# Centro de Estatística Aplicada

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# Sumário

| nálise Descritiva                      |
|--|
| Medidas Resumo                         |
| Análise das curvas bolus lado esquerdo |
| Análise das curvas bolus lado direito  |

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#### library(matrixStats)

```
##
## Attaching package: 'matrixStats'

## The following object is masked from 'package:plyr':
##
## count

## The following object is masked from 'package:dplyr':
##
## count

## The following objects are masked from 'package:robustbase':
##
## colMedians, rowMedians

library(ggplot2)
```

## Análise Descritiva

```
setwd("C:\\Users\\Rodrigo Araujo\\Documents\\IME-USP\\CEA 2")
data = read.csv('dataset_utrassom.csv', sep = ';', dec = ',')
head(data)
```

```
##
          SEXO BOLUS.CURVA.ESQ.A BOLUS.CURVA.ESQ.B BOLUS.CURVA.ESQ.K
## 1 Feminino
                        447.000
                                          -62.674
                                                              79.000
## 2 Feminino
                           5.470
                                           -61.034
                                                               0.095
## 3 Feminino
                           8.225
                                           -62.653
                                                               0.041
## 4 Masculino
                           0.484
                                          -62.457
                                                              12.539
## 5 Feminino
                                           -62.909
                                                             123.000
                           2.502
## 6 Feminino
                          13.633
                                           -67.085
                                                               0.039
## BOLUS.CURVA.ESQ.MSE BOLUS.CURVA.ESQ.TTOPK BOLUS.CURVA.ESQ.AREA
## 1
                322.000
                                        25.069
                                                            18.624
## 2
                  1.279
                                        23.930
                                                            118.391
## 3
                 13.834
                                        37.061
                                                            372.306
## 4
                 21.389
                                        29.208
                                                             86.211
## 5
                 907.000
                                        46.060
                                                             87.158
## 6
                 15.700
                                        36.622
                                                            425.336
   BOLUS.CURVA.ESQ.GRAD BOLUS.CURVA.ESQ.ATM BOLUS.CURVA.DIR.A BOLUS.CURVA.DIR.B
##
                                                       107.390
## 1
                  87.000
                                      120.00
                                                                          -65.918
## 2
                    0.268
                                         0.24
                                                        105.000
                                                                          -60.836
## 3
                    0.764
                                         0.00
                                                                          -65.577
                                                         4.820
## 4
                   0.440
                                         0.00
                                                                          -63.519
                                                        -0.126
                                         0.00
## 5
                  83.000
                                                        607.000
                                                                          -63.992
## 6
                   0.842
                                         0.00
                                                        5.348
                                                                          -64.533
```

```
BOLUS.CURVA.DIR.K BOLUS.CURVA.DIR.MSE BOLUS.CURVA.DIR.TTOPK
## 1
                0.008
                                  11,100
                                                        28.788
## 2
                3.192
                                  16.003
                                                        21.171
## 3
                0.056
                                   4.853
                                                        51.953
## 4
                4.304
                                  15.369
                                                        26.449
## 5
                2.137
                                 598.000
                                                        53.677
               -0.109
                                 12.045
##
    BOLUS.CURVA.DIR.AREA BOLUS.CURVA.DIR.GRAD BOLUS.CURVA.DIR.ATM
## 1
                 290.757
                                     626.000
## 2
                 78.961
                                      0.416
                                                            0.6
## 3
                 236.720
                                      0.427
                                                            0.0
## 4
                                       0.471
                                                            0.0
                 41.857
## 5
                                      59,000
                                                            60.0
                 35.105
## 6
                111.946
                                       0.658
                                                            0.0
## REFIL.CURVA.ESQ.A REFIL.CURVA.ESQ.B REFIL.CURVA.ESQ.K REFIL.CURVA.ESQ.MSE
## 1
              -3.411
                              -47.261
                                                551.000
                                                                    561.000
## 2
               1.171
                               -55.835
                                                   0.083
                                                                      0.193
## 3
                  NA
                                 NA
                                                     NA
                                                                         NA
## 4
               -0.029
                               -49.826
                                                  1.315
                                                                      0.339
## 5
               1.730
                               -60.777
                                                 207.000
                                                                    292.000
## 6
                  NA
                                   NA
                                                     NA
                                                                         NA
## REFIL.CURVA.ESQ.TTOPK REFIL.CURVA.ESQ.AREA REFIL.CURVA.ESQ.GRAD
## 1
                                     -55.809
                   1.919
                                                           299.000
## 2
                   15.953
                                       20.191
                                                            0.107
## 3
                     NA
                                                               NA
                                        NA
## 4
                   2.159
                                       8.476
                                                            0.630
## 5
                   11.035
                                       30.157
                                                           175.000
## 6
                     NA
                                           NA
## REFIL.CURVA.ESQ.ATM REFIL.CURVA.DIR.A REFIL.CURVA.DIR.B REFIL.CURVA.DIR.K
## 1
                 48.763
                                  -1.033
                                                  -48.978
                                                                      1.279
## 2
                 45.836
                                   2.692
                                                   -58.837
                                                                    203.000
## 3
                    NΑ
                                      NA
                                                       NΑ
                                                                         NA
## 4
                 34.314
                                  -1.824
                                                   -50.979
                                                                      0.068
## 5
                 58.163
                                   1.988
                                                   -63.550
                                                                      2.369
## 6
                 NA
                                   1.320
                                                   -57.677
                                                                      0.112
## REFIL.CURVA.DIR.MSE REFIL.CURVA.DIR.TTOPK REFIL.CURVA.DIR.AREA
## 1
                956.000
                                     18.607
                                                        -36.415
## 2
                194.000
                                       9.476
                                                          66.809
## 3
                    NA
                                          NA
                                                              NA
## 4
                  0.097
                                       3.119
                                                         -25.610
## 5
                  2.048
                                      26.686
                                                          45.167
                                      8.570
## 6
                  1.463
                                                         -22.646
## REFIL.CURVA.DIR.GRAD REFIL.CURVA.DIR.ATM Controle
## 1
                 27.000
                                     37.025
## 2
                 331.000
                                     35.702
                                                   0
## 3
                                        NA
                   NA
## 4
                  0.302
                                     29.354
## 5
                189.000
                                     60.440
## 6
                 0.419
                                     40.575
```

