

Recap :-

Landauer Buttiker approach

~10 mins → # Ohm's law like Behaviour

Landauer Buttiker approach

G^{-1} → calculated for different regimes

Buttiker Formula / Landauer + Buttiker

$$I = \frac{2e}{n} F(U_1 - U_2)$$

Two terminal \rightarrow not a scalar

$$I_p = \frac{2e}{n} \sum_q [G_{qp} V_p - G_{pq} V_q]$$

$$I_p = \sum_q [G_{qp} V_p - G_{pq} V_q]$$

$$G_{pq} = \frac{2e^2}{n} T_{p \leftarrow q}$$

Current conservation

$$\sum_q G_{pq} = \sum_p G_{qp}$$

⇒ Datta's book → Buttiker formula

$T_{q \leftarrow p}$: transmission for anode going from p to q.

$$I_p = \sum_q [G_{qp} V_p - G_{pq} V_q]$$

$\underbrace{\quad}_{\text{pairwise conductance from } p \leftarrow q}$

$$G_{pq} = \frac{2e^2}{n}$$

$I_p = \frac{2e}{n} F(U_1 - U_2)$

Two terminal

$$I_p = \frac{2e}{n} \sum_q [G_{qp} V_p - G_{pq} V_q]$$

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$$G_{pq} = \frac{2e^2}{n} T_{p \leftarrow q}$$

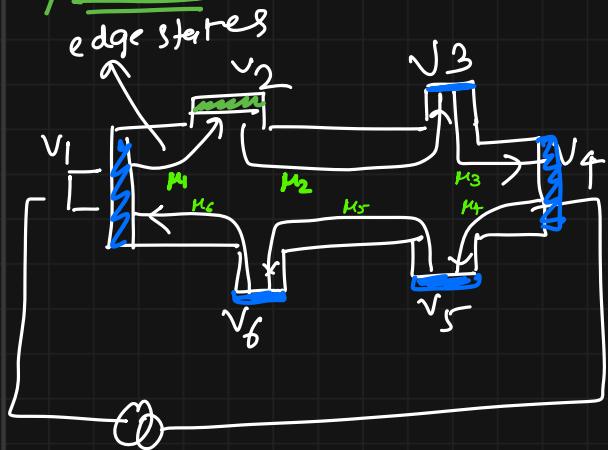
Current conservation

$$\sum_q G_{pq} = \sum_p G_{qp}$$

$$I_p = \sum_q G_{pq} [V_p - V_q]$$

\rightarrow allows us to get different terminal currents (???)

Problems :- come found in Datta's book



$\varphi_{\text{parallel}}$
 $\hookrightarrow = \text{edge states}$

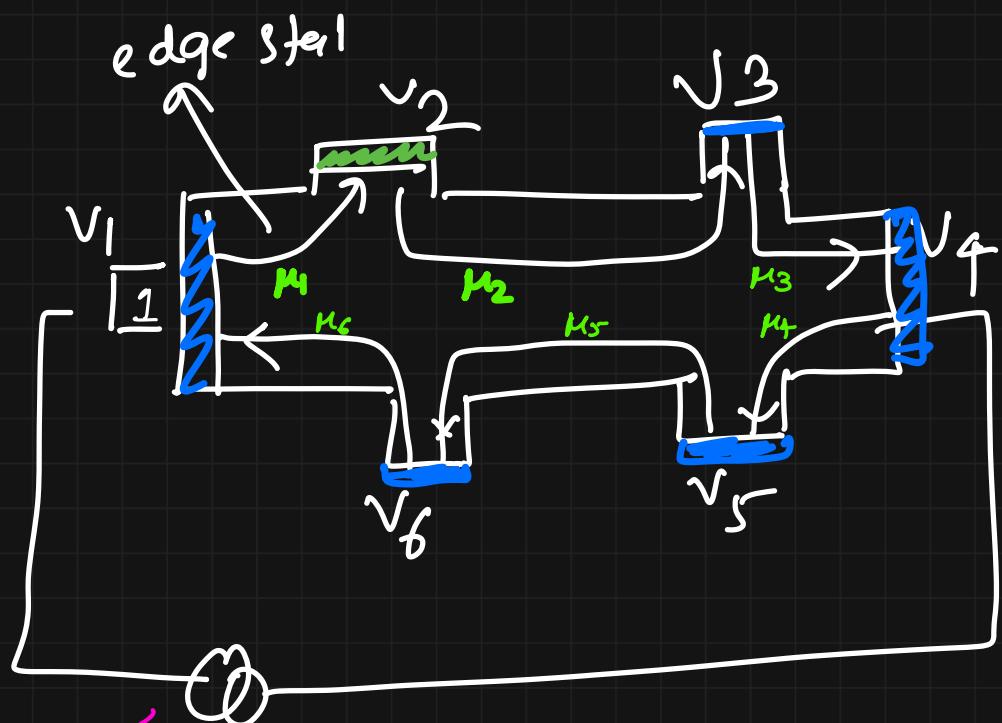
\therefore no net current flow
in this Geometry.

