

1st Year Common  
Subject : Applied Mathematics

Time : 3 Hrs.

M.M. : 60

Section-A

Note: Multiple Choice questions. All questions are compulsory. (6x1=6)

Q.1 If  $h(x) = 5 - 3x + 2x^2 - x^3$ , then  $h(1) =$  (CO10)  
(a) 0 (b) 4  
(c) 3 (d) none of these

Q.2  $\frac{d}{dx}(\cot x) =$  (CO10)  
(a)  $-\operatorname{cosec}^2 x$  (b)  $-\cos^2 x$   
(c)  $-\cot^2 x$  (d) none of these

Q.3  $\int \frac{10}{x} dx =$  (CO12)  
(a)  $10x^{-2} + c$  (b)  $10 \log |x^{-2} - 1| + c$   
(c)  $10 \log |x| + c$  (d) All of these

Q.4  $\int_0^1 e^x dx =$  (CO14)  
(a)  $e - 2$  (b)  $e^x - 1$   
(c)  $e$  (d)  $e - 1$

Q.5 Which of the following is a non linear Ordinary Differential Equation? (CO17)

- (a)  $\frac{dy}{dx} - y = e^{-x}$  (b)  $\frac{dy}{dx} - y \cos y = e^{-y}$   
(c)  $\frac{dy}{dx} + xy = e^x$  (d)  $\frac{dy}{dx} - y = e^x \cos x$

Q.6 What is the Mode of the data 8, 10, 12, 14, 14, 14, 12, 10, 8? (CO18)

- (a) 14 (b) 8  
(c) 12 (d) 10

Section-B

Note: Objective/Completion type questions. All questions are compulsory. (6x1=6)

Q.7 Fill in the blank

$$\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a} =$$

Q.8 Is  $\frac{d}{dx} \left( \frac{1}{x} \right) = \log x$ ? (TRUE/FALSE) (CO10)

Q.9 Evaluate  $\int_0^2 1 dx$  (CO14)

Q.10 What is the value of  $\int 7^x dx$ ? (CO12)

Q.11 Give an example of Linear Ordinary Differential Equation. (CO17)

Q.12 Find the Median of 4, 8, 12, 16, 20, 24. (CO18)

Section-C

Note: Short type questions. Attempt any eight questions out of ten questions. (8x4=32)

Q.13 Define even function. Also evaluate the following (CO10)

$$\lim_{y \rightarrow 2} (3y^3 - 2y^3)$$

Q.14 Evaluate the following limits  $\lim_{x \rightarrow 0} \frac{7^x - 4^x}{\tan 2x}$  (CO10)

Q.15 Differentiate  $y = (x+1)^3 \cos(3-7x)$  with respect to  $x$ . (CO10)

Q.16 Find  $\frac{d^2y}{dx^2}$ , if  $y = \frac{\log x}{x}$ . (CO10)

Q.17 Find the rate of change of area of a circle with respect to its radius  $r$  when  $r = 7$  c.m. (CO10)

Q.18 Evaluate the following. (CO12)

$$\int x^2 e^{-x} dx$$

Q.19 Evaluate the following. (CO14)

$$\int_1^4 \left( e^{2x} + \frac{5}{x} + x^2 \right) dx$$

Q.20 Evaluate the following. (CO14)

$$\int_0^{\pi/2} \sin^6 x \cos^6 x dx$$

Also write the formula used to evaluate the above integration. <https://www.hsbteonline.com>

Q.21 Find the area under the curve  $y = x^2 + 3x + 2$ , between the  $x$ -axis and  $3 \leq x \leq 8$ . (CO15)

Q.22 i) Find the order and degree of the differential equation. (CO17)

$$x^3 + 3 = y^3 + \left( \frac{dy}{dx} \right)^2 - \left( \frac{d^2y}{dx^2} \right)^3$$

ii) Find the mean of the following data (CO18)

3, 6, 9, 12, 15

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## Section-D

**Note:** Long answer type questions. Attempt any two questions out of three questions. (2x8=16)

Q.23 Find all the points of maxima and minima and their corresponding maximum and minimum values of the function  $f(x) = x^3 - 6x^2 + 9x - 2$  (CO11)

Q.24 Apply Simpson's rule to evaluate (CO16)

$$\int_3^{10} (5 + 7x) dx$$

by taking 7 equal subintervals of  $3 \leq x \leq 10$ .

