

# Exercício Videopaula 07 Gustavo J. - 769678

(1) Máquina de Moore para determinar o módulo de 5.

$$(x) \bmod 5 = \text{resto} \left( \frac{x}{5} \right) = r \quad / \quad r \text{ está em } \{0, 1, 2, 3, 4\}$$

$$(x)_{10} = a_0 \cdot 2^m + a_1 \cdot 2^{m-1} + \dots + a_m \cdot 2^0 \quad \text{para } m \geq 0$$

$$(x)_{10} = 2 \underbrace{(a_0 \cdot 2^{m-1} + a_1 \cdot 2^{m-2} + \dots + a_{m-1})}_{(y)_{10}} + a_m$$

$$(x)_{10} = 2 \cdot (y)_{10} + a_m$$

⇓

$$\begin{cases} a_m = 0 \rightarrow (x)_{10} = 2 \cdot (y)_{10} \\ a_m = 1 \rightarrow (x)_{10} = 2 \cdot (y)_{10} + 1 \end{cases}$$

$$\downarrow \text{resto} \left( \frac{x}{5} \right) = r_x$$

$$\begin{cases} a_m = 0 \rightarrow r_x = \text{resto} \left( \frac{2 \cdot r_y}{5} \right) = 2 \cdot r_y \bmod 5 \end{cases}$$

$$\begin{cases} a_m = 1 \rightarrow r_x = \text{resto} \left( \frac{2 \cdot r_y + 1}{5} \right) = (2 \cdot r_y + 1) \bmod 5 \end{cases}$$

para  $a_m = 0$  para  $r_y = 0, 1, 2, 3, 4$ ,  $r_x = 0, 2, 4, 1, 3$   
 para  $a_m = 1$  para  $r_y = 0, 1, 2, 3, 4$ ,  $r_x = 1, 3, 0, 2, 4$

$$M = (Q, \Sigma, \Delta, \delta, \lambda, q_0), \quad \Sigma = \{0, 1\}; \quad \Delta = \{0, 1, 2, 3, 4\}$$

$$Q = \{q_0, q_1, q_2, q_3, q_4\}, \quad \lambda(q_j) = j \quad \text{para } j = 0, 1, 2, 3, 4$$

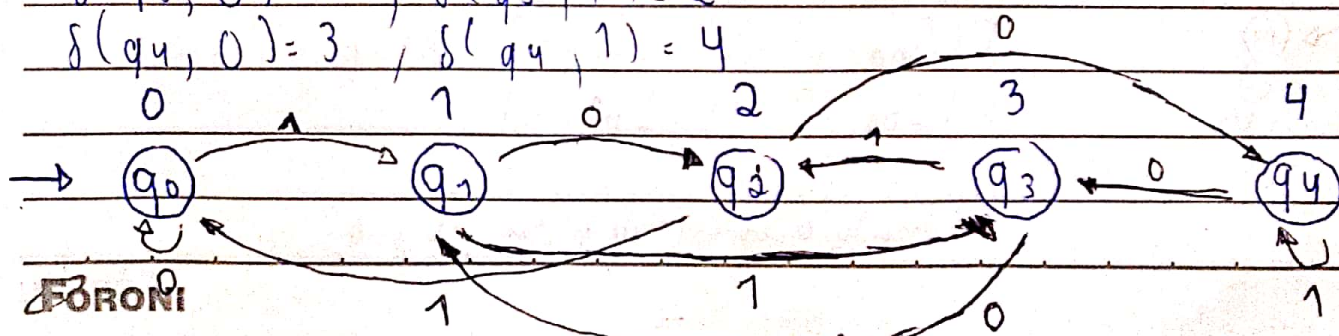
$$\delta(q_0, 0) = 0, \quad \delta(q_0, 1) = 1$$

$$\delta(q_1, 0) = 2, \quad \delta(q_1, 1) = 3$$

$$\delta(q_2, 0) = 4, \quad \delta(q_2, 1) = 0$$

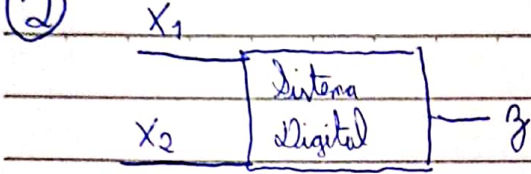
$$\delta(q_3, 0) = 1, \quad \delta(q_3, 1) = 2$$