metal contact
equilibrates
an
incoming
electron

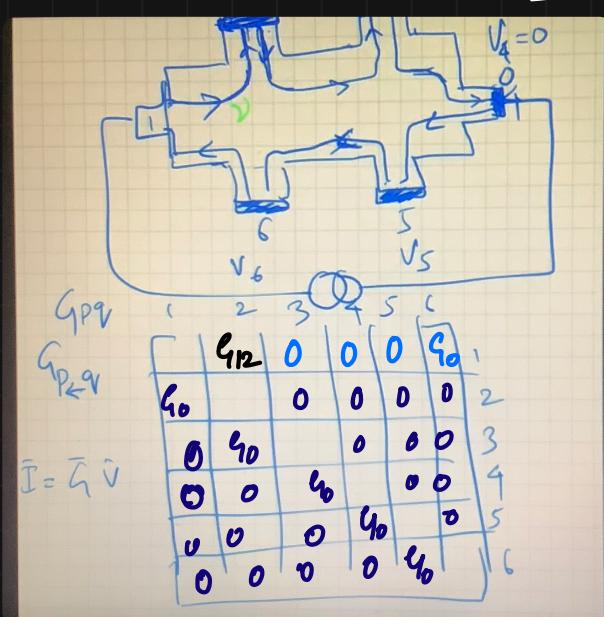


bulk will have edge states & backscatter.
backscattering take

Current source



Current cons.:- ~~$\sum \text{row} = 0$ or $\sum \text{column} = 0$~~



$G_{12} \leftarrow$ transmission
from electrode 2 to 1.

