# ÁLGEBRA

## Operações Aritméticas

$$a(b+c) = ab + ac$$

$$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$$

$$\frac{a+c}{b} = \frac{a}{b} + \frac{c}{b}$$

$$\frac{\frac{a}{b}}{\frac{c}{d}} = \frac{a}{b} \times \frac{d}{c} = \frac{ad}{bc}$$

#### Expoentes e Radicais

$$x^m x^n = x^{m+n}$$

$$\frac{x^m}{x^n} = x^{m-n}$$

$$(x^m)^n = x^{mn}$$

$$x^{-n} = \frac{1}{x^n}$$

$$(xy)^n = x^n y^n$$

$$\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n}$$

$$x^{1/n} = \sqrt[n]{x}$$

$$x^{m/n} = \sqrt[n]{x^m} = (\sqrt[n]{x})^m$$

$$\sqrt[n]{xy} = \sqrt[n]{x}\sqrt[n]{y}$$

$$\sqrt[n]{\frac{x}{y}} = \frac{\sqrt[n]{x}}{\sqrt[n]{y}}$$

#### Fatoração de Polinômios Especiais

$$x^2 - y^2 = (x + y)(x - y)$$

$$x^3 + y^3 = (x + y)(x^2 - xy + y^2)$$

$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

#### Teorema Binomial

$$(x + y)^2 = x^2 + 2xy + y$$

$$(x + y)^2 = x^2 + 2xy + y^2$$
  $(x - y)^2 = x^2 - 2xy + y^2$ 

$$(x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

$$(x - y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

$$(x + y)^n = x^n + nx^{n-1}y + \frac{n(n-1)}{2}x^{n-2}y^2$$

$$+\cdots+\binom{n}{k}x^{n-k}y^k+\cdots+nxy^{n-1}+y^n$$

onde 
$$\binom{n}{k} = \frac{n(n-1)\cdots(n-k+1)}{1\cdot 2\cdot 3\cdot \cdots \cdot k}$$

## Fórmula Quadrática

Se 
$$ax^2 + bx + c = 0$$
, então,  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

#### Desigualdades e Valor Absoluto

Se a < b e b < c, então a < c.

Se a < b, então a + c < b + c.

Se a < b e c > 0, então ca < cb.

Se a < b e c < 0, então ca > cb.

Se a > 0, então

$$|x| = a$$
 significa que  $x = a$  ou  $x = -a$ 

|x| < a significa que -a < x < a

|x| > a significa que x > a ou x < -a

## **GEOMETRIA**

#### Fórmulas Geométricas

Fórmulas para área A, circunferência C e volume V:

Triângulo

Círculo

Setor do Círculo

 $A = \frac{1}{2}bh$ 

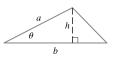
 $A = \pi r^2$ 

 $A = \frac{1}{2}r^2\theta$ 

 $=\frac{1}{2}ab \operatorname{sen} \theta$ 

 $C = 2\pi r$ 

 $s = r\theta (\theta \text{ em radianos})$ 







Esfera

 $V = \frac{4}{3} \pi r^3$  $A = 4\pi r^2$  Cilindro  $V = \pi r^2 h$  Cone

 $V = \frac{1}{3} \pi r^2 h$ 

 $A = \pi r \sqrt{r^2 + h^2}$ 







#### Fórmulas de Distância e Ponto Médio

Distância entre  $P_1(x_1, y_1)$  e  $P_2(x_2, y_2)$ :

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Ponto Médio de 
$$\overline{P_1P_2}$$
:  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$ 

Retas

Inclinação da reta através de  $P_1(x_1, y_1)$  e  $P_2(x_2, y_2)$ :

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Coeficiente angular da reta através de  $P_1(x_1, y_1)$  com inclinação m:

$$y - y_1 = m(x - x_1)$$

Função afim da reta com inclinação m e interceptando o eixo y em b:

$$y = mx + b$$

Circulos

Equação do círculo com centro (h, k) e raio r:

$$(x - h)^2 + (y - k)^2 = r^2$$

## TRIGONOMETRIA

#### Medição do Ângulo

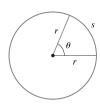
 $\pi$  radianos =  $180^{\circ}$ 

$$1^{\circ} = \frac{\pi}{180}$$
 rad

$$1 \text{ rad} = \frac{180^{\circ}}{\pi}$$



 $(\theta \text{ em radianos})$ 



## Trigonometria de Ângulo Reto

$$sen \theta = \frac{opo}{hip}$$

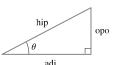
$$\operatorname{cossec} \theta = \frac{\operatorname{hip}}{\operatorname{opo}}$$

