

Next week last class fuck!! (exam probably at end of this month)

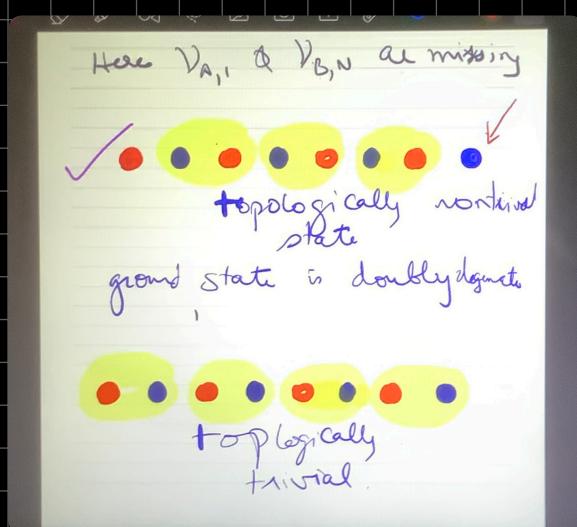
Topological Superconductivity

Majorana fermions in condensed matter

[Easiest realization in a Quantum vortex in a $\text{Pb}^{1-x}\text{Bi}_x$ superconductor
expt = 2/3 years earlier]

[Kitaev's toy model :- Spinless β -wave SC
exciton on the boundary = linear combination of
fermionic operators.]

Here $\nu_{A,\downarrow}$ & $\nu_{B,N}$ are missing



SOC + Superconductor

\Rightarrow Primary \Rightarrow Qubits that have
some
topological protection.

@ Microsoft, @ Google, @ IBM

Weyl Semi-metals :-

→ what are weyl "particles/exitations" from high en. physics?

→ "Bulk itself is conducting" → what are the interesting properties of weyl particles

- Chiral anomaly

Reference
RMP
Vanderbilt book

→ flow does one realize a weyl hamiltonian in cold matter systems

→ Role of symmetry → Dimensions = odd (1 or 3)

→ Berry Curvature hotspots → Surface states /

Fermi arcs

→ expt tests

→ ARPES

→ transport

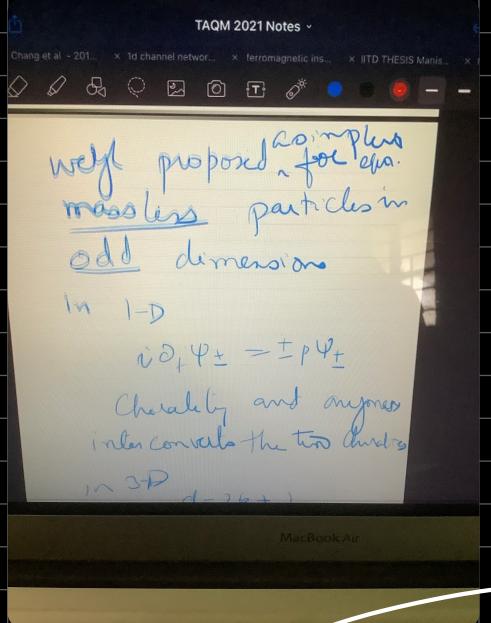
→ Majorana with Weyl

→ "Topological" weyl Superconductors

VANDERBILT

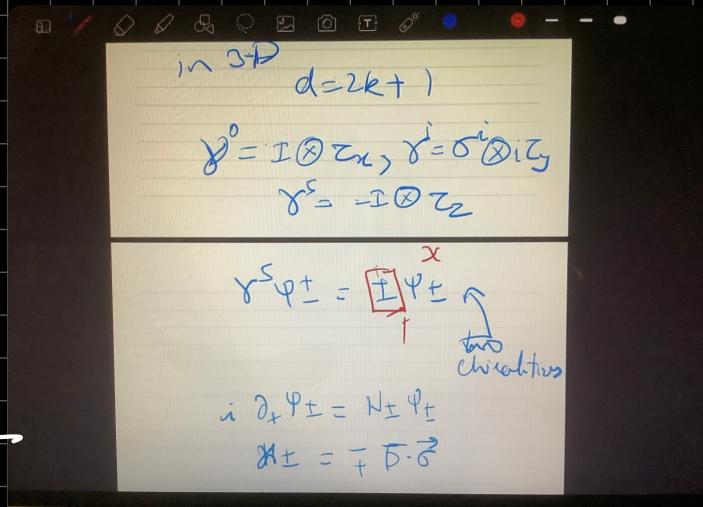
* Weyl from high energy physics.

