

$$\begin{cases} \dot{x} = \sigma(y-x) & \sigma = 10 \\ \dot{y} = rx - y - xz & r = 8/3 \\ \dot{z} = xy - bz & b = 28 \end{cases}$$

a) $\dot{x} = \dot{y} = \dot{z} = 0 \Rightarrow$

$$0 = y - x \Rightarrow x = y \quad (1)$$

$$0 = rx - y - xz \stackrel{(1)}{\Rightarrow} y(r-1-z) \Rightarrow y_1^* = 0 \Rightarrow z = r-1$$

$$0 = xy - bz \Rightarrow z_1^* = 0 \quad x_1^* = 0$$

$$y^2 - bz \Rightarrow z = \frac{y^2}{b} = r-1 \Rightarrow y = \pm \sqrt{b(r-1)} = x$$

fp's \Rightarrow

- 1) $(0,0,0)$
- 2) $(\sqrt{2}, \sqrt{2}, 27)$
- 3) $(-\sqrt{2}, -\sqrt{2}, 27)$

c) $J = \begin{bmatrix} -\sigma & \sigma & 0 \\ r-z & -1 & -x \\ y & x & -b \end{bmatrix}$

d) $-(\sigma + 1 + b)$

a) Mathematica gives changing sign in eigenvalues
 \rightarrow all unstable