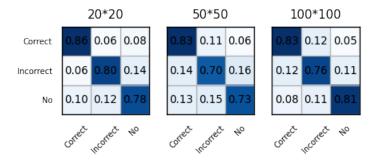
confusion100 = train_model(svm.SVC(C=1, kernel='linear', cache_size=4000),

data100_hog, labels100)

plot_confusion_matrix([confusion20, confusion50, confusion100])
```

accuracy: 0.8125

accuracy: 0.7521929824561403 accuracy: 0.8004385964912281

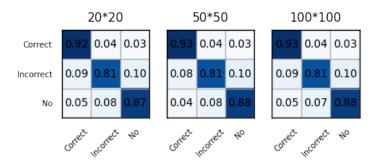


Although the classification accuracy was slightly improved after the HoG feature was used, the overall performance of the model was still unsatisfactory, which indicates that Linear kernel has reached its performance limit, and we must find an alternative methodology to replace it.

accuracy: 0.868421052631579

accuracy: 0.875

accuracy: 0.8739035087719298



Here we introduced the 3 degree class polynomial kernel. As can be seen from the figure below, the classification accuracy of all categories has been significantly improved.

```
[]: # SVM with 3 degree polynomial kernel, using hog images as data.

confusion20 = train_model(svm.SVC(C=1, kernel='poly', degree=3,

cache_size=4000), data20_hog, labels20)

confusion50 = train_model(svm.SVC(C=1, kernel='poly', degree=3,

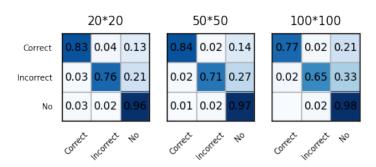
cache_size=4000), data50_hog, labels50)

confusion100 = train_model(svm.SVC(C=1, kernel='poly', degree=3,

cache_size=4000), data100_hog, labels100)

plot_confusion_matrix([confusion20, confusion50, confusion100])
```

accuracy: 0.8530701754385965 accuracy: 0.8464912280701754 accuracy: 0.8037280701754386



Different from the previous control groups, when we replaced gray graphics with Hog features, the classification accuracy did not significantly improve

```
[]: # SVM with rbf kernel, using gray images as data. Beta is set to 1 / n_features. confusion20 = train_model(svm.SVC(C=1, kernel='rbf', gamma='auto', ⊔ → cache_size=4000), data20_gray, labels20)
```

```
confusion50 = train_model(svm.SVC(C=1, kernel='rbf', gamma='auto', __

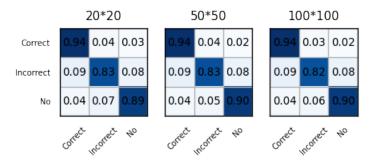
→cache_size=4000), data50_gray, labels50)

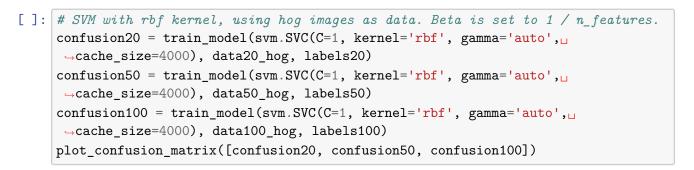
confusion100 = train_model(svm.SVC(C=1, kernel='rbf', gamma='auto', __

→cache_size=4000), data100_gray, labels100)

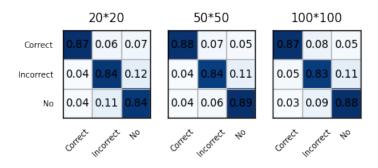
plot_confusion_matrix([confusion20, confusion50, confusion100])
```

accuracy: 0.8859649122807017 accuracy: 0.8914473684210527 accuracy: 0.8903508771929824





accuracy: 0.8530701754385965 accuracy: 0.8728070175438597 accuracy: 0.8607456140350878

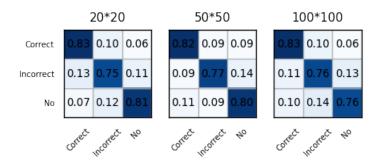


Finally, we test the effect of RBF kernel. Compared with linear kernel, both RBF kernel and POLY kernel can significantly improve the effect of the model. Meanwhile, when gray Scale image (50×50) was used as the input, we obtained the highest accuracy of the SVM model of 89.1%

In this experiment, we can see that the result of rbf kernel is better than polynomial, which is better than linear kernel. The hog method lead to worse results using each kernel function. The reason is that models need more information other than edge information to make right decision. The most interesting thing we can see is that, the highest resolution of image doesn't produce the best results. The reason may be that it is harder for SVM to split high dimension data space.

The next model we choose is decision tree. Decision Trees (DTs) are a non-parametric supervised learning method used for classification and regression. The goal is to create a model that predicts the value of a target variable by learning simple decision rules inferred from the data features. A tree can be seen as a piecewise constant approximation. In our setting, the maximum depth of the tree is nor specified, nodes are expanded until all leaves are pure or until all leaves contain less than 2 samples. And we compare the results of using gray, hog and canny dataset.

accuracy: 0.7993421052631579 accuracy: 0.793859649122807 accuracy: 0.7828947368421053



```
[]: # Decision Tree on hog image.

confusion20 = train_model(tree.DecisionTreeClassifier(), data20_hog, labels20)

confusion50 = train_model(tree.DecisionTreeClassifier(), data50_hog, labels50)

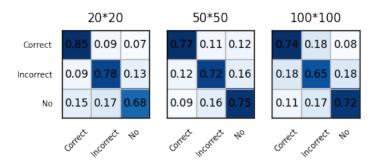
confusion100 = train_model(tree.DecisionTreeClassifier(), data100_hog, □

→labels100)

plot_confusion_matrix([confusion20, confusion50, confusion100])
```

accuracy: 0.7675438596491229 accuracy: 0.7467105263157895

accuracy: 0.7039473684210527



```
[]: # Decision Tree on canny image.

confusion20 = train_model(tree.DecisionTreeClassifier(), data20_edge, labels20)

