

1. Kalman Filter

X_k k 时刻滤波器状态

$$\begin{cases} X_{k+1} = \Phi_k^{k+1} X_k + W_k \\ Z_{k+1} = H_{k+1} X_{k+1} + V_{k+1} \end{cases}$$

KF流程:

$$\hat{X}_{k+1|k} = \Phi_k^{k+1} \hat{X}_{k|k}$$

$$P_{k+1|k} = \Phi_k^{k+1} P_{k|k} \Phi_k^{k+1T} + Q_k$$

} 递推预测

$$K_{k+1} = P_{k+1|k} H_{k+1}^T (H_{k+1} P_{k+1|k} H_{k+1}^T + R_{k+1})^{-1}$$

$$\hat{X}_{k+1|k+1} = \hat{X}_{k+1|k} + K_{k+1} (Z_{k+1} - H_{k+1} \hat{X}_{k+1|k})$$

$$P_{k+1|k+1} = (I - K_{k+1} H_{k+1}) P_{k+1|k}$$

} 测量更新

2. 采用误差状态的KF (反馈修正法)

符号代换 $x \rightarrow \delta x$ 滤波器状态

$z \rightarrow r$

$$P_{k+1|k} = \Phi_k^{k+1} P_{k|k} \Phi_k^{k+1T} + Q_k$$

$$K_{k+1} = P_{k+1|k} H_{k+1}^T (H_{k+1} P_{k+1|k} H_{k+1}^T + R_{k+1})^{-1}$$

$$\delta X_{k+1|k+1} = K_{k+1} \cdot r_{k+1}$$

$$P_{k+1|k+1} = (I - K_{k+1} H_{k+1}) P_{k+1|k}$$

$r_{k+1} = Z_{k+1} - \hat{Z}(\hat{X}_{k+1})$
实际测量 - 估计值
的测量

3. 一个完整的采用误差状态的 EKF 的系统:

一套单独的 状态递推方程, 用来预测系统状态:

$$\hat{x}_{k+1|k} = f_k^{k+1}(\hat{x}_{k|k})$$

误差状态的 EKF 值, 直到观测到来时才进行计算:

$$P_{k+1|k} = f_k^{k+1} P_{k|k} f_k^{k+1T} + Q_k$$

$$K_{k+1} = P_{k+1|k} h_{k+1}^T (h_{k+1} P_{k+1|k} h_{k+1}^T + R_{k+1})^{-1}$$

$$\delta \hat{x}_{k+1|k} = K_{k+1} r_{k+1} = K_{k+1} (z_{k+1} - h_{k+1}(\hat{x}_{k+1|k}))$$

$$P_{k+1|k+1} = (1 - K_{k+1} h_{k+1}) P_{k+1|k}$$

其中 f 与 h 所代表的意义:

$$\begin{cases} \delta x_{k+1} = f_k^{k+1} \delta x_k + w \\ y = h \delta x + v \end{cases} \quad \text{滤波器状态的预测与观测.}$$

最终的系统输出:

$$\hat{x}_{k+1|k+1} = \hat{x}_{k+1|k} + \delta \hat{x}_{k+1|k+1}$$

滤波器状态比较好近似线性时, EKF 效果好.

误差状态是一个小量, 线性化效果比较好!