

Exercise 1

Write in the simplest way the following vectors and matrices.

$$v1 = (5 \ 6 \ 7 \ 8 \ 9 \ 10) \quad v2 = (0 \ 0 \ 0 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10 \ 1 \ 1 \ 1 \ 1)$$

$$v3 = (0 \ 1 \ 2 \ 3 \ 4 \ 9 \ 7 \ 5 \ 3 \ 1)$$

$$M1 = \begin{pmatrix} 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 \end{pmatrix} \quad M2 = \begin{pmatrix} 1 & 3 & 5 & 7 & 9 \\ 8 & 6 & 4 & 2 & 0 \\ 8 & 6 & 4 & 2 & 0 \end{pmatrix} \quad M3 = \begin{pmatrix} 0 & 0 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 2 & 3 & 4 & 5 \end{pmatrix}$$

Exercise 2

Write in the simplest way the following matrix.

$$M4 = \begin{pmatrix} 2. & 1. & 0. & 0. & 0. & 0. & 0. & 0. \\ 1. & 4. & 1. & 0. & 0. & 0. & 0. & 0. \\ 0. & 1. & 4. & 1. & 0. & 0. & 0. & 0. \\ 0. & 0. & 1. & 4. & 1. & 0. & 0. & 0. \\ 0. & 0. & 0. & 1. & 4. & 1. & 0. & 0. \\ 0. & 0. & 0. & 0. & 1. & 4. & 1. & 0. \\ 0. & 0. & 0. & 0. & 0. & 1. & 4. & 1. \\ 0. & 0. & 0. & 0. & 0. & 0. & 1. & 2. \end{pmatrix}$$

Exercise 3

Triangle of Pascal. Write a program in Python computing each line “ n ” of the triangle of Pascal for $0 \leq n \leq N_{\max}$ as below.

```
Enter N_max : 7
n = 0 : [ 1.]
n = 1 : [ 1.  1.]
n = 2 : [ 1.  2.  1.]
n = 3 : [ 1.  3.  3.  1.]
n = 4 : [ 1.  4.  6.  4.  1.]
n = 5 : [ 1.  5. 10. 10.  5.  1.]
n = 6 : [ 1.  6. 15. 20. 15.  6.  1.]
n = 7 : [ 1.  7. 21. 35. 35. 21.  7.  1.]
```

Exercise 4

Sieve of Eratosthenes. Write a program in Python allowing to determine all the prime numbers lower than N_{\max} , with an algorithm using the “sieve of Eratosthenes”.

```
Enter N_max : 154
[ 2  3  5  7 11 13 17 19 23 29 31 37 41 43
```

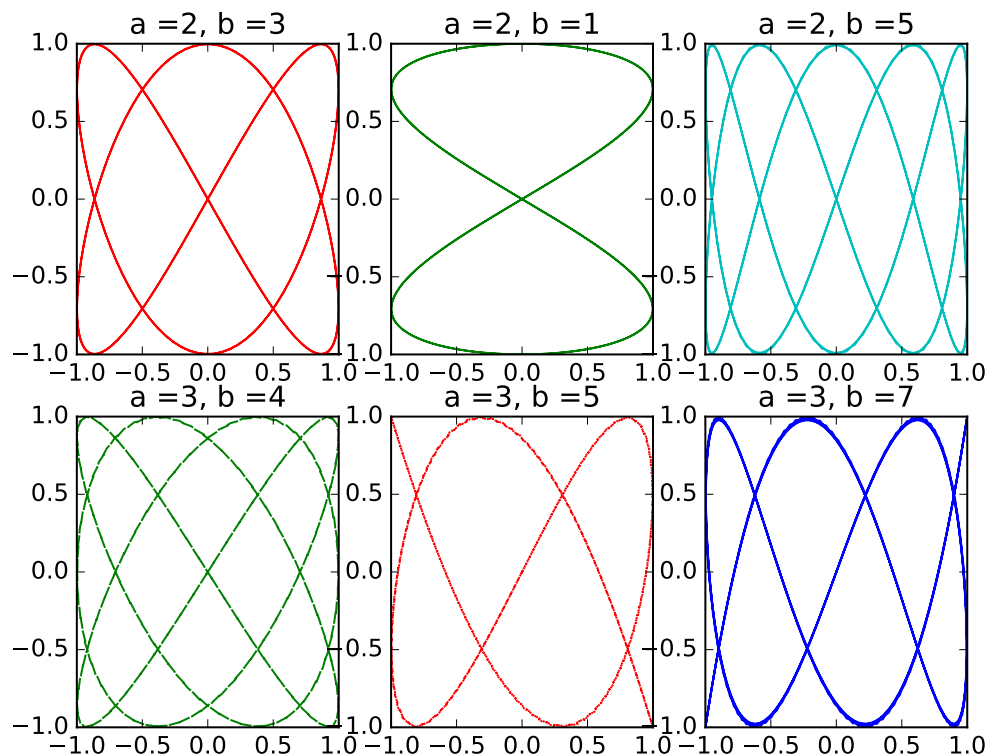
47 53 59 61 67 71 73 79 83 89 97 101 103 107
109 113 127 131 137 139 149 151]

Exercise 5

Write a Python program to draw the Lissajous curves $t \in [0, 2\pi] \mapsto (\sin(at), \sin(bt))$, as shown in the figure below. For this purpose, create the file `exoLissajousTools.py` given below and create a second Python file `exoLissajousDrawing.py` using the function "sinatsinbt".

```
# File exof41LissajousTools.py
import numpy as np

def sinatsinbt(t,a,b):
    x = np.sin(a*t)
    y = np.sin(b*t)
    return x,y
```



Le compte rendu de ce TP consistera en un fichier pdf dont le nom sera `TP1_NOM1_NOM2.pdf`. Ce fichier pdf contiendra en entête les noms `NOM1` et `NOM2`, puis

- le script Python demandé pour chacun des exercices
- la sortie graphique demandée dans le dernier exercice.