$$\cos\,\theta = \frac{\mathrm{adj}}{\mathrm{hip}}$$

$$\sec \theta = \frac{\text{hip}}{\text{adj}}$$

$$tg \theta = \frac{opo}{adj}$$

$$\cot \theta = \frac{\text{adj}}{\text{opo}}$$



## Funções Trigonométricas

$$sen \theta = \frac{y}{x}$$

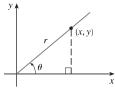
$$cossec \ \theta = \frac{r}{v}$$

$$\cos \theta = \frac{1}{2}$$

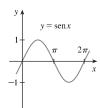
$$\cos \theta = \frac{x}{r} \qquad \qquad \sec \theta = \frac{r}{x}$$

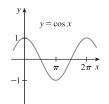
$$tg \theta = \frac{y}{x}$$

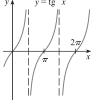
$$\cot \theta = \frac{x}{y}$$

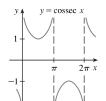


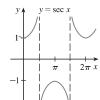
## Gráficos de Funções Trigonométricas

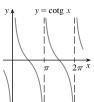












## Funções Trigonométricas de Ângulos Importantes

$\theta$	radianos	sen $\theta$	$\cos \theta$	tg $\theta$
0°	0	0	1	0
30°	$\pi/6$	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$
45°	$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
60°	$\pi/3$	$\sqrt{3}/2$	1/2	$\sqrt{3}$
90°	$\pi/2$	1	0	_

#### Identidades Fundamentais

$$\operatorname{cossec} \theta = \frac{1}{\operatorname{sen} \theta}$$

$$\sec \theta = \frac{1}{\cos \theta}$$

$$tg \theta = \frac{sen \theta}{cos \theta}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta}$$

$$\cot \theta = \frac{1}{\operatorname{tg} \, \theta}$$

$$\sin^2\theta + \cos^2\theta = 1$$

$$1 + tg^2\theta = \sec^2\theta$$

$$1 + \cot^2\theta = \csc^2\theta$$

$$sen(-\theta) = -sen \ \theta$$

$$\cos(-\theta) = \cos\,\theta$$

$$tg(-\theta) = -tg \ \theta$$

$$\operatorname{sen}\left(\frac{\pi}{2} - \theta\right) = \cos\theta$$

$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin\theta$$

$$tg\left(\frac{\pi}{2} - \theta\right) = \cot\theta$$

#### Lei dos Senos

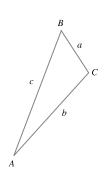
$$\frac{\operatorname{sen} A}{a} = \frac{\operatorname{sen} B}{b} = \frac{\operatorname{sen} C}{c}$$

## Lei dos Cossenos

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$b^2 = a^2 + c^2 - 2ac\cos B$$

$$c^2 = a^2 + b^2 - 2ab\cos C$$



### Fórmulas de Adição e Subtração

$$sen(x + y) = sen x cos y + cos x sen y$$

$$sen(x - y) = sen x cos y - cos x sen y$$

$$\cos(x + y) = \cos x \cos y - \sin x \sin y$$

$$cos(x - y) = cos x cos y + sen x sen y$$

$$tg(x + y) = \frac{tg x + tg y}{1 - tg x tg y}$$

$$tg(x - y) = \frac{tg x - tg y}{1 + tg x tg y}$$

### Fórmulas de Ângulo Duplo

$$\cos 2x = \cos^2 x - \sin^2 x = 2\cos^2 x - 1 = 1 - 2\sin^2 x$$

$$tg \ 2x = \frac{2 tg \ x}{1 - tg^2 x}$$

#### Fórmulas de Metade do Ângulo

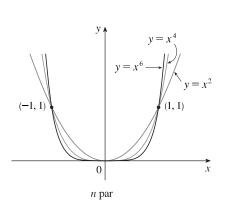
$$\sin^2 x = \frac{1 - \cos 2x}{2} \qquad \cos^2 x = \frac{1 + \cos 2x}{2}$$

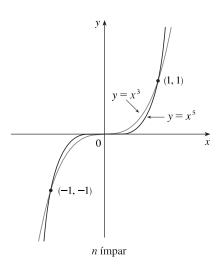
$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

