

# HWRS 505: Vadose Zone Hydrology

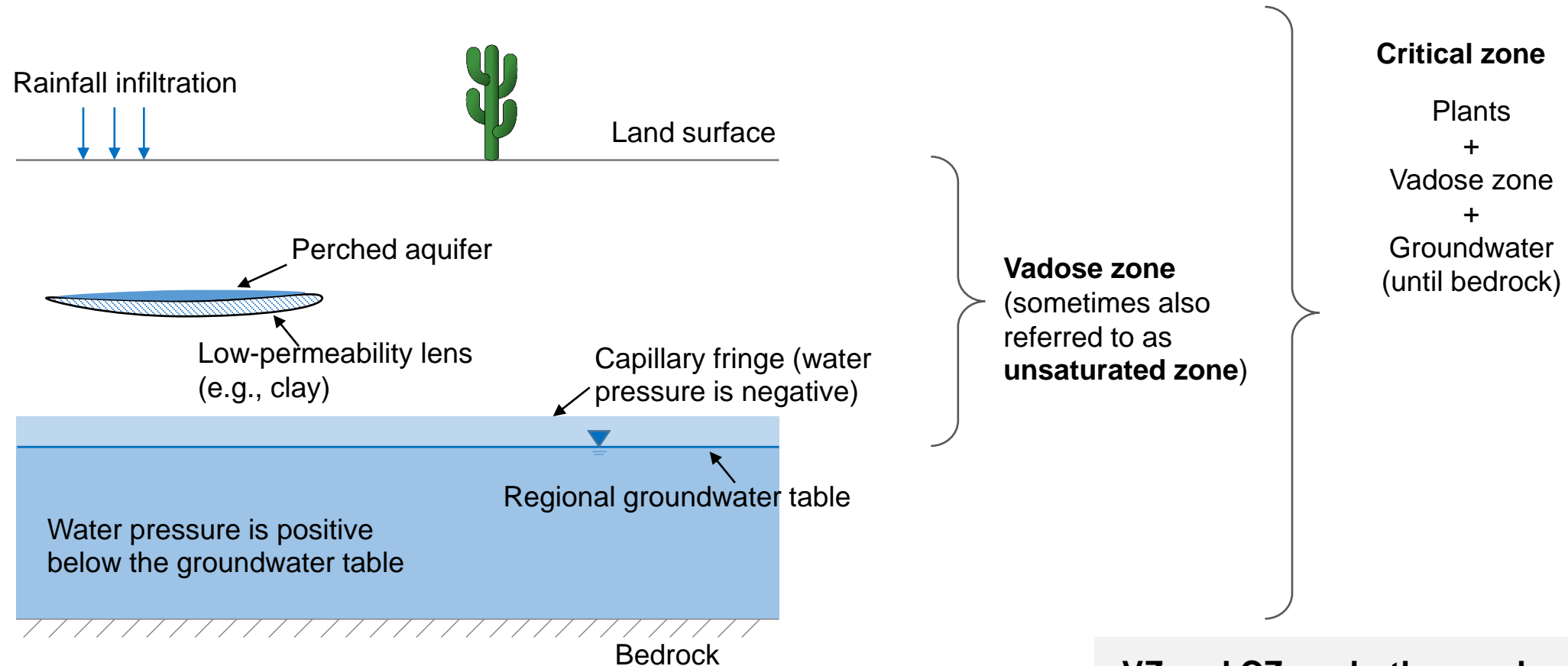
Lecture 1

8/22/2023

Today:

1. Overview of the course
2. Review: Steady-state saturated flow

# Vadose Zone: Conceptual picture



## VZ and CZ are both complex systems:

- Fluid flow processes
- Geomechanical processes
- Geochemical processes
- Microbial processes

...