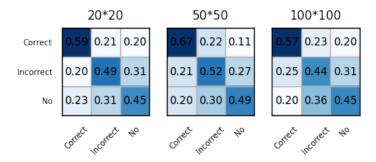
confusion50 = train_model(tree.DecisionTreeClassifier(), data50_edge, labels50)

confusion100 = train_model(tree.DecisionTreeClassifier(), data100_edge, u

→labels100)

plot_confusion_matrix([confusion20, confusion50, confusion100])
```

accuracy: 0.5098684210526315 accuracy: 0.5603070175438597 accuracy: 0.4857456140350877

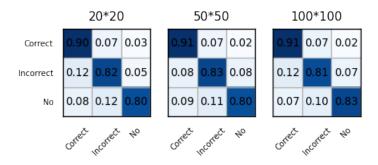


We can see that hog extractor has bad influence on the results, while canny extractor has very bad influence on the results. And the accuarcy of a single tree is worse than SVM with rbf kernel.

Then, we try the random forest algorithm. The Random forest is a special estimator that fits a certain number of single trees on various sub-samples of the dataset and uses averaging to improve the classification accuracy and control the situation of over-fitting. In our setting, The maximum depth of the tree is nor specified, nodes are expanded until all leaves are pure or until all leaves contain less than 2 samples. And we compare the results of 5, 10 and 50 subtrees on only gray dataset.

[]: # Random Forest using 5 subtrees on gray image. confusion20 = train_model(ensemble.RandomForestClassifier(n_estimators= 5),___ data20_gray, labels20) confusion50 = train_model(ensemble.RandomForestClassifier(n_estimators= 5),___ data50_gray, labels50) confusion100 = train_model(ensemble.RandomForestClassifier(n_estimators= 5),___ data100_gray, labels100) plot_confusion_matrix([confusion20, confusion50, confusion100])

accuracy: 0.8410087719298246 accuracy: 0.8475877192982456 accuracy: 0.8464912280701754



[]: # Random Forest using 10 subtrees on gray image.

confusion20 = train_model(ensemble.RandomForestClassifier(n_estimators= 10), □

data20_gray, labels20)

confusion50 = train_model(ensemble.RandomForestClassifier(n_estimators= 10), □

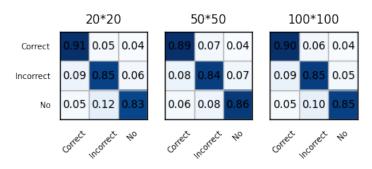
data50_gray, labels50)

confusion100 = train_model(ensemble.RandomForestClassifier(n_estimators= 10), □

data100_gray, labels100)

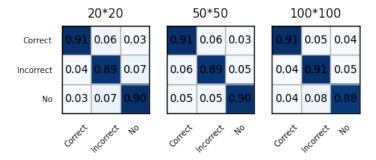
plot_confusion_matrix([confusion20, confusion50, confusion100])

accuracy: 0.8640350877192983 accuracy: 0.8662280701754386 accuracy: 0.868421052631579



[]: # Random Forest using 50 subtrees on gray image. confusion20 = train_model(ensemble.RandomForestClassifier(n_estimators= 50),___ data20_gray, labels20) confusion50 = train_model(ensemble.RandomForestClassifier(n_estimators= 50),__ data50_gray, labels50) confusion100 = train_model(ensemble.RandomForestClassifier(n_estimators= 50),__ data100_gray, labels100) plot_confusion_matrix([confusion20, confusion50, confusion100])

accuracy: 0.9002192982456141 accuracy: 0.8991228070175439 accuracy: 0.9013157894736842



Since the growth of each tree in the random forest has grow to the maximum extent and has a certain degree of randomness, the performance and robustness of the overall model are largely improved when we integrate them together. We can see that random forest has higher accuarcy than a single tree, and the more subtress we use, the higher accuarcy we can gain.

Finally, instead of using scikit learn package, we implement a linear model from scratch. Linear classifier is a very common and efficient classification algorithm in machine learning. In this project we will compare its results as a baseline with the other three classification algorithms. Its result can be illustrated as below:

• Linear Classification Result Summation (Baseline)

Parameter setting:

Study Rate: diminishing α , decay from 0.02 ($\alpha = 0.02$ /iteration)

<u>Optimization Method</u>: gradient decent Cost Function: Multiclass SoftMax

Problems & Solutions

1. When we choose a fixed learning rate, the cost of training will show significant fluctuations, indicating that our choice of learning rate is too large. However, when we choose a smaller learning rate, the model convergence speed will slow down, that will result in a low training efficiency.

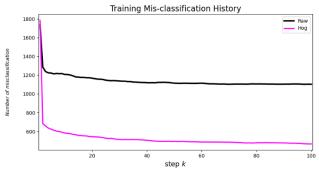
Solution: Using diminishing study rate

2. The appearance and shape of a face cannot be well represented by using the original image data, so the classification accuracy of the model trained by using the original image is low.

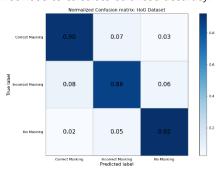
Solution: Using HoG algorithm to extract the image feature

Result

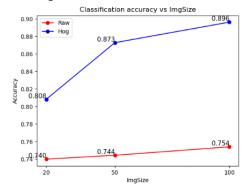
1. **Significant Improvement in Accuracy:** By using the image features extracted from the Hog algorithm as the model input, we improved the accuracy by at least 15 (about 800 less misclass samples) percentage points, which is quite remarkable. (*Input size 4500×100×100×3)



2. *Classification Accuracy of Different Categories:* Among the three categories, Incorrect masking has the lowest identification accuracy of only 86%, while No masking has the highest accuracy of 92%. As the data of the three types are almost equal in this project, we do not need to calculate balanced accuracy.



3. Sensitive to Change in Image Sharpness: As the input image size(sharpness) increases, the classification accuracy of the model increases. As can be seen from the following figure, compared with the Raw dataset, the Hog dataset is more sensitive to the improvement of image sharpness and its accuracy rate increases by nearly 10 percentage points, while the Raw control group has almost no change.



Appendix

> Random Forest.py