#### Medidas Resumo

```
## Medias
data1 = data[, -1]
colMeans(data1, na.rm = TRUE)
##
       BOLUS.CURVA.ESQ.A
                              BOLUS.CURVA.ESQ.B
                                                     BOLUS.CURVA.ESQ.K
##
              -16.223870
                                     -61.172522
                                                             11.351126
##
     BOLUS.CURVA.ESQ.MSE BOLUS.CURVA.ESQ.TTOPK
                                                 BOLUS.CURVA.ESQ.AREA
##
               60.280609
                                      28.576565
                                                             96.885870
##
    BOLUS.CURVA.ESQ.GRAD
                            BOLUS.CURVA.ESQ.ATM
                                                     BOLUS.CURVA.DIR.A
##
               50.820913
                                      46.990435
                                                             40.054417
##
       BOLUS.CURVA.DIR.B
                              BOLUS.CURVA.DIR.K
                                                   BOLUS.CURVA.DIR.MSE
##
              -63.496375
                                       7.418708
                                                             35.479583
##
  BOLUS.CURVA.DIR.TTOPK
                          BOLUS.CURVA.DIR.AREA
                                                 BOLUS.CURVA.DIR.GRAD
                                      95.724292
                                                             90.639792
##
               31.673292
##
     BOLUS.CURVA.DIR.ATM
                                                     REFIL.CURVA.ESQ.B
                              REFIL.CURVA.ESQ.A
##
               50.045000
                                     -10.038087
                                                            -54.270609
       REFIL.CURVA.ESQ.K
##
                            REFIL.CURVA.ESQ.MSE REFIL.CURVA.ESQ.TTOPK
##
               63.435613
                                      62.491045
                                                              7.676696
##
    REFIL.CURVA.ESQ.AREA
                           REFIL.CURVA.ESQ.GRAD
                                                   REFIL.CURVA.ESQ.ATM
##
               13.507304
                                      27.436500
                                                             47.795136
##
       REFIL.CURVA.DIR.A
                              REFIL.CURVA.DIR.B
                                                     REFIL.CURVA.DIR.K
##
               14.756583
                                     -52.000792
                                                             16.034000
                                                 REFIL.CURVA.DIR.AREA
     REFIL.CURVA.DIR.MSE REFIL.CURVA.DIR.TTOPK
##
##
               52.986042
                                      23.322167
                                                             -3.740375
    REFIL.CURVA.DIR.GRAD
##
                            REFIL.CURVA.DIR.ATM
                                                              Controle
##
               39.768512
                                      38.508792
                                                              0.360000
#install.packages('matrixStats')
require(matrixStats)
paste(colnames(data1), colSds(as.matrix(data1), na.rm = TRUE))
    [1] "BOLUS.CURVA.ESQ.A 227.483308423498"
    [2] "BOLUS.CURVA.ESQ.B 2.93601224405369"
##
##
    [3] "BOLUS.CURVA.ESQ.K 29.2747761305347"
##
    [4] "BOLUS.CURVA.ESQ.MSE 196.002319652725"
##
    [5] "BOLUS.CURVA.ESQ.TTOPK 7.5477075618187"
##
    [6] "BOLUS.CURVA.ESQ.AREA 116.505325312663"
##
    [7]
       "BOLUS.CURVA.ESQ.GRAD 131.081623982198"
##
    [8] "BOLUS.CURVA.ESQ.ATM 117.16614029497"
    [9] "BOLUS.CURVA.DIR.A 124.324443301603"
##
   [10] "BOLUS.CURVA.DIR.B 3.39840816716476"
  [11] "BOLUS.CURVA.DIR.K 12.4904215457082"
   [12] "BOLUS.CURVA.DIR.MSE 120.21694881227"
## [13] "BOLUS.CURVA.DIR.TTOPK 10.9141330810666"
```

