

Echidna Workshop Series: Part 3

Justin Jacob - Security Engineer I

Previous & Upcoming Workshops

Beginner

- Part 1: The Basics (Week of Nov 16, 2022)
- Part 2: Breaking ABDK Math (Week of Nov 21, 2022)

Intermediate

- **Part 3: Breaking Uniswap I (today)**
- Part 4: Breaking Uniswap II (Week of Dec 5, 2022)

Advanced

- Part 5: Breaking Primitive Finance I (Week of Dec 12, 2022)
- Part 6: Breaking Primitive Finance II (Week of Dec 19, 2022)

Who am I?

Justin Jacob, Security Engineer I

Who You Should Follow

- Troy Sargent ([@0xalpharush](#))
- Josselin Feist ([@montyly](#))
- Nat Chin ([@0xicingdeath](#))
- Anish Naik ([@anishrnaik](#))

Who are we?

Trail of Bits ([@trailofbits](#))

- We help developers to build safer software
- R&D focused: we use the latest program analysis techniques
- Slither, Echidna, Tealer, Amarna, solc-select, ..

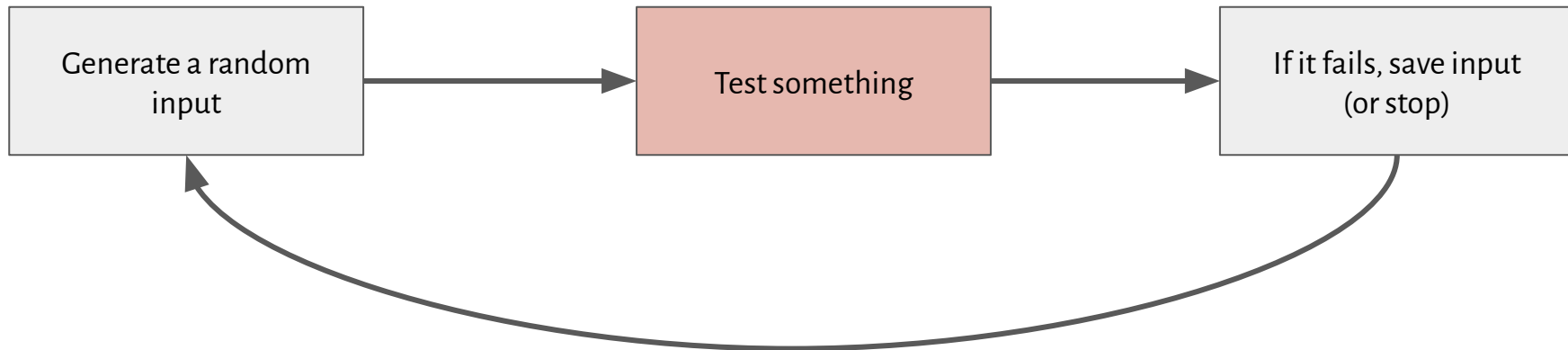
Today's Agenda:

- **Recap**
- **What is an AMM?**
 - How does it work?
 - Swaps, Liquidity Provisions
- **Go through the codebase**
- **Invariants and testing**

Recap -

- What is fuzzing?
- How do we fuzz contracts?
- What do we need to keep in mind when using Echidna?

What is fuzzing?



So how do I start fuzzing?

1. Identify your invariants / system properties in English
2. Convert your properties to code
3. **Run Echidna**
4. **FIND BUGS**

Useful optimizations:

- **Tests should have precondition, action, postcondition**
 - Pre-conditions: Scope the input space
 - Action: What we are testing
 - Post-conditions: The “truths” after the action

Useful optimizations:

- **Tests should have precondition, action, postcondition**
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 - Post-conditions: The “truths” after the action
- **Coverage is your friend!**
 - Echidna saves coverage in corpus

