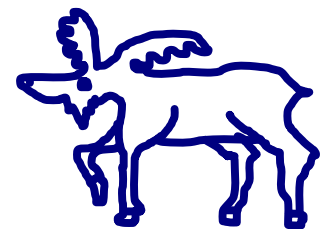


# Lecture 21

## Direct-Mapped Cache

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# 5. Large and Fast: Exploiting Memory Hierarchy

## 5.1 Introduction

## 5.2 The Basics of Caches

## 5.3 Measuring and Improving Cache Performance

## 5.4 Virtual Memory

## 5.5 A Common Framework for Memory Hierarchies

## 5.6 Virtual Machines

## 5.7 Using a Finite-State Machine to Control a Simple Cache

## 5.8 Parallelism and Memory Hierarchies: Cache Coherence

# Direct Mapped Cache

- Each memory location is mapped to exactly one cache location
  - ❖ Many lower level blocks must share blocks in the cache
- Cache address (i.e. Index)

(Block address) *modulo* (Number of blocks in the cache)
- When the number of entries in the cache is  $2^N$ ,

Cache address = low-order N bits of the memory address
- Fields on a cache line
  - ❖ Valid bit
  - ❖ Data
  - ❖ Tag
    - ◆ The information required to identify the original location
    - ◆ High-order part of memory address except index