Q.25 Find the mean deviation about mean for the following frequency distribution:

$x_i$	2	4	6	8	10	12
$f_i$	5	4	3	3	4	1

where  $f_i$  represents the frequency of  $x_i$ . (CO18)

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**SECTION-A**

**Note:** Multiple choice questions. All questions are compulsory (6x1=6)

**(Course Outcome/CO)**

Q.1 The value of  $\lim_{x \rightarrow 0} \frac{\sin x}{x}$  is (CO-10)

- a) 0                                      b) 1  
c)  $\infty$                                       d)  $\cos x$

Q.2  $\frac{d}{dx} (5x^2)$  is equal to (CO-10)

- a)  $5x$                                       b)  $2x$   
c)  $10x^2$                                       d)  $10x$

Q.3 The value of  $\frac{d}{dx} (\cos x)$  is equal to (CO-10)

- a)  $\sin x$                                       b) 1  
c)  $-\sin x$                                       d)  $\sec x$

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Q.4  $\int \sin x \, dx$  is equal to (CO-12)

- a)  $\cos x$                                       b)  $-\cos x$   
c)  $\operatorname{cosec} x$                                       d) 0

Q.5  $\int x^3 \, dx$  is equal to (CO-12)

- a)  $3x^2$                                       b)  $\frac{x^4}{4}$   
c)  $6x$                                       d)  $x^4$

Q.6 The order of the differential equation (CO-17)

$$\frac{d^3 y}{dx^3} + 2 \frac{d^2 y}{dx^2} + 4 \frac{dy}{dx} = \sin x \text{ is}$$

- a) 2                                      b) 3  
c) 4                                      d) 1

**SECTION-B**

**Note:** Objective/ Completion type questions. All questions are compulsory. (6x1=6)

Q.7 If  $f(x) = x^2 + 6x + 4$ , then  $f(1) = \dots\dots\dots$  (CO-10)

Q.8 If  $y = x^2 + x + 1$ , then  $\frac{dy}{dx} = \dots\dots\dots$  (CO-10)

Q.9  $\int e^x \, dx = \dots\dots\dots$  (CO-12)

Q.10 The order of the differential equation (CO-17)

$$\frac{d^2 y}{dx^2} + 2 \left( \frac{dy}{dx} \right)^3 + 2y = 0 \text{ is } \dots\dots\dots$$

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Q.11 The degree of the differential equation(CO-17)

$$\frac{d^2y}{dx^2} + 2\left(\frac{dy}{dx}\right)^3 + 2y = 0 \text{ is } \dots\dots$$

Q.12 The median of the value : (CO-18)

15, 6, 16, 8, 22, 21, 9, 18, 25

### SECTION-C

**Note:** Short answer type questions. Attempt any eight questions out of ten questions. (8x4=32)

Q.13 Differentiate  $y = x^3 e^x$  with respect to  $x$ . (CO-10)

Q.14 Differentiate (CO-10)

$$y = \frac{2x+1}{x^2-1} \text{ with respect to } x$$

Q.15 If  $y = x^3 \log x$ , find  $\frac{d^2y}{dx^2}$  (CO-10)

Q.16 Evaluate  $\int (x^2 + 2x - x + \frac{1}{x}) dx$  (CO-12)

Q.17 Evaluate  $\int x \cos x dx$  (CO-12)

Q.18 Evaluate  $\int_0^{\frac{\pi}{2}} \cos^6 x dx$  (CO-14)