Visualizing internal testing

Target system

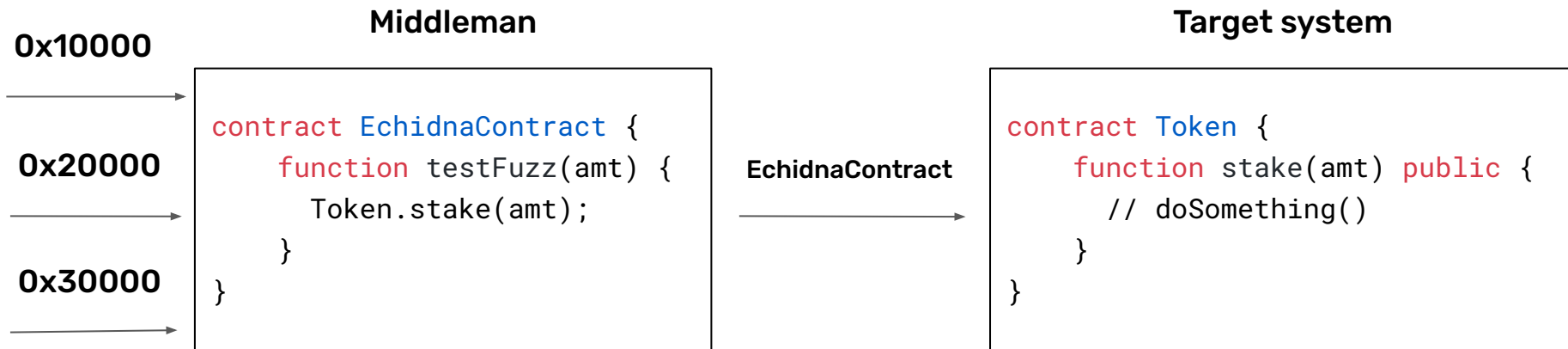
0x10000

0x20000

0x30000

```
contract TestToken is Token {  
    // inherited state and functions  
    uint256 totalSupply;  
    mapping (address => uint256) balances;  
    function transfer(address to, uint256 amount) {  
    }  
    function echidna_total_supply() public returns(bool) {  
        return balances[msg.sender] <= totalSupply()  
    }  
}
```

Visualizing External Testing



Finding invariants of something very
important...



What is an AMM?

- **Traditional Orderbook Model:**
 - Match buyers \longleftrightarrow sellers
 - Bid Price: max price buyer will pay
 - Ask Price: lowest price seller will sell
 - Market makers: add orders to orderbook
 - Market takers: execute orders

What is an AMM?

- **AMM Model:**
 - Exchange without orderbook
 - Pricing is based on pool's liquidity formula
 - Simplest example: $xy = k$ (Uniswap!)
 - Price is calculated as ratio between two assets
 - Exchanges keep k (pool invariant) constant

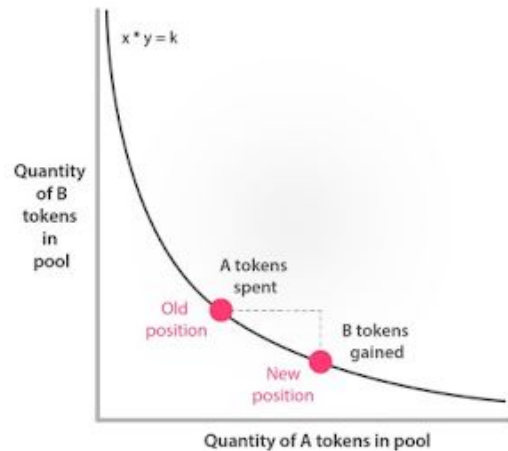
But why tho?

Orderbook model is really inefficient for blockchain!

- Have to find counterparties every time!
 - Keep track of all pending orders
 - Uses storage
 - Costs a lot of gas
- Need third party (market makers, takers)

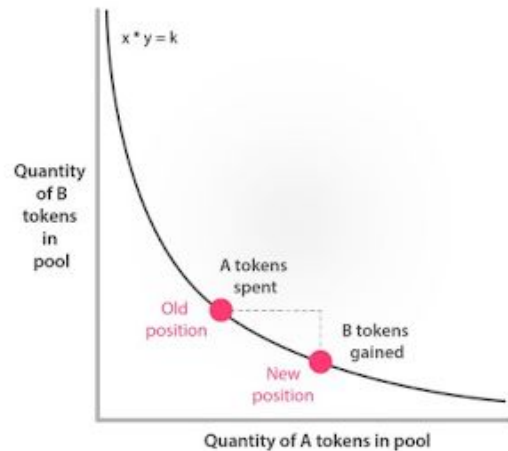
Example

- Swap x amt of tokenA for tokenB
- How much of token B do we get out?



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- Swap x amt of tokenA for tokenB
- How much of token B do we get out?
- Solution:
 - We have $x*y=k$
 - All trades keep k constant
 - Therefore ...



