

Truth bomb :- Berry Curvature can be measured even at room temperatures.

Recap :- ① B.curv. affects electron dynamics

$$\textcircled{2} \quad T_H = \gamma \frac{e^2}{\eta}$$

Chern #  $\Rightarrow$  is going to be integer

③ Symmetry properties

$$\begin{aligned} -\Omega(\vec{k}) &= -\Omega(-\vec{k}) & TR \\ -\Omega(\vec{k}) &= -\Omega(-\vec{k}) \\ \rightarrow \underline{\underline{\Omega(\vec{k}) = 0}} \end{aligned}$$

$C \neq 0$

only when TRS is broken

Today's agenda :- Valley Hall effect in MoS<sub>2</sub>

↓  
detection of Hall effect

Cousin of  
graphene

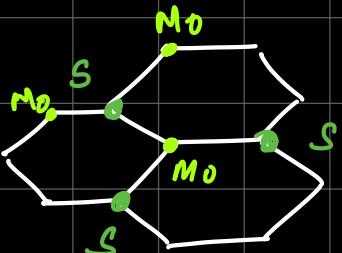
→ graphene like system, honeycomb lattice

⇒ "has Gap" 2 in #

⇒ turns out valleys have opposite Berry curvature.

↓  
electrons belonging to 1 valley get deflected to 1 side

→ electrons on other side get deflected to other side.



Spirited off 1 layer, it's gas 3 layers



one molecule  
brick  
not 1 atom  
brick as in graphene

$\therefore \omega(\vec{k}) \neq 0$  [We know that it'll happen,  
dirac eqn]

$\Rightarrow TB$

$\Rightarrow$  effective hamiltonian.

$\delta$   $\rightarrow$  essentially  
separates into  
 $-\delta$   $\pi + \Delta$

```
In[17]:= MatrixForm[ham]
Out[17]/MatrixForm=

$$\begin{bmatrix} \delta & e^{i\sqrt{3}k_x} + e^{i(-\frac{\pi}{2} - \frac{1}{2}\sqrt{3}ik_y)} & e^{i\sqrt{3}k_x} + e^{i(-\frac{\pi}{2} - \frac{1}{2}\sqrt{3}ik_y)} & e^{i\sqrt{3}k_x} + e^{i(\frac{\pi}{2} + \frac{1}{2}\sqrt{3}ik_y)} \\ e^{i\sqrt{3}k_x} + e^{i(-\frac{\pi}{2} - \frac{1}{2}\sqrt{3}ik_y)} & \delta & e^{i(-\frac{\pi}{2} - \frac{1}{2}\sqrt{3}ik_y)} & e^{i(\frac{\pi}{2} + \frac{1}{2}\sqrt{3}ik_y)} \\ e^{i\sqrt{3}k_x} + e^{i(-\frac{\pi}{2} - \frac{1}{2}\sqrt{3}ik_y)} & e^{i(-\frac{\pi}{2} - \frac{1}{2}\sqrt{3}ik_y)} & \delta & e^{i(\frac{\pi}{2} + \frac{1}{2}\sqrt{3}ik_y)} \\ e^{i\sqrt{3}k_x} + e^{i(\frac{\pi}{2} + \frac{1}{2}\sqrt{3}ik_y)} & e^{i(\frac{\pi}{2} + \frac{1}{2}\sqrt{3}ik_y)} & e^{i(\frac{\pi}{2} + \frac{1}{2}\sqrt{3}ik_y)} & \delta \end{bmatrix}$$

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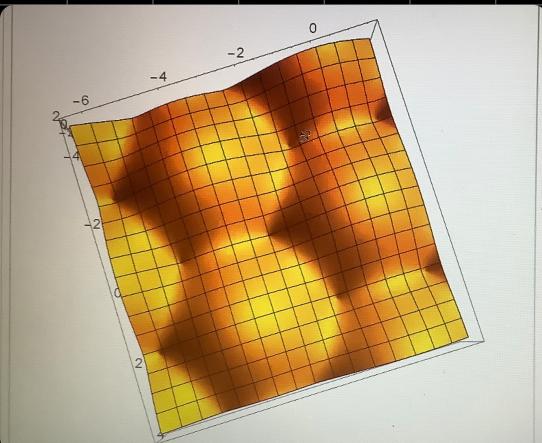
```
In[31]:= Out[31]=  $\left\{ -\frac{i}{2} - \frac{1}{2}i e^{-\frac{2i\pi}{3}} + i e^{\frac{2i\pi}{3}}, \frac{i\sqrt{3}}{2} - \frac{1}{2}i\sqrt{3}e^{-\frac{2i\pi}{3}} \right\}$ 
```