Q.19 Solve the differential equation (CO-17)

$$\frac{dy}{dx} = 2x + \frac{1}{x} - x^2$$

Q.20 Find the mean of following frequency distribution. (CO-18)

$x$	5	7	9	10	12	15
$f$	8	6	2	2	2	6

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Q.21 Find the Median of following table (CO-18)

Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
frequency	2	18	30	45	35	20	6	3

Q.22 Find the standard deviation of following data (CO-18)

4, 6, 10, 12, 18

### SECTION-D

**Note:** Long answer type questions. Attempt any two questions out of three questions. (2x8=16)

Q.23 Find the maximum and minimum value of the function (CO-11)

$$f(x) = -x^3 + 12x^2 - 5$$

Q.24 Use trapezoidal rule to evaluate  $\int_0^7 x^2 dx$ , by taking eight ordinates (CO-16)

Q.25 The following table show the rank of 10 students according to their achievement in practical and theory paper of science, Find the coefficient of rank correlation. (CO-18)

Practical	8	3	9	2	7	10	4	6	1	5
Theory	9	5	10	1	8	7	3	4	2	1

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प्र.5  $\int x^3 dx$  के बराबर है। (CO-12)

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**भाग - क**

प्र.6 अवकल समीकरण  $\frac{d^3y}{dx^3} + 2\frac{d^2y}{dx^2} + 4\frac{dy}{dx} = \sin x$  की कोटि है। (CO-17)

क) 2                      ख) 3  
ग) 4                      घ) 1

क) 0                      ख) 1  
ग)  $\infty$                   घ)  $\cos x$

**नोट:-** वस्तुनिष्ठ प्रश्न। सभी प्रश्न अनिवार्य हैं। (6x1=6)

क)  $5x$                       ख)  $2x$   
ग)  $10x^2$                       घ)  $10x$

प्र.7 यदि  $f(x) = x^2 + 6x + 4$ , तब  $f(1) = \dots\dots\dots$   
(CO-10)

प्र.8 यदि  $y = x^2 + x + 1$ , तब  $\frac{dy}{dx} = \underline{\hspace{2cm}}$  (CO-10)

क)  $\sin x$                       ख) 1  
ग)  $-\sin x$                       घ)  $\sec x$

प्र.9  $\int e^x dx =$  \_\_\_\_\_ (CO-12)

प्र.10  $\frac{d^2y}{dx^2} + 2\left(\frac{dy}{dx}\right)^3 + 2y = 0$  अवकल समीकरण की कोटि है।  
(CO-17)

क)  $\cos x$                       ख)  $-\cos x$   
ग)  $\operatorname{cosec} x$                       घ)  $0$

प्र.11  $\frac{d^2y}{dx^2} + 2\left(\frac{dy}{dx}\right)^3 + 2y = 0$  अवकल समीकरण की घात है।  
(CO-17)

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प्र.12 15, 6, 16, 8, 22, 21, 9, 18, 25 मानों का माध्यक है।  
(CO-18)

### भाग - ग

नोट:- लघु उत्तरीय प्रश्न। 10 में से किन्हीं 8 प्रश्नों को हल कीजिए।  
(8x4=32)

प्र.13  $x$  के सापेक्ष में  $y = x^3 e^x$  को अवकलित करें। (CO-10)

प्र.14  $x$  के सापेक्ष में  $y = \frac{2x+1}{x^2-1}$  को अवकलित करें। (CO-10)

प्र.15 यदि  $y = x^3 \log x$ , तब  $\frac{d^2y}{dx^2}$  ज्ञात करें। (CO-10)

प्र.16  $\int (x^2 + 2x - x + \frac{1}{x}) dx$  मूल्यांकन करें। (CO-12)

प्र.17 मूल्यांकन करें  $\int (x \cos x) dx$  (CO-12)

प्र.18 मूल्यांकन करें  $\int_0^{\frac{\pi}{2}} \cos^6 x dx$  (CO-14)

प्र.19  $\frac{dy}{dx} = 2x + \frac{1}{x} - x^2$  अवकल समीकरण हल करें।  
(CO-17)