```
import sys
from matplotlib import pyplot as plt
from lib.nonlinear_superlearn_library.recursive_tree_lib.ClassificationTree import ClassificationStump
from lib import edge_extract
import autograd.numpy as np
import copy
sys.path.append('..')
class Tree:
   def init (self):
      self.split = None
      self.node = None
      self.left = None
      self.right = None
      self.left leaf = None
      self.right leaf = None
      self.number mis class left = 0
      self.number_mis_class_right = 0
      self.all miss = 0
class Random Forest Algorithm:
   def __init__(self, data_name, depth, train_portion, img_size):
      self.gray = []
      self.red = []
      self.blue = []
      self.green = []
      file path = "../Data/Pixel" + str(img size[0]) + "/"
      x, y = self.fetchData(file path, data name, img size)
      self.feature extraction(x, img size)
      self.x = self.hog extractor(np.array(self.gray).T)
      print("feature extraction finished")
      self.y = y
      self.depth = depth
      self.colors = ['salmon', 'cornflowerblue', 'lime', 'bisque', 'mediumaquamarine', 'b', 'm', 'g']
      self.plot colors = ['lime', 'violet', 'orange', 'lightcoral', 'chartreuse', 'aqua', 'deeppink']
```

```
self.make train val split(train portion)
   # build root regression stump
   self.tree = Tree()
   stump = ClassificationStump.Stump(self.x train, self.y train)
   # build remainder of tree
   self.build tree(stump, self.tree, depth)
   # compute train / valid errors
   self.compute_train_val_accuracies()
   self.best depth = np.argmax(self.valid accuracies)
@staticmethod
def fetchData(file path, data name, img size):
   y = []
   x = np.empty(shape=(0, img_size[0], img_size[1], 3))
   tag = 0
   number = 0
   for name in data name:
      data subset = np.load(file path + name)
      x = np.append(x, data subset, axis=0)
      y.extend(np.shape(data subset)[0] * [tag])
      number += np.shape(data_subset)[0]
      tag += 1
   return x, np.reshape(np.array(y), (1, number))
def feature extraction(self, data, img size):
   for i in range(np.shape(data)[0]):
      self.gray image(data[i, :], img size)
def gray_image(self, img, img_size):
   blue = []
   green = []
   red = []
   for i in range(img size[0]):
      for j in range(img size[1]):
         red.append(img[i][j][0])
         green.append(img[i][j][1])
         blue.append(img[i][j][2])
   gray = list(0.07 * np.array(blue) + 0.72 * np.array(green) + 0.21 * np.array(red))
   self.gray.append(gray)
   self.red.append(red)
```

```
self.blue.append(blue)
@staticmethod
{\tt def} hog_extractor(x):
   kernels = np.array([
      [[-1, -1, -1],
       [0, 0, 0],
       [1, 1, 1]],
       [[-1, -1, 0],
       [-1, 0, 1],
       [0, 1, 1]],
       [[-1, 0, 1],
       [-1, 0, 1],
       [-1, 0, 1]],
       [[0, 1, 1],
       [-1, 0, 1],
       [-1, -1, 0]],
       [[1, 0, -1],
       [1, 0, -1],
       [1, 0, -1]],
       [[0, -1, -1],
       [1, 0, -1],
       [1, 1, 0]],
       [[1, 1, 1],
       [0, 0, 0],
       [-1, -1, -1]],
       [[1, 1, 0],
       [1, 0, -1],
       [0, -1, -1]])
   extractor = edge_extract.tensor_conv_layer()
   x_transformed = extractor.conv_layer(x.T, kernels).T
   return x transformed
def make_train_val_split(self, train_portion):
   self.train portion = train portion
   r = np.random.permutation(self.x.shape[1])
   train num = int(np.round(train portion * len(r)))
   self.train_inds = r[:train_num]
   self.valid inds = r[train num:]
   self.x_train = self.x[:, self.train_inds]
   self.x_valid = self.x[:, self.valid_inds]
   self.y train = self.y[:, self.train inds]
   self.y_valid = self.y[:, self.valid_inds]
```

self.green.append(green)

```
def build subtree(self, stump):
      # get params from input stump
      best split = stump.split
      best dim = stump.dim
      left x = stump.left x
      right x = stump.right x
      left_y = stump.left_y
      right y = stump.right y
      left stump = stump
      right_stump = stump
      if np.size(np.unique(left y)) > 1:
         left stump = ClassificationStump.Stump(left x, left y)
      if np.size(np.unique(right y)) > 1:
          right_stump = ClassificationStump.Stump(right_x, right_y)
      return left_stump, right_stump
   def build tree(self, stump, node, depth):
      if depth > 1:
         node.split = stump.split
         node.dim = stump.dim
         node.left leaf = stump.left leaf
         node.right_leaf = stump.right_leaf
         node.step = stump.step
         left stump, right stump = self.build subtree(stump)
         node.left = Tree()
         node.right = Tree()
         depth -= 1
         return self.build_tree(left_stump, node.left, depth), self.build_tree(right_stump,
node.right, depth)
      else:
         node.split = stump.split
         node.dim = stump.dim
         node.left leaf = stump.left leaf
         node.right leaf = stump.right leaf
         node.step = stump.step
   def compute_train_val_accuracies(self):
      self.train accuracies = []
      self.valid accuracies = []
      for j in range(self.depth):
```

```
# compute training error
      train evals = np.array([self.predict(v[:, np.newaxis], depth=j) for v in self.x train.T]).T
      valid_evals = np.array([self.predict(v[:, np.newaxis], depth=j) for v in self.x_valid.T]).T
       # compute cost
      train miss = 0
      if self.y train.size > 0:
          train_miss = 1 - len(np.argwhere(train_evals != self.y_train)) / self.y_train.size
      valid miss = 0
      if self.y_valid.size > 0:
          valid miss = 1 - len(np.argwhere(valid evals != self.y valid)) / self.y valid.size
      self.train accuracies.append(train miss)
      self.valid_accuracies.append(valid_miss)
def predict(self, val, **kwargs):
   depth = self.depth
   if 'depth' in kwargs:
      depth = kwargs['depth']
   # search tree
   tree = copy.deepcopy(self.tree)
   d = 0
   while d < depth:</pre>
      split = tree.split
      dim = tree.dim
      if val[dim, :] <= split:</pre>
         tree = tree.left
      else:
         tree = tree.right
      d += 1
   # get final leaf value
   split = tree.split
   dim = tree.dim
   if val[dim, :] <= split:</pre>
      tree = tree.left leaf
   else:
      tree = tree.right_leaf
   # return evaluation
   return tree(val)
def evaluate tree(self, val, depth):
```

