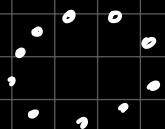


- ① 3rd May
- ② poor wed of 3rd May



$$b_k^+ = a_{k\uparrow}^+ a_{-k\downarrow}^+$$

$$b_k^{+2} = 0$$

$$b_{-k}^2 = 0$$

$$b_k^+ b_{-k}^+ = 0$$

$$[b_k, b_k^+] =$$

$$\pi_k^+ = b_k^+ - b_{-k}$$

not wrong abt  $\pi_k$

$$[b_k, b_k^+]$$

$$= [a_{k\uparrow}^+ a_{-k\downarrow}^+, a_{k\uparrow}^+ a_{-k\downarrow}^+]$$

$$= -a_{k\uparrow}^+ a_{k\uparrow}^+ a_{-k\downarrow}^+ a_{-k\downarrow}^+ + a_{k\uparrow}^+ a_{-k\downarrow}^+ a_{k\uparrow}^+ a_{-k\downarrow}^+$$

$$= -n_{k\uparrow} n_{-k\downarrow} + (1 - n_{k\uparrow})(1 - n_{-k\downarrow})$$

$$= 1 - n_{k\uparrow} - n_{-k\downarrow} + n_{k\uparrow} n_{-k\downarrow}$$

$$b_k^+ b_k = \hat{n}_{k\uparrow} + a_{k\uparrow}^+ a_{-k\downarrow}^+ a_{k\uparrow} a_{-k\downarrow}$$

$$+ a_{k\uparrow}^+ a_{k\uparrow} + a_{-k\downarrow}^+ a_{-k\downarrow} + (1 - n_{k\uparrow})(1 - n_{-k\downarrow})$$

$$= [b_k, b_k^+]$$

$$\psi_N = \mathcal{N} \left( \sum_k c_k b_k^\dagger \right)^N |0\rangle \quad \sum_k \frac{|c_k|^2}{1+|c_k|^2} = N$$

$$= \mathcal{N} \hat{\Omega}^N |0\rangle$$

$$\exp \hat{\Omega} |0\rangle = \prod_k (1 + c_k b_k^\dagger) |0\rangle = \sum a_n \psi_n$$

$$a_n = \int_0^{2\pi} e^{-in\phi} \prod_k (1 + e^{i\phi} c_k b_k^\dagger) \frac{d\phi}{2\pi}$$

$$\Rightarrow a_n / \langle \psi_n | = \int_0^{2\pi} \frac{d\phi}{2\pi} e^{-in\phi} \prod_k (1 + e^{i\phi} c_k b_k^\dagger) |0\rangle$$

$$\psi_n = \left( \sum_k c_k b_k^\dagger \right)^n |0\rangle$$

$\underbrace{\psi_n}_{\text{\# of Cooper pairs}}$

$a_n \approx N$

$$a_n = \int_0^{2\pi} \frac{d\phi}{2\pi} e^{-in\phi} \langle \psi_n | \exp \left[ \sum e^{i\phi} c_k b_k^\dagger \right] |0\rangle$$

$$\Rightarrow a_n = \int_0^{2\pi} \frac{d\phi}{2\pi} e^{-in\phi} \langle 0 | \Omega^{+n} \exp [e^{i\phi} \hat{\Omega}] |0\rangle$$

$$|\psi_{BCS}\rangle = \mathcal{N}_{BCS} \sum_n \frac{\Omega^n}{n!} |0\rangle$$

$$\mathcal{N}_{BCS}^2 = \prod_k (1 + |c_k|^2) = 1$$

$$a_n = \frac{\mathcal{N}_{BCS}}{n!}$$

$$\mathcal{N}_{BCS} = \frac{1}{\prod_k [1 + |c_k|^2]^{1/2}}$$

$$\sum_k \frac{|c_k|^2}{1 + |c_k|^2} = N$$

$$N_{BCS} = \prod_k \frac{1}{\sqrt{1+|g_k|^2}} \quad a_n = \frac{1}{n!} \prod_k \frac{1}{\sqrt{1+|g_k|^2}}$$

$$a_n = \frac{1}{n!} \prod_k \frac{1}{\sqrt{1+|g_k|^2}}$$

$$a_n = \frac{N_{BCS}}{n! N_n} \quad \frac{N_{BCS}}{N} \quad \frac{N \Omega_n |0\rangle}{n!}$$

$$\frac{1}{N} = \sum_n \left( \sum_k g_k b_k^\dagger \right)^n |0\rangle$$

$$\Omega^{n|vac}$$

$$\Omega^+ = \sum_k g_k b_k$$

$$\Omega^+ \Omega^-$$

$$b_k^\dagger \cdot b_k$$