## [14] "BOLUS.CURVA.DIR.AREA 88.2201267253282"
## [15] "BOLUS.CURVA.DIR.GRAD 194.351835637684"
## [16] "BOLUS.CURVA.DIR.ATM 108.566232919977"
## [17] "REFIL.CURVA.ESQ.A 31.9805914436085"

```
## [18] "REFIL.CURVA.ESQ.B 4.44522710064228"
## [19] "REFIL.CURVA.ESQ.K 182.504082175611"
## [20] "REFIL.CURVA.ESQ.MSE 145.389970627595"
## [21] "REFIL.CURVA.ESQ.TTOPK 7.13554209213404"
## [22] "REFIL.CURVA.ESQ.AREA 60.5533105096318"
## [23] "REFIL.CURVA.ESQ.GRAD 72.6566569307806"
## [24] "REFIL.CURVA.ESQ.ATM 52.6494504527874"
## [25] "REFIL.CURVA.DIR.A 77.8185679557804"
## [26] "REFIL.CURVA.DIR.B 12.469889414032"
## [27] "REFIL.CURVA.DIR.K 74.2101756657928"
## [28] "REFIL.CURVA.DIR.MSE 196.720207298607"
## [29] "REFIL.CURVA.DIR.TTOPK 75.3997817864831"
## [30] "REFIL.CURVA.DIR.AREA 58.2695096806081"
## [31] "REFIL.CURVA.DIR.GRAD 95.2952704549269"
## [32] "REFIL.CURVA.DIR.ATM 9.66680339224272"
## [33] "Controle 0.489897948556636"
\#colSds(as.matrix(data[, -1]), na.rm = TRUE)
```

### Análise das curvas bolus lado esquerdo

Criando a função gamma para simulação das curvas

```
data2 = data[-c(11, 12),]
rownames(data2) <- seq(1, 23)
# simulação da função gamma
simulacao <- function(A, B, k){
    (A*(1 + (-1*exp(-1*k*x))) + B)
}</pre>
```

Aplicação da função gamma usando os parâmetros em função dos paciêntes.