```
In[32]:= hamapprox = {{\delta, comp, {qx, qy}}, {comp2, {qx, qy}, -\delta}};
Out[32]=  $\left\{ \left\{ \delta, \left( -\frac{i}{2} - \frac{1}{2}i e^{-\frac{2i\pi}{3}} + i e^{\frac{2i\pi}{3}} \right) qx + \left( \frac{i\sqrt{3}}{2} - \frac{1}{2}i\sqrt{3}e^{-\frac{2i\pi}{3}} \right) qy \right\}, \left\{ \left( -\frac{i}{2} - \frac{1}{2}i e^{-\frac{2i\pi}{3}} + i e^{\frac{2i\pi}{3}} \right) qx + \left( \frac{i\sqrt{3}}{2} - \frac{1}{2}i\sqrt{3}e^{-\frac{2i\pi}{3}} \right) qy, -\delta \right\} \right\}$ 
```

```
In[33]:= MatrixForm[FullSimplify[hamapprox]]
Out[33]/MatrixForm=

$$\begin{pmatrix} \delta & -\frac{3}{4}(i + \sqrt{3})(qx - i qy) \\ -\frac{3}{4}(i + \sqrt{3})(qx - i qy) & -\delta \end{pmatrix}$$

```



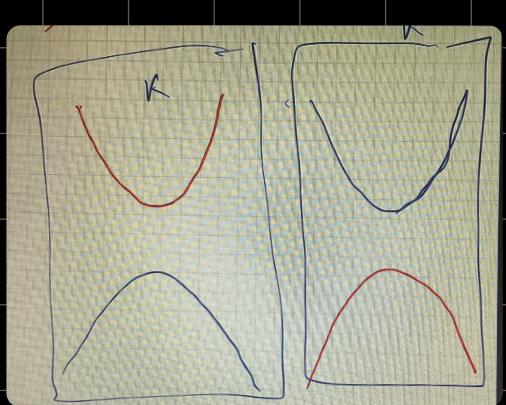
will be different for  
both valleys  $\rightarrow$  dispersion is same

graphene lightbinding effective hamiltonian with mass term 2021.nb \* - Wolfram Mathematica 12.1

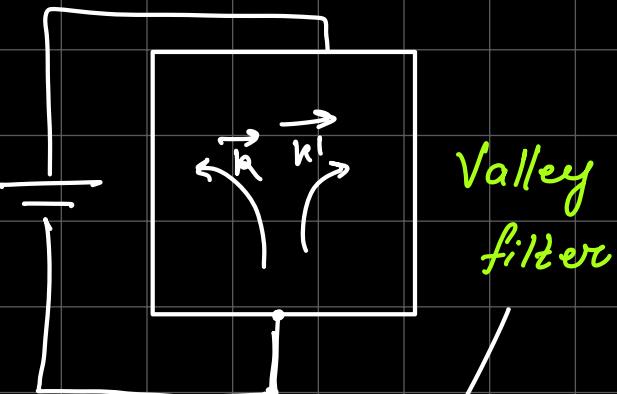
```
In[40]:= MatrixForm[FullSimplify[hamapprox2]]
Out[40]/MatrixForm=
```

$$\begin{pmatrix} \delta & -\frac{3}{4} (i + \sqrt{3}) (qx + i qy) \\ -\frac{3}{4} (i + \sqrt{3}) (qx + i qy) & -\delta \end{pmatrix}$$

