

2022.06. 대한산업공학회 추계학술대회

딥 클러스터링을 통한 가계 금융 다양성 분석

황윤태 (UNIST 산업공학과) 이용재 (UNIST 산업공학과)

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이 용 재 금융공학연구실 산업공학과



연구 배경

- 금융경제학 연구에서의 가계금융 다양성
 - Consumption-based CAPM: 소비와 portfolio allocation을 연결지음
 - Merton (1973), Lucas (1978), Breeden (1979, 1986), Grossman and Shiller (1982) 등
 - Equity premium puzzle (Mehra and Prescott, 1985): Representative consumer를 기반으로 한 consumer-based CAPM으로는 equity premium이 작게 측정된다
 - 이를 위해 income, stock holding 여부, savings, wealth등의 다양성을 모형에 반영하기 시작
 - Mankiw and Zeldes (1991), Lucas (1994), Heaton and Lucas (1997), Krueger, Mitman, and Perri (2016) 등

연구 배경

■ Krueger, Mitman, and Perri (2016):

"실제 데이터에서 우리가 관측하는 wealth, income, expenditure의 joint distribution을 더 정확하게 모델에 반영하기 위해서는 더 많은 차원의 heterogeneity를 고려해야한다"

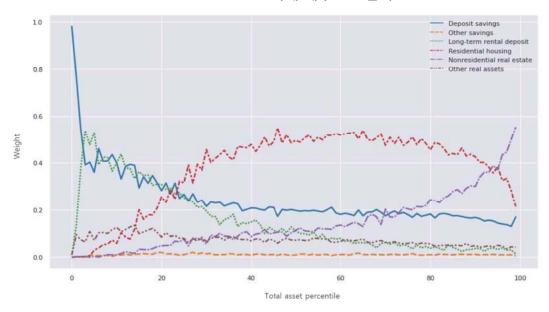
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연구 배경

2017~2020 가계 재무 포트폴리오

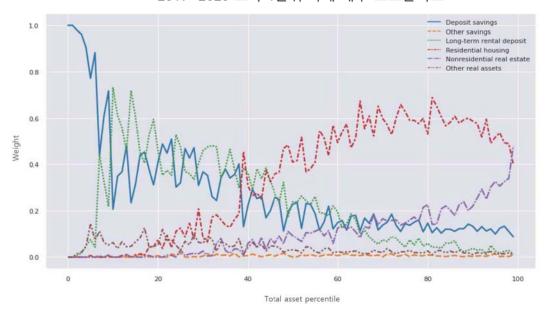


자산 총액이 증가함에 따라 유형별 자산의 비중은 비선형적으로 변화

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연구 배경





자산 총액이 증가함에 따라 유형별 자산의 비중은 비선형적으로 변화

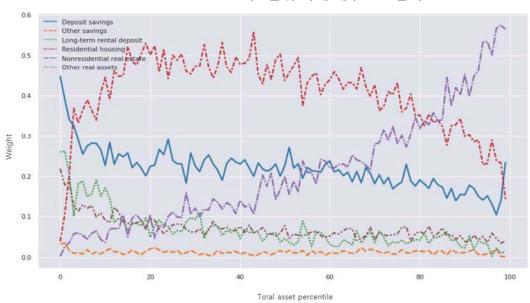
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연구 배경