```
if depth > self.depth:
        return ('desired depth greater than depth of tree')
     tree = copy.deepcopy(self.tree)
     d = 0
     while d < depth:</pre>
        split = tree.split
        dim = tree.dim
        if val[dim, :] <= split:</pre>
           tree = tree.left
        else:
           tree = tree.right
        d += 1
     # get final leaf value
     split = tree.split
     dim = tree.dim
     if val[dim, :] <= split:</pre>
        tree = tree.left_leaf
     else:
        tree = tree.right leaf
     return tree(val)
  def draw fused model(self, runs):
     # get visual boundary
     xmin1 = np.min(self.x[0, :])
     xmax1 = np.max(self.x[0, :])
     xgap1 = (xmax1 - xmin1) * 0.05
     xmin1 -= xgap1
     xmax1 += xgap1
     xmin2 = np.min(self.x[1, :])
     xmax2 = np.max(self.x[1, :])
     xgap2 = (xmax2 - xmin2) * 0.05
     xmin2 -= xgap2
     xmax2 += xgap2
     ind0 = np.argwhere(self.y == +1)
     ind0 = [v[1]  for v  in ind0]
     linewidth=1, zorder=3)
     ind1 = np.argwhere(self.y == -1)
     ind1 = [v[1]  for v  in ind1]
     linewidth=1, zorder=3)
     plt.xlim([xmin1, xmax1])
     plt.ylim([xmin2, xmax2])
```

```
plt.title("Final Model of " + str(num trees) + " Bagged Models")
      plt.xlabel(r'$x 1$', fontsize=14)
      plt.ylabel(r'$x_2$', rotation=0, fontsize=14, labelpad=10)
      s1 = np.linspace(xmin1, xmax1, 50)
      s2 = np.linspace(xmin2, xmax2, 50)
      a, b = np.meshgrid(s1, s2)
      a = np.reshape(a, (np.size(a), 1))
      b = np.reshape(b, (np.size(b), 1))
      h = np.concatenate((a, b), axis=1)
      a.shape = (np.size(s1), np.size(s2))
      b.shape = (np.size(s1), np.size(s2))
      t_ave = []
      for k in range(len(runs)):
         tree = runs[k]
         depth = tree.best depth
         t = []
         for val in h:
             val = val[:, np.newaxis]
             out = tree.evaluate tree(val, depth)
             t.append(out)
         t = np.array(t)
         t.shape = (np.size(s1), np.size(s2))
         col = np.random.rand(1, 3)
         plt.contour(s1, s2, t, linewidths=2.5, levels=[0], colors=self.plot colors[k], zorder=2,
alpha=0.4)
         t ave.append(t)
      t ave = np.array(t ave)
      t_ave1 = np.median(t_ave, axis=0)
      plt.contour(s1, s2, t ave1, linewidths=3.5, levels=[0], colors='k', zorder=4, alpha=1)
      plt.show()
def plot(y, label):
   x = range(1, len(y[1]) + 1)
   colors = ['dimgray', 'coral', 'aquamarine', 'crimson', 'blueviolet', 'chartreuse']
   plt.title(label)
   for i in range(len(y)):
      plt.plot(x, y[i], marker='o', color=colors[i])
   plt.xticks(x, rotation=0)
   plt.xlabel("Depth of Decision Tree")
   plt.ylabel("Accuracy")
   plt.show()
```

```
if __name__ == "__main__":
   # xx = np.load('testdata.npy')
   data_name = ['Correct.npy', 'Incorrect.npy', 'NoMask.npy', ]
   trees = []
   train_acc = []
   valid acc = []
   num trees = 5
   depth = 7
   train portion = 0.67
   for i in range(num_trees):
      print("training fold: " + str(i))
      tree = Random_Forest_Algorithm(data_name, depth, train_portion=train_portion, img_size=[20, 20])
      trees.append(tree)
      train_acc.append(tree.train_accuracies)
      valid acc.append(tree.valid accuracies)
   # Compare the acc of training set and validation set
   plot(train_acc, label='Training set accuracy')
   plot(valid_acc, label='Validation set accuracy')
   # Draw 5+1 models all in one
   tree = Random Forest Algorithm(data name, depth, train portion=1, img size=[20, 20])
   tree.draw fused model(runs=trees)
```

> ClassificationStump.py

```
from autograd import numpy as np
import copy

left_his = []
right_his = []

# class for building regression stump

class Stump:
    def __init__(self, x, y):
        # globals
        self.x = x
        self.y = y
        # find best stump given input data
        self.make stump()
```

```
def counter(self, step, x, y):
   # compute predictions
   y_hat = step(x)[np.newaxis, :]
   # compute total counts
   vals, counts = np.unique(y, return_counts=True)
   # compute misclass on each class, compute balanced accuracy
   balanced = 0
   for i in range(len(vals)):
      v = vals[i]
      c = counts[i]
      ind = np.argwhere(y == v)
      miss val = 1
      if ind.size > 0:
         ind = [a[1] for a in ind]
         miss = np.argwhere(y_hat[:, ind] != y[:, ind])
         if miss.size > 0:
             miss = len([a[1] for a in miss])
             miss val = (1 - miss / c)
      balanced += miss val
   balanced = balanced / len(vals)
   return balanced
### create prototype steps ###
def make_stump(self):
   \# important constants: dimension of input N and total number of points P
   N = np.shape(self.x)[0]
   P = np.size(self.y)
   # begin outer loop - loop over each dimension of the input - create split points and dimensions
   acc_matrix_right = [0] * N
   acc matrix left = [0] * N
   best_split = np.inf
   best dim = np.inf
   best val = -np.inf
   best left leaf = []
   best right leaf = []
   best_left_ave = []
   best right ave = []
   best_step = []
   c_vals, c_counts = np.unique(self.y, return_counts=True)
   self.c counts = c counts
```