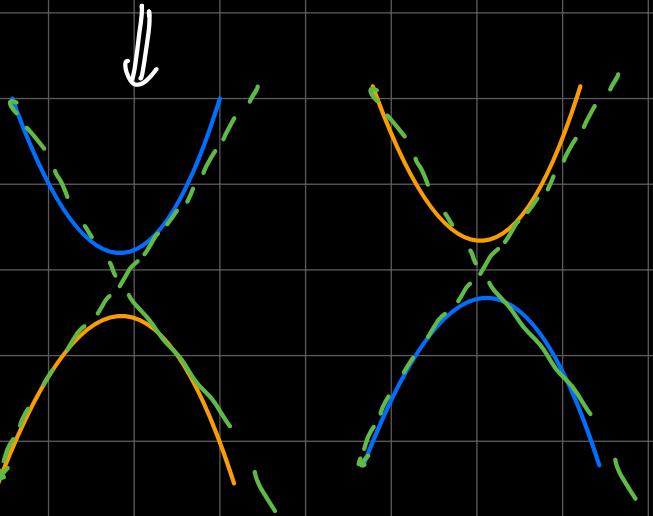
$\therefore$  CB band in  $\bar{K}$  valley  
has some eigenvector as  
VB in the other valley.



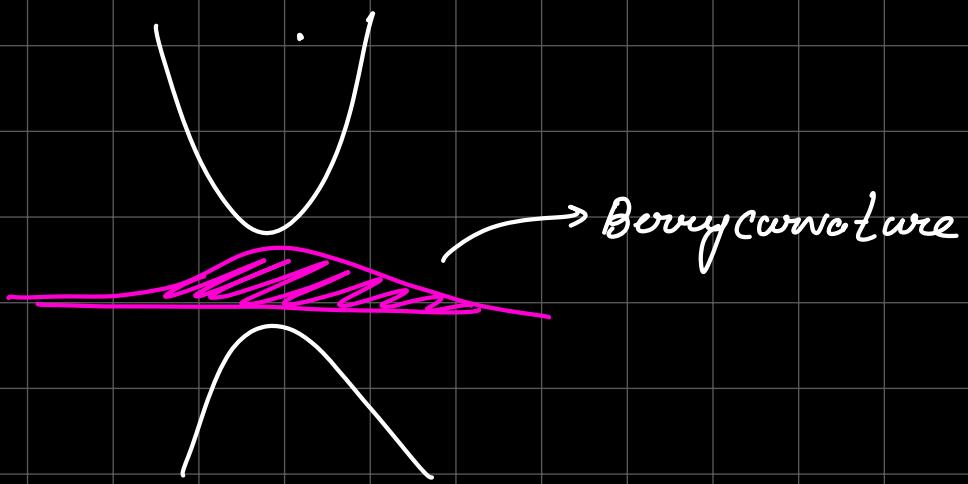
$\rightarrow$  2 → on one valley  
 $\rightarrow$  2 → on another valley



For graphene  $\Rightarrow I_R + T_{RS}$   
 $\Downarrow$   
B. Curv. is 0.  
 happens only  
 because the  
 Berry curvature  
 is non-zero



Check  
only that  
state possesses  
Berry curvature  
 $\rightarrow$  however DDE is 0 here.

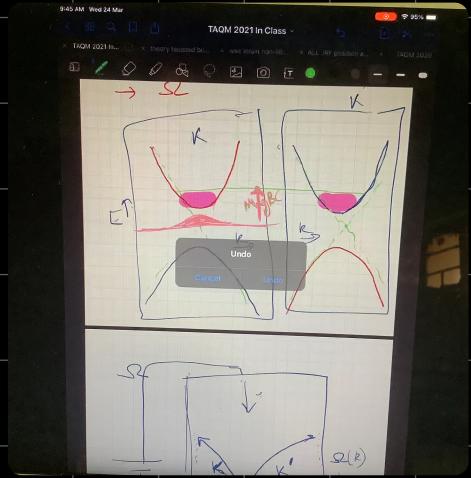
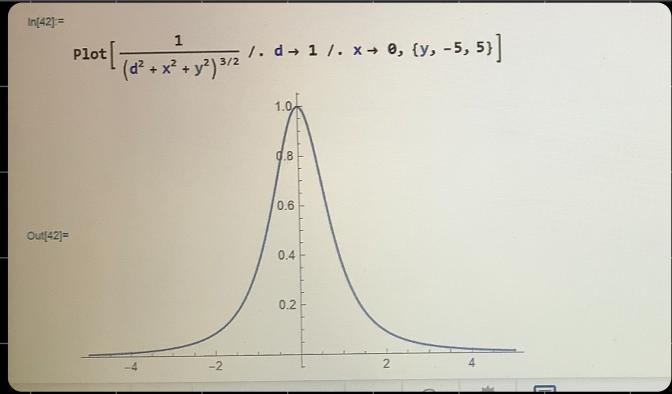


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```
In[4]:= berrycurvature = Im[bc[[3]] / ((2) * Sqrt[d^2 + x^2 + y^2])^2]
Out[4]= -1/2 Re[d r / (d^2 + x^2 + y^2)^{3/2}]

In[5]:= Integrate[d r / (2 (r^2 + d^2)^{3/2}), {r, 0, Infinity}, {t, 0, 2 \pi}]
Out[5]= \frac{d \pi}{Abs[d]} if d \neq 0

In[6]:= Integrate[d r / (2 (r^2 + d^2)^{3/2}), {r, 0, r \theta}, {t, 0, 2 \pi}]
Out[6]= d \pi \left(-\frac{1}{Sqrt[d^2 + r \theta^2]} + \frac{1}{Abs[d]}\right) if d \neq 0 \& Re[r \theta] \geq 0 \& Im[r \theta] = 0
```



