

# Lexical Analysis (Scanning)

## ◆ Basic Concepts & Regular Expressions

- What does a Lexical Analyzer do?
- How does it Work?
- Formalizing Token Definition & Recognition

## ◆ LEX - A Lexical Analyzer Generator

# The Role of the Lexical Analyzer

- ◆ **Lexical Analyzer** (词法分析器) is the first phase of a compiler, it reads the source program character by character to produce tokens for syntax analysis.
- ◆ Normally a lexical analyzer doesn't return a list of tokens at one shot, it returns a token when the parser asks a token from it.
- ◆ **Lexical analyzer = scanning + lexical analysis**

# Lexical Analysis

- Lexical analysis: Characters into Tokens

- Characters  $\rightarrow$  Scanner  $\rightarrow$  Tokens

- \* but that's not the whole story

- i:=i+1  $\rightarrow$  Scanner  $\rightarrow$  i:=i+1

- \* also filter whitespace (e.g. blank, tab)

- (/\*xz\*)  $\not\rightarrow$  Scanner  $\rightarrow$

- \* also filter comments

# Lexical Analysis (cont.)

- ◆ Reading the source program as a file of characters.
- ◆ Dividing the file up into tokens.
- ◆ **Tokens** (单词) : represents a unit of information in the source program.
- ◆ Examples: keywords (关键词/保留字), identifiers (标识符), arithmetic symbols, multicharacter symbols(>=, <>).
- ◆ **Emphasis:**
  - specification and recognition of tokens—Regular expression (正规/正则表达式)
  - how to recognize tokens--Finite automata (有限自动机)
  - design of a lexical analyzer—programming in C or LEX

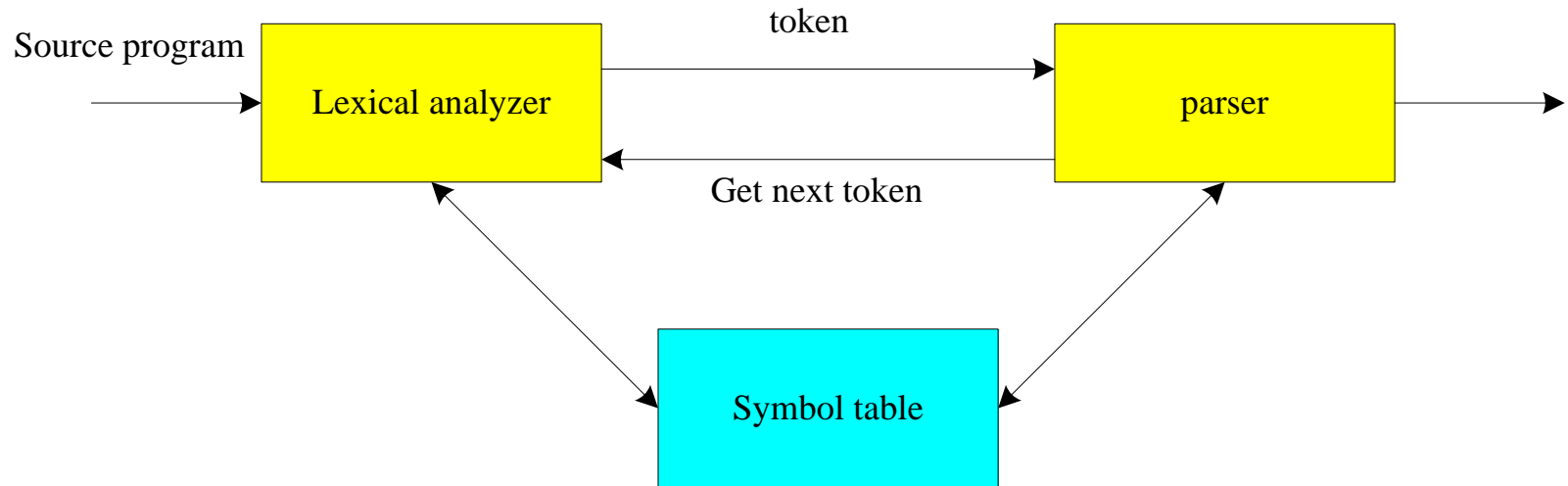


Fig.3.1. interaction of lexical analyzer with parser

What are responsibilities of each box ?