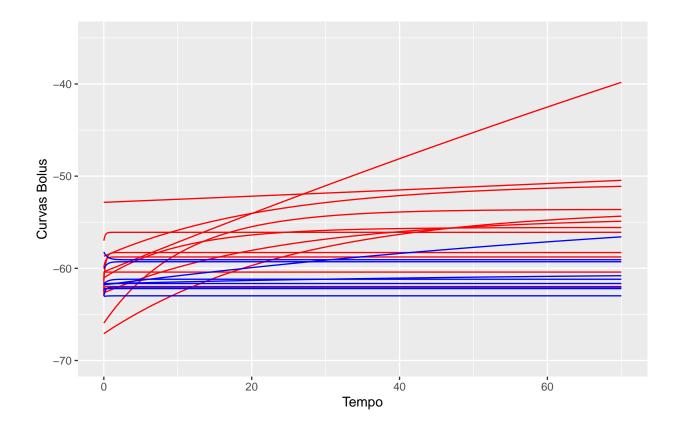
```
x <- seq(0, 70, 0.01)
data_y <- data.frame('y' = rep(0, 7001))
for (i in 1:nrow(data2)){
    y_1 <- simulacao(data2[i, 2], data2[i, 3], data2[i, 4])
    data_y <- cbind(data_y, y_1)
}
curvas = rep('curva', ncol(data_y))
curvas2 = seq(0, 23)
curvas2 = as.character(curvas2)
names_data_y <- paste(curvas, curvas2)</pre>
```

```
colnames(data_y) <- names_data_y
data_y$X <- x</pre>
```

Gerando as curvas para todos os paciêntes.

```
ggplot(data_y, aes(X)) +
  geom_line(aes(y='curva 1'), colour="red") +
  geom_line(aes(y='curva 2'), colour="red") +
  geom line(aes(y='curva 3'), colour="red") +
  geom_line(aes(y='curva 4'), colour="red") +
  geom line(aes(y='curva 5'), colour="red") +
  geom_line(aes(y='curva 6'), colour="red") +
  geom_line(aes(y='curva 7'), colour="red") +
  geom_line(aes(y='curva 8'), colour="red") +
  geom_line(aes(y='curva 9'), colour="red") +
  geom_line(aes(y='curva 10'), colour="red") +
  geom_line(aes(y='curva 11'), colour="red") +
  geom_line(aes(y='curva 12'), colour="red") +
  geom_line(aes(y='curva 13'), colour="red") +
  geom_line(aes(y='curva 14'), colour="red") +
  geom_line(aes(y='curva 15'), colour="blue") +
  geom_line(aes(y='curva 16'), colour="blue") +
  geom_line(aes(y='curva 17'), colour="blue") +
  geom_line(aes(y='curva 18'), colour="blue") +
  geom_line(aes(y='curva 19'), colour="blue") +
  geom line(aes(y='curva 20'), colour="blue") +
  geom_line(aes(y='curva 21'), colour="blue") +
  geom_line(aes(y='curva 22'), colour="blue") +
  geom_line(aes(y='curva 23'), colour="blue") +
  ylim(-70, -35) +
  xlab("Tempo") + ylab("Curvas Bolus")
```

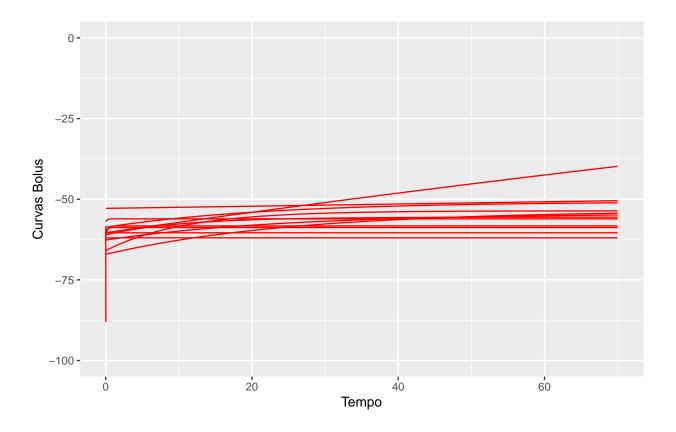
```
## geom_path: Each group consists of only one observation. Do you need to adjust
## the group aesthetic?
## geom_path: Each group consists of only one observation. Do you need to adjust
## the group aesthetic?
```