```
for n in range(N):
   \# make a copy of the n^th dimension of the input data (we will sort after this)
   x_n = copy.deepcopy(self.x[n, :])
   y n = copy.deepcopy(self.y)
   \# sort x_n and y_n according to ascending order in x_n
   sorted inds = np.argsort(x n, axis=0)
   # 将元素从小到大排列,提取对应得 index
   x n = x n[sorted inds]
   y_n = y_n[:, sorted_inds]
   # loop over points and create stump in between each
   # in dimension n
   for p in range(P - 1):
      if y_n[:, p] != y_n[:, p + 1] and x_n[p] != x_n[p + 1]:
         # compute split point
         split = (x n[p] + x n[p + 1]) / float(2)
         \#\# determine most common label relative to proportion of each class present \#\#
          # compute various counts and decide on levels
         y n left = y n[:, :p + 1]
         y n right = y n[:, p + 1:]
         c left vals, c left counts = np.unique(y n left, return counts=True)
         c_right_vals, c_right_counts = np.unique(y_n_right, return_counts=True)
         prop_left = []
         prop right = []
         for i in range(np.size(c vals)):
            val = c_vals[i]
             count = c counts[i]
             val ind = np.argwhere(c left vals == val)
             val count = 0
             if np.size(val ind) > 0:
                val_count = c_left_counts[val_ind][0][0]
             prop left.append(val count / count)
             # check right side
             val ind = np.argwhere(c right vals == val)
             val_count = 0
             if np.size(val ind) > 0:
                val_count = c_right_counts[val_ind][0][0]
             prop right.append(val count / count)
          # array it
```

```
best left = np.argmax(prop left)
                 left_ave = c_vals[best_left]
                 best acc left = prop left[best left]
                 # left = y n left.size / y n.size
                 prop right = np.array(prop right)
                 best_right = np.argmax(prop_right)
                 right ave = c vals[best right]
                 best_acc_right = prop_right[best_right]
                  # right = y n right.size / y n.size
                 val = (best_acc_left + best_acc_right) / 2
                  # define leaves
                 \texttt{left leaf = lambda} \ \texttt{x, left ave=left ave, dim=n: np.array([left ave \ \textbf{for} \ \texttt{v} \ \textbf{in} \ \texttt{x}[\texttt{dim}, :]])}
                 right leaf = lambda x, right ave=right ave, dim=n: np.array([right ave for v in
x[dim, :]])
                  # create stump
                 step = lambda x, split=split, left ave=left ave, right ave=right ave, dim=n: np.array(
                     [(left ave if v <= split else right ave) for v in x[dim, :]])</pre>
                  # compute cost value on step
                  # val = self.counter(step,self.x,self.y)
                 if val > best val:
                     acc matrix right = prop right
                     acc_matrix_left = prop_left
                     best left leaf = copy.deepcopy(left leaf)
                     best right leaf = copy.deepcopy(right leaf)
                     best_dim = copy.deepcopy(n)
                     best_split = copy.deepcopy(split)
                     best_val = copy.deepcopy(val)
                     best left ave = copy.deepcopy(left ave)
                     best right ave = copy.deepcopy(right ave)
                     best step = copy.deepcopy(step)
       # define globals
       self.step = best step
       self.left_leaf = best_left_leaf
       self.right leaf = best right leaf
       self.dim = best dim
       self.split = best split
```

prop_left = np.array(prop_left)

```
\# sort x n and y n according to ascending order in x n
       sorted inds = np.argsort(self.x[best_dim, :], axis=0)
       self.x = self.x[:, sorted inds]
       self.y = self.y[:, sorted inds]
       # cull out points on each leaf
       left inds = np.argwhere(self.x[best dim, :] <= best split).flatten()</pre>
       right inds = np.argwhere(self.x[best dim, :] > best split).flatten()
       self.left x = self.x[:, left inds]
       self.right x = self.x[:, right inds]
       self.left y = self.y[:, left inds]
       self.right y = self.y[:, right inds]
       self.number mis class left = self.caculate mis class(acc matrix right, acc matrix left)[0]
       self.number mis class right = self.caculate mis class(acc matrix right, acc matrix left)[1]
       right_his.append(self.number_mis_class_right)
       left_his.append(self.number_mis_class_left)
   def caculate mis class(self, prop right, prop left):
      leaf label ind left = np.argmax(prop left)
      left label count = self.c counts[leaf label ind left]
      leaf_label_ind_right = np.argmax(prop_right)
       right_label_count = self.c_counts[leaf_label_ind_right]
      mis class left = self.left x.shape[1] - round(left label count * prop left[leaf label ind left])
      mis class right = self.right x.shape[1] - round(right label count *
prop right[leaf label ind right])
       return mis class left, mis class right
```

Conventional_ML_Method.py

```
import sys
from lib.math_optimization_library import static_plotter
import autograd.numpy as np
from autograd.misc.flatten import flatten_func
from autograd import grad as gradient
from lib import edge_extract
from sklearn.metrics import confusion_matrix
import matplotlib.pyplot as plt
```

```
\verb"sys.path.append" ("..")
plotter = static_plotter.Visualizer()
def linear model(x, w):
   a = w[0] + np.dot(x.T, w[1:])
   return a.T
def multiclass softmax(w, x, y, iter):
   x_p = x[:, iter]
   y_p = y[:, iter]
   all_evals = linear_model(x_p, w)
   a = np.log(np.sum(np.exp(all evals), axis=0))
   b = all evals[y p.astype(int).flatten(), np.arange(np.size(y p))]
   cost = np.sum(a - b)
   return cost / float(np.size(y_p))
class FaceMask Classification(object):
   def __init__(self, data_name, img_size):
      self.gray = []
      self.red = []
      self.blue = []
      self.green = []
      self.mismatching his = []
      file path = ".../Data/Pixel" + str(img size[0]) + "/"
      x, y = self.fetchData(file path,data name, img size)
      self.feature extraction(x, img size)
      self.y = y
      self.x = np.array(self.gray).T
      self.shuffle data(n sample=4500, x=self.x, y=self.y)
      self.standard_normalizer(self.x_rand.T)
      self.x rand = self.normalizer(self.x rand.T).T
      self.x_edge = self.hog_extractor(self.x_rand)
       self.cost function = multiclass softmax
   @staticmethod
   def fetchData(file_path, data_name, img_size):
      y = []
      x = np.empty(shape=(0, img size[0], img size[1], 3))
      tag = 0
```