\hookrightarrow edge states \rightarrow chiral

$G_{112} = 0 \rightarrow$ since no states

$G_{\text{matrix}} > 0$ g_0 form
 \hookrightarrow ② to ①

o take only direct transmission

$$G_0 = \nu \left(\frac{2e^2}{h} \right)$$

↓

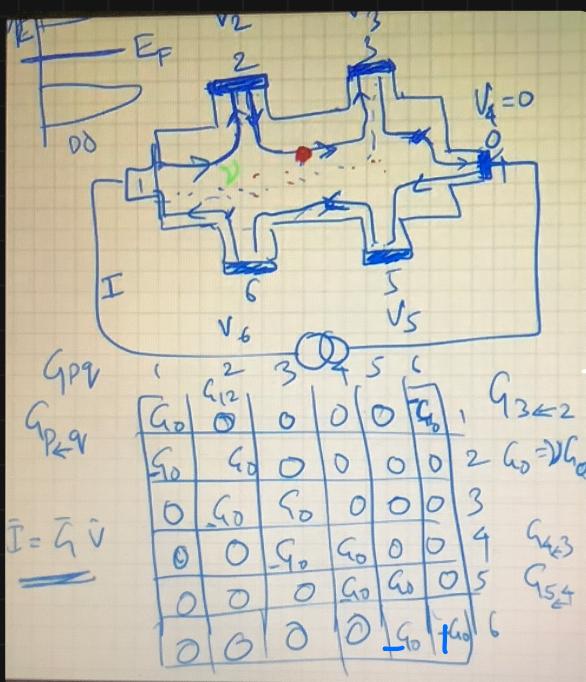
$\nu = \text{filling factor}$

$G_{65} = G_{6 \leftarrow 5}$

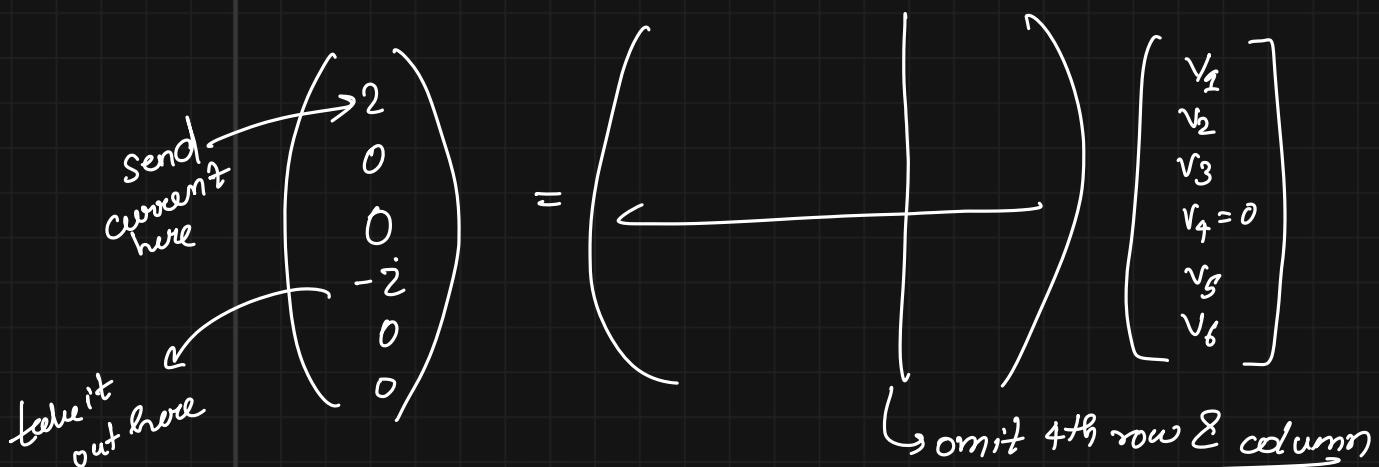
Quantum of conductance

To get current cons, make all row sums & column summations

Label 0.



→ we conserve the current by flipping the sign on an off diagonal element (just a convention)



simple Hall bar 2021nb - Wolfram Mathematica 12.1

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In[1]:= mat = {{(g, 0, 0, 0, 0, -g), (-g, g, 0, 0, 0, 0), (0, -g, g, 0, 0, 0), (0, 0, -g, g, 0, 0), (0, 0, 0, -g, g, 0), (0, 0, 0, 0, g, 0)}, {0, 0, 0, 0, g, 0}, {0, 0, 0, 0, 0, g}, {0, 0, 0, 0, 0, 0}, {0, 0, 0, 0, 0, 0}, {0, 0, 0, 0, 0, 0}}
Out[1]= {{(g, 0, 0, 0, 0, -g), (-g, g, 0, 0, 0, 0), (0, -g, g, 0, 0, 0), (0, 0, -g, g, 0, 0), (0, 0, 0, -g, g, 0), (0, 0, 0, 0, g, 0)}, {0, 0, 0, 0, g, 0}, {0, 0, 0, 0, 0, g}, {0, 0, 0, 0, 0, 0}, {0, 0, 0, 0, 0, 0}, {0, 0, 0, 0, 0, 0}}

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In[2]:= MatrixForm[mat]

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Out[2]= MatrixForm[mat]

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In[3]:= geff = Drop[mat, {4}, {4}]

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Out[3]= {{(g, 0, 0, 0, -g), (-g, g, 0, 0, 0), (0, -g, g, 0, 0), (0, 0, 0, g, 0), (0, 0, 0, -g, g)}}

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In[4]:= Inverse[geff]