#### Grupo dos pacientes

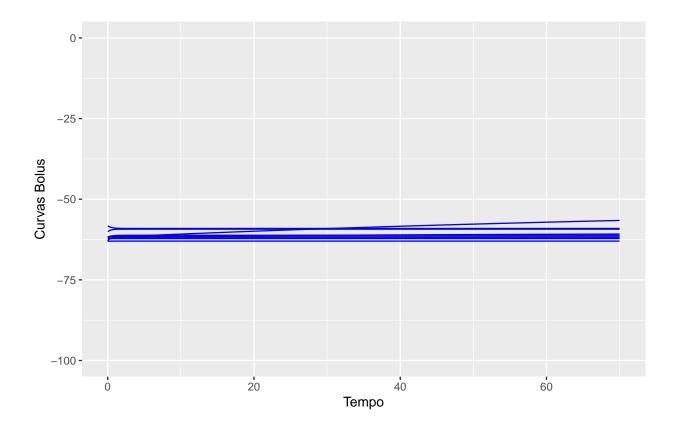
```
ggplot(data_y, aes(X)) +
  geom_line(aes(y='curva 1'), colour="red") +
  geom_line(aes(y='curva 2'), colour="red") +
  geom_line(aes(y='curva 3'), colour="red") +
  geom_line(aes(y='curva 4'), colour="red") +
  geom_line(aes(y='curva 5'), colour="red") +
  geom_line(aes(y='curva 6'), colour="red") +
  geom_line(aes(y='curva 7'), colour="red") +
  geom_line(aes(y='curva 8'), colour="red") +
  geom_line(aes(y='curva 9'), colour="red") +
  geom_line(aes(y='curva 10'), colour="red") +
  geom_line(aes(y='curva 11'), colour="red") +
  geom_line(aes(y='curva 12'), colour="red") +
  geom_line(aes(y='curva 13'), colour="red") +
  geom_line(aes(y='curva 14'), colour="red") +
  ylim(-100, 0) +
  xlab("Tempo") + ylab("Curvas Bolus")
```

## geom\_path: Each group consists of only one observation. Do you need to adjust
## the group aesthetic?



#### Grupo controle

```
ggplot(data_y, aes(X)) +
  geom_line(aes(y='curva 15'), colour="blue") +
  geom_line(aes(y='curva 16'), colour="blue") +
  geom_line(aes(y='curva 17'), colour="blue") +
  geom_line(aes(y='curva 18'), colour="blue") +
  geom_line(aes(y='curva 19'), colour="blue") +
  geom_line(aes(y='curva 20'), colour="blue") +
  geom_line(aes(y='curva 21'), colour="blue") +
  geom_line(aes(y='curva 22'), colour="blue") +
  geom_line(aes(y='curva 23'), colour="blue") +
  ylin(-100, 0) +
  xlab("Tempo") + ylab("Curvas Bolus")
```



## Análise das curvas bolus lado direito

Aplicação da função gamma usando os parâmetros em função dos paciêntes.

```
data2 = data[-c(16),]
rownames(data2) <- seq(1, 24)

x <- seq(0, 70, 0.01)

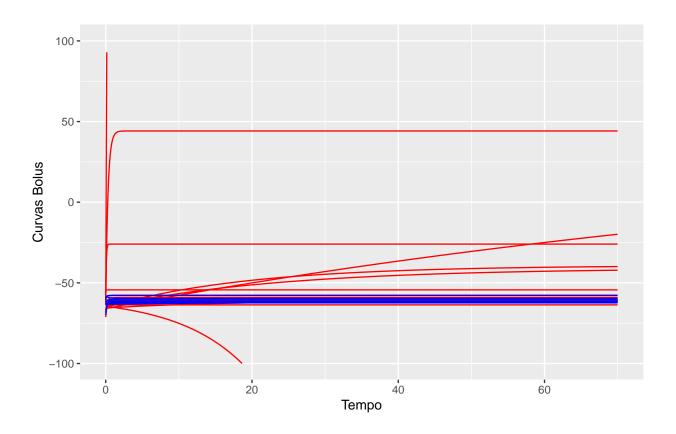
data_y <- data.frame('y' = rep(0, 7001))

for (i in 1:nrow(data2)){
    y_1 <- simulacao(data2[i, 10], data2[i, 11], data2[i, 12])
    data_y <- cbind(data_y, y_1)
}

curvas = rep('curva', ncol(data_y))
curvas2 = seq(0, 24)
curvas2 = seq(0, 24)
curvas2 = as.character(curvas2)
names_data_y <- paste(curvas, curvas2)
colnames(data_y) <- names_data_y
data_y$X <- x</pre>
```