# FUNÇÕES ESPECIAIS

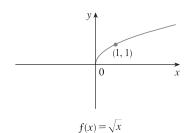
Funções Potências  $f(x) = x^a$ 

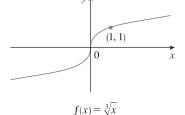
(i)  $f(x) = x^n$ , *n* um inteiro positivo



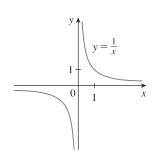


(ii)  $f(x) = x^{1/n} = \sqrt[n]{x}$ , n um inteiro positivo





(iii)  $f(x) = x^{-1} = \frac{1}{x}$ 

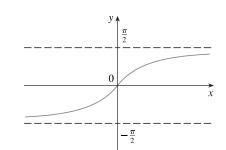


Funções Trigonométricas Inversas

$$\arcsin x = \sin^{-1} x = y \iff \sin y = x \text{ e } -\frac{\pi}{2} \le y \le \frac{\pi}{2}$$

$$\arccos x = \cos^{-1} x = y \iff \cos y = x \text{ e } 0 \le y \le \pi$$

$$\operatorname{arctg} x = \operatorname{tg}^{-1} x = y \iff \operatorname{tg} y = x \text{ e } -\frac{\pi}{2} < y < \frac{\pi}{2}$$



 $y = tg^{-1}x = arctg x$ 

$$\lim_{x \to -\infty} \mathsf{tg}^{-1} x = -\frac{\pi}{2}$$

$$\lim_{x \to \infty} \mathsf{tg}^{-1} x = \frac{\pi}{2}$$

# FUNÇÕES ESPECIAIS

Funções Exponenciais e Logarítmicas

$$\log_a x = y \iff a^y = x$$

$$\ln x = \log_e x$$
, onde  $\ln e = 1$ 

$$\ln x = y \iff e^y = x$$

Equações de Cancelamento

 $\log_a(a^x) = x \qquad a^{\log_a x} = x$ 

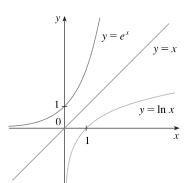
$$\ln(e^x) = x \qquad e^{\ln x} = x$$

Leis de Logaritmos

$$1. \log_a(xy) = \log_a x + \log_a y$$

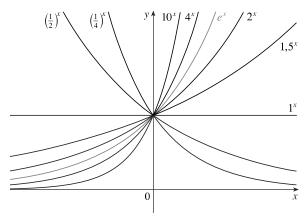
$$2. \log_a \left(\frac{x}{y}\right) = \log_a x - \log_a y$$

$$3. \log_a(x^r) = r \log_a x$$

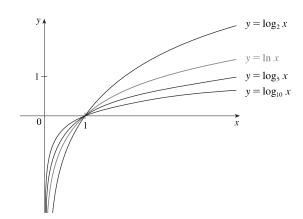


$$\lim_{x \to -\infty} e^x = 0 \qquad \qquad \lim_{x \to \infty} e^x = \infty$$

$$\lim_{x \to 0^+} \ln x = -\infty \qquad \qquad \lim_{x \to \infty} \ln x = \infty$$



Funções Exponenciais



Funções Logarítmicas

#### Funções Hiperbólicas

$$senh x = \frac{e^x - e^{-x}}{2}$$
 cossech  $x = \frac{1}{senh x}$ 

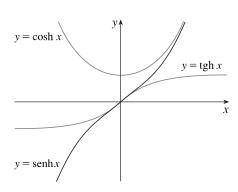
$$\operatorname{cossech} x = \frac{1}{\operatorname{senh} x}$$