```
number = 0
   for name in data name:
      data_subset = np.load(file_path+name)
      x = np.append(x, data subset, axis=0)
      y.extend(np.shape(data subset)[0] * [tag])
      number += np.shape(data subset)[0]
      tag += 1
   return x, np.reshape(np.array(y), (1, number))
def feature extraction(self, data, img size):
   for i in range(np.shape(data)[0]):
      self.gray_image(data[i, :], img_size)
def gray_image(self, img, img_size):
   blue = []
   green = []
   red = []
   for i in range(img_size[0]):
      for j in range(img_size[1]):
          red.append(img[i][j][0])
          green.append(img[i][j][1])
          blue.append(img[i][j][2])
   gray = list(0.07 * np.array(blue) + 0.72 * np.array(green) + 0.21 * np.array(red))
   self.gray.append(gray)
   self.red.append(red)
   self.green.append(green)
   self.blue.append(blue)
def shuffle_data(self, n_sample, x, y):
   inds = np.random.permutation(y.shape[1])[:n sample]
   self.x rand = np.array(x)[:, inds]
   self.y_rand = y[:, inds]
def standard_normalizer(self, x):
   x_ave = np.nanmean(x, axis=1)[:, np.newaxis]
   x_std = np.nanstd(x, axis=1)[:, np.newaxis]
   self.normalizer = lambda data: (data - x ave) / x std
@staticmethod
def hog extractor(x):
   kernels = np.array([
      [[-1, -1, -1],
       [0, 0, 0],
       [1, 1, 1]],
```

```
[[-1, -1, 0],
       [-1, 0, 1],
       [0, 1, 1]],
       [[-1, 0, 1],
       [-1, 0, 1],
       [-1, 0, 1]],
      [[0, 1, 1],
       [-1, 0, 1],
       [-1, -1, 0]],
      [[1, 0, -1],
       [1, 0, -1],
       [1, 0, -1]],
      [[0, -1, -1],
       [1, 0, -1],
       [1, 1, 0]],
      [[1, 1, 1],
       [0, 0, 0],
       [-1, -1, -1]],
      [[1, 1, 0],
       [1, 0, -1],
       [0, -1, -1]])
   extractor = edge extract.tensor conv layer()
   x_transformed = extractor.conv_layer(x.T, kernels).T
   return x transformed
def gradient_descent(self, loss_fun, w, x_train, y_train, alpha, max_its, batch_size):
   g flat, unflatten, w = flatten func(loss fun, w)
   grad = gradient(g_flat)
   num_train = y_train.size
   w hist = [unflatten(w)]
   train_hist = [g_flat(w, x_train, y_train, np.arange(num_train))]
   num_batches = int(np.ceil(np.divide(num_train, batch_size)))
   for k in range(max its):
      for b in range(num_batches):
          batch_inds = np.arange(b * batch_size, min((b + 1) * batch_size, num_train))
          grad_eval = grad(w, x_train, y_train, batch_inds)
          grad eval.shape = np.shape(w)
          w = w - (alpha / (k + 1)) * grad eval
      train_cost = g_flat(w, x_train, y_train, np.arange(num_train))
      w hist.append(unflatten(w))
      train_hist.append(train_cost)
   return w hist, train hist
def misclass counting(self, x, y, weight his):
```

```
mis_his = []
      for w in weight his:
         all_evals = linear_model(x, w)
         y predict = (np.argmax(all evals, axis=0))[np.newaxis, :]
         count = np.shape(np.argwhere(y != y predict))[0]
         mis his.append(count)
      return mis his
   # Plotting
   def confusion_matrix(self, mis_history, x, y, weight_his, labels, normalize=False, title='Confusion
Matrix',
                     precision="%0.f"):
      ind = np.argmin(mis history)
      w p = weight his[ind]
      tick marks = np.array(range(len(labels))) + 0.5
      all evals = linear model(x, w p)
      y predict = np.argmax(all evals, axis=0)
      count = np.shape(np.argwhere(y != y_predict))[0]
      acc = 1 - (count / np.shape(all evals)[1])
      print("the prediction accuracy is:" + str(acc))
      cm = confusion matrix(y[0], y predict)
      if normalize:
         cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
         title = "Normalized " + title
         precision = "%0.2f"
      plt.figure(figsize=(12, 8), dpi=120)
      ind array = np.arange(len(labels))
      x, y = np.meshgrid(ind_array, ind_array)
      for x val, y val in zip(x.flatten(), y.flatten()):
         c = cm[y val][x val]
         if c > 0.0:
             plt.text(x_val, y_val, precision % (c,), color='k', fontsize=17, va='center',
ha='center')
      plt.gca().set_xticks(tick_marks, minor=True)
      plt.gca().set yticks(tick marks, minor=True)
      plt.gca().xaxis.set ticks position('none')
      plt.gca().yaxis.set ticks position('none')
      plt.grid(True, which='minor', linestyle='-')
      plt.gcf().subplots_adjust(bottom=0.15)
      plt.imshow(cm, interpolation='nearest', cmap='Blues')
      font = {'size': 13}
      plt.title(title, font)
      plt.colorbar()
      xlocations = np.array(range(len(labels)))
```

```
plt.xticks(xlocations, labels, rotation=0)
      plt.yticks(xlocations, labels)
      plt.ylabel('True label', font)
      plt.xlabel('Predicted label', font)
      plt.show()
   @staticmethod
   def weight_normalizer(w):
      w \text{ norm} = sum([v ** 2 for v in w[1:]]) ** 0.5
      return [v / w_norm for v in w]
if name == " main ":
   data_name = ['Correct.npy', 'Incorrect.npy', 'NoMask.npy', ]
   FaceMask = FaceMask_Classification(data_name, img_size=[20, 20])
   N = FaceMask.x rand.shape[0]
   C = len(np.unique(FaceMask.y rand))
   w = 0.1 * np.random.randn(N + 1, C)
   weight_his, cost_his = FaceMask.gradient_descent(FaceMask.cost_function, w, FaceMask.x_rand,
FaceMask.y rand, alpha=0.02,
                                         max its=100, batch size=300)
   N = FaceMask.x edge.shape[0]
   w = 0.1 * np.random.randn(N + 1, C)
   weight edge his, cost edge his = FaceMask.gradient descent(FaceMask.cost function, w,
FaceMask.x edge, FaceMask.y rand,
                                                  alpha=0.02,
                                                  max its=100, batch size=300)
   mis1 = FaceMask.misclass counting(FaceMask.x rand, FaceMask.y rand, weight his)
   FaceMask.confusion matrix(mis1, FaceMask.x rand, FaceMask.y rand, weight his,
                      labels=["Correct Masking", "Incorrect Masking", "No Masking"],
                      normalize=True,
                      title="Confusion matrix: Raw Dataset")
   mis2 = FaceMask.misclass_counting(FaceMask.x_edge, FaceMask.y_rand, weight_edge_his)
   FaceMask.confusion_matrix(mis2, FaceMask.x_edge, FaceMask.y_rand, weight_edge_his,
                      labels=["Correct Masking", "Incorrect Masking", "No Masking"],
                      normalize=True,
                      title="Confusion matrix: HoG Dataset")
   plotter.plot mismatching histories(histories=[mis1, mis2], start=1,
                                labels=['Raw', 'Hog'],
                                title="Training Mis-classification History")
   plotter.plot cost histories(histories=[cost his, cost edge his], start=0,
```