2017~2020 소득 5분위 가계 재무 포트폴리오

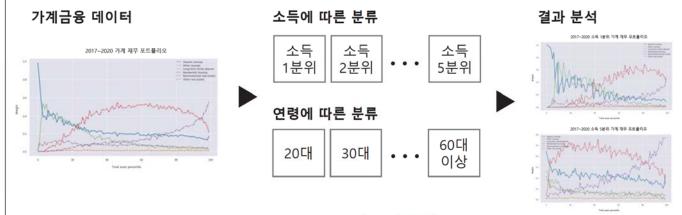


자산 총액이 증가함에 따라 유형별 자산의 비중은 비선형적으로 변화

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연구 배경

■ 과거의 접근법



- 한두개의 항목 별로 분류하고 분석
- 분류를 하고 난 뒤에도 그룹 내의 heterogeneity가 많이 사라지지 않음

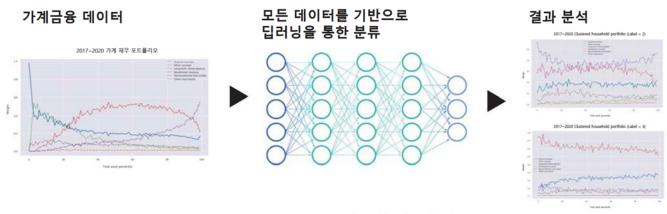
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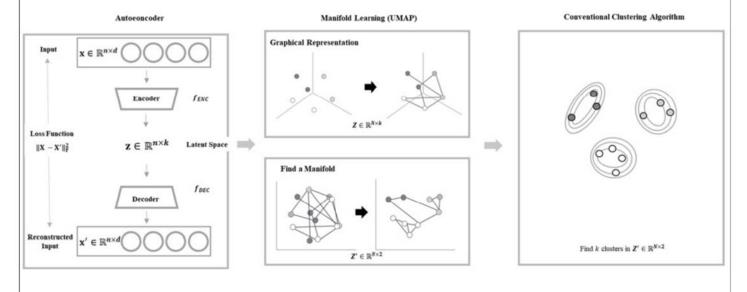
■ 본 연구의 접근법



- 모든 데이터를 바탕으로 딥 러닝 기반으로 분류
- 데이터 안의 복잡한 비선형적 관계를 딥러닝을 통해 포착하여 분류 후 그룹 내 heterogeneity가 많이 줄어들 것으로 예상

연구 방법

Figure 1 N2D framework for deep clustering by McConville et al. (2021)



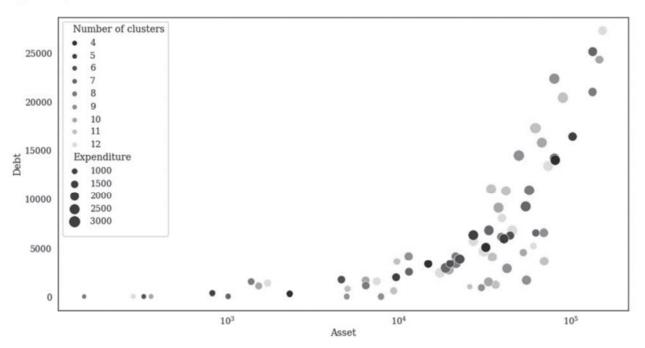
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분석 결과

Figure 2 Optimal household clusters with different number of clusters



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분석 결과

Table 2 Average values (proportions) of asset, debt, expenditure variables of different household clusters