# Accessing a Cache

- Example: 8-byte direct mapped cache

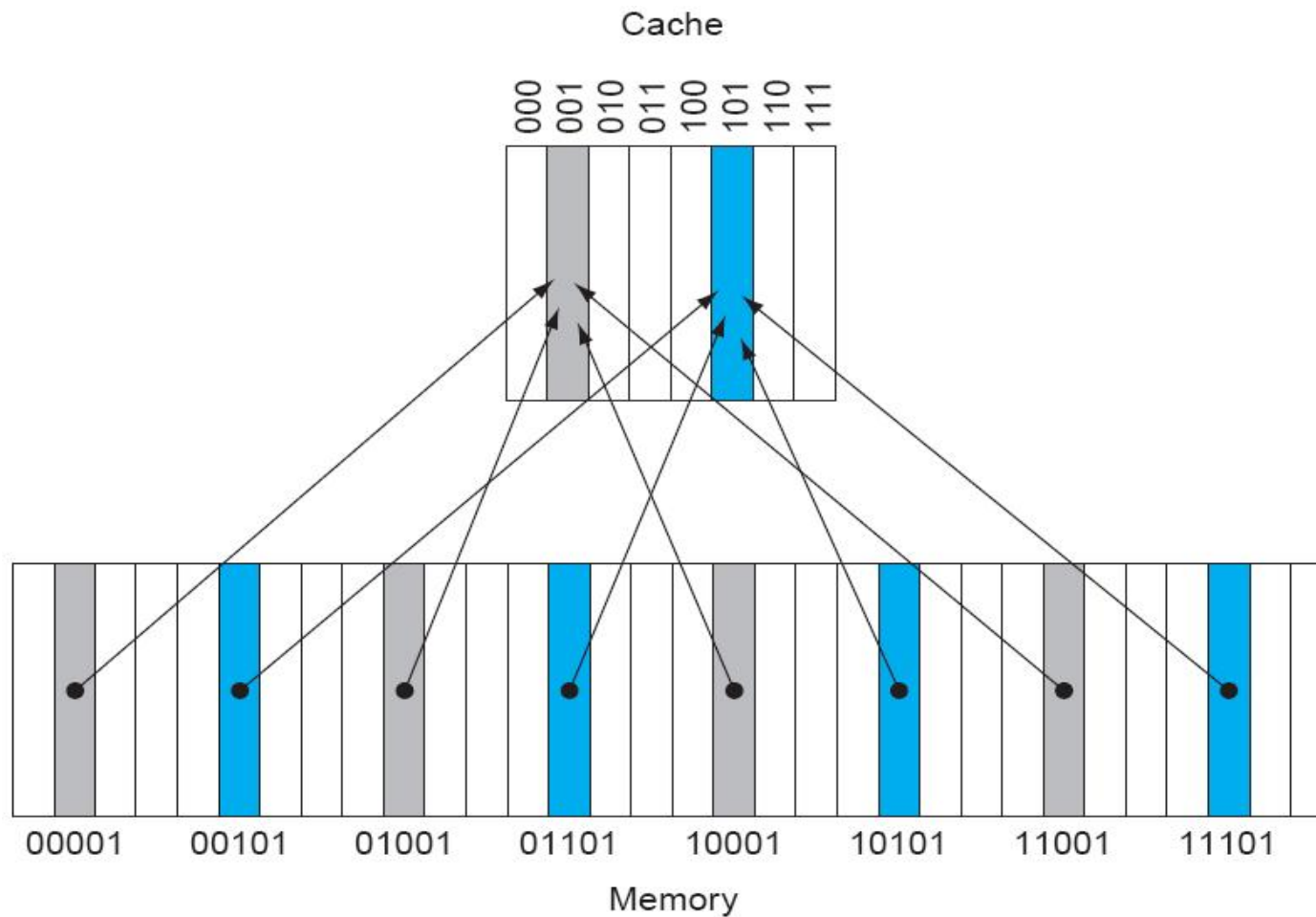


Figure 5.5

# States of the Cache

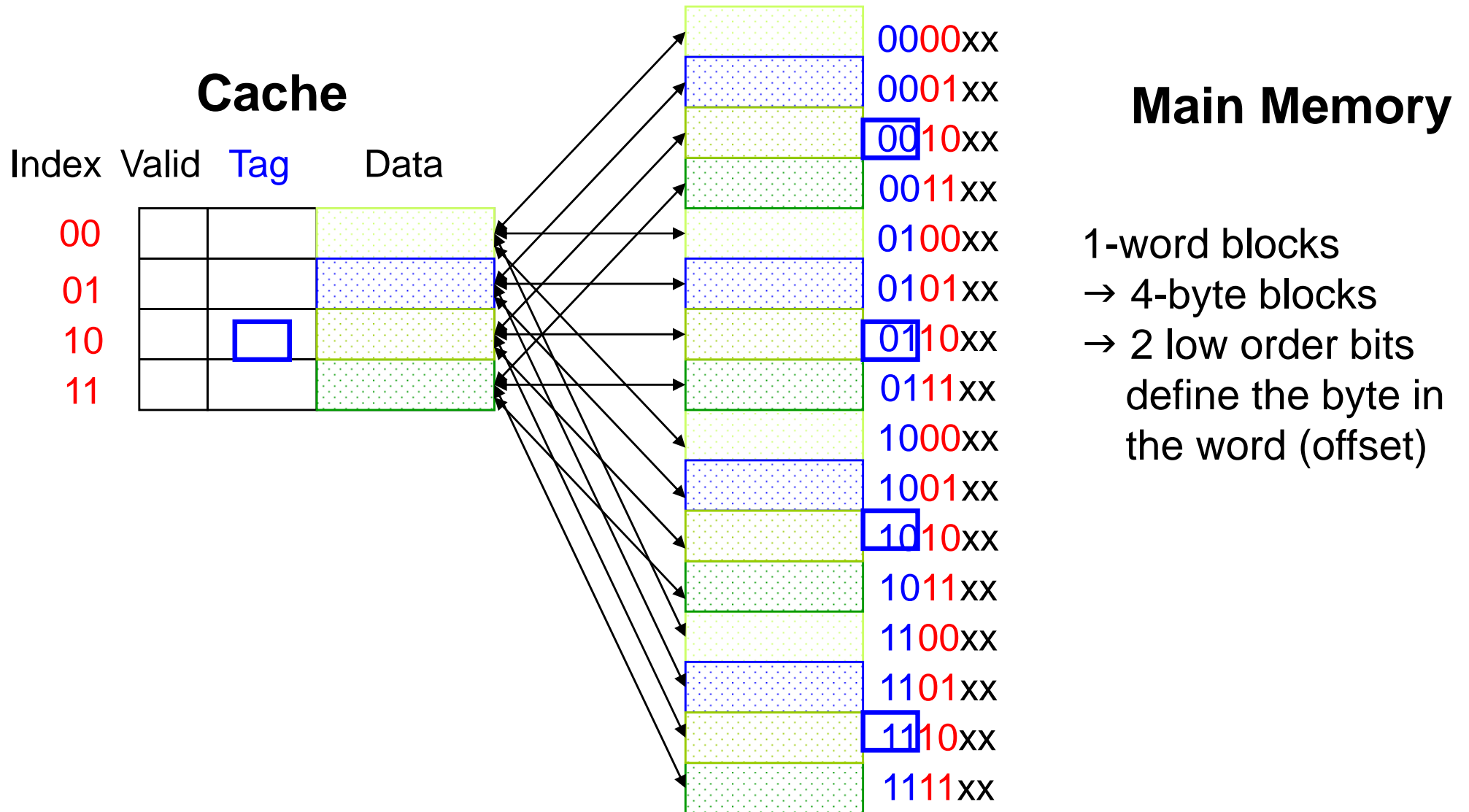
Index	V	Tag	Data
000	Y	10	M[16]
001			
010	Y	10	M[26]
011	Y	00	M[3]
100			
101			
110	Y	10	M[22]
111			