Cute trick  $\Rightarrow$

shine circularly polarized light couples to 1 valley  $\rightarrow$  hence creates an imbalance

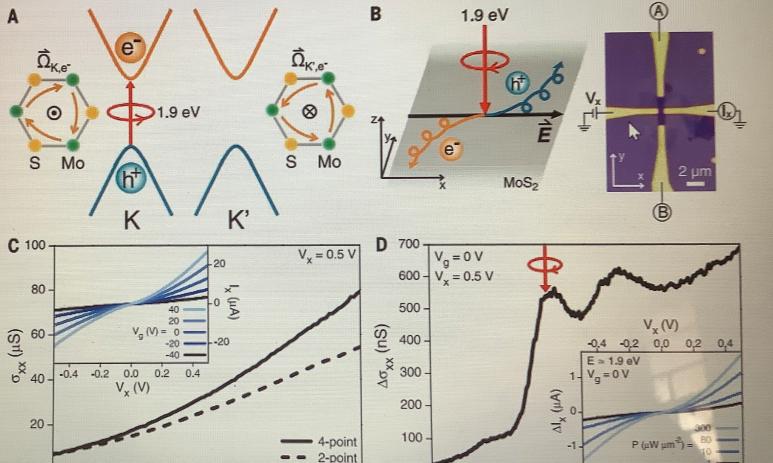
valley  $\rightarrow$  imbalance

valley coupled now due to unequal # of charge carriers in 2 valleys, we measure a voltage difference.

the possible strong (29) on-current injection of valley-polarized carriers (II, 29). Shown in the inset is the photocurrent  $\Delta I_x$  as a function of  $V_g$  at  $V_g = 0$  V under different laser excitation intensities.

from right- to left-handed, or  $\theta = -45^\circ$ , in which the polarization is modulated from left- to right-handed, we use the notations R-L and L-R below, of a net valley polarization under the optical excitation of the A resonance with circularly polarized light (10–14). The sine dependence of

**Fig. 1. Monolayer MoS<sub>2</sub> Hall bar device.** (A) Schematics of the valley-dependent optical selection rules and the electrons at the K and K' valleys that possess opposite Berry curvatures  $\vec{\Omega}$ . The orange arrows represent the clockwise and counterclockwise hopping motions of the K and K' electrons. (B) Schematic of a photoinduced AHE driven by a net valley polarization (left) and an image of the Hall bar device (right). In the schematic, the intrinsic plus side-jump contribution as predicted by Eq. 1 is shown. (C) Two-point (dashed line,  $V_g = 0.5$  V) and four-point (solid line) conductivities of the device as a function of back gate voltage  $V_g$ . (D) Inset) Source-drain bias ( $V_s$ ) dependence of the current along the longitudinal channel ( $I_x$ ) at