# Issues in lexical analysis

- ◆ Separation of Lexical Analysis From Parsing Presents a **Simpler Conceptual Model**
  - ◆ From a **Software Engineering Perspective** Division Emphasizes
    - ◆ High Cohesion and Low **Coupling**
    - ◆ Implies Well Specified  $\Rightarrow$  **Parallel** Implementation
- ◆ Separation Increases Compiler **Efficiency** (I/O Techniques to Enhance Lexical Analysis)
- ◆ Separation Promotes **Portability** (可移植性) .
  - ◆ This is critical today, when platforms (OSs and Hardware) are numerous and varied!
  - ◆ Emergence of Platform Independence – Java

# Lexical Analyzer in Perspective

## ◆ LEXICAL ANALYZER

- Scan Input
- Remove WS, NL, ...
- Identify Tokens
- Create Symbol Table
- Insert Tokens into ST
- Generate Errors
- Send Tokens to Parser

## ◆ PARSER

- Perform Syntax Analysis
- Actions Dictated by Token Order
- Update Symbol Table Entries
- Create Abstract Rep. of Source
- Generate Errors
- And More.... (We'll see later)

# Introducing Basic Terminology

What are Major Terms for Lexical Analysis?

## ◆TOKEN

- A classification for a common set of strings
- Examples Include <Identifier>, <number>, etc.

## ◆PATTERN

- The rules which characterize the set of strings for a token
- Recall File and OS Wildcards ([A-Z]\*. \*)

## ◆LEXEME

- Actual sequence of characters that matches pattern and is classified by a token
- Identifiers: x, count, name, etc...



# Token, pattern, lexemes

- ◆ Since a token can represent more than one lexeme, additional information should be held for that specific lexeme. This additional information is called as the *attribute* (属性) of the token.
- ◆ For simplicity, a token may have a single attribute which holds the required information for that token.
  - ◆ For identifiers, this attribute a pointer to the symbol table, and the symbol table holds the actual attributes for that token.
- ◆ Token type and its attribute uniquely identifies a lexeme.
- ◆ *Regular expressions* (正规表达式) are widely used to specify patterns.

# Token, pattern, lexemes

◆ Token is a logical unit in the scanner.

◆ A lexeme is an instance of token.

Token	Sample Lexemes	Informal Description of Pattern
const	const	const
if	if	if
relation	<, <=, =, < >, >, >=	< or <= or = or < > or >= or >
id	pi, <u>count</u> , <u>D2</u>	letter followed by letters and digits
<u>num</u>	<u>3.1416</u> , 0, 6.02E23	any numeric constant
literal	“core dumped”	any characters between “ and “ except “

Classifies  
Pattern

Actual values are critical. Info is :

1. Stored in symbol table
2. Returned to parser

Fig.3.2 Examples of tokens.

# Attributes for tokens

- ◆ An attribute of the token : any value associated to a token
- ◆ The lexical analyzer collects information about tokens into their associated attributes.
- ◆ The tokens influence parsing decisions; the attributes influence the translation of tokens.
- ◆ Usually a token has only a single attribute—a pointer to the symbol table entry in which the information about the token is kept.
- ◆ Some attributes: (cf. example 3.1)
  - `<id,attr>` where attr is pointer to the symbol table
  - `<assgop,_>` no attribute is needed (if there is only one assignment operator)
  - `<num,val>` where val is the actual value of the number.

# Scanning process

- ◆ tokens : the logical units which the scanner generates.
- ◆ Tokens fall into several categories:
  - **Reserved words**: IF, THEN
  - **Identifiers**: ID
  - **operation symbols**: PLUS, MINUS
  - **Numbers**: NUM
  - **Character and string**: STR
  - **Others**: {, }, (, ), :, ", ', /, \*

# Scanning process (cont.)

- ◆ Lexeme (string value): the strings of characters represented by a token.
- ◆ Tokens  $\longleftrightarrow$  one lexeme or many lexemes
- ◆ An attribute of the token : any value associated to a token
- ◆ Tokens  $\longleftrightarrow$  many attributes
- ◆ The scanner needs to compute at least as many attributes of a token .