22	10110
26	11010
22	10110
26	11010
16	10000
3	00011
16	10000
18	10010

# Example Sequence of References

Decimal addr.	Binary addr.	Hit or miss	Assigned cache block
22	10 <b>110</b>	miss	<b>110</b> = 6
26	11 <b>010</b>	miss	<b>010</b> = 2
22	10 <b>110</b>	hit	<b>110</b> = 6
26	11 <b>010</b>	hit	<b>010</b> = 2
16	10 <b>000</b>	miss	<b>000</b> = 0
3	00 <b>011</b>	miss	<b>011</b> = 3
16	10 <b>000</b>	hit	<b>000</b> = 0
18	10 <b>010</b>	miss	<b>010</b> = 2

# 4-Block Cache with 4-Byte Blocks

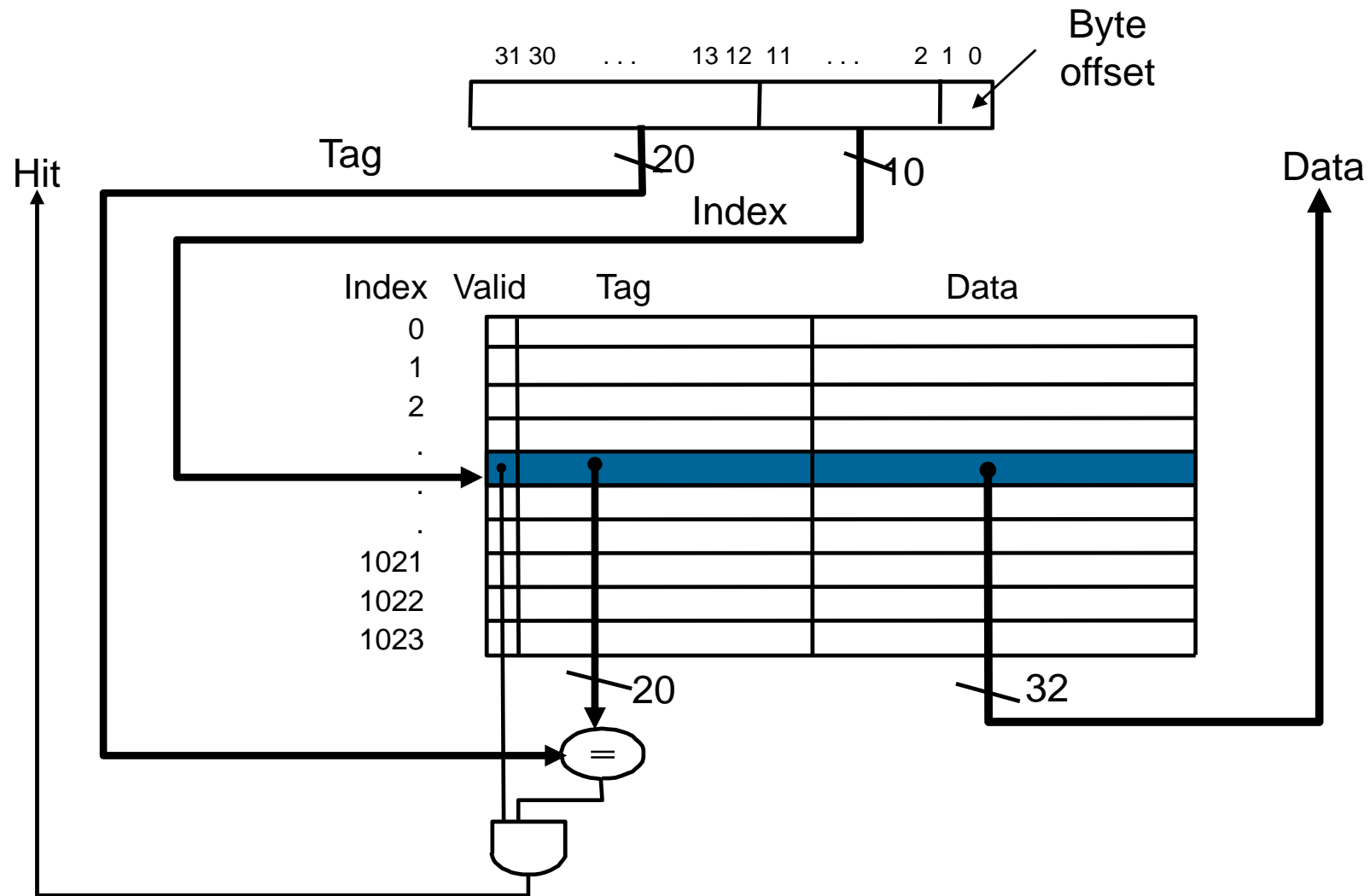


# Cache with 1-Word Block

- **32-bit address**
- **$2^n$  words with one-word blocks**
- **Byte offset**  
Least significant 2 bits (not used in cache)
- **Index**  
Next  $n$  bits
- **Tag**  
 $32 - (n + 2)$  bits
- **Total number of bits**  
 $2^n \times (\text{valid bit} + \text{tag} + \text{block size})$   
 $= 2^n \times (1 + (32 - n - 2) + 32)$   
 $= 2^n \times (63 - n)$