```
labels=['Raw', 'Hog'],
title="Training Cost History")
```

> Static plotter.py

```
import autograd.numpy as np
import matplotlib.pyplot as plt
 def confusion_matrix(cm_collection, labels, precision="%0.f", normalize=True):
     tick marks = np.array(range(len(labels))) + 0.5
     title = ["Image Size = 20", "Image Size = 50", "Image Size = 100"]
     plt.figure(figsize=(16, 8), dpi=120)
     for i in range(len(cm_collection)):
        cm = cm_collection[i]
        plt.subplot(1, len(cm collection), i + 1)
        if normalize:
           cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
           title[i] = "Normalized " + title[i]
           precision = "%0.2f"
        ind_array = np.arange(len(labels))
        x, y = np.meshgrid(ind array, ind array)
        for x val, y val in zip(x.flatten(), y.flatten()):
           c = cm[y_val][x_val]
           if c > 0.0:
               {\tt plt.text(x\_val, y\_val, precision % (c,), color='k', fontsize=11, va='center', ha='center')}
        plt.gca().set xticks(tick marks, minor=True)
        plt.gca().set_yticks(tick_marks, minor=True)
        plt.gca().xaxis.set_ticks_position('none')
        plt.gca().yaxis.set_ticks_position('none')
        plt.grid(True, which='minor', linestyle='-')
        plt.gcf().subplots adjust(bottom=0.15)
        plt.imshow(cm, interpolation='nearest', cmap='Blues')
        font = {'size': 9}
        plt.title(title[i], font)
        xlocations = np.array(range(len(labels)))
        plt.xticks(xlocations, labels, rotation=45)
        if i == 0:
           plt.yticks(xlocations, labels)
        else:
           plt.yticks([])
     @staticmethod
def plot mismatching histories(histories=list, start=int, title='', **kwargs):
    # plotting colors
```

```
colors = ['k', 'magenta', 'aqua', 'blueviolet', 'chocolate']
   # initialize figure
   fig = plt.figure(figsize=(10, 5))
   # create subplot with 1 panel
   gs = gridspec.GridSpec(1, 1)
   ax = plt.subplot(gs[0])
   # any labels to add?
   labels = [' ', ' ', ' ']
   if 'labels' in kwargs:
      labels = kwargs['labels']
   # plot points on cost function plot too?
   points = False
   if 'points' in kwargs:
      points = kwargs['points']
   # run through input histories, plotting each beginning at 'start' iteration
   for c in range(len(histories)):
      history = histories[c]
      label = 0
      if c == 0:
         label = labels[0]
      elif c == 1:
         label = labels[1]
      else:
         label = labels[2]
      # check if a label exists, if so add it to the plot
      if np.size(label) == 0:
         ax.plot(np.arange(start, len(history), 1), history[start:], linewidth=3 * 0.8 ** c,
color=colors[c])
      else:
         ax.plot(np.arange(start, len(history), 1), history[start:], linewidth=3 * 0.8 ** c,
color=colors[c],
                label=label)
          # check if points should be plotted for visualization purposes
      if points:
         ax.scatter(np.arange(start, len(history), 1), history[start:], s=90, color=colors[c],
edgecolor='w',
                  linewidth=2, zorder=3)
```

```
# clean up panel
   xlabel = 'step $k$'
   if 'xlabel' in kwargs:
      xlabel = kwargs['xlabel']
   ylabel = '$Number\ of\ misclassification$'
   if 'ylabel' in kwargs:
      ylabel = kwargs['ylabel']
   ax.set xlabel(xlabel, fontsize=14)
   ax.set_ylabel(ylabel, fontsize=10, rotation=90, labelpad=25)
   if np.size(label) > 0:
      anchor = (1, 1)
      if 'anchor' in kwargs:
         anchor = kwargs['anchor']
      plt.legend(loc='upper right', bbox to anchor=anchor)
      # leg = ax.legend(loc='upper left', bbox to anchor=(1.02, 1), borderaxespad=0)
   ax.set_xlim([start - 0.5, len(history) - 0.5])
   plt.title(title, fontsize=16)
   plt.show()
@staticmethod
def plot_cost_histories(histories=list, start=int, title='', **kwargs):
   # plotting colors
   colors = ['k', 'magenta', 'aqua', 'blueviolet', 'chocolate']
   # initialize figure
   fig = plt.figure(figsize=(10, 5))
   # create subplot with 1 panel
   gs = gridspec.GridSpec(1, 1)
   ax = plt.subplot(gs[0])
   # any labels to add?
   labels = [' ', ' ', ' ']
   if 'labels' in kwargs:
      labels = kwargs['labels']
   # plot points on cost function plot too?
   points = False
   if 'points' in kwargs:
      points = kwargs['points']
```

```
# run through input histories, plotting each beginning at 'start' iteration
   for c in range(len(histories)):
      history = histories[c]
      label = 0
      if c == 0:
         label = labels[0]
      elif c == 1:
         label = labels[1]
      else:
          label = labels[2]
      # check if a label exists, if so add it to the plot
      if np.size(label) == 0:
          ax.plot(np.arange(start, len(history), 1), history[start:], linewidth=3 * 0.8 ** c,
color=colors[c])
      else:
          ax.plot(np.arange(start, len(history), 1), history[start:], linewidth=3 * 0.8 ** c,
color=colors[c],
                label=label)
          # check if points should be plotted for visualization purposes
      if points:
          ax.scatter(np.arange(start, len(history), 1), history[start:], s=90, color=colors[c],
edgecolor='w',
                   linewidth=2, zorder=3)
          # clean up panel
   xlabel = 'step $k$'
   if 'xlabel' in kwargs:
      xlabel = kwargs['xlabel']
   ylabel = r'$g\left(\mathbf{w}^k\right)$'
   if 'ylabel' in kwargs:
      ylabel = kwargs['ylabel']
   ax.set xlabel(xlabel, fontsize=14)
   ax.set ylabel(ylabel, fontsize=14, rotation=0, labelpad=25)
   if np.size(label) > 0:
      anchor = (1, 1)
      if 'anchor' in kwargs:
         anchor = kwargs['anchor']
      plt.legend(loc='upper right', bbox_to_anchor=anchor)
      # leg = ax.legend(loc='upper left', bbox to anchor=(1.02, 1), borderaxespad=0)
   ax.set xlim([start - 0.5, len(history) - 0.5])
```