# Scanning process (cont.)

- ◆ A token record :

```
typedef struct
{ TokenType tokenval;
  char *stringval;
  int numval;
} TokenRecord
```

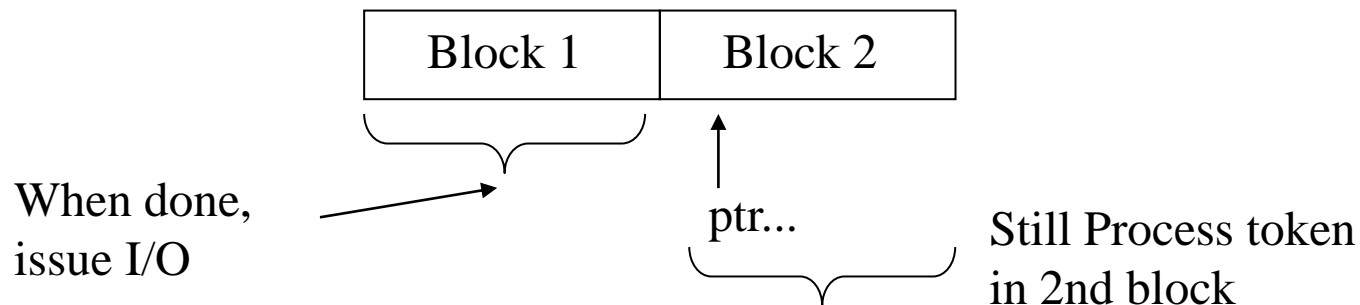
- ◆ A more common arrangement: the scanner return the token value only and place the other attributes in variables (such as in LEX and YACC).
- ◆ The string of input characters is kept in a **buffer** or provided by the system input facilities.

# Input buffering

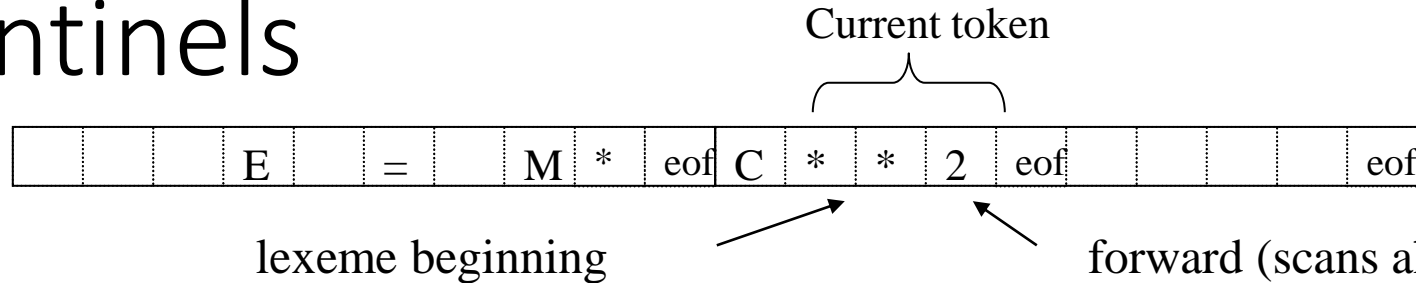
## ◆ Character-at-a-time I/O (getc, ungetc)

## ◆ Block / Buffered I/O

- Utilize Block of memory
- Stage data from source to buffer block at a time
- Maintain two blocks - Why (Recall OS)?
  - Asynchronous I/O - for 1 block
  - While Lexical Analysis on 2nd block



# Algorithm: Buffered I/O with Sentinels



```

forward := forward + 1 ;
if forward ↑ = eof then begin
  if forward at end of first half then begin
    reload second half ; ← Block I/O
    forward := forward + 1
  end
else if forward at end of second half then begin
  reload first half ; ← Block I/O
  move forward to beginning of first half
end
else /* eof within buffer signifying end of input */
  terminate lexical analysis
end
2nd eof ⇒ no more input !
  
```

Algorithm performs  
I/O's. We can still  
have get & ungetchar  
Now these work on  
real memory buffers !

Fig.3.6 Lookahead  
code with sentinels.