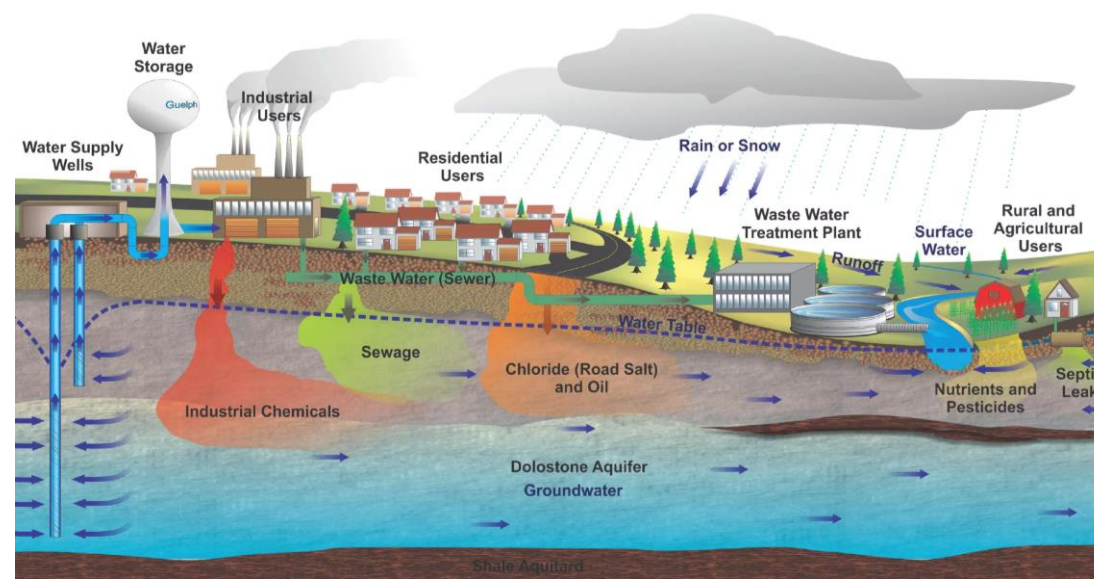
# Vadose Zone: Context and who cares?

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## Agriculture and food production



## Drinking water safety



## Other examples?

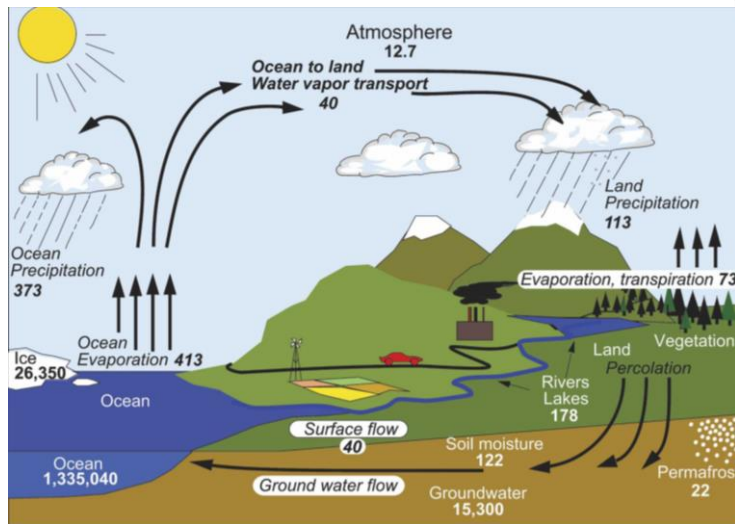
- Natural hazards management (flooding, landslide, and erosion)
- Infrastructure development (buildings, roads, bridges, ...)
- ...