```
plt.title(title, fontsize=16)
plt.show()
```

➢ lib fun.py

```
import numpy as np
import matplotlib.pyplot as plt
import cv2
import sklearn.svm as svm
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import StandardScaler
from sklearn.model_selection import train_test_split
from sklearn import metrics
from skimage import feature
import os
def RGBtoGray(data):
   new data = np.zeros((1, data.shape[1], data.shape[2]))
   for im in data:
      new data = np.append(new data,
cv2.cvtColor(im.astype('float32'),cv2.COLOR_RGB2GRAY).reshape(1,data.shape[1], data.shape[2]), axis=0)
   return new data[1:,:,:]
def RGBtoHOG(data):
   new data = np.zeros((1, data.shape[1], data.shape[2]))
   for im in data:
      fd, hog image = feature.hog(im, orientations=8, pixels per cell=(2, 2),
                cells_per_block=(1, 1), visualize=True, multichannel=True)
      new data = np.append(new data, hog image.reshape((1, data.shape[1], data.shape[2])), axis=0)
   return new_data[1:,:,:]
def GRAYtoEDGE(data, sigma):
   new_data = np.zeros((1, data.shape[1], data.shape[2]))
   for im in data:
      edges = feature.canny(im, sigma=sigma)
      new data = np.append(new data, edges.reshape((1, data.shape[1], data.shape[2])), axis=0)
   return new_data[1:,:,:]
def Flatten(images):
   images = images.reshape(images.shape[0], -1)
```

```
def load(data path):
   for i, set in enumerate(['Correct', 'Incorrect', 'NoMask']):
      if i == 0.
          data = np.load(data path+set+'.npy')
          labels = np.array([i]*len(data))
         i += 1
      else:
          data = np.load(data path+set+'.npy')
          data = np.append(data,data , axis=0)
          labels = np.append(labels, np.array([i]*len(data_)), axis=0)
   print('X shape: {}'.format(data.shape, np.array(labels).shape))
   return data, labels
def VisualizeRGB(data20, data50, data100):
   f, axes = plt.subplots(1,9, figsize=(18,2))
   axes[0].imshow(data20[0,:,:,:].astype('uint8'))
   axes[1].imshow(data20[2000,:,:,:].astype('uint8'))
   axes[2].imshow(data20[-1,:,:,:].astype('uint8'))
   axes[3].imshow(data50[0,:,:,:].astype('uint8'))
   axes[4].imshow(data50[2000,:,:,:].astype('uint8'))
   axes[5].imshow(data50[-1,:,:,:].astype('uint8'))
   axes[6].imshow(data100[0,:,:,:].astype('uint8'))
   axes[7].imshow(data100[2000,:,:,:].astype('uint8'))
   axes[8].imshow(data100[-1,:,:,:].astype('uint8'))
   for ax in axes:
      ax.set xticks([])
      ax.set yticks([])
def VisualizeGray(data20, data50, data100):
   f, axes = plt.subplots(1,9, figsize=(18,2))
   axes[0].imshow(data20[0,:,:].astype('uint8'),cmap ='gray')
   axes[1].imshow(data20[2000,:,:].astype('uint8'),cmap ='gray')
   axes[2].imshow(data20[-1,:,:].astype('uint8'),cmap ='gray')
   axes[3].imshow(data50[0,:,:].astype('uint8'),cmap ='gray')
   axes[4].imshow(data50[2000,:,:].astype('uint8'),cmap ='gray')
   axes[5].imshow(data50[-1,:,:].astype('uint8'),cmap ='gray')
   axes[6].imshow(data100[0,:,:].astype('uint8'),cmap ='gray')
   axes[7].imshow(data100[2000,:,:].astype('uint8'),cmap ='gray')
   axes[8].imshow(data100[-1,:,:].astype('uint8'),cmap ='gray')
   for ax in axes:
      ax.set xticks([])
```

return images

ax.set yticks([])

```
def plot_confusion_matrix(cm_collection, labels=["Correct", "Incorrect", "No"], precision="%0.f",
normalize=True):
   tick marks = np.array(range(len(labels))) + 0.5
   title = ["20*20", "50*50", "100*100"]
   plt.figure(figsize=(4, 2), dpi=120)
   for i in range(len(cm collection)):
      cm = cm collection[i]
      plt.subplot(1, len(cm_collection), i + 1)
       if normalize:
          cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
          title[i] = title[i]
          precision = "%0.2f"
       ind array = np.arange(len(labels))
       x, y = np.meshgrid(ind array, ind array)
       for x_val, y_val in zip(x.flatten(), y.flatten()):
         c = cm[y_val][x_val]
          if c > 0.0:
             {\tt plt.text(x\_val, y\_val, precision \% (c,), color='k', fontsize=8, va='center', ha='center')}
      plt.gca().set xticks(tick marks, minor=True)
      plt.gca().set yticks(tick marks, minor=True)
      plt.gca().xaxis.set ticks position('none')
      plt.gca().yaxis.set_ticks_position('none')
      plt.grid(True, which='minor', linestyle='-')
      plt.gcf().subplots_adjust(bottom=0.15)
      plt.imshow(cm, interpolation='nearest', cmap='Blues')
      font = {'size': 9}
      plt.title(title[i], font)
      xlocations = np.array(range(len(labels)))
      plt.xticks(xlocations, labels, rotation=45, fontsize=6)
      if i == 0:
          plt.yticks(xlocations, labels, fontsize=6)
       else:
         plt.yticks([])
   plt.show()
```