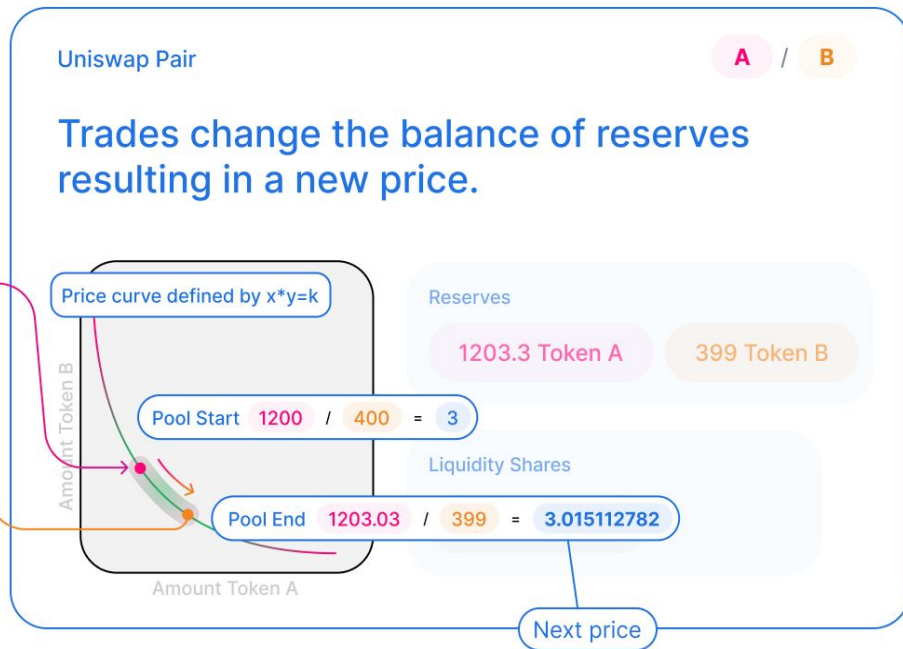
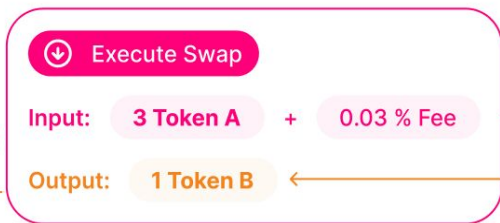
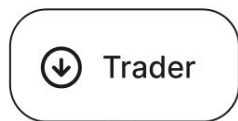
Solution:

Let Δx be the amount we are swapping token A for Δy of token b.

$$x * y = k$$

$$(x + \Delta x) * (y - \Delta y) = k \text{ (the pool gains } \Delta x, \text{ loses } \Delta y)$$

$$\Delta y = y - (k / (x + \Delta x))$$



Liquidity Providers (LPs)

- People provide ratio of tokens to the pool, get minted special LP token
- This LP token represents provided liquidity to the pool
- Initial LP Provider sets $k \Rightarrow$ sets token price
- To get tokens back, must burn these LP tokens

Why should I?

- In practice, there are fees on each swap
- **This fee goes back to the LPs**
 - Passive way to make money!

Example

- **Bob wants to create a DAI/WETH pool:**
 - Uni V2
 - He puts up 100000 DAI and 1 WETH
 - Therefore he gets minted $\sqrt{100000 * 1} \approx 316$ DAI-WETH LP tokens
- **Bob is encouraged to put up “fair price” of DAI/WETH**
 - If not, there is an arbitrage opportunity and pool will be rebalanced

⬇️ Liquidity Provider

⬇️ Liquidity Deposit

Input: 3 Token A + 1 Token B

Output: 12.4 Pool Tokens

Uniswap Pair

A / B

Increased liquidity reduces price slippage for trades.

Price curve defined by $x*y=k$

Amount Token B

Amount Token A

More liquidity increases low slippage area

Reserves

1210 Token A

399 Token B

Liquidity Shares

12 Pool Tokens

Impermanent Loss

- **Impermanent loss: \$ value of the LP's share decrease if the tokens change price**
- **In practice, trading fees should account for this**

Now...

Let's examine the code!

Core

- **Where the main logic of uniswap resides**
- **Extremely minimal and simplistic**
 - Uniswap themselves say it is “quite minimal, possibly even brutalist”

- Two contracts: factory and pairs

Core

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- **Factory: creates pairs**
 - Creates unique pair contracts for each pool via CREATE2
 - Also has logic to turn on fees

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- **Two contracts: factory and pairs**
- **Factory: creates pairs**
 - Creates unique pair contracts for each pool via CREATE2
 - Also has logic to turn on fees
- **Pairs:**
 - Represent liquidity pool, keep track of token balances
 - Also an ERC20 token
 - Contains the basic swapping logic

Now for the fun part...

Let's find some invariants!

LP Invariants:

- Providing liquidity increases invariant
 - $x * y = k \Rightarrow$ increasing x and y increases k !

Homework:

Think of more invariants!

Write your own tests and make PRs!

Thanks everyone for attending!

See you next week!

**TRAIL
OF
BITS**