$$f = \Omega(\log(\frac{n}{b}))$$