# Example: 4KB Cache with 1-Word Block

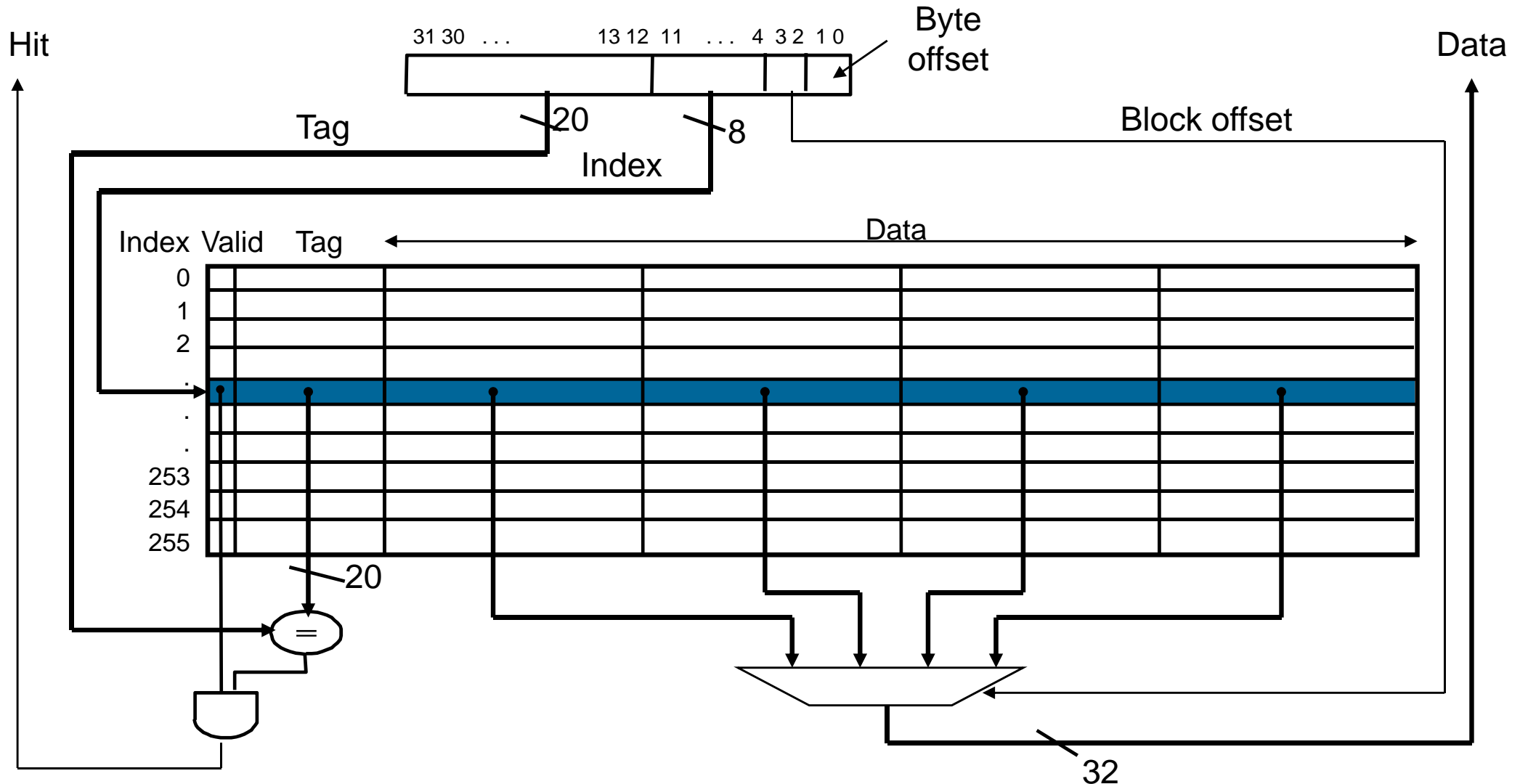


# Cache with $2^m$ -Word Block

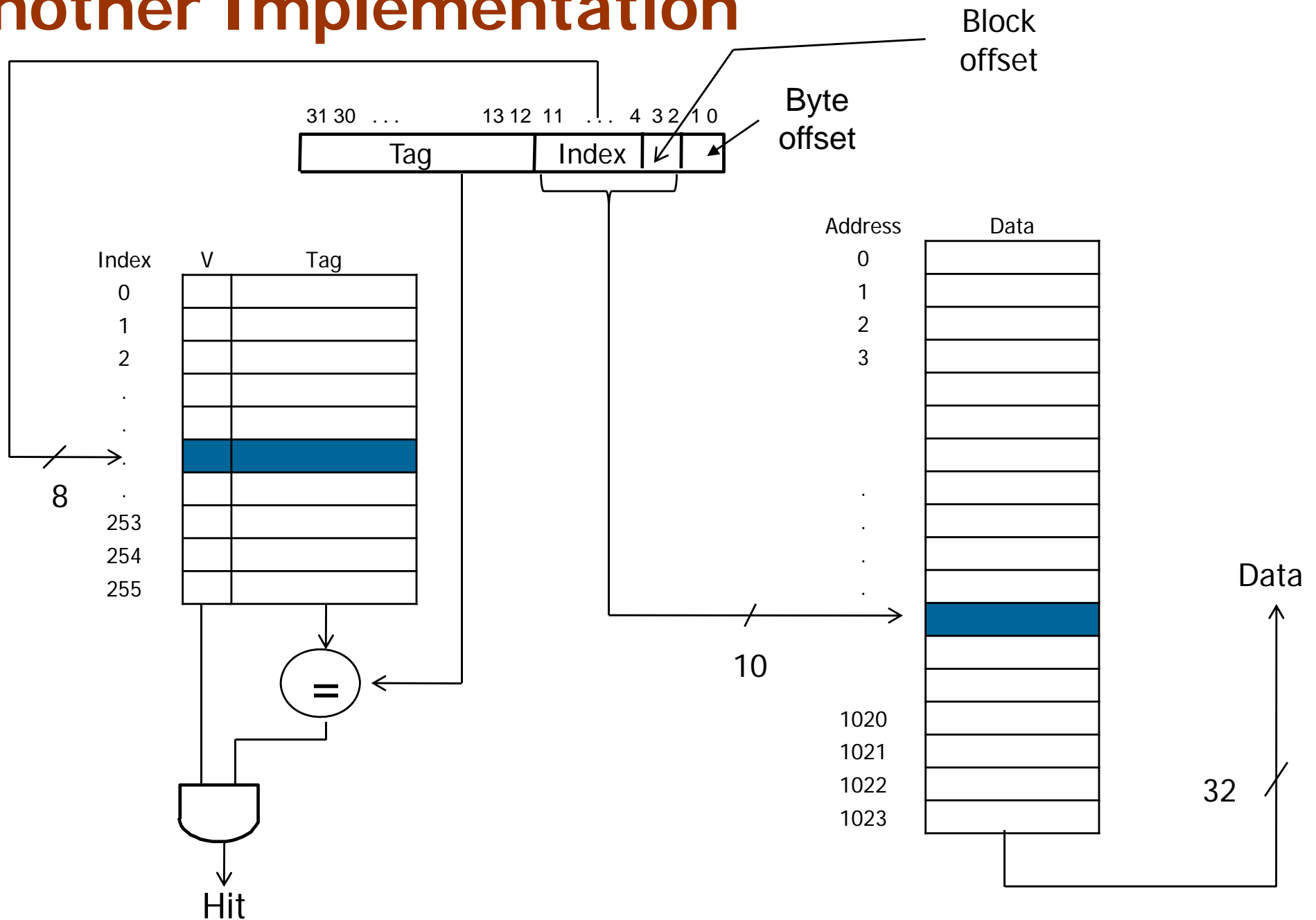
- 32-bit address
- $2^n$  blocks with  $2^m$ -word blocks
- Byte offset : 2 bits
- Block offset :  $m$  bits
- Index :  $n$  bits
- Tag :  $32 - (n + m + 2)$  bits
- Total number of bits
  - $2^n \times (\text{block size} + \text{tag size} + \text{valid field size})$
  - $= 2^n \times (2^m \times 32 + (32 - n - m - 2) + 1)$
  - $= 2^n \times (2^m \times 32 + 31 - n - m)$

# Multiword Block Direct Mapped Cache

- 2<sup>2</sup> words/block, cache size = 4 KB (m=2, n=8)



# Another Implementation



# Direct Mapped Cache (Block Size=1)

- Reference string: 0 1 2 3 4 3 4 15