प्र.20 निम्नलिखित बारम्बारता बंटन का माध्य ज्ञात करें। (CO-18)

$x$	5	7	9	10	12	15
$f$	8	6	2	2	2	6

प्र.21 निम्नलिखित तालिका का माध्यक ज्ञात करें। (CO-18)

अंक	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
बारम्बारता	2	18	30	45	35	20	6	3

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प्र.22 निम्नलिखित आंकड़ों का मानक विचरण ज्ञात करें।

4, 6, 10, 12, 18 (CO-18)

### भाग - घ

नोट:- दीर्घ उत्तरीय प्रश्न। तीन में से किन्हीं दो प्रश्नों को हल कीजिए।  
(2x8=16)

प्र.23  $f(x) = -x^3 + 12x^2 - 5$  फलन का अधिकतम और न्यूनतम मान ज्ञात करें। (CO-11)

प्र.24 8 कोटि अंक लेते हुए  $\int_0^7 x^2 dx$ , ट्रेपेजोडियल नियम द्वारा मूल्यांकन कीजिए। (CO-16)

प्र.25 निम्नलिखित तालिका में 10 विद्यार्थियों की उनके विज्ञान विषय में व्यावहारिक और सिद्धांत के श्रेणी को दिखाया गया है। रैंक सहसम्बन्ध के गुणांक को ज्ञात कीजिए। (CO-18)

Practical	8	3	9	2	7	10	4	6	1	5
Theory	9	5	10	1	8	7	3	4	2	1

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**Common**

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**SECTION-A**

**Note:** Multiple choice questions. All questions are compulsory (6x1=6)

**(Course Outcome/CO)**

Q.1 If  $f(x) = 3x^3 - x + 2$ , then value of  $f(-1)$  is (CO-10)

- a) 4                                      b) 6  
c) 0                                      d) 12

Q.2 The value of  $\lim_{x \rightarrow 0} (4\cos x - \tan x)$  (CO-10)

- a) 4                                      b) 3  
c) -1                                    d)  $\infty$

Q.3  $\int \sin 5x \, dx =$  (CO-12)

- a)  $5 \cos 5x + c$                       b)  $\frac{\cos 5x}{5} + c$   
c)  $\frac{-\cos 5x}{5} + c$                       d) None of these

Q.4  $\int e^{-x} \, dx =$  (CO-12)

- a)  $e^{-x} + c$                               b)  $-e^{-x} + c$   
c)  $-xe^{-x-1} + c$                       d)  $\frac{e^{-x+1}}{-x+1} + c$

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Q.5 The value of  $\int_1^1 \tan x \, dx$  (CO-14)

- a) 1                                      b)  $\frac{\pi}{2}$   
c)  $\frac{\pi}{4}$                                       d) 0

Q.6 The degree of the differential equation  $(\frac{dy}{dx})^3 + y^5 = \sin^2 x$  is (CO-17)

- a) 5                                      b) 15  
c) 1                                      d) 3

**SECTION-B**

**Note:** Objective/ Completion type questions. All questions are compulsory. 6x1=6

Q.7 Fill in the blank: (CO-10)

$$\lim_{x \rightarrow 0} \frac{5^x - 1}{x} = \underline{\hspace{2cm}}$$

Q.8 If  $y = e^{-x}$ , then  $\frac{dy}{dx} =$  (CO-10)

Q.9  $-\int \operatorname{cosec}^2 x \, dx =$  (CO-12)

Q.10 Evaluate  $\int_0^2 x^2 \, dx$  (CO-14)

Q.11 The differential equation (CO-17)

$$\frac{d^2 y}{dx^2} + x \frac{dy}{dx} - y = \sec x$$

is a \_\_\_\_\_ differential equation. (linear/non-linear)

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Q.12 Write the formula to find coefficient of rank correlation. (CO-18)

### SECTION-C

**Note:** Short answer type questions. Attempt any eight questions out of ten questions. 8x4=32

Q.13 Evaluate (CO-10)

$$\lim_{x \rightarrow 0} \frac{3 \sin 5x}{\tan 30x}$$

Also, write the formulae which are used to simplify the problem.