No.	Deposit savings	Other savings	Long-term rer	ntal Resident	ial housing	Nonre		Other real assets		
1	16089.8 (12.1 %)	662.4 (0.5 %)	deposit	42702	42702.6 (32.2 %)		estate 3.6 (50.6 %)	4673.1 (3.5 %)		
2	10386.6 (18.4 %)	801.0 (1.4 %)	1343.1 (1.0 % 2470.8 (4.4 %				9.5 (39.3 %)	4167.7 (7.4 %)		
3					16426.5 (29.1 %)					
4	6507.1 (16.6 %)	353.3 (0.9 %)	1.1 (0.0 %		30408.0 (77.8 %)		7.3 (0.6 %)	1589.6 (4.1 %)		
3	5189.1 (24.4 %) 5822.6 (28.5 %)	219.9 (1.0 %) 327.1 (1.6 %)	82.1 (0.4 % 12501.0 (61.3		12662.5 (59.5 %)		4.7 (3.3 %)	1612.5 (7.6 %) 1076.2 (5.3 %)		
6	2735.1 (43.2 %)	336.3 (5.3 %)	2016.5 (31.8		18.5 (0.3 %)		5.4 (1.5 %)	1132.5 (17.9 %)		
7	469.7 (34.3 %)	33.0 (2.4 %)	474.8 (34.7		31.3 (2.3.%)		8.5 (1.4 %)	339.4 (24.8 %)		
8	62.7 (42.5 %)	1.3 (0.6 %)	78.2 (52.9		0 (0.0 %)		0.2 (0.1 %)	5.2 (3.6 %)		
_	B-1. Debts (Morts		10.2 (32.9	76) 0.	0:(0.0 74)		0.2 (0.1 74)	3.2 (3.0 %)		
No.	Residential	Nonresidential real	Long-term rer	tal Living	avnanca	Due	iness funds	Refinance		
NO.				nat Living	Living expense		mess runus	Retinance		
	housing	estate	deposit							
	2185.7 (19.1 %)	4906.1 (42.9 %)	87.4 (0.8 %		9 (1.1.%)	3208.7 (28.1 %)		123.9 (1.1 %)		
2	1699.0 (26.3 %)	1959.3 (30.3 %)	228.2 (3.5 %		1 (1.8 %)		2.6 (21.4 %)	108.4 (1.7 %)		
3	4189.9 (81.8 %)	24.2 (0.5 %)	27.5 (0.5 %		9 (2.8 %)		9.5 (5.1 %)	82.4 (1.6 %		
4	1712.2 (62.2 %)	90.3 (3.3 %)	26.2 (1.0 %		3 (5.0 %)		2.6 (9.2 %)	75.3 (2.7 %)		
5	9.7 (0.3 %)	75.9 (2.2 %)	2456.7 (70.7		56.8 (1.6 %)		2.5 (1.8 %)	16.9 (0.5 %		
6	0.4 (0.1 %)	3.7 (0.5 %)	146.4 (20.9		60.6 (8.7 %)		4.1 (10.6 %)	14.9 (2.1 %		
7	7.7 (1.3 %)	0.5 (0.1 %)	8.2 (1.3 %		15.5 (2.5 %)		8.3 (3.0 %)	5.1 (0.8 %		
8	0.0 (0.0 %)	0.0 (0.0 %)	0.0 (0.0 %	0.	0.0 (0.0 %)		0.0 (0.0 %)	0.0 (0.0 %)		
Panel	B-2. Debts (Credi	t loans)	134							
No.	Residential	Nonresidential real	Long-term rer	tal Living	Living expense		iness funds	Refinance		
	housing	estate	deposit							
1	57.1 (0.5 %)	232.3 (2.0 %)	22.7 (0.2 %	100.	100.5 (0.9 %)		2.8 (3.0 %)	36.1 (0.3 %)		
2	102.9 (1.6 %)	213.4 (3.3 %)	55.0 (0.9 %		161.6 (2.5 %)		0.0 (5.9 %)	50.9 (0.8 %)		
3	95.9 (1.9 %)	15.5 (0.3 %)	5.8 (0.1 %) 135.	135.4 (2.6 %)		9.2 (2.3 %)	25.4 (0.5 %)		
4	71.6 (2.5 %)	32.9 (1.2 %)	9.9 (0.4 %		187.6 (6.8 %)		4.8 (4.5 %)	31.4 (1.1%)		
	64.4 (1.9 %)	100 100 100	336.1 (9.7 %	110	119.5 (3.4 %)		6.5 (3.9 %)	16.0 (0.5 %)		