Dirac eqn \Rightarrow



Chirality of the system

in 3D



two chiralities $\rightarrow \pm 1$ $\gamma^5 \Psi_\pm = \pm \Psi_\pm$

no real particles are identified as coWeyl fermions.

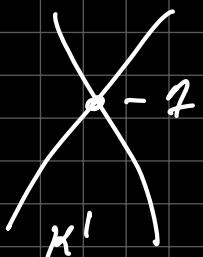
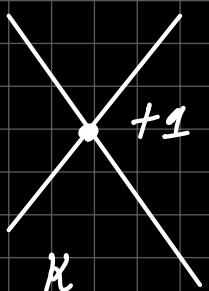
Weyl fermions propagate parallel or antiparallel

to their spin.

Chirality

2 of them come in pairs

\Rightarrow linear dispersion in 3 dimensions



\Rightarrow might seem like
Graphene

\Rightarrow "effective low energy Hamiltonian" \rightarrow graphene Circularly symmetric

Chiral Anomaly

large en.
scale

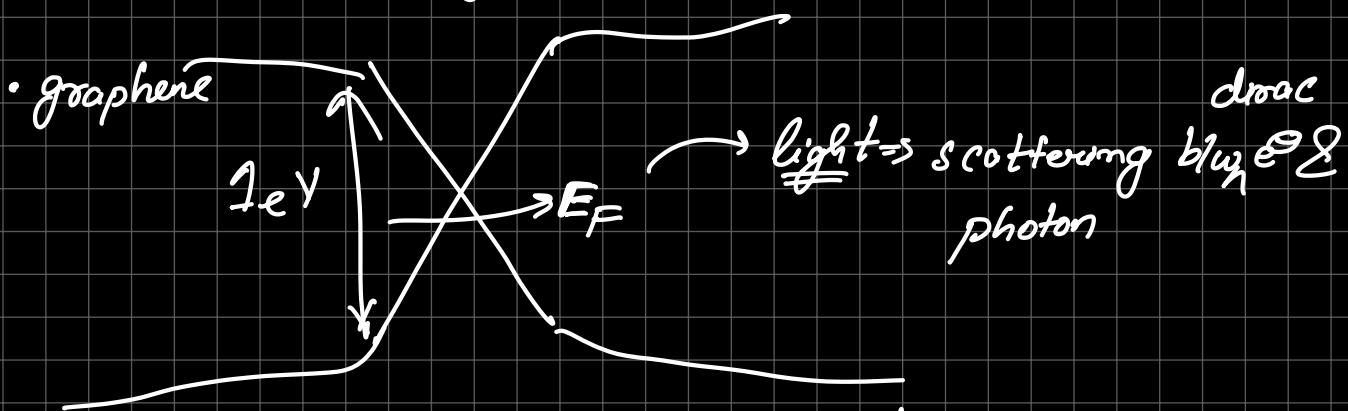
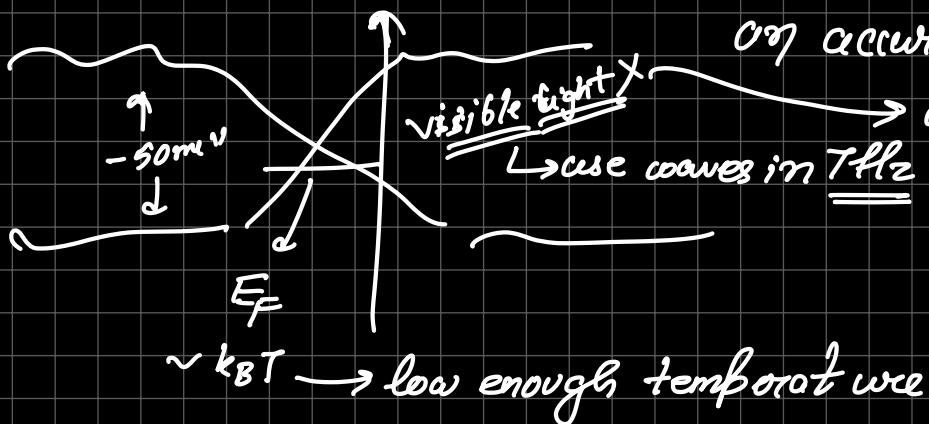
but for $\omega \ll \Gamma$, β is smaller