0 miss

00	Mem(0)

1 miss

00	Mem(0)
00	Mem(1)

2 miss

00	Mem(0)
00	Mem(1)
00	Mem(2)

3 miss

00	Mem(0)
00	Mem(1)
00	Mem(2)
00	Mem(3)

4 miss

<del>00</del>	<del>Mem(0)</del>
00	Mem(1)
00	Mem(2)
00	Mem(3)

3 hit

01	Mem(4)
00	Mem(1)
00	Mem(2)
00	Mem(3)

4 hit

01	Mem(4)
00	Mem(1)
00	Mem(2)
00	Mem(3)

15 miss

01	Mem(4)
00	Mem(1)
00	Mem(2)
<del>00</del>	<del>Mem(3)</del>

- 8 requests, 6 misses

# Direct Mapped Cache (Block Size=2)

- Reference string: 0 1 2 3 4 3 4 15

0 miss

00	Mem(1)	Mem(0)

1 hit

00	Mem(1)	Mem(0)

2 miss

00	Mem(1)	Mem(0)
00	Mem(3)	Mem(2)

3 hit

00	Mem(1)	Mem(0)
00	Mem(3)	Mem(2)

4 miss

<sup>01</sup> <del>00</del>	<sup>5</sup> <del>Mem(1)</del>	<sup>4</sup> <del>Mem(0)</del>
00	Mem(3)	Mem(2)