$$\cosh x = \frac{e^x + e^{-x}}{2}$$

$$\operatorname{sech} x = \frac{1}{\cosh x}$$

$$tgh x = \frac{\operatorname{senh} x}{\cosh x}$$

$$\operatorname{cotgh} x = \frac{\cosh x}{\sinh x}$$



## Funções Hiperbólicas Inversas

$$y = \operatorname{senh}^{-1} x \iff \operatorname{senh} y = x$$

$$y = \cosh^{-1} x \iff \cosh y = x \text{ e } y \ge 0$$

$$y = tgh^{-1}x \iff tgh \ y = x$$

$$\operatorname{senh}^{-1} x = \ln(x + \sqrt{x^2 + 1})$$

$$\cosh^{-1}x = \ln(x + \sqrt{x^2 - 1})$$

$$tgh^{-1}x = \frac{1}{2}\ln\left(\frac{1+x}{1-x}\right)$$

# REGRAS DE DIFERENCIAÇÃO

Fórmulas Gerais

$$1. \ \frac{d}{dx}(c) = 0$$

**3.** 
$$\frac{d}{dx}[f(x) + g(x)] = f'(x) + g'(x)$$

**5.** 
$$\frac{d}{dx} [f(x)g(x)] = f(x)g'(x) + g(x)f'(x)$$
 (Regra de Produto)

7. 
$$\frac{d}{dx} f(g(x)) = f'(g(x))g'(x)$$
 (Regra da Cadeia)

$$2. \frac{d}{dx} [cf(x)] = cf'(x)$$

**4.** 
$$\frac{d}{dx}[f(x) - g(x)] = f'(x) - g'(x)$$

**6.** 
$$\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{g(x)f'(x) - f(x)g'(x)}{[g(x)]^2}$$
 (Regra do Quociente)

**8.** 
$$\frac{d}{dx}(x^n) = nx^{n-1}$$
 (Regra da Potência)

Funções Exponenciais e Logarítmicas

$$9. \ \frac{d}{dx}(e^x) = e^x$$

$$11. \frac{d}{dx} \ln|x| = \frac{1}{x}$$

$$\mathbf{10.} \ \frac{d}{dx}(a^x) = a^x \ln a$$

$$12. \ \frac{d}{dx} (\log_a x) = \frac{1}{x \ln a}$$

Funções Trigonométricas

$$\mathbf{13.} \, \frac{d}{dx} (\operatorname{sen} x) = \cos x$$

**16.** 
$$\frac{d}{dx}$$
 (cossec  $x$ ) =  $-$ cossec  $x$  cotg  $x$ 

$$14. \ \frac{d}{dx}(\cos x) = -\sin x$$

17. 
$$\frac{d}{dx}(\sec x) = \sec x \operatorname{tg} x$$

Funcões Trigonométricas Inversas

**19.** 
$$\frac{d}{dx} (\text{sen}^{-1}x) = \frac{1}{\sqrt{1-x^2}}$$

**22.** 
$$\frac{d}{dx} (\operatorname{cossec}^{-1} x) = -\frac{1}{x\sqrt{x^2 - 1}}$$

**20.** 
$$\frac{d}{dx}(\cos^{-1}x) = -\frac{1}{\sqrt{1-x^2}}$$

**23.** 
$$\frac{d}{dx}(\sec^{-1}x) = \frac{1}{x\sqrt{x^2 - 1}}$$

**21.** 
$$\frac{d}{dx}(tg^{-1}x) = \frac{1}{1+x^2}$$

**24.** 
$$\frac{d}{dx}(\cot g^{-1}x) = -\frac{1}{1+x^2}$$

Funções Hiperbólicas

**25.** 
$$\frac{d}{dx} (\operatorname{senh} x) = \cosh x$$

**28.** 
$$\frac{d}{dx}$$
 (cossech  $x$ ) =  $-$ cossech  $x$  cotgh  $x$ 

**26.** 
$$\frac{d}{dx}(\cosh x) = \sinh x$$

**29.** 
$$\frac{d}{dx}(\operatorname{sech} x) = -\operatorname{sech} x \operatorname{tgh} x$$

$$27. \frac{d}{dx} (tgh x) = sech^2 x$$

**30.** 
$$\frac{d}{dx}(\cot h x) = -\operatorname{cossech}^2 x$$

Funções Hiperbólicas Inversas

**31.** 
$$\frac{d}{dx} (\operatorname{senh}^{-1} x) = \frac{1}{\sqrt{1 + x^2}}$$

**32.** 
$$\frac{d}{dx} \left( \cosh^{-1} x \right) = \frac{1}{\sqrt{x^2 - 1}}$$

**34.** 
$$\frac{d}{dx} (\operatorname{cossech}^{-1} x) = -\frac{1}{|x|\sqrt{x^2 + 1}}$$
 **35.**  $\frac{d}{dx} (\operatorname{sech}^{-1} x) = -\frac{1}{x\sqrt{1 - x^2}}$ 

**33.** 
$$\frac{d}{dx} (tgh^{-1}x) = \frac{1}{1 - x^2}$$

**36.** 
$$\frac{d}{dx} \left( \coth^{-1} x \right) = \frac{1}{1 - x^2}$$