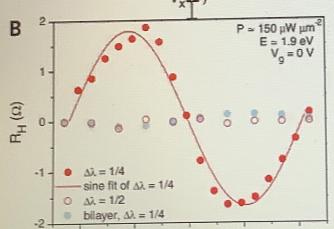
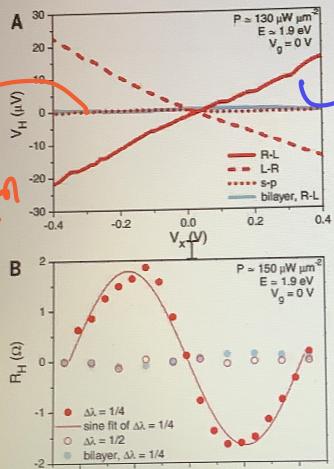
under on-resonance excitation and is shown in Fig. 2A [electrical characterization of our bilayer device is provided in (29), section 2.7]. No noticeable Hall voltage (more than a factor of 10

intervalley population imbalance) can drive the AHE. No such imbalance can be produced in bilayer MoS<sub>2</sub> (4–6) because the inversion symmetry is restored in its crystal structure (II, 14, 31).

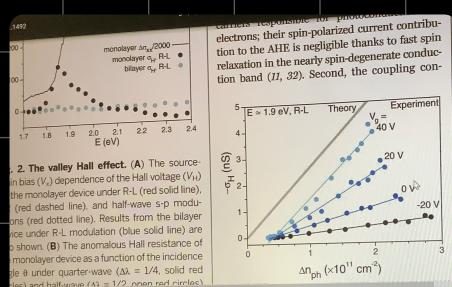
Last, the effect of the intervalley relaxation of excited carriers on the monolayer MoS<sub>2</sub> monolayers is depicted in Fig. 3. The dependences of the anomalous Hall conductivity  $\sigma_H = \sigma_{\text{AHE}} + \sigma_{\text{H}} \sigma_{\text{xx}}$  and of the change in conductivity  $\Delta \sigma_{\text{xx}}$  on the incident photon energy  $E$  are shown. Whereas  $\Delta \sigma_{\text{xx}}$  remains large and keeps increasing with increased photon energy beyond the A and B resonances (thank to an enhancement in optical absorption), the anomalous Hall conductivity  $\sigma_H$  peaks near the A feature and decreases quickly to almost zero at higher photon energies. Our observation is consistent with recent optical results that indicate poor injection of valley polarization under off-resonance excitation because of the rapid intervalley relaxation of high-energy excited carriers (II, 29). For comparison, no detectable Hall conductivity is observed in the bilayer device (Fig. 2C, blue dots).

Our experimental observation of a finite AHE only in monolayer MoS<sub>2</sub> under on-resonance, circularly polarized excitation strongly supports our interpretation of the signal as originating from the VHE. Whereas a net spin polarization could also give rise to a finite AHE, the effect

intensity ( $P$ ) dependence of the photoinduced AHE under 1.9 eV excitation. For this, we measured the gate dependence of the AHE under different incident laser powers [(29, 32)]. The effective change in the photoinduced carrier density  $\Delta n_{\text{ph}}$  can then be estimated using the relation  $\Delta \sigma_{\text{xx}} = \Delta n_{\text{ph}} \sigma_H$ , where  $\sigma_H$  is extracted from the dark electrical measurement (Fig. 1C) with  $C_g = 1.2 \times 10^{-8} \text{ F cm}^{-2}$  the gate capacitance of our device ( $\Delta n_{\text{ph}}$  is difficult to measure with conventional methods because of a large background density and finite longitudinal-trapping in our devices). The quantity  $\Delta \sigma_{\text{xx}}$  is equal to  $\Delta n_{\text{ph}}$  if the change in conductivity is solely driven by the valley-polarized carriers that are directly excited by resonance polarized light. In reality, however, it includes contributions from both valley and unpolarized carriers; therefore, it provides an upper bound for  $\Delta n_{\text{ph}}$ . The Hall conductivities under R-L modulation at different gate voltages  $V_g$  are shown as a function of  $\Delta n_{\text{ph}}$  in Fig. 3. We also show the theoretical result predicted by Eq. 1 in the line in the same figure. For all gate voltages,  $\sigma_H$  increases linearly with  $\Delta n_{\text{ph}}$ , which is in agreement with the theoretical prediction. The anomalous Hall conductivity  $\sigma_H$  also has the



bilayer MoS<sub>2</sub> → doesn't break Inv. symmetry  
bilayer MoS<sub>2</sub> → breaks Inv. symmetry  
Trilayer MoS<sub>2</sub> → breaks Inv. symmetry



So Berry phase/curvature have been tested in expt settings.