3 hit

01	Mem(5)	Mem(4)
00	Mem(3)	Mem(2)

4 hit

01	Mem(5)	Mem(4)
00	Mem(3)	Mem(2)

15 miss

<sup>11</sup> <del>01</del>	<sup>15</sup> <del>Mem(5)</del>	<sup>14</sup> <del>Mem(4)</del>
<del>00</del>	<del>Mem(3)</del>	<del>Mem(2)</del>

- 8 requests, 4 misses

# Example: Bits in a Cache

- **Calculate total number of bits for the cache.**

- ❖ Direct-mapped
- ❖ 16 KB of data with 4-word blocks
- ❖ 32-bit address

## **[Answer]**

16 KB = 4K words =  $2^{12}$  words

Number of blocks =  $2^{12} / 4 = 2^{10}$

Block size = 4 words = 4x4 bytes = 4x4x8 bits = 128 bits

Cache size =  $2^{10} \times (128 + (32-10-2-2) + 1)$

=  $2^{10} \times 147$

= 147 Kbits = 18.4 KBytes

Almost 1.15 times as large as data size of the cache.

# Miss rate vs. Block size

## ■ Larger blocks

- ❖ Increased spatial locality
- ❖ Decreased miss rate
- ❖ But ?

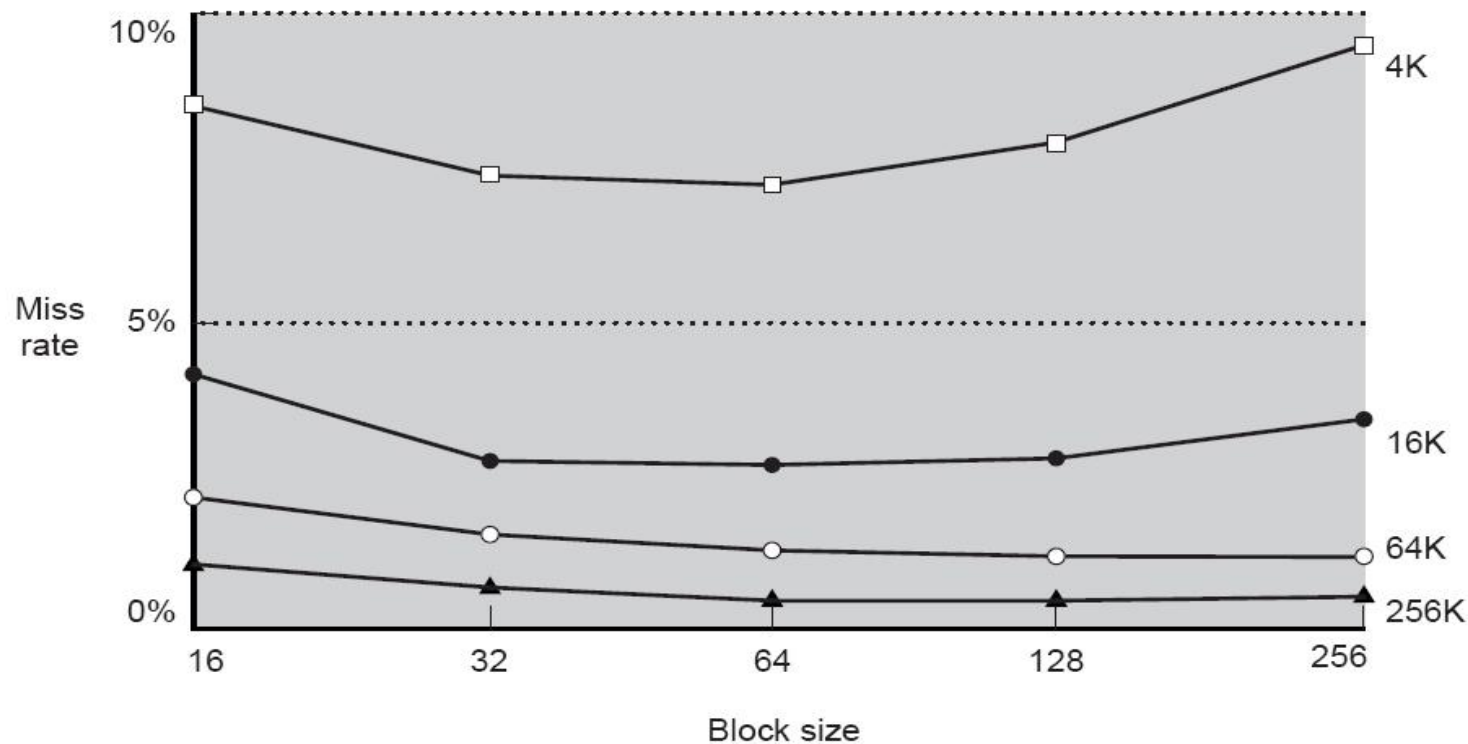


Figure 5.8



# Block Size vs. Performance

## ■ Too large blocks

- ❖ Small number of blocks in the cache
- ❖ Increased miss rate
- ❖ Increased miss penalty

