

ASEN 5050 - HW2 (Pg2) GUST AND Grinsteins 02/02/2021

P1) b) (ont. Velocity Vetor in Rotating frame:

$$\frac{3}{7} = \sqrt{\frac{2}{n}} - \frac{4}{n} = \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} - \frac{4}{n} = \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} = \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} = \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}} = \sqrt{\frac{2}{n}} - \sqrt{\frac{2}{n}}$$

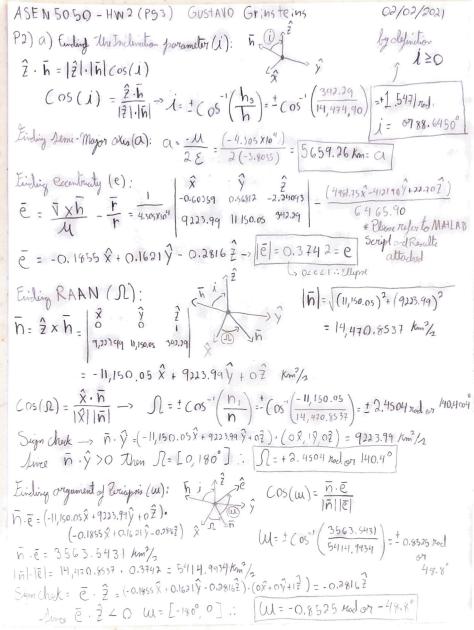
$$|\vec{r}| = \sqrt{(4981.75)^2 + (-4121.90)^2 + (22.70)^2} = 6465.90 \text{ km}$$

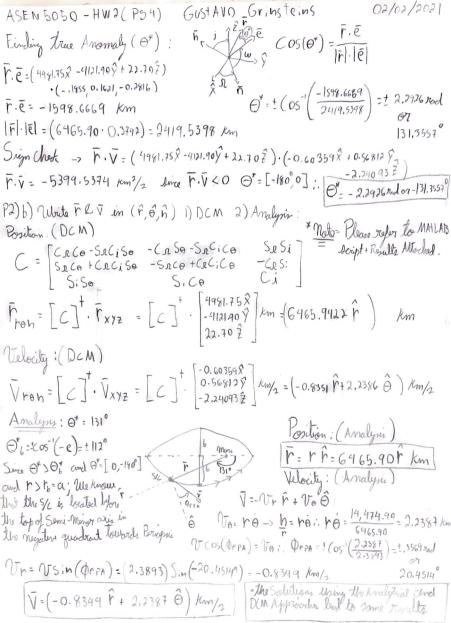
$$|\vec{V}| = \sqrt{(-0.60359)^2 + (0.56812)^2 + (-2.24093)^2} = 2.3893 \text{ km/2}$$

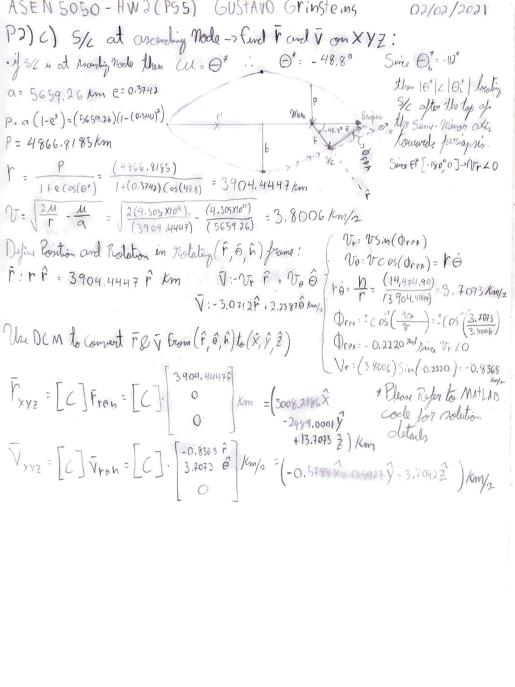
$$|\vec{r} \times \vec{V}| = \vec{h} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ 4991.75 & -4121.90 & 22.70 \\ -0.60359 & 0.56812 & -2.24093 \end{vmatrix} = 9.223.99 \hat{x} + 11,150.05 \hat{y} + 342.29 \hat{z} + 12.29 \hat{z} + 12$$

 $\mathcal{E} = \frac{\eta r^2}{2} - \frac{\mathcal{K}}{r} = \frac{(2.3893)^2}{2} - \frac{(4.305 \times 10^4)}{(6465.90)} = -3.8035 \, \text{Km}^2/2^2$ 

02/02/2021







ASEN 5050 - HW2 (P96) GustAVO Grinsteins 02/02/2021 PZ) d) Shotch orbid of MAVEN using a, e, 1, 2, w, 0\* · 1:89.6 · RAAN (SL)= 140.4) · A OP (w) = -44.8° i(Individion) 7 (Time of moder) · 0\* =-131.3° Harry WYNEN Ascirding Mocle W(AOP) E (Recentricity) D(RAAN)