# Character-at-a-time I/O

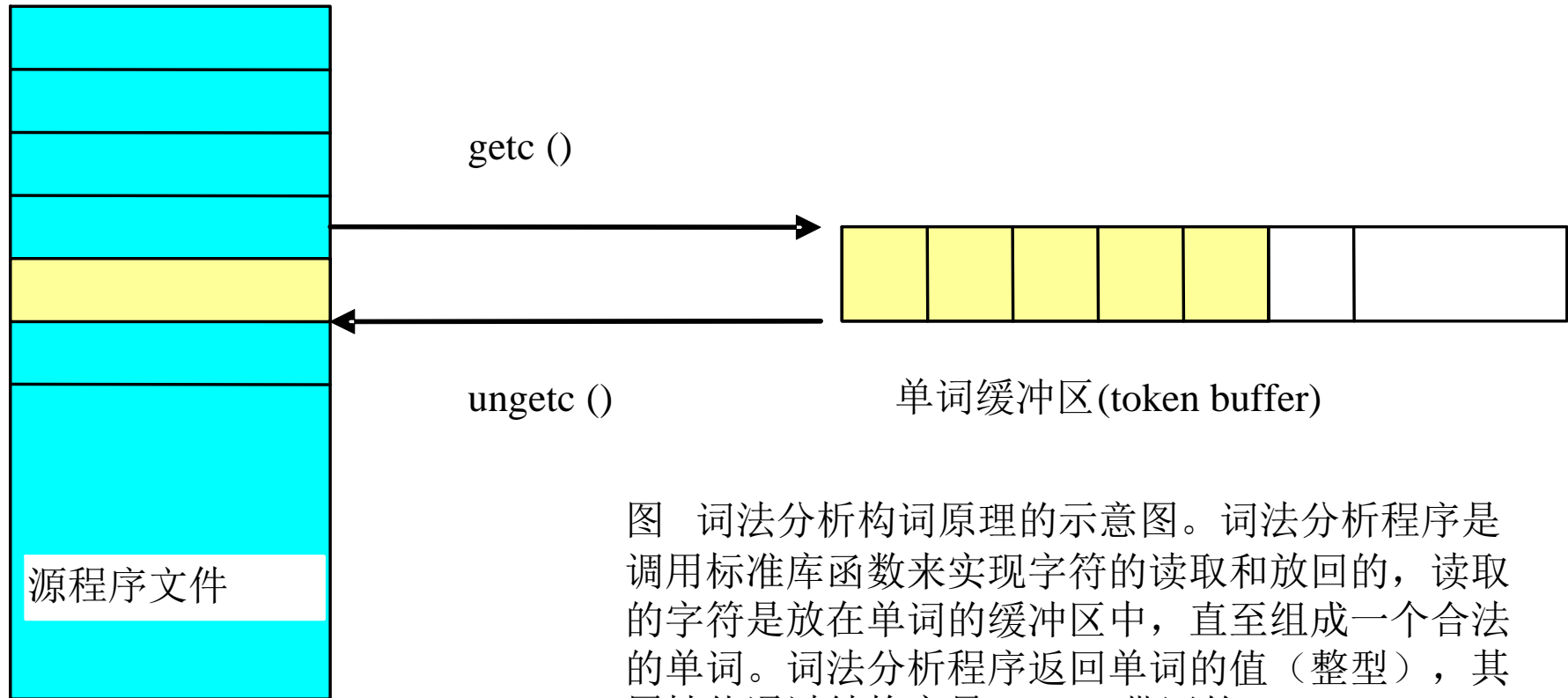


图 词法分析构词原理的示意图。词法分析程序是调用标准库函数来实现字符的读取和放回的，读取的字符是放在单词的缓冲区中，直至组成一个合法的单词。词法分析程序返回单词的值（整型），其属性值通过结构变量yyvalue带回的。

# Specification of tokens

Language Concepts :

A **language, L**, is simply any set of strings over a fixed alphabet.