Vadose zone processes can have profound societal impacts

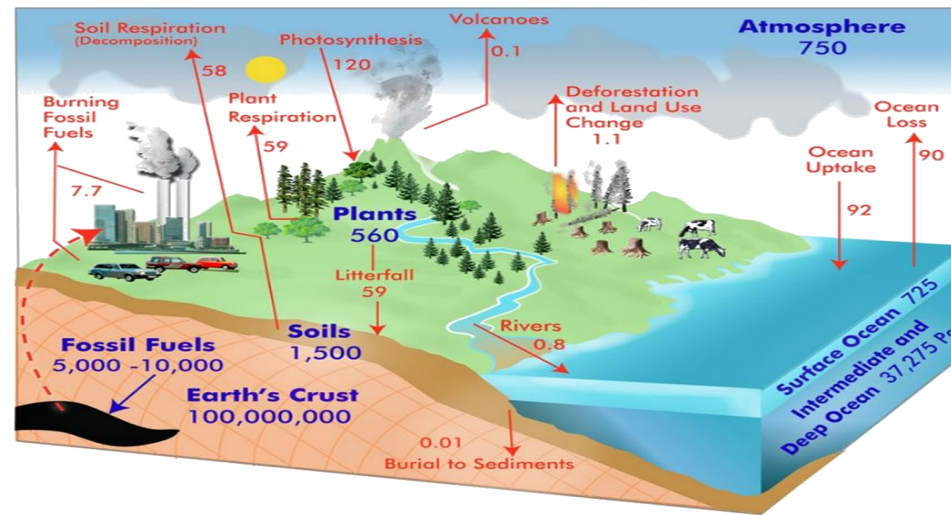
# Vadose Zone: Context and who cares?

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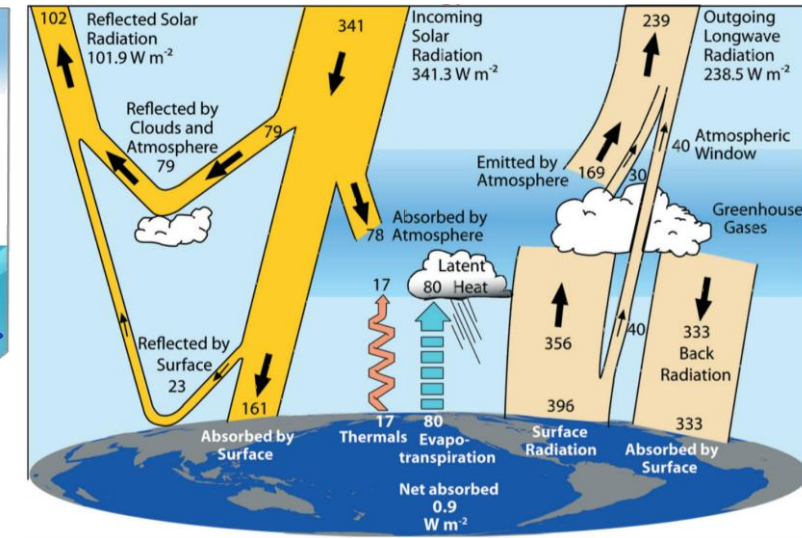
## Hydrological cycle



## Carbon cycle



## Surface energy balance



Vadose zone processes play key roles in the global water, carbon, and energy balances

# Vadose Zone Hydrology: Scope of the course

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## Goal:

water + solutes  
↙ ↘ Energy potential.

- Understanding and quantifying the processes related to matter and energy in the vadose zone

## Approach:

- Conceptual pictures
- Physical laws and fundamental principles
- Mathematical formulations and analytical/numerical solutions
- Model vs. reality (measurements)