## ■ Miss penalty

- ❖ Miss penalty = block fetch time + cache load time
- ❖ Block fetch time = latency to the first word  
+ transfer time for the rest of the block
- ❖ Transfer time  $\propto$  block size
- ❖ Increased as the block size increases

# Handling Cache Misses

- **Handling instruction cache miss**

- 1) Send PC-4 to the memory.
- 2) Instruct main memory to perform a read and wait for the memory to complete its access.
- 3) Write the cache entry. (Update data and tag fields and turn on the valid bit.)
- 4) Restart the instruction execution at the first step.

- **Data cache miss**

- ❖ Stall the processor until the memory responds with the data.

# Handling Writes

- **Write-through policy**

- ❖ Always write the data into both the memory and the cache.
- ❖ Keep the main memory and the cache consistent.

- **On write-miss**

1. Fetch the block containing the word.
2. Overwrite the word into the cache block.
3. Also write the word to main memory.

- **On write-hit**

1. Overwrite the word into the cache block.
2. Also write the word to main memory.

# Problems of Write-through

- **Performance degradation**

- ❖ Every write causes the data to be written to main memory.
- ❖ Slow down the machine considerably.

- **SPEC2000 integer benchmarks**

- ❖ 10% of the instructions are stores.
- ❖ If the CPI without cache miss = 1.0,  
spending 100 extra cycles on every write,

$$\text{CPI} = 1.0 + 100 \times 10\% = 11$$

- **Solution: write buffer**

- ❖ Holds data waiting to be written to memory
- ❖ CPU continues immediately
  - ◆ Only stalls on write if write buffer is already full

# Write-Back

- The new value is written only to the cache.
  - ❖ Dirty bit or modified bit
- The modified block is written to the main memory when it is replaced.
- Better performance
- More complex to implement

## Elaboration

### 1. Write allocate

- ❖ Most write-through caches

### 2. No write allocate

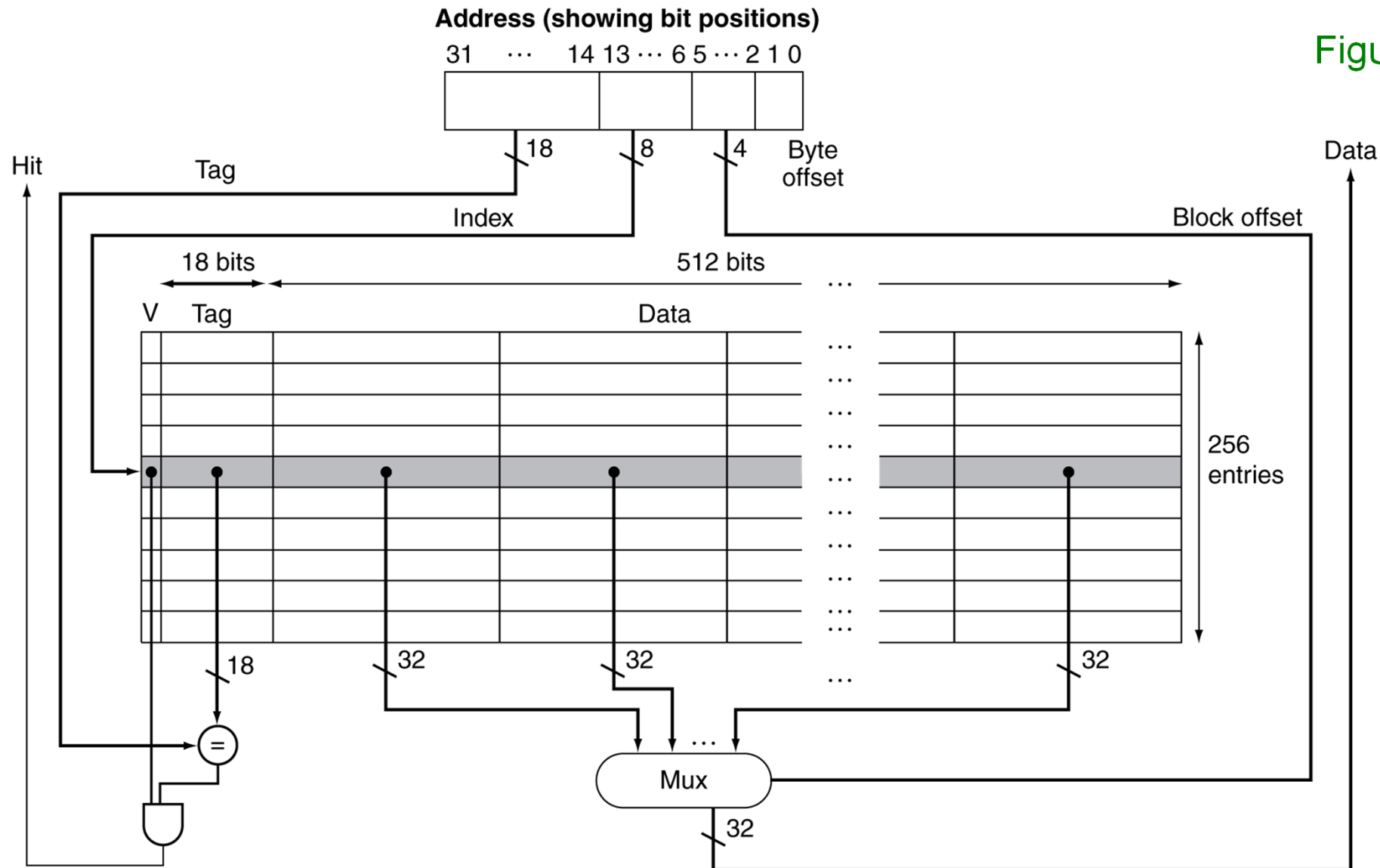
# An Example Cache: The Intrinsity FastMATH processor