Alphabet

Languages

$\{0,1\}$

$\{0,10,100,1000,100000\dots\}$

$\{0,1,00,11,000,111,\dots\}$

$\{a,b,c\}$

$\{abc,aabbcc,aaabbbccc,\dots\}$

$\{A, \dots, Z\}$

$\{TEE,FORE,BALL,\dots\}$

$\{FOR,WHILE,GOTO,\dots\}$

$\{A,\dots,Z,a,\dots,z,0,\dots 9,$   
 $+, -, \dots, <, >, \dots\}$

$\{\text{All legal PASCAL progs}\}$

$\{\text{All grammatically correct English sentences}\}$

Special Languages:  $\emptyset$  - EMPTY LANGUAGE

$\{\epsilon\}$  - contains  $\epsilon$  string only

# Terminology of Languages

◆ **Alphabet** : a finite set of symbols (ASCII characters)

◆ **String** :

- Finite sequence of symbols on an alphabet
- Sentence and word are also used in terms of string
- $\epsilon$  is the empty string
- $|s|$  is the length of string  $s$ .

# Terminology of Languages

## EXAMPLES AND OTHER CONCEPTS:

Suppose:  $S$  is the string `banana`

**Prefix** : `ban`, `banana`

**Suffix** : `ana`, `banana`

**Substring** : `nan`, `ban`, `ana`, `banana`

**Subsequence**: `bnan`, `nn`

**Proper** prefix, suffix, or substring *cannot* be all of  $S$

# Terminology of Languages (cont.)

## ◆ Language: sets of strings over some fixed alphabet

- $\emptyset$  the empty set is a language.
- $\{\epsilon\}$  the set containing empty string is a language
- The set of all possible identifiers is a language.

## ◆ Operators on Strings:

- *Concatenation*:  $xy$  represents the concatenation of strings  $x$  and  $y$ .  $s \epsilon = s$        $\epsilon s = s$
- $s^n = s s s \dots s$  (  $n$  times)       $s^0 = \epsilon$

# Operations on Languages

OPERATION	DEFINITION
<i>union</i> of L and M written $L \cup M$	$L \cup M = \{s \mid s \text{ is in } L \text{ or } s \text{ is in } M\}$
<i>concatenation</i> of L and M written LM	$LM = \{st \mid s \text{ is in } L \text{ and } t \text{ is in } M\}$
<i>Kleene closure</i> of L written $L^*$	$L^* = \bigcup_{i=0}^{\infty} L^i$ <p><math>L^*</math> denotes “zero or more concatenations of” L</p>
<i>positive closure</i> of L written $L^+$	$L^+ = \bigcup_{i=1}^{\infty} L^i$ <p><math>L^+</math> denotes “one or more concatenations of” L</p>

Fig.3.8 Definitions of operations on languages.

# Operations on Languages (Ex3.2)

$$L = \{A, B, C, D\}$$

$$D = \{1, 2, 3\}$$

$$L \cup D = \{A, B, C, D, 1, 2, 3\}$$

$$LD = \{A1, A2, A3, B1, B2, B3, C1, C2, C3, D1, D2, D3\}$$

$$L^2 = \{AA, AB, AC, AD, BA, BB, BC, BD, CA, \dots DD\}$$

$$L^4 = L^2 L^2 = ?? \quad \text{\textcolor{violet}{\{is the set of all four-letter strings\}}}$$

$$L^* = \{ \text{All possible strings of } L \text{ plus } \epsilon \}$$

$$L^+ = L^* - \epsilon \quad \text{\textcolor{brown}{\{is the set of strings beginning with a letter followed by a letter or digit\}}}$$

$$L(L \cup D)^* = ?? \quad \text{\textcolor{violet}{\{is the set of all strings of letters and digits beginning with a letter\}}}$$

# Language & Regular Expressions

- ◆ A **Regular Expression** is a Set of Rules / Techniques for Constructing Sequences of Symbols (Strings) From an Alphabet.
- ◆ Let  $\Sigma$  be an Alphabet,  $r$  a Regular Expression. Then  $L(r)$  is the Language, that is Characterized by the Rules of  $r$ .



# Regular Expressions

- ◆ We use regular expressions to describe tokens of a programming language.
- ◆ A regular expression is built up of simpler regular expressions using a set of defining rules.
- ◆ Each regular expression  $r$  denotes a language  $L(r)$ .
- ◆ A language  $L(r)$  denoted by a regular expression  $r$  is called as a **regular set**.