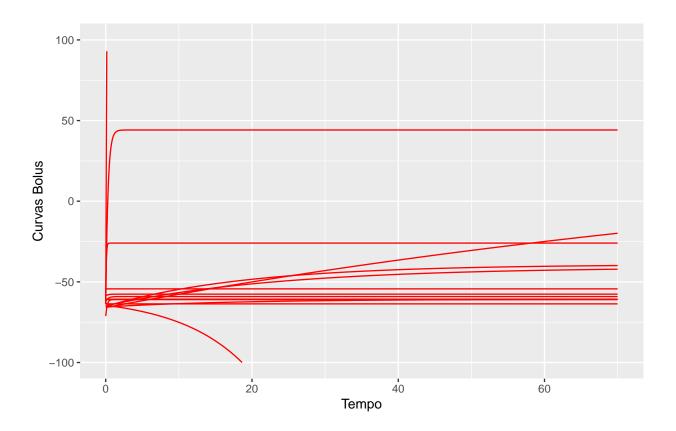
Gerando as curvas para todos os paciêntes.

```
ggplot(data_y, aes(X)) +
  geom_line(aes(y='curva 1'), colour="red") +
  geom_line(aes(y='curva 2'), colour="red") +
  geom line(aes(y='curva 3'), colour="red") +
  geom line(aes(y='curva 4'), colour="red") +
  geom_line(aes(y='curva 5'), colour="red") +
  geom_line(aes(y='curva 6'), colour="red") +
  geom_line(aes(y='curva 7'), colour="red") +
  geom_line(aes(y='curva 8'), colour="red") +
  geom_line(aes(y='curva 9'), colour="red") +
  geom_line(aes(y='curva 10'), colour="red") +
  geom_line(aes(y='curva 11'), colour="red") +
  geom_line(aes(y='curva 12'), colour="red") +
  geom_line(aes(y='curva 13'), colour="red") +
  geom_line(aes(y='curva 14'), colour="red") +
  geom line(aes(y='curva 15'), colour="red") +
  geom_line(aes(y='curva 16'), colour="blue") +
  geom_line(aes(y='curva 17'), colour="blue") +
  geom_line(aes(y='curva 18'), colour="blue") +
  geom_line(aes(y='curva 19'), colour="blue") +
  geom_line(aes(y='curva 20'), colour="blue") +
  geom_line(aes(y='curva 21'), colour="blue") +
  geom_line(aes(y='curva 22'), colour="blue") +
  geom_line(aes(y='curva 23'), colour="blue") +
  geom_line(aes(y='curva 24'), colour="blue") +
  ylim(-100, 100) +
  xlab("Tempo") + ylab("Curvas Bolus")
```



#### Grupo dos pacientes

```
ggplot(data_y, aes(X)) +
  geom_line(aes(y='curva 1'), colour="red") +
  geom_line(aes(y='curva 2'), colour="red") +
  geom_line(aes(y='curva 3'), colour="red") +
  geom_line(aes(y='curva 4'), colour="red") +
  geom_line(aes(y='curva 5'), colour="red") +
  geom_line(aes(y='curva 6'), colour="red") +
  geom_line(aes(y='curva 7'), colour="red") +
  geom_line(aes(y='curva 8'), colour="red") +
  geom_line(aes(y='curva 9'), colour="red") +
  geom_line(aes(y='curva 10'), colour="red") +
  geom line(aes(y='curva 11'), colour="red") +
  geom_line(aes(y='curva 12'), colour="red") +
  geom_line(aes(y='curva 13'), colour="red") +
  geom_line(aes(y='curva 14'), colour="red") +
  geom_line(aes(y='curva 15'), colour="red") +
 ylim(-100, 100) +
  xlab("Tempo") + ylab("Curvas Bolus")
```



#### Grupo controle

```
ggplot(data_y, aes(X)) +
  geom_line(aes(y='curva 16'), colour="blue") +
  geom_line(aes(y='curva 17'), colour="blue") +
  geom_line(aes(y='curva 18'), colour="blue") +
  geom_line(aes(y='curva 19'), colour="blue") +
  geom_line(aes(y='curva 20'), colour="blue") +
  geom_line(aes(y='curva 21'), colour="blue") +
  geom_line(aes(y='curva 22'), colour="blue") +
  geom_line(aes(y='curva 23'), colour="blue") +
  geom_line(aes(y='curva 24'), colour="blue") +
  ylim(-70, -50) +
  xlab("Tempo") + ylab("Curvas Bolus")
```