(~ 50 meV) over which it's linear.
 \Downarrow

"System specific"

- β is an energy scale over which its on accurate description of reality

will easily probe the large en. physics



"not a description of all quasiparticles at all energies."

Quasiparticles

"emergent excitation
of a system."

Chiral Anomaly

$$\partial_\mu j^\mu = 0 \quad \& \quad \partial_\mu j^\mu 5 = 0 \quad \rightarrow \text{conversion b/w right handed to left handed}$$

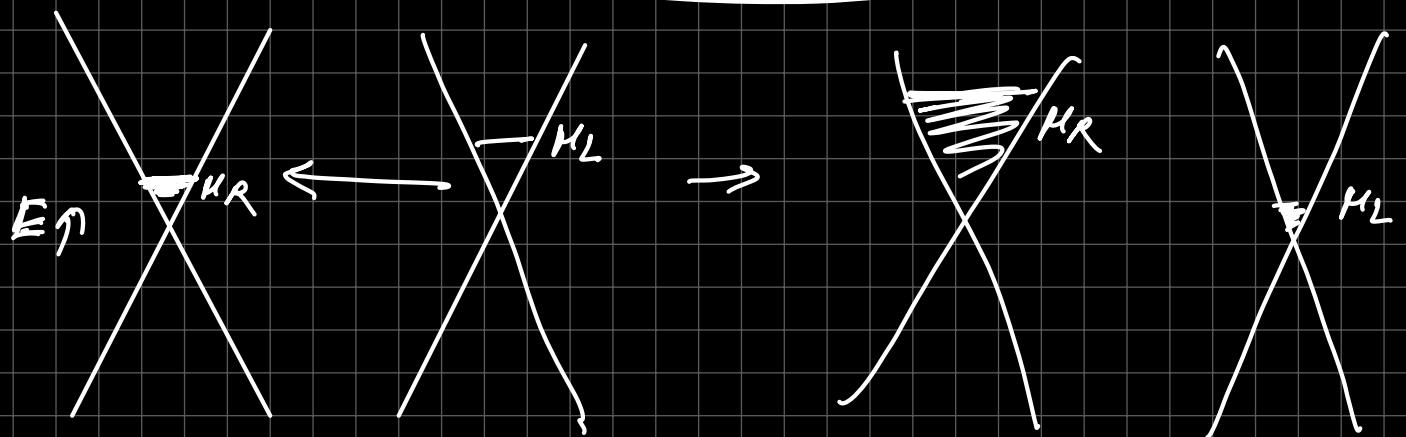
\hookrightarrow independently of left or right handed
every fermions aren't conserved.

$\partial \mu \neq 0 \Rightarrow$ Cons. of each species isn't possible
 \rightarrow conv. b/w right handed to left handed
weyl fermions.

"Total # of
spins ↑ resp. ↓ is
cons."

$$\partial_L (n_R + n_L) = 0$$

$$\partial_L (n_R - n_L) \neq 0$$



Total # is still
conserved.

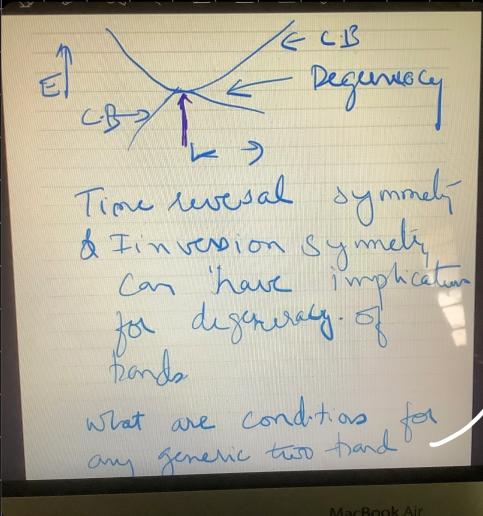
Smoking Gun confirmation

"Chiral anomaly"

\rightarrow ARPES :- Bandstructure

Cond mat realization of Weyl Hamiltonian.