# Syllabus + Readings

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## SCHEDULE OF TOPICS

Week	Date	Topic	Readings	Problem Sets
1	8/22	Introduction; Steady-state saturated flow	L01	
	8/24	Steady-state saturated flow	L01	
2	8/29	Transient saturated flow; saturated solute transport	L02	
	8/31	saturated solute transport	L03	
3	9/5	Multiphase fluids in capillary tubes	L04	Release #1
	9/7	Multiphase fluids in capillary tubes	L05	
4	9/12	Porous medium models and characteristic curves	J&H Ch 3	#1 DUE
	9/14	Macroscopic description of two-phase flow	P&C – Ch 11	Release #2
5	9/19	Richards' assumptions; Richards' Equation	P&C – Ch 11	
	9/21	Steady-state unsaturated flow	L08	#2 DUE
6	9/26	Numerical solution of steady-state unsat. flow	L09	Release #3
	9/28	Numerical solution of steady-state unsat. flow		
7	10/3	Transient unsaturated flow	J&H Ch 3	
	10/5	Transient unsaturated flow		
8	10/10	Transient unsaturated flow	J&H Ch 3	#3 DUE
	10/12	Numerical solution for transient unsat. flow	Celia 1990	
9	10/17	Use HYDRUS to study 1D transient unsat flow (In class)		
	10/19	2D unsaturated flow	L12	
10	10/24	Review session for the midterm exam		Release #4
	10/26	<b>Midterm Oral Exam</b>		
11	10/31	Comments on midterm; Measurement methods	L15	
	11/2	Visit the soil physics lab of Dr. Markus Tuller (TBD)		#4 DUE
12	11/7	Parameter estimation/Inverse modeling; Use spreadsheet model	L13	
	11/9	Inverse modeling w/ HYDRUS (in class)	L16, L13a	
13	11/14	Introduction to PFAS		
	11/16	Transport of PFAS under unsat. flow	Guo 2020	Release #5
14	11/21	Fluid-fluid interfacial area		
	11/23	Thanksgiving recess (no class)		
15	11/28	Informal presentation of "Art of Porous Media Flow"; Review session for the final exam		#5 DUE
	11/30	No class (work on final project)		
16	12/5	Presentation of final projects		
	12/7	No class (reading day)		
	12/8	<b>Final Exam</b>		

## Readings:

1. **Ferre, Vadose Zone Hydrology Lecture Notes**
2. **Jury & Horton, Soil Physics (sixth edition), 2004**
3. Pinder & Celia, Subsurface Hydrology, 2006
4. Stephens, Vadose zone Hydrology, 1995

## Grading:

### Undergraduate students

Homework	55%
Midterm exam (oral)	20%
Final exam (written)	20%
Participation	5%

### Graduate students

Homework	35%
Midterm exam (oral)	20%
Final exam (written)	20%
Final project	20%
Participation	5%

*Art of porous media flow submission* +5%

## Class websites:

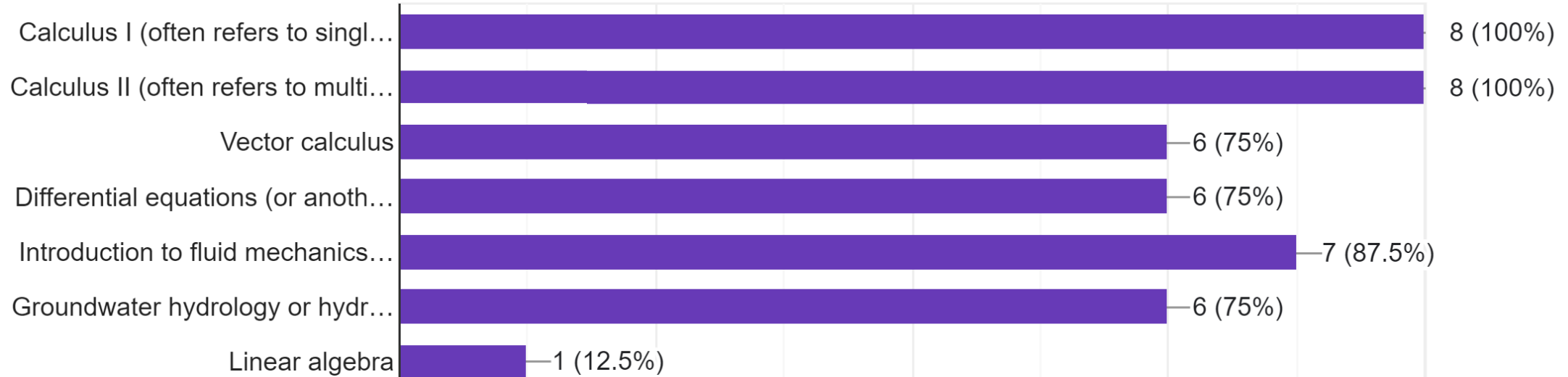
### 1. GitHub

- <https://github.com/GuoPorousMediaLab/HWRS505-405-2023Fall>
- The **primary** site that we use for sharing course materials.