$$\delta(q_4, 0) = 3, \quad \delta(q_4, 1) = 4$$



②

$\lambda(q_0, x_1) = 0$   
 $\lambda(q_0, x_2) = 0$   
 $\lambda(q_1, x_1) = 0$   
 $\lambda(q_1, x_2) = 0$   
 $\lambda(q_2, x_1) = 0$   
 $\lambda(q_2, x_2) = 1$   
 $\lambda(q_3, x_1) = 0$   
 $\lambda(q_3, x_2) = 0$



$Z = 1$  se termina em  $X_1 - X_2 - X_2$   
 $Z = 0$  caso contrário

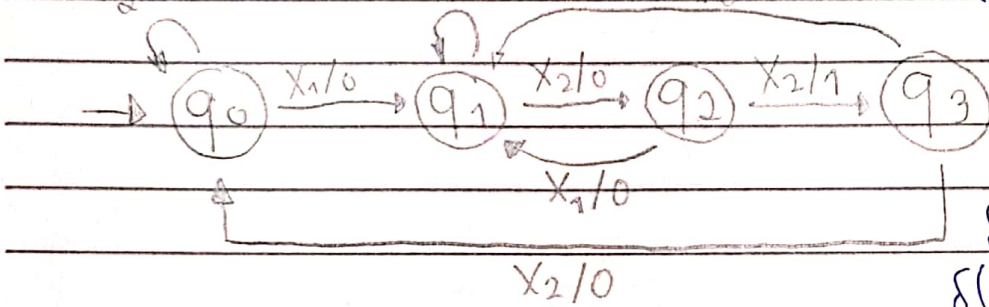
$M_1 = X_2/0$

$X_1/0$

$X_1/0$

$Q = \{q_0, q_1, q_2, q_3\}$

$\Sigma = \{X_1, X_2\} \Delta = \{0, 1\}$



$\delta(q_0, x_1) = q_1$

$\delta(q_0, x_2) = q_0$

$\delta(q_1, x_1) = q_1$

$\delta(q_1, x_2) = q_2$   $\delta(q_3, x_1) = q_1$

$\delta(q_2, x_1) = q_1$   $\delta(q_3, x_2) = q_0$

$\delta(q_2, x_2) = q_3$

$\omega = X_1 - X_1 - X_2 - X_2 - X_2 - X_1 - X_2 - X_2$

$estados = q_0 - q_1 - q_1 - q_2 - q_3 - q_0 - q_1 - q_2 - q_3$

$saídas = 0 - 0 - 0 - 1 - 0 - 0 - 0 - 1$

③ Utilizando o Teorema 2.7.

$Q' = \{[q_0, 0], [q_1, 0], [q_2, 0], [q_3, 1]\}$

$\Sigma = \{x_1, x_2\} \Delta = \{0, 1\} q_0 = [q_0, 0] \cdot l_0 = 0$

$\delta'([q_0, 0], x_1) = [q_1, 0] \quad \lambda'([q_0, 0]) = 0$

$\delta'([q_0, 0], x_2) = [q_0, 0]$

$\delta'([q_1, 0], x_1) = [q_1, 0] \quad \lambda'([q_1, 0]) = 0$

$\delta'([q_1, 0], x_2) = [q_2, 0]$

$\delta'([q_2, 0], x_1) = [q_1, 0] \quad \lambda'([q_2, 0]) = 0$

$\delta'([q_2, 0], x_2) = [q_3, 1]$

$\delta'([q_3, 1], x_1) = [q_1, 0] \quad \lambda'([q_3, 1]) = 1$

$\delta'([q_3, 1], x_2) = [q_0, 0]$

$\omega = X_1 X_1 X_2 X_2 X_2 X_1 X_2 X_2$

$estados = [q_0, 0] - [q_1, 0] - [q_1, 0] - [q_2, 0] -$

$[q_3, 1] - [q_0, 0] - [q_1, 0] - [q_2, 0] - [q_3, 1]$

$saídas = 000010001$