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Out[4]= {{1, 0, 0, 1, 1}, {1, 1, 0, 1, 1}, {1, 1, 1, 1, 1}, {0, 0, 0, 1, 0}, {0, 0, 0, 1, 1}}

```

we want to find other voltages

$\Rightarrow \text{Q23} \rightarrow 0$ Longitudinal resistance = 0

hallmark of hall effect

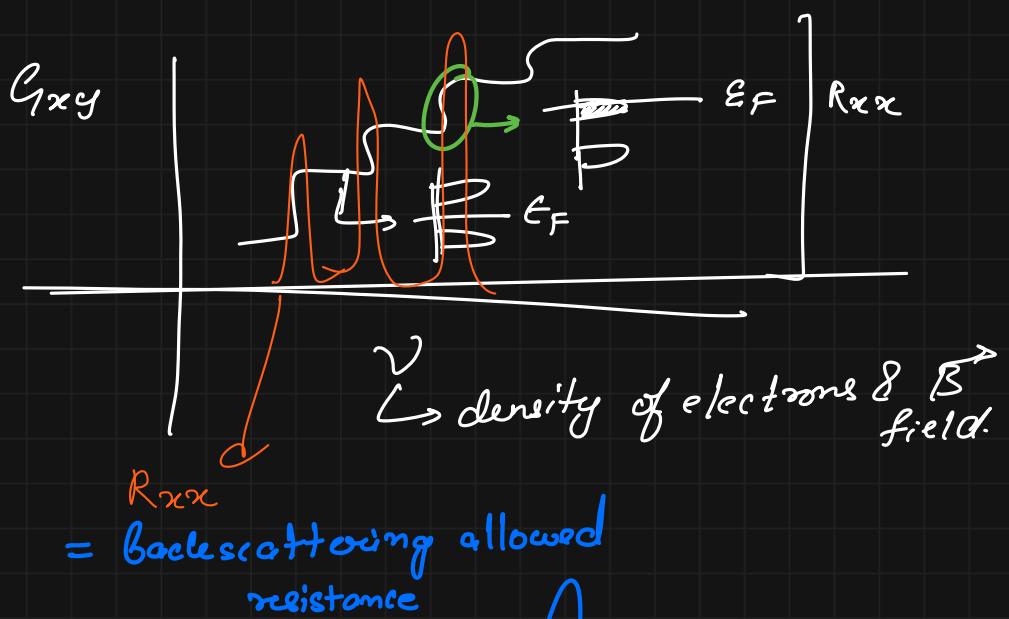
Q Hall hallmark \rightarrow transverse voltage

↳ is same & related to
conductance ↳ filling factors

\Rightarrow no backscattering \rightarrow # of channels are same
 \therefore conductance is same

no density gradient \rightarrow magnetic field has
to be uniform.

\Rightarrow E_F below L levels, then things are complicated.



\curvearrowright exponentially goes to zero

Note:- We currently work at 0 Temp.

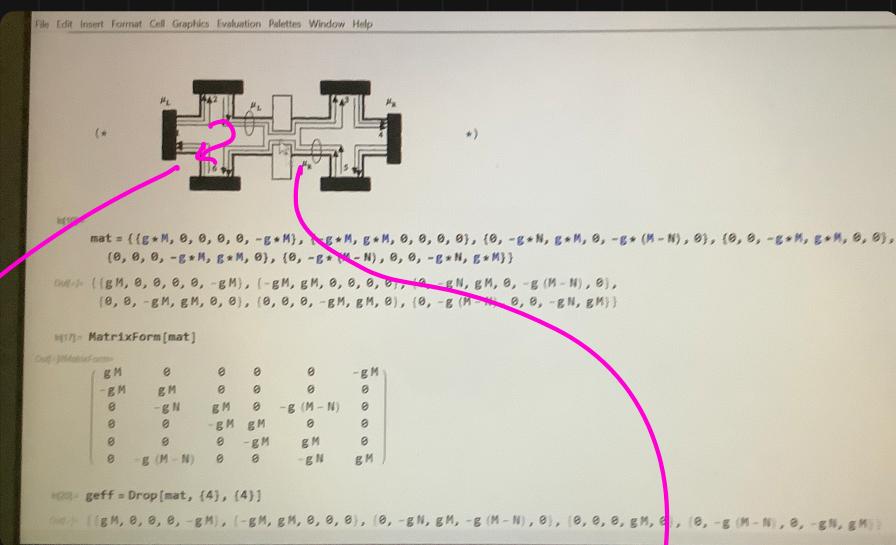
In 2D, resistance \rightarrow conductance matrix transf.'s

↓

tricky

$G_{xx} \rightarrow 0$ in b/w the Landau levels

Example 2 :-



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(*)
*)