### 2. D2L

- Materials for Homework and Exams.
- Submit Homework and Exams.

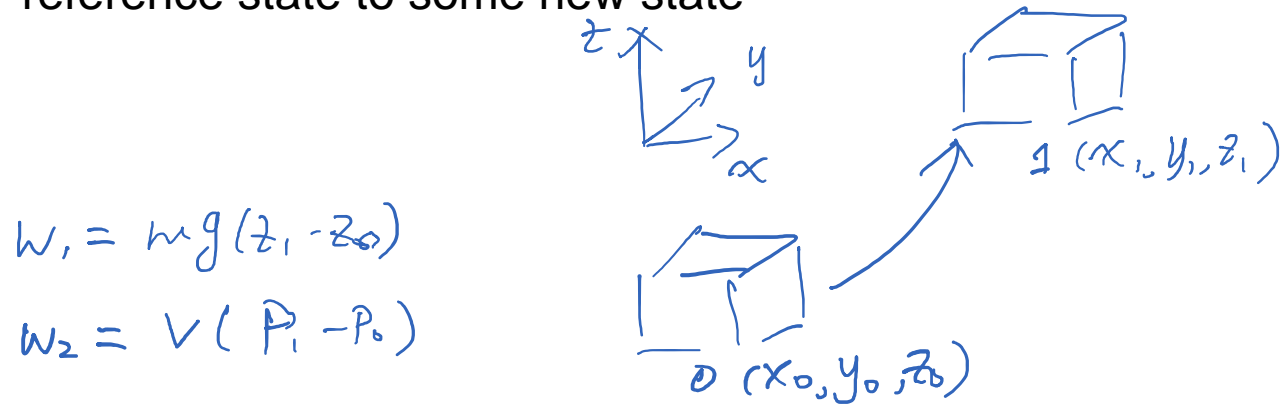
# Results of Pre-class Survey



- Glad to see many of you have taken most of the classes.
- No worries if you have not taken one or multiple classes. I will introduce the basic concepts when we use them.
  - ✓ Make sure to ask questions in class if an unfamiliar concept is used and I do not explain it.
  - ✓ Come to office hours.
  - ✓ Use Wikipedia and other resources to establish a basic understanding of these concepts.

# Steady-state saturated flow

**Energy potential ( $\Phi$ ):** work done on a unit mass of fluid in transferring it from a reference state to some new state



$$W_1 = mg(z_1 - z_0)$$

$$W_2 = V(P_1 - P_0)$$

Total work applied:

$$W = W_1 + W_2 = mg(z_1 - z_0) + V(P_1 - P_0)$$

Energy potential: "per unit mass"

$$\Phi = \frac{W}{m} = g(z_1 - z_0) + \frac{1}{\rho} (P_1 - P_0)$$

Hydraulic head: "per unit weight"

$$H = \frac{W}{mg} = (z_1 - z_0) + \frac{1}{\rho g} (P_1 - P_0)$$

$P_0$ : often chosen as atmospheric pressure ( $P_0 = 0$ )

$z_0$ : datum ( $z_0 = 0$ )