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Problem 2 Part A
r is 6465.94 \text{ Km}, v is 2.3893 \text{ Km/s}
H in XYZ frame is <9223.99,11150.05,342.29> Km^2/s
h is 14474.90 Km<sup>2</sup>/s
Specific Energy = -3.8035 \text{ Km}^2/\text{s}^2
inclination angle i = 88.6450 deg
semi-major axis a = 5659.20 Km
Eccentricity vector in XYZ frame is <-0.1855,0.1621,-0.2816>
e is 0.3742
N vector in XYZ frame is <-11150.0515,9223.9930,0.0000> Km^2/s
n is 14470.8568 Km<sup>2</sup>/s
RAAN angle Omega = 140.4004 deg
Argument of Periapsis w = -48.8298 \text{ deg}
True Anomaly ThetaStar = -131.3714 deg
Problem 2 Part B
R vector in (r,theta,h) frame is <6465.9422,-0.0000,0.0000> Km
V vector in (r,theta,h) frame is <-0.8351,2.2386,-0.0000> Km/s
Problem 2 Part C
R vector in XYZ frame is <3008.2186,-2489.0001,13.7073> Km
V vector in XYZ frame is <-0.5788,0.5927,-3.7092> Km/s
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%Gustavo Grinsteins
%ASEN 5050
%HW2 Problem 2
%House Keeping
clc;
clear;
%% Part A
fprintf('Problem 2 Part A \n')
%Position Vector
R = [4981.75, -4121.90, 22.70]; %Km
%Velocity Vector
V = [-0.60359, 0.56812, -2.24093]; %Km/s
%Gravitational Constant
mu = 4.305*10^4; %Km^3/s^2
%magnitudes
r = norm(R); %Km
v = norm(V); %Km/s
fprintf('r is %4.2f Km, v is %1.4f Km/s \n\n',r,v)
%Calculating specific angular momentum
H = cross(R,V); %Km^2/s
h = norm(H); %Km^2/s
fprintf('H in XYZ frame is <%4.2f,%2.2f,%4.2f> Km^2/s\n',H)
fprintf('h is %4.2f Km^2/s \n\n',h)
%Calculating Specific Energy
Sp_E = ((v)^2)/(2) - (mu/r); %Km^2/s^2
fprintf('Specific Energy = %4.4f Km^2/s^2 \n\n',Sp_E)
%Inclination angle
Zhat = [0,0,1];
i = \max(\min(\det(H, Zhat)/(\operatorname{norm}(H) * \operatorname{norm}(Zhat)), 1), -1); Radians
iDegrees = real(acosd(i));%Degrees
fprintf('inclination angle i = %4.4f deg \n\n',iDegrees)
%Semi-major axis
a = -mu/(2*Sp_E);%Km
fprintf('semi-major axis a = %4.2f Km\n\n',a)
%Eccentricity Vector
Ecc = cross(V,H)*(1/mu) - R/r;%Unitless
ecc = norm(Ecc);%Unitless
fprintf('Eccentricity vector in XYZ frame is <%4.4f,%2.4f,%4.4f> \n',Ecc)
fprintf('e is %4.4f\n\n',ecc)
%RAAN
N = cross(Zhat,H);%Km^2/s
n = norm(N);%Km^2/s
fprintf('N vector in XYZ frame is <%4.4f,%4.4f,%4.4f> Km^2/s\n',N)
fprintf('n is %4.4f Km^2/s\n\n',n)
Xhat = [1,0,0];
Om = max(min(dot(N,Xhat)/(norm(N)*norm(Xhat)),1),-1);Radians
OmDegrees = real(acosd(Om));%Degrees
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fprintf('RAAN angle Omega = %4.4f deg \n\n',OmDegrees)
%Argument of periapsis
w = max(min(dot(N,Ecc)/(norm(N)*norm(Ecc)),1),-1); Radians
wDegrees = -1*real(acosd(w));%Degrees
fprintf('Argument of Periapsis w = %4.4f deg \n\n',wDegrees)
%True Anomaly
ThetaStar = max(min(dot(R,Ecc)/(norm(R)*norm(Ecc)),1),-1);Radians
TSDegrees = -1*real(acosd(ThetaStar));%Degrees
fprintf('True Anomaly ThetaStar = %4.4f deg \n\n',TSDegrees)
%Rotation matrix
theta = TSDegrees+wDegrees;%Degrees
%Rotation matrix
R1 = [1,0,0;0,cosd(iDegrees),sind(iDegrees);0,-sind(iDegrees),cosd(iDegrees)];
R3_Om = [cosd(OmDegrees), sind(OmDegrees),0;-sind(OmDegrees),cosd(OmDegrees),0;0,0,1];
R3_theta = [cosd(theta),sind(theta),0;-sind(theta),cosd(theta),0;0,0,1];
C = R3\_theta*R1*R3\_0m;
%% Part B
fprintf('Problem 2 Part B \n')
%Transforming position from XYZ to r,theta,h
Rrot = C*transpose(R);
fprintf('R vector in (r,theta,h) frame is <%4.4f,%4.4f,%4.4f> Km\n\n',Rrot)
%Transforming velocity from XYZ to r,theta,h
Vrot = C*transpose(V);
fprintf('V vector in (r,theta,h) frame is <%4.4f,%4.4f, Km/s\n\n',Vrot)</pre>
% Part C S/C at ascending node
fprintf('Problem 2 Part C \n')
PositionRot = [3904.4447;0;0];
VelocityRot = [-0.8368; 3.7073; 0];
%Transforming position from r,theta,h to XYZ
PositionXYZ = C.'*PositionRot;
fprintf('R vector in XYZ frame is <%4.4f,%4.4f, %4.4f > Km\n\n', PositionXYZ)
%Transforming velocity from r,theta,h to XYZ
VelocityXYZ = C.'*VelocityRot;
fprintf('V vector in XYZ frame is <%4.4f,%4.4f,%4.4f> Km/s\n\n',VelocityXYZ)
```