# Additional Experiments for Paper 5433

### July 31, 2022

In this report we present the additional experiments for DSPL/DSEPL on robust nonlinear regression problem with larger size. We also kindly remind the reviewer of our additional experiments on blind deconvolution problem, which is available in the appendix section **C**.

Given sample data  $\{a_i \in \mathbb{R}^n\}_{i=1,\dots,m}$  and corresponding observations  $\{y_i\}_{i=1,\dots,m}$ , the robust non-linear regression problem aims to fit  $y_i$  using nonlinear model  $y = f(\langle a, x \rangle)$  by solving

$$\min_{x \in \mathbb{R}^n} \quad \frac{1}{m} \sum_{i=1}^m |f(\langle a_i, x \rangle) - b_i|,$$

where f is a given nonlinear function. When  $f(x) = x^2$ , we get the robust phase retrieval problem. We report the performance in asynchronous environment.

#### Experiment setup

- 1) Dataset. We take m = 7500, n = 2500 in the experiment. Given some nonlinear function f, we generate sample data  $A \in \mathbb{R}^{m \times n}$ , true signal  $x^*$  as in phase retrieval and let  $y_i = f(a^{\top}x)$ .
- 2) Initial point. We generate  $x' \sim \mathcal{N}(0, I_n)$  and start from  $x^0 = x^1 = \frac{x'}{\|x'\|}$ .
- 3) Stepsize. We tune the stepsize parameter setting  $\gamma = \sqrt{K/\alpha}, \alpha \in \{0.1, 0.5, 1.0\}$  for asynchronous environment and  $\alpha \in [10^0, 10^1]$  for the simulated experiment.
- 4) Nonlinear function. We choose functions  $f \in \{f_1 = 2x + \cos x, f_2 = 10 + e^x, f_3 = x^3 + x^2, f_4 = x^2\}$  to characterize the nonlinear relation. Note that  $f_4$  corresponds to larger phase retrieval data.
- 5) Others. The rest of the setup is consistent with phase retrieval.

#### Asynchronous environment

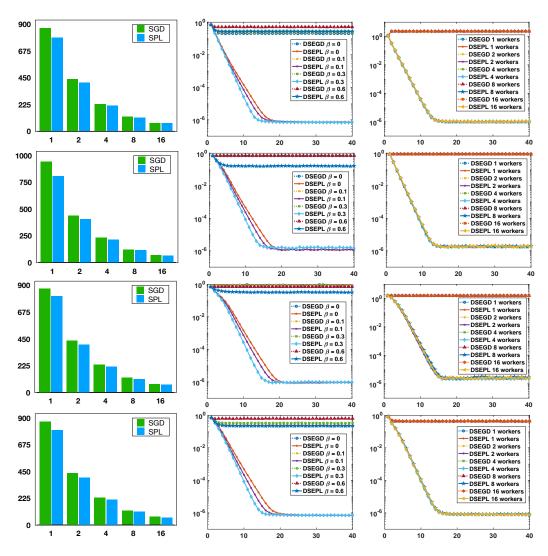


Figure 1: From the first row to the last:  $f_1 = 2x + \cos x$ ,  $f_2 = 10 + e^x$ ,  $f_3 = x^3 + x^2$ ,  $f_4 = x^2$ . In each row, the first figure indicates speedup as the number of workers increases; the second plots  $||x^k - x^*||$  for  $\alpha = 0.5$  and different  $\beta$ ; the last plots  $f(x^k) - f^*$  for  $\alpha = 0.5$ ,  $\beta = 0.3$  ( $f_4$  uses  $\alpha = 0.1$ ).

## Simulated delay

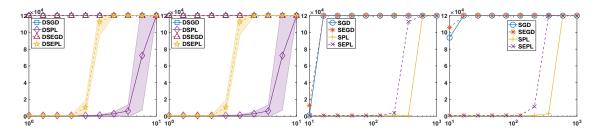


Figure 2: Experiments of simulated delay for the robust nonlinear regression problem using  $f_2 = 10 + e^x$ ,  $\kappa = 10$ ,  $p_{\rm fail} = 0.25$ . Two figures on the left: the number of iterations with different stepsize  $\alpha$  and  $\beta = 0.3$ ,  $\tau \in \{216, 360\}$ ; Two figures on the right: the number of iterations with different  $\tau \in [1, 1000]$  and  $\beta = 0.3$ ,  $\alpha \in \{3.60, 4.65\}$ .