mat = ({(g*M, 0, 0, 0, 0, -g*M), {-g*M, g*M, 0, 0, 0, 0}, {0, -g*N, g*M, 0, -g*(M-N), 0}, {0, 0, -g*M, g*M, 0, 0}, {0, 0, 0, -g*(M-N), 0, 0}, {0, 0, 0, 0, -g*N, g*M}}, {(0, 0, 0, 0, 0, -g*M), (0, -g*(M-N), 0, 0, 0, 0), {0, -g*N, g*M, 0, -g*(M-N), 0}, {0, 0, -g*M, g*M, 0, 0}, {0, 0, 0, -g*(M-N), 0, 0}, {0, 0, 0, 0, -g*N, g*M}})

Out[7]= MatrixForm[mat]

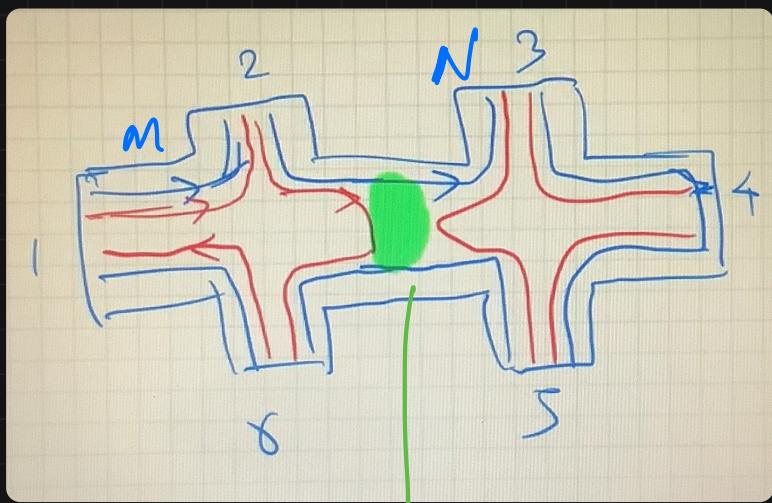
Out[8]= {{gM, 0, 0, 0, 0, -gM}, {gM, gM, 0, 0, 0, 0}, {0, -gN, gM, 0, -g(M-N), 0}, {0, 0, -gM, gM, 0, 0}, {0, 0, 0, -gM, gM, 0}, {0, -g(M-N), 0, 0, -gN, gM}}, {{gM, 0, 0, 0, -gM}, {-gM, gM, 0, 0, 0, 0}, {0, -gN, gM, -g(M-N), 0}, {0, 0, 0, gM, 0}, {0, 0, -g(M-N), 0, -gN, gM}}]

In[9]= geff = Drop[mat, {4}, {4}]
Out[9]= {{gM, 0, 0, 0, -gM}, {-gM, gM, 0, 0, 0}, {0, -gN, gM, -g(M-N), 0}, {0, 0, 0, gM, 0}, {0, -g(M-N), 0, -gN, gM}}

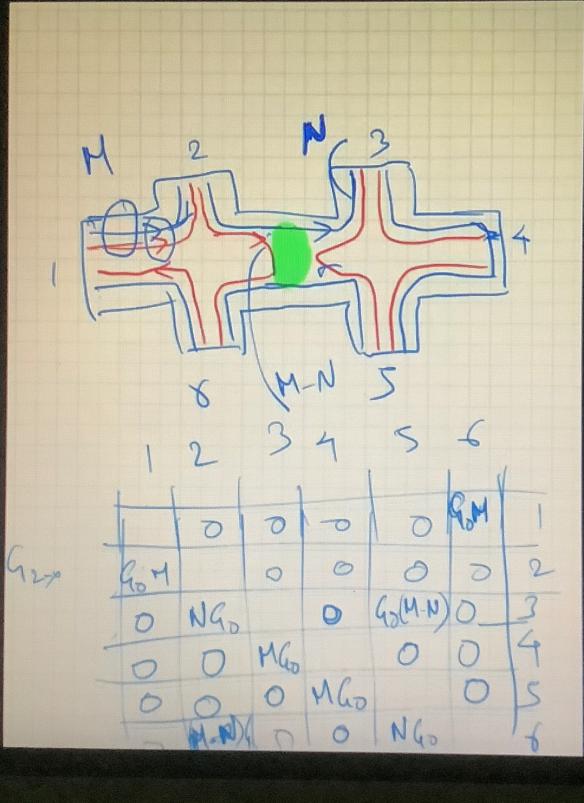
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few edge
modes
shall
get
reflected

charge density is different



region of non-uniform density



G_{2x}	1	2	3	4	5	6	R_M
R_M	0	0	0	0	0	0	1
R_M	0	0	0	0	0	0	2
0	NG_0	0	0	$G_0(M-N)$	0	0	3
0	0	MG_0	0	0	0	0	4
0	0	0	MG_0	0	0	0	5
0	0	0	0	NG_0	0	0	6