5		125.4((3.6 %)		119.		126.9 (18.1 %)		28.5 (4.1 %)		
6	6.0 (0.9 %)	125.4 (3.6 %)	76.7 (11.0		7 (20.2 %)	12	6.9 (18.1 %)	28.5 (4.1 %)		
			76.7 (11.0	%) 141.			(6.9 (18.1 %) (1.2 (32.9 %)			
6	6.0 (0.9 %)	20.1 (2.9 %)		%) 141. 6) 188.	7 (20.2 %)	20		28.5 (4.1 %) 111.8 (18.3 %) 0.0 (0.0 %)		
6 7 8	6.0 (0.9 %) 1.6 (0.3 %)	20.1 (2.9 %) 9.0 (1.5 %)	76.7 (11.0 ° 44.8 (7.3 °	%) 141. 6) 188.	7 (20.2 %) 5 (30.8 %)	20	1.2 (32.9 %)	111.8 (18.3 %)		
6 7 8	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %)	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %)	76.7 (11.0 ° 44.8 (7.3 °	%) 141. 6) 188.	7 (20.2 %) 5 (30.8 %)	20	1.2 (32.9 %)	111.8 (18.3 %) 0.0 (0.0 %)		
6 7 8 Panel	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E	76.7 (11.0 44.8 (7.3 % 0.0 (0.0 % ducation	%) 141. 6) 188. 6) 0. Medical	7 (20.2 %) 5 (30.8 %) 6 (100.0%)	ation	01.2 (32.9 %) 0.0 (0.0 %)	111.8 (18.3 %) 0.0 (0.0 %) n Others		
6 7 8 Panel No.	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures Foodstuffs	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E 292.0 (12.9 %) 15	76.7 (11.0 ° 44.8 (7.3 ° 0.0 (0.0 % ducation 5.7 (6.9 %)	%) 141. 6) 188. 6) 0.	7 (20.2 %) 5 (30.8 %) 6 (100.0%) Transports	26 ation 6 %)	0.0 (0.0 %) Communication	111.8 (18.3 %) 0.0 (0.0 %) n Others) 572.7 (25.3 %)		
6 7 8 Panel No.	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures Foodstuffs 712.3 (31.4 %)	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E 292.0 (12.9 %) 15 325.7 (10.5 %) 38	76.7 (11.0 44.8 (7.3 % 0.0 (0.0 % ducation 5.7 (6.9 %) 8.3 (12.5 %)	%) 141. 6) 188. 6) 0. Medical 89.3 (8.4 %)	7 (20.2 %) 5 (30.8 %) 6 (100.0%) Transports 218.1 (9.	ation 6 %)	0.0 (0.0 %) Communication 125.0 (5.5 %	111.8 (18.3 %) 0.0 (0.0 %) 0 Others 0 572.7 (25.3 %) 801.4 (25.8 %)		
6 7 8 Panel No.	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures Foodstuffs 712.3 (31.4 %) 856.1 (27.8 %)	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E 292.0 (12.9 %) 15 325.7 (10.5 %) 38 257.9 (11.4 %) 23	76.7 (11.0 44.8 (7.3 % 0.0 (0.0 % ducation 5.7 (6.9 %) 8.3 (12.5 %) 2.9 (10.2 %)	Medical 89.3 (8.4 %) 119.1 (7.0 %)	7 (20.2 %) 5 (30.8 %) 6 (100.0%) Transports 218.1 (9. 327.3 (10	ation 6 %) 0.5 %) 6 %)	0.0 (0.0 %) Communication 125.0 (5.5 % 181.7 (5.8 %)	111.8 (18.3 %) 0.0 (0.0 %) n Others) 572.7 (25.3 %)) 801.4 (25.8 %)) 537.5 (23.8 %)		