\rightarrow Hamiltonian to touch

$$H_0(k) =$$

What are conditions for
any generic two hand

Hamiltonian to touch

$$h(k) = f_0(k)\mathbb{I} + f_1(k)\delta_n \\ \quad \quad \quad + f_2(k)\delta_y \\ \quad \quad \quad + f_3(k)\delta_z$$

nothing to do
with spine just

two hands

To bring two bonds into
one, keep the set

$$h(k) = f_0(k)\mathbb{I} + f_1(k)\vec{\sigma}_n \\ \qquad\qquad\qquad + f_2(k)\vec{\sigma}_y \\ \qquad\qquad\qquad + f_3(k)\vec{\sigma}_z$$

two hands

To bring two bonds into coincidence. $r_1 = r_2 = r_3 = 0$

One Care creates a WSM
Profile

At certain points in k -space, then we "get" a wavy cone.

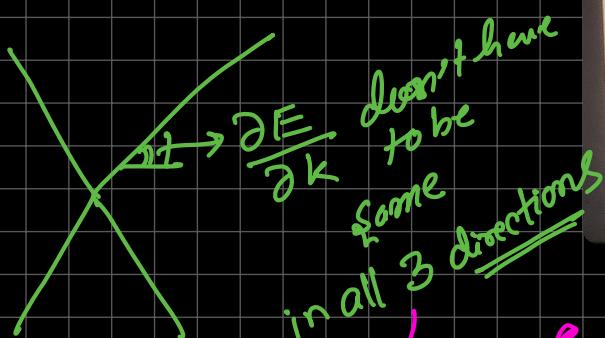
non-degenerate bands and
breaking symmetries

Now we write hamiltonian
in the effective low-energy
form

$$H(k) \sim f_0(k_0) \mathbb{I} + U_0 \cdot \delta k \mathbb{I}$$

$$+ \sum_{\alpha \neq x, y, z} U_\alpha \cdot \delta k^\alpha$$

In general in C.H.
realizations of WSM



nt₃ invasions may not be obtained

why do Weyl nodes
occur in pairs

$$C_2 + 1 \times \cancel{X} \quad \cancel{X} \times C_{-1}$$

• Chirality ($\equiv \text{Sgn}(V_x \cdot V_y \times V_z)$)
integrated
over B.Z., Berry curvature

maintained.

$\propto B \cdot \epsilon$

why do Weyl nodes
occur in pairs

$$C_2 + 1 \times \cancel{X} \quad \cancel{X} \times C_{-1}$$

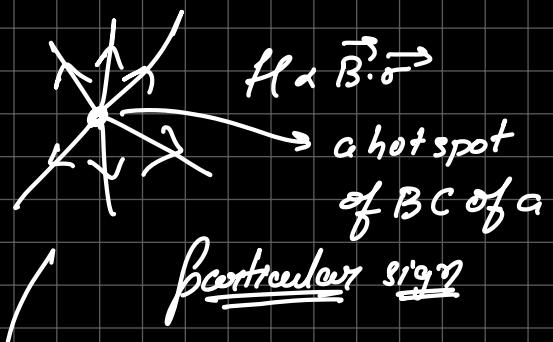
• Chirality ($\equiv \text{Sgn}(V_x \cdot V_y \times V_z)$)
integrated
over B.Z., Berry curvature

Another node \rightarrow existence
 $C =$

IRT + TRS

Net BC = 0

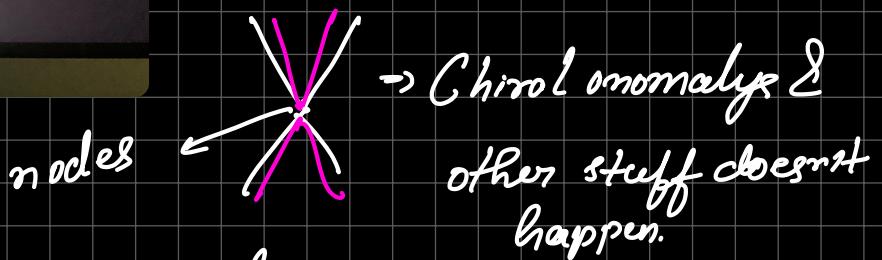
"physically justified way to
argue for it is net Osam
of B.C."



if $C=0$, then another
hotspot of opposite sense has to
be here.

