

# HWRS 505: Vadose Zone Hydrology

Lecture 12

9/28/2023

Today: 1D steady-state flow with excel spreadsheet model

# Review of Lecture 11

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1. Steady-state unsaturated flow in 1D:
  - The key idea of numerical solution: Divide the domain into many boxes or layers and convert the **differential equation** to a system of nonlinear **algebraic equations**.
  - Boundary conditions.
2. Solving nonlinear systems of equations: Newton-Raphson method
  - Fundamental idea
    - ✓ Linearize the nonlinear equation using truncated Taylor series
    - ✓ Use iterations to converge to the solution
3. Steady-state spreadsheet model
  - Using the tool to build intuition on unsaturated flow

# 1D Steady-state Flow: Excel Spreadsheet Model

## 1. Vertical column p top

- Set  $p_{\text{top}} = 50$  cm, and change  $p_{\text{base}}$  from 100 cm to -100 cm with an interval of 20 cm. Record the flux for each change and plot the flux as a function of the base pressure. Try to make sense of the flux-base pressure plot.
- Set  $p_{\text{top}} = 200$  cm, repeat the above but change  $p_{\text{base}}$  from 200 cm to -100 cm. Compare the flux vs. base pressure plot with the plot made from above.

## 3. Horizontal column p right

Set  $p_{\text{right}} = -50$  cm, and change  $p_{\text{left}}$  to -50, -25, 0, 25 cm. Try to make sense of the plots for the heads and volumetric content for each  $p_{\text{left}}$  value. How do they change with the  $p_{\text{left}}$  value?

## 2. Vertical column q top

Set  $q_{\text{top}} = 100$  cm/day, and change  $p_{\text{base}}$  to 40, 20, 0, -20 cm. Try to make sense of the plots for the heads and volumetric content for each base  $p$  value. How do they change with the base  $p$  value?

## 4. Horizontal column q right

Set  $q_{\text{right}} = 1\text{E-}6$  cm/s, and change  $p_{\text{left}}$  to 1, -1, -2, -10 cm. Try to make sense of the plots for the heads and volumetric content for each  $p_{\text{left}}$  value. How do they change with the  $p_{\text{left}}$  value?

**Note:** Copy the plots to a PowerPoint file so that you can save the results to do comparisons and analyses.

Q: For #3 and #4, can the domain be unsaturated if  $p$  at the boundaries are non-negative?