6 7 8 Panel No. 1 2 3	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures Foodstuffs 712.3 (31.4 %) 856.1 (27.8 %) 708.7 (31.4 %)	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E 292.0 (12.9 %) 15 325.7 (10.5 %) 38 257.9 (11.4 %) 23 296.5 (9.5 %) 41	76.7 (11.0 44.8 (7.3 % 0.0 (0.0 % ducation 5.7 (6.9 %) 8.3 (12.5 %) 9.9 (10.2 %) 8.5 (13.5 %) 2	Medical 89.3 (8.4 %). 19.1 (7.0 %) 64.2 (7.3 %)	7 (20.2 %) 5 (30.8 %) 6 (100.0%) Transports 218.1 (9. 327.3 (10. 217.3 (9.	ation 6 %) 0.5 %) 6 %) 0.4 %)	0.0 (0.0 %) 0.0 (0.0 %) Communication 125.0 (5.5 %) 181.7 (5.8 %) 142.5 (6.3 %)	111.8 (18.3 %) 0.0 (0.0 %) 0 Others 0 572.7 (25.3 %) 0 801.4 (25.8 %) 0 537.5 (23.8 %) 759.9 (24.4 %)		
6 7 8 Panel No. 1 2 3 4	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures Foodstuffs 712.3 (31.4 %) 856.1 (27.8 %) 708.7 (31.4 %) 885.2 (28.5 %)	20.1 (2.9 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E 292.0 (12.9 %) 325.7 (10.5 %) 325.7 (10.5 %) 296.5 (9.5 %) 41 260.5 (12.0 %) 23	76.7 (11.0 44.8 (7.3 % 0.0 (0.0 % ducation 5.7 (6.9 %) 8.3 (12.5 %) 8.5 (13.5 %) 8.5 (13.5 %)	Medical 89.3 (8.4 %) 19.1 (7.0 %) 64.2 (7.3 %) 27.9 (7.3 %)	7 (20.2 %) 5 (30.8 %) 6 (100.0%) Transport 218.1 (9 327.3 (1) 217.3 (9 323.7 (1)	ation 6 %) 0.5 %) 6 %) 0.4 %) 6 %)	0.0 (0.0 %) Communication 125.0 (5.5 %) 181.7 (5.8 %) 142.5 (6.3 %) 196.6 (6.3 %)	111.8 (18.3 %) 0.0 (0.0 %) Others 1 572.7 (25.3 %) 801.4 (25.8 %) 759.9 (24.4 %) 528.3 (24.3 %)		
6 7 8 Panel No. 1 2 3 4 5	6.0 (0.9 %) 1.6 (0.3 %) 0.0 (0.0 %) C. Expenditures Foodstuffs 712.3 (31.4 %) 856.1 (27.8 %) 708.7 (31.4 %) 885.2 (28.5 %) 677.6 (31.2 %)	20.1 (2.9 %) 9.0 (1.5 %) 9.0 (1.5 %) 0.0 (0.0 %) Housing E 292.0 (12.9 %) 1325.7 (10.5 %) 2352.7 (10.5 %) 246.5 (12.0 %) 2368.2 (17.9 %) 16.0 %	76.7 (11.0 44.8 (7.3 7 0.0 (0.0 %) ducation 5.7 (6.9 %) 1.8.3 (12.5 %) 2.9.9 (10.2 %) 13.5 %) 2.4.3 (10.8 %) 5.8 (8.1 %)	Medical 89.3 (8.4 %). 119.1 (7.0 %). 64.2 (7.3 %). 27.9 (7.3 %). 117.5 (5.3 %).	7 (20.2 %) 5 (30.8 %) 6 (100.0%) Transports 218.1 (9 327.3) (11 217.3 (9. 323.7) (10 209.0 (9.	ation 6 %) 0.5 %) 6 %) 0.4 %) 6 %) 0.1 %)	1.2 (32.9 %) 0.0 (0.0 %) Communication 125.0 (5.5 %) 181.7 (5.8 %) 142.5 (6.3 %) 196.6 (6.3 %)	111.8 (18.3 %) 0.0 (0.0 %) on Others) 572.7 (25.3 %)) 891.4 (25.8 %)) 537.5 (33.8 %) 759.9 (24.4 %)) 528.3 (24.3 %) 447.2 (21.7 %)		