Two Weyl nodes are sitting
on top of each other.

\hookrightarrow "Dirac semi-metals"



\Rightarrow Weyl nodes = must occur in "pairs"

\hookrightarrow simple argument $\Rightarrow \int BC d^2r = 0$

Lattice models of Weyl fermions

Chirality.

In general

$$H = \sigma_z L(\sigma, k) + m\sigma_x + b\sigma_z$$

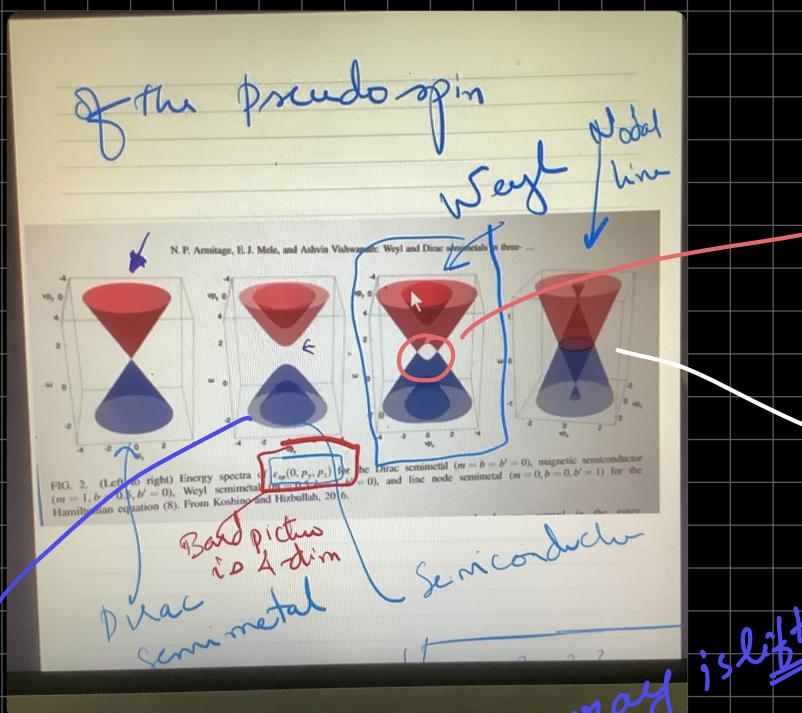
$$+ b' \sigma_z \delta_{\sigma}$$

$$= \begin{pmatrix} m\sigma_x + b\sigma_z & L(\sigma, k) \\ L(\sigma, k) & -m\sigma_x - b\sigma_z \end{pmatrix}$$

where σ are Pauli matrices

as b, b' are varied, mimics all kinds of band str.
at some point \exists Weyl nodes

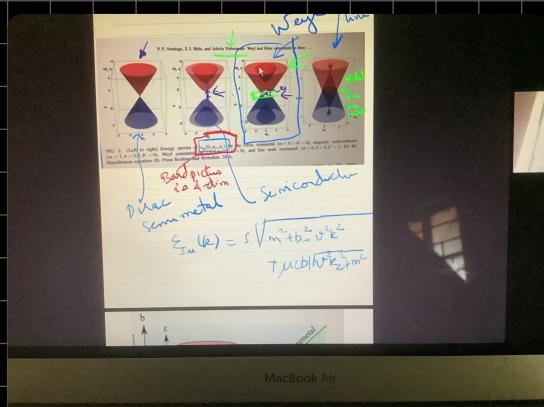
@ Armitage's paper



Touching fint is a circle/loop
Projected surface shown here

"nodal line semimetal"

magnetic SC
↑↓ degeneracy



"Band touching
are extremely
common" → what en. window is it a linear approximation
good?

Touching shouldn't be
buried under the
fermi energy