Buzz words → berry curvature dipole

$\Downarrow$   
 strain  $\rightarrow$  uniaxial strain  $\rightarrow$  if Berry curvature hotspots don't cancel each other.

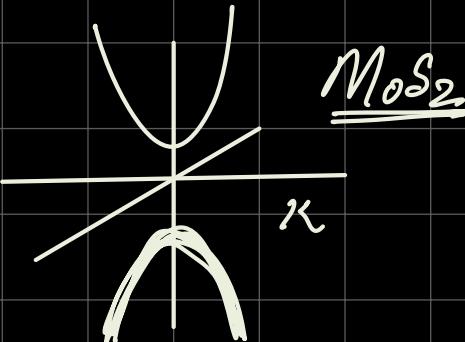
Comment  
 hotspots of BC are just at the degeneracy points & hence don't affect stuff at large k points.

### MoS<sub>2</sub> Day Ralph problem

$$H_K = \delta \sigma_2 + v_f (\sigma_x k_x + \sigma_y k_y) \rightarrow IR^{\checkmark}, TRSX$$

$$H_K' = \delta \sigma_2 + v_f (-\sigma_x k_x + \sigma_y k_y) \rightarrow IR^{\checkmark}, TRSX$$

$$\underline{K} = H = \begin{pmatrix} \delta & v_f (k_x - iky) \\ v_f (k_x + iky) & -\delta \end{pmatrix}$$



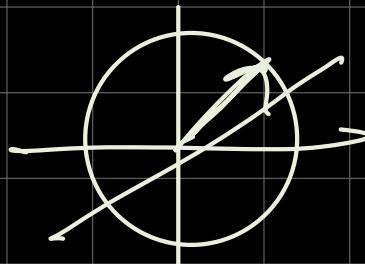
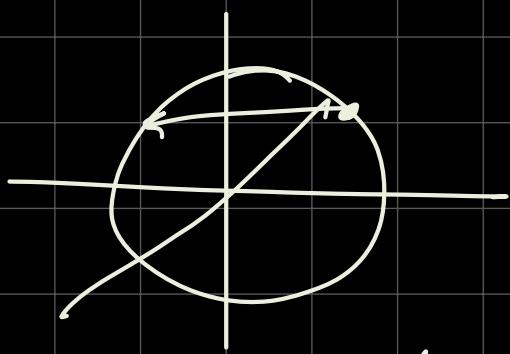
$$\mathcal{E} = \pm \sqrt{v_f^2 (\vec{k} \cdot \vec{k})_{2D} + \delta^2}$$

$$\underline{BC}: P = |E_F| \quad H = P \begin{bmatrix} \cos \theta & \sin \theta e^{-i\phi} \\ \sin \theta e^{i\phi} & -\cos \theta \end{bmatrix}$$

$$e^{\nu} = \left| \uparrow \right\rangle = \begin{pmatrix} e^{-i\phi} \cos \theta / 2 \\ \sin \theta / 2 \end{pmatrix}_{\frac{1}{\sqrt{2}}} \quad \left| \downarrow \right\rangle = \gamma \left| \nu_1 \right\rangle = \begin{pmatrix} + \sin \theta / 2 \\ -e^{i\phi} \cos \theta / 2 \end{pmatrix}$$

where  $\cos\theta = \frac{S}{E_+}$

$$\frac{v_f^2(k_x^2 + k_y^2)}{E_+^2} = |\sin\theta|$$



~~Position space~~  
 $\sin\theta \approx \pm \sin\phi$

$\phi \rightarrow \phi + \pi$

$$|\Psi\rangle = \begin{pmatrix} e^{-i\phi} \cos\theta/2 \\ \sin\theta/2 \end{pmatrix} \times \frac{1}{\sqrt{2}}$$

$$A_\phi = \left(\frac{1}{2}\right) \cos^2\theta/2$$

$$A_\theta = 0$$

$$F_{\theta\phi} = \frac{\partial A_\theta}{\partial \phi} - \frac{\partial A_\phi}{\partial \theta} = +\cos\theta/2 \left(\frac{1}{2}\right) \sin\theta/2 = \frac{1}{4} \sin\theta$$