

`In[*]:= Clear[γ];`

$$\kappa = \frac{4 K}{\gamma} + \frac{\gamma}{4 - \gamma};$$

`In[*]:= r = $\left(\frac{\kappa - 1}{\kappa + 1}\right)$ // FullSimplify`

`Out[*]=`

$$\frac{8 K - 2 (1 + K) \gamma + \gamma^2}{-2 K (-4 + \gamma) + 2 \gamma}$$

`In[*]:= FullSimplify[$\forall_{K, K \geq 1} r^2 \geq \left(\frac{K}{\gamma + K}\right)^2$, Assumptions $\rightarrow 0 \leq \gamma \leq 4$]`

`Out[*]=`
True