## ■ **Intrinsity FastMATH**

- ❖ Embedded microprocessor
- ❖ MIPS architecture with a simple cache implementation
- ❖ 12-stage pipeline
- ❖ Split caches
  - ◆ Each cache: 16KB with 16-word block and 256 blocks
- ❖ Write policy
  - ◆ OS selectable: write-through or write-back
- ❖ Miss rate
  - ◆ Instruction: 0.4%
  - ◆ Data: 11.4%
  - ◆ Effective combined: 3.2%

# Cache of Intrinsity FastMATH

Figure 5.9



# Elaboration

- **Split caches vs. Combined (or Unified) cache**
  - ❖ Combined cache: better hit rate
  - ❖ Split cache: larger bandwidth
- **Miss rates for Intrinsity FastMATH**
  - ❖ Total cache size: 32 KB
  - ❖ Split cache: 3.24%
  - ❖ Combined cache: 3.18%
- **High bandwidth is more effective than high hit rate.**
- **Thus, we cannot use miss rate as the sole measure of cache performance.**



# Supplement

# Example: Prob. 3 of 2011-1 Terminal Exam

- Direct-mapped cache with block size = 8 bytes
- Initial state

	V	Tag	Data
00	1	0100	?
01	1	0100	?
10	1	0001	?
11	1	1010	?

- Address

4 bits	2 bits	3 bits
tag	index	offset

# Example: Prob. 3 of 2011-1 Terminal Exam

- Direct-mapped cache with block size = 8 bytes
- Initial state

	V	Tag	Data
00	1	0100	M[080] ~ M[087]
01	1	0100	M[088] ~ M[08F]
10	1	0001	M[030] ~ M[037]
11	1	1010	M[158] ~ M[15F]

- Block 00: 0100 00 xxx  $\Rightarrow$   $080_{16} \sim 087_{16}$
- Block 01: 0100 01 xxx  $\Rightarrow$   $088_{16} \sim 08F_{16}$
- Block 10: 0001 10 xxx  $\Rightarrow$   $030_{16} \sim 037_{16}$
- Block 11: 1010 11 xxx  $\Rightarrow$   $158_{16} \sim 15F_{16}$

# Reference String (in byte address)

- 083, 007, 034, 15F, 002, 080, 1A8, 038, 001, 1AF

Address				
Hex	Binary	Tag	Index	
083	0 1000 0011	0100	00	Hit
007	0 0000 0111	0000	00	Miss
034	0 0011 0100	0001	10	Hit
15F	1 0101 1111	1010	11	Hit
002	0 0000 0010	0000	00	Hit
080	0 1000 0000	0100	00	Miss
1A8	1 1010 1000	1101	01	Miss
038	0 0011 1000	0001	11	Miss
001	0 0000 0001	0000	00	Miss
1AF	1 1010 1111	1101	01	Hit

Cache							
Block 00		Block 01		Block 10		Block 11	
Tag	Data	Tag	Data	Tag	Data	Tag	Data
0100	M[080]~	0100	M[088]~	0001	M[030]~	1010	M[158]~
0100							
0000	M[000]~						
				0001			
						1010	
0000							
0100	M[080]~						
		1101	M[1A8]~				
						0001	M[038]~
0000	M[000]~						
		1101					