Q.14 Differentiate  $\log 3x - e^{3x} + 3^x - x^3$  with respect to  $x$ . (CO-10)

Q.15 Differentiate  $y = \frac{(2x+1)}{\tan x}$  with respect to  $x$ . Also, write the quotient rule of differentiation. (CO-10)

Q.16 Find the rate of change of area of the square with respect to its side when side length is 7c.m. (CO-10)

Q.17 Find  $\frac{d^2y}{dx^2}$  at  $x = 0$ , if  $y = x, \cos x$ . (CO-10)

Q.18 Evaluate (CO-14)

$$\int_0^{\frac{\pi}{2}} \sin^4 x \cos^6 x \, dx$$

Q.19 Evaluate (CO-12)

$$\int \left( \frac{5}{x} - 3 \sec x \tan x + 2^x - 5 \right) dx$$

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Q.20 Find the area under the curve  $y = 8x^3 + 2x - 5$ , between  $x$ -axis and  $0 \leq x \leq 5$ . (CO-15)

Q.21 Solve the differential equation (CO-17)

$$\frac{dy}{dx} = 4^x + 2 \sin x$$

Q.22 Find the mode and median for the following data: (CO-18)

35, 25, 45, 24, 37, 42, 35, 41, 35, 52, 48, 55

### SECTION-D

**Note:** Long answer type questions. Attempt any two questions out of three questions. 2x8=16

Q.23 Find all the points of maxima/minima and their corresponding maximum/minimum values of the functions  $f(x) = x^3 - 18x^2 + 15$ . (CO-11)

Q.24 Using Trapezoidal rule, evaluate (CO-16)

$$\int_0^5 (4x - 1) dx$$

by taking 5 equal intervals.

Q.25 Find the standard deviation for the following frequency distribution: (CO-18)

$x_i$	3	5	7	9	1	4
$f_i$	6	2	7	5	4	6

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**भाग - क**

**नोट:-** वस्तुनिष्ठ प्रश्न। सभी प्रश्न अनिवार्य हैं:- (6x1=6)

**(Course Outcome/CO)**

प्र.1  $f(-1)$  का मान है यदि  $f(x) = 3x^3 - x + 2$  (CO-10)

- a) 4                                      b) 6  
c) 0                                      d) 12

प्र.2  $\lim_{x \rightarrow 0} (4\cos x - \tan x)$  का मान (CO-10)

- a) 4                                      b) 3  
c) -1                                      d)  $\infty$

प्र.3  $\int \sin 5x \, dx =$  (CO-12)

- a)  $5 \cos 5x + c$                       b)  $\frac{\cos 5x}{5} + c$   
c)  $\frac{-\cos 5x}{5} + c$                       d) उपरोक्त कोई नहीं

प्र.4  $\int e^{-x} \, dx =$  (CO-12)

- a)  $e^{-x} + c$                               b)  $-e^{-x} + c$   
c)  $-xe^{-x+1} + c$                       d)  $\frac{e^{-x+1}}{-x+1} + c$

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प्र.5  $\int_1^1 \tan x \, dx$  का मान (CO-14)

- a) 1                                      b)  $\frac{\pi}{2}$   
c)  $\frac{\pi}{4}$                                       d) 0

प्र.6  $(\frac{dy}{dx})^3 + y^5 = \sin^2 x$  अवकलन समीकरण की डिग्री है। (CO-17)

- a) 5                                      b) 15  
c) 1                                      d) 3

**भाग - ख**

**नोट:-** वस्तुनिष्ठ प्रश्न। सभी प्रश्न अनिवार्य हैं:- (6x1=6)

प्र.7 खाली स्थान भरिए:- (CO-10)

$$\lim_{x \rightarrow 0} \frac{5^x - 1}{x} = \underline{\hspace{2cm}}$$

प्र.8 यदि  $y = e^{-x}$ , तब  $\frac{dy}{dx} = \underline{\hspace{2cm}}$ . (CO-10)

