

Solution to Q1.3.4

Mayank Gupta

Question: Find the intersection \mathbf{H} of altitudes BE_1 and CF_1

Solution: Equation of BE_1

$$\begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = 2 \quad (1)$$

Equation of CF_1

$$\begin{pmatrix} 5 & -7 \end{pmatrix} \mathbf{x} = 20 \quad (2)$$

Therefore, we need to solve the following equation to get \mathbf{H} :

$$\begin{pmatrix} 1 & 1 \\ 5 & -7 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 2 \\ 20 \end{pmatrix} \quad (3)$$

Solving the above equation by Gauss-Jordan method

$$\begin{pmatrix} 1 & 1 & 2 \\ 5 & -7 & 20 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - 5R_1} \begin{pmatrix} 1 & 1 & 2 \\ 0 & -12 & 10 \end{pmatrix} \quad (4)$$

$$\xrightarrow{R_2 \leftarrow \frac{R_2}{-12}} \begin{pmatrix} 1 & 1 & 2 \\ 0 & 1 & -\frac{5}{6} \end{pmatrix} \quad (5)$$

$$\xrightarrow{R_1 \leftarrow R_1 - R_2} \begin{pmatrix} 1 & 0 & \frac{17}{6} \\ 0 & 1 & -\frac{5}{6} \end{pmatrix} \quad (6)$$

Therefore point of intersection \mathbf{H} is

$$\mathbf{x} = \begin{pmatrix} \frac{17}{6} \\ -\frac{5}{6} \end{pmatrix} \quad (7)$$

$$= \begin{pmatrix} 2.833 \\ -0.833 \end{pmatrix} \quad (8)$$

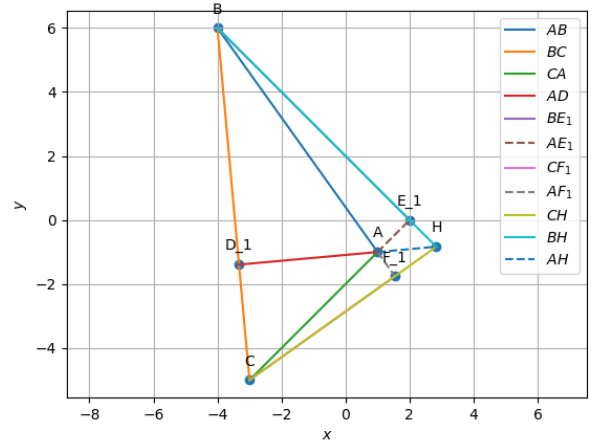


Fig. 0. Intersection point \mathbf{H} of altitudes BE_1 and CF_1 plotted using python