# Regular Expressions (cont.)

- ◆ a regular expression  $r$  is defined by the set of strings that it matches.
- ◆  $L(r)$ : language generated by the regular expression.
- ◆ **Character set**: be set of the ASCII characters or some subset of it
- ◆  $\Sigma$ : legal symbols, called alphabet.
- ◆ A regular repression symbols indicates patterns, metacharacters (metasymbols).
- ◆ Backslash and quotes(escape character): turns off the special meaning of a metacharacter.

# Rules for Specifying Regular Expressions

fix alphabet  $\Sigma$

- ◆  $\epsilon$  is a regular expression denoting  $\{\epsilon\}$
- ◆ If  $a$  is in  $\Sigma$ ,  $a$  is a regular expression that denotes  $\{a\}$
- ◆ Let  $r$  and  $s$  be regular expressions with languages  $L(r)$  and  $L(s)$ .  
Then

- $(r) \mid (s)$  is a regular expression  $\Rightarrow L(r) \cup L(s)$
- $(r)(s)$  is a regular expression  $\Rightarrow L(r) L(s)$
- $(r)^*$  is a regular expression  $\Rightarrow (L(r))^*$
- $(r)$  is a regular expression  $\Rightarrow L(r)$

All are Left-Associative. Parentheses are dropped as allowed by precedence rules.

# Rules for Specifying Regular Expressions (cont.)

Regular expressions over alphabet  $\Sigma$

<u>Reg. Expr</u>	<u>Language it denotes</u>
$\varepsilon$	$\{\varepsilon\}$
$a \in \Sigma$	$\{a\}$
$(r_1) \mid (r_2)$	$L(r_1) \cup L(r_2)$
$(r_1) (r_2)$	$L(r_1) L(r_2)$
$(r)^*$	$(L(r))^*$
$(r)$	$L(r)$
• $(r)^+ = (r)(r)^*$	$L(r)(L(r))^*$
• $(r)? = (r) \mid \varepsilon$	$L(r) \cup \{\varepsilon\}$

# Regular Expressions (Ex.)

## ◆ Ex:

➤  $\Sigma = \{0,1\}$

➤  $0 \mid 1 \Rightarrow \{0,1\}$

➤  $(0 \mid 1)(0 \mid 1) \Rightarrow \{00,01,10,11\}$

➤  $0^* \Rightarrow \{\epsilon, 0, 00, 000, 0000, \dots\}$

➤  $(0 \mid 1)^* \Rightarrow$  all strings with 0 and 1, including the empty string

➤

# Regular Expressions (Ex.)

$$L = \{A, B, C, D\} \quad D = \{1, 2, 3\}$$

$$L = A \mid B \mid C \mid D$$

$$L^2 = (A \mid B \mid C \mid D)(A \mid B \mid C \mid D)$$

$$L^* = (A \mid B \mid C \mid D)^*$$

$$L(L \cup D) = (A \mid B \mid C \mid D)((A \mid B \mid C \mid D) \mid (1 \mid 2 \mid 3))$$

AXIOM	DESCRIPTION
$r \mid s = s \mid r$	$\mid$ is commutative
$r \mid (s \mid t) = (r \mid s) \mid t$	$\mid$ is associative
$(r \ s) t = r (s \ t)$	concatenation is associative
$r (s \mid t) = r s \mid r t$ $(s \mid t) r = s r \mid t r$	concatenation distributes over $\mid$
$\epsilon r = r$ $r \epsilon = r$	$\epsilon$ is the identity element for concatenation
$r^* = (r \mid \epsilon)^*$	relation between $*$ and $\epsilon$
$r^{**} = r^*$	$*$ is idempotent

Fig.3.9 Algebraic Properties of Regular Expressions (P.96)

# Regular Expressions (Exercise)

◆  $\Sigma = \{A, \dots, Z, a, \dots, z\}$

All Strings that start with “**tab**” or end with “**bat**”:

$$\text{tab}[A, \dots, Z, a, \dots, z]^* \mid [A, \dots, Z, a, \dots, z]^* \text{bat}$$

◆  $\Sigma = \{A, \dots, Z\}$

All Strings in Which Digits **1,2,3** exist in ascending numerical order:

$$[A, \dots, Z]^* \text{1} [A, \dots, Z]^* \text{2} [A, \dots, Z]^* \text{3} [A, \dots, Z]^*$$




# Regular Definitions

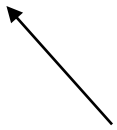
- ◆ To write regular expression for some languages can be difficult, because their regular expressions can be quite complex. In those cases, we may use *regular definitions*.
- ◆ We can give names to regular expressions, and we can use these names as symbols to define other regular expressions.