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분석 결과

Figure 3 Major asset class of households with different level of wealth

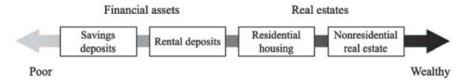
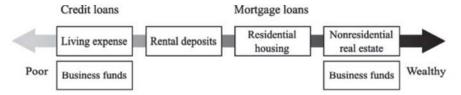
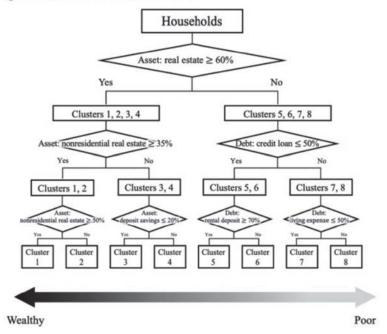


Figure 4 Major loan types of households with different level of wealth'



분석 결과

Figure 5 Decision tree for household clusters



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분석 결과

Table 4 Logistic regression results of clusters with respect to socio-demographic variables

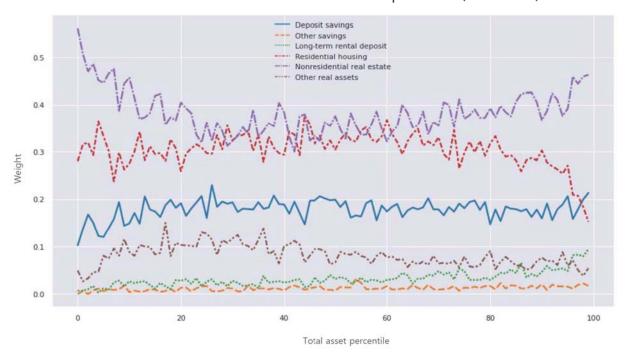
	Cluster 1		Cluster 2		Cluster 3		Cluster 4		Cluster 5		Cluster 6		Cluster 7		Cluster 8	
Variables	Coeff	Odds ratio	Coeff	Odds ratio	Coeff	Odds ratio	Coeff	Odds ratio	Coeff	Odds ratio	Coeff	Odds ratio	Coeff	Odds ratio	Coeff	Odds ratio
Constant	-5.224***	0.005	-3.972***	0.019	-2.833***	0.059	-3.025***	0.049	-1.402***	0.246	-0.367***	0.693	-0.088	0.916	-0.107***	0.899
Metropolitan area	0.642***	1.900	-0.646***	0.524	0.622***	1.863	-0.977***	0.376	0.794***	2.212	0.013	1.013	0.021	1.022	-0.205**	0.815
Gender (male)	0.224***	1.251	0.474***	1.607	-0.109***	0.897	-0.014	0.986	-0.411***	0.663	-0.225***	0.799	0.005	1.005	0.137**	1.147
Number of members	-0.349***	0.705	0.062***	1.064	-0.047***	0.954	0.338***	1.402	-0.098***	0.906	0.004	1.004	-0.068***	0.934	-0.525***	0.592
Education (Under middle school)																
High school	0.246***	1.279	-0.064*	0.938	-0.053	0.949	-0.353***	0.702	-0.050	0.951	0.204***	1.227	0.017	1.017	-0.599***	0.549
Higher education	0.773***	2.166	0.129***	1.138	0.134***	1.143	-0.751***	0.472	0.310***	1.363	-0.188***	0.829	-0.435***	0.647	-1.330***	0.264
Home ownership (None)																
Long-term rental	0.489***	1.630	0.597***	1.816	0.063	1.065	-0.463***	0.629	2.197***	8.995	-0.979***	0.376	-2.421***	0.089	-2.414***	0.089
Homeowner	1.486***	4.421	0.656***	1.927	2.806***	16.547	1.648***	5.197	-1.674***	0.187	-2.840***	0.058	-2.911***	0.054	-2.758***	0.063
Age (Under 39)																
40~49	0.665***	1.945	0.596***	1.815	-0.304***	0.738	0.385***	1.470	-0.578***	0.561	-0.170***	0.843	-0.177***	0.838	-0.139	0.870
50~59	1.330***	3.780	1.000***	2.718	-0.584***	0.558	0.164***	1.178	-0.850***	0.427	-0.368***	0.692	-0.251***	0.778	-0.019	0.981
Upper 60	2.539***	12.66	1.235***	3,440	-0.472***	0.624	-0.485***	0.616	-0.957***	0.384	-0.823***	0.439	-0.810***	0.445	-0.168	0.845
Income level (Low-income)																
Mid-income	0.338***	1.403	0.356***	1.428	-0.119***	0.888	-0.031***	0.734	-0.043	0.958	-0.326***	0.722	-0.855***	0.425	-1.753***	0.173
High-income	0.812***	2.252	0.799***	2.224	-0.358***	0.699	-0.257	0.773	-0.331***	0.718	-1.018***	0.361	-2.040***	0.130	-2.299***	0.100
Employment	0.012	1.012	0.628***	1.875	-0.491***	0.612	0.193***	1.213	-0.031	0.970	0.328***	1.388	-0.262***	0.769	-1.091***	0.336
Number of households	useholds 5,937		10,644		10,699		10,001		5,614		6,204		4,223		1,598	

*p < .05, **p < .01, ***p < .001

2022

분석 결과

2017~2020 Clustered household portfolio (Label = 2)



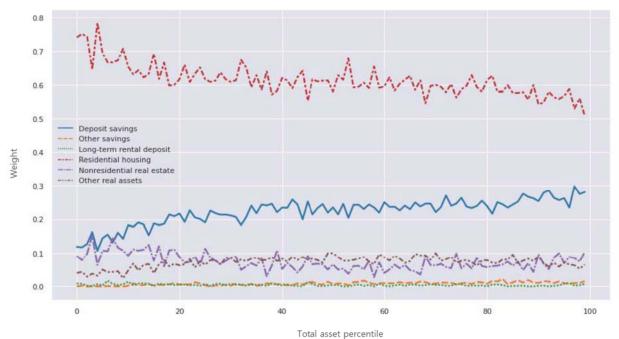
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분석 결과

2017~2020 Clustered household portfolio (Label = 4)



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결론

- 앞서 매우 비선형적이었던 자산 총액과 자산 유형별 비중의 관계가 훨씬 더 선형에 가까운 모습으로 나타나는 것을 확인 할 수 있음
- 딥 러닝은 고차원의 복잡한 관계성을 분석하는데 매우 유리함
- 즉, 본 연구에서는 고차원의 복잡한 관계성을 지니는 가구의 portfolio allocation을 딥 러닝을 통해 여러 군집으로 나누어 각 군집 안에서는 선형에 가깝게 나타낼 수 있었다
- 이렇게 실제 데이터를 몇 개의 군집으로 나누어 각각을 선형의 관계성으로 나타낼 수 있다면 consumption-based CAPM도 군집에 따라 따로 모델링하고 이를 통합하여 실제 데이터의 특성을 최대한 잘 반영하는 것도 가능하지 않을까?

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Thank you for listening!