प्र.9  $-\int \operatorname{cosec}^2 x \, dx = \underline{\hspace{2cm}}$  (CO-12)

प्र.10 मूल्यांकन  $\int_0^2 x^2 \, dx$  (CO-14)

प्र.11 अवकल समीकरण (CO-17)

$$\frac{d^2 y}{dx^2} + x \frac{dy}{dx} - y = \sec x$$

                     अवकल समीकरण है। (रैखीय/अरैखीय)

प्र.12 रैंक-सहसंबंध का गुणांक ज्ञात करने का सूत्र लिखिए। (CO-18)

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### भाग - ग

नोट:- लघु उत्तरीय प्रश्न। दस प्रश्नों में से किन्हीं आठ प्रश्नों के उत्तर दीजिए:- 8x4=32

प्र.13 मूल्यांकन :- (CO-10)

$$\lim_{x \rightarrow 0} \frac{3 \sin 5x}{\tan 30x}$$

उपरोक्त को हल करने के लिए प्रयोग किया जाने वाला सूत्र लिखिए।

प्र.14  $x$  के सापेक्ष में  $\log 3x - e^{3x} + 3^x - x^3$  अवकलन ज्ञात कीजिए। (CO-10)

प्र.15  $x$  के सापेक्ष में  $y = \frac{(2x+1)}{\tan x}$  अवकलन ज्ञात कीजिए।

अवकलन का भागफल नियम लिखिए। (CO-10)

प्र.16 वर्ग के क्षेत्रफल के बदलने की दर इसकी भुजा के सापेक्ष में निकालिए जबकि भुजा की लम्बाई 7 सेमी. है। (CO-10)

प्र.17 यदि  $y = x$ ,  $\cos x =$  तब  $\frac{d^2y}{dx^2}$  ज्ञात करें,  $x=0$  पर (CO-10)

प्र.18 मूल्यांकन (CO-14)

$$\int_0^{\frac{\pi}{2}} \sin^4 x \cos^6 x \, dx$$

प्र.19 मूल्यांकन (CO-12)

$$\int \left( \frac{5}{x} - 3 \sec x \tan x + 2^x - 5 \right) dx$$

(7)

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प्र.20 वक्र  $y = 8x^3 + 2x - 5$  के नीचे  $x$  - अक्ष के बीच  $0 \leq x \leq 5$  का क्षेत्रफल ज्ञात कीजिए। (CO-15)

प्र.21 अवकल समीकरण को हल करें। (CO-17)  
 $\frac{dy}{dx} = 4^x + 2 \sin x$

प्र.22 निम्नलिखित आँकड़ों का बहुलक और माध्यक ज्ञात कीजिए। (CO-18)

35, 25, 45, 24, 37, 42, 35, 41, 35, 52, 48, 55

### भाग - घ

नोट:- दीर्घ उत्तरीय प्रश्न। तीन प्रश्नों में से किन्हीं दो प्रश्नों के उत्तर दीजिए:- 2x8=16

प्र.23  $f(x) = x^3 - 18x^2 + 15$  फलन का अधिकतम/न्यूनतम सभी बिन्दु निकालिए तथा उसके अनुसार अधिकतम/न्यूनतम मान निकालिए। (CO-11)

प्र.24 5 बराबर अंतराल लेते हुए ट्रेपेजोडियल नियम का प्रयोग करते हुए मूल्यांकन कीजिए। (CO-16)

$$\int_0^5 (4x - 1) dx$$

प्र.25 निम्नलिखित बारम्बारता बंटन का मानक विचलन ज्ञात कीजिए। (CO-18)

$x_i$	3	5	7	9	1	4
$f_i$	6	2	7	5	4	6

(26080)

(8)

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