- ◆ A *regular definition* is a sequence of the definitions of the form:

$$\begin{array}{ll}
 d_1 \rightarrow r_1 & \text{where } d_i \text{ is a distinct name and} \\
 d_2 \rightarrow r_2 & r_i \text{ is a regular expression over symbols in} \\
 \vdots & \Sigma \cup \{d_1, d_2, \dots, d_{i-1}\} \\
 d_n \rightarrow r_n &
 \end{array}$$



basic symbols



previously defined names

# Regular Definitions (cont.)

## Regular Definitions: Associate names with Regular Expressions

### Example 3.4 : PASCAL IDs

letter  $\rightarrow$  A | B | C | ... | Z | a | b | ... | z

digit  $\rightarrow$  0 | 1 | 2 | ... | 9

id  $\rightarrow$  letter ( letter | digit ) \*

#### Shorthand Notation:

- ✓ “+” : one or more  $r^* = r^+ \mid \in \& \quad r^+ = r r^*$
- ✓ “?” : zero or one  $r^? = r \mid \in$
- ✓ [range] : set range of characters (replaces “|”)

[A-Z] = A | B | C | ... | Z

#### Example Using Shorthand : PASCAL IDs

id  $\rightarrow$  [A-Za-z][A-Za-z0-9]\*

# Exercise in class

1. Given:  $\Sigma = \{a, b, c\}$ , describing the set of all strings that contain at most one  $b$  with regular expression.

2. Example 3.5:

Given: letter  $\rightarrow A \mid B \mid \dots \mid Z \mid a \mid b \mid \dots \mid z$

digit  $\rightarrow 0 \mid 1 \mid \dots \mid 9$

Describing identifiers and numbers in Pascal or C with regular expression.

# Exercise in class (cont.)

## ◆ EX: $\Sigma = \{a, b, c\}$

the set of all strings that contain at most one b.

$$(a|c)^*(b|\epsilon)(a|c)^*$$

$$(a|c)^* | (a|c)^*b(a|c)^*$$

the same language may be generated by many different regular expressions.

## ◆ Ex: Identifiers in Pascal or C

$$\text{letter} \rightarrow A | B | \dots | Z | a | b | \dots | z$$

$$\text{digit} \rightarrow 0 | 1 | \dots | 9$$

$$\text{id} \rightarrow \text{letter} (\text{letter} | \text{digit})^*$$

If we try to write the regular expression representing identifiers without using regular definitions, that regular expression will be complex.

$$(A|\dots|Z|a|\dots|z) \left( (A|\dots|Z|a|\dots|z) | (0|\dots|9) \right)^*$$

# Exercise in class (cont.)

Ex: Unsigned numbers in Pascal or C

digit  $\rightarrow$  0 | 1 | ... | 9

digits  $\rightarrow$  digit<sup>+</sup>

opt-fraction  $\rightarrow$  ( . digits ) ?

opt-exponent  $\rightarrow$  ( E ( + | - ) ? digits ) ?

unsigned-num  $\rightarrow$  digits opt-fraction opt-exponent

# Review

- ◆ Lexical analyzer (scanner) 词法分析器
- ◆ Syntax analyzer (parser) 语法分析器
- ◆ Token 单词
- ◆ Attribute 属性
- ◆ Regular expression 正规/正则表达式
- ◆ Regular definition 正规定义
- ◆ Transition Diagram (TD) 转换图
- ◆ Finite Automata (FA) 有限自动机
- ◆ Nondeterministic Finite Automata (NFA) 不确定的有限自动机
- ◆ Deterministic Finite Automata (DFA) 确定的有限自动机

# Review

- ◆ Reviewing Finite Automata Concepts
  - Non-Deterministic and Deterministic FA
  - Conversion Process
    - Regular Expressions to NFA
    - NFA to DFA
    - Regular Expressions to DFA
- ◆ Relating NFAs/DFAs /Conversion to Lexical Analysis
- ◆ Concluding Remarks /Looking Ahead