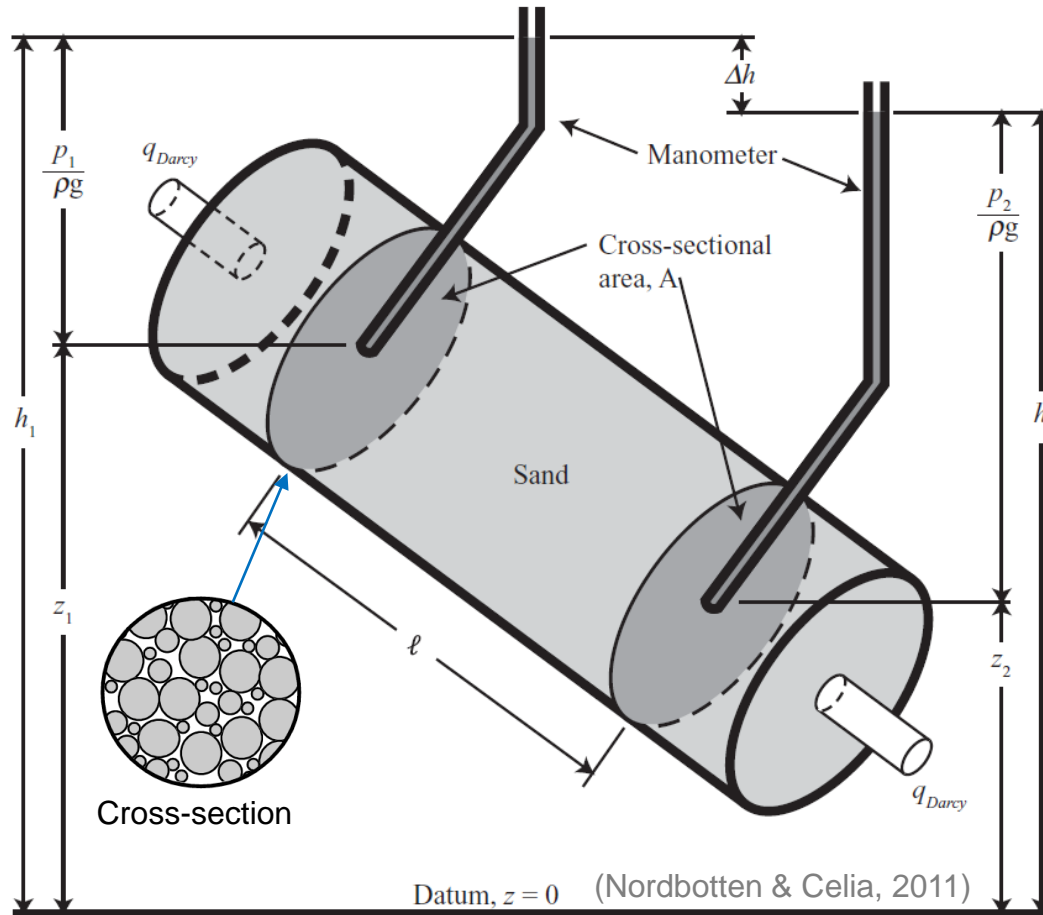
$$H = z + \frac{P}{\rho g}$$

Elevation head

pressure head ( $\psi = \frac{P}{\rho g}$ )



# Steady-state saturated flow



Schematic of Darcy's experiment [1856]

## Flux Law: Darcy's Equation

$$Q = - \underset{\substack{\uparrow \\ \text{Saturated hydraulic} \\ \text{conductivity } [L/T]}}{\bar{K}} A \frac{h_2 - h_1}{L} \quad [L^3/T]$$

(property of the porous medium and fluid)

$$\bar{K} = \frac{k \rho g}{\mu_w} \quad \text{permeability } [L^2]$$

$$q = \frac{Q}{A} = - \underset{\substack{\uparrow \\ \text{Darcy flux}}}{\bar{K}} \frac{h_2 - h_1}{L} \quad [L/T]$$

Darcy flux

$$v = \frac{q}{\phi} \quad \text{porosity} \quad [L/T]$$

Interstitial velocity  
(pore water velocity)