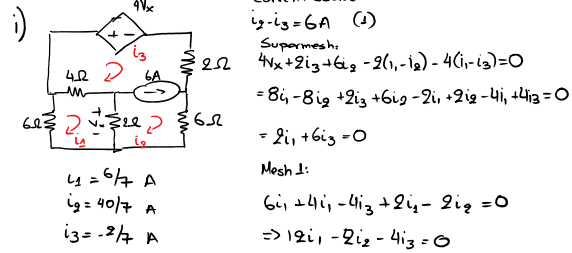
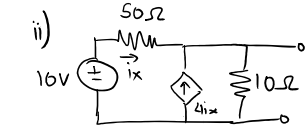


Question 1:

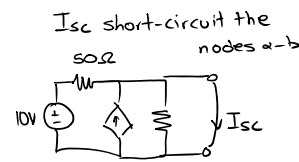


b) $i_{4\Omega} = i_1 - i_3 = 8/4 A$
 $i_2 = 40/7 A$
 $i_3 = -2/4 A$
d) $V_x = 2 \cdot (i_1 - i_2) = 2 \cdot (\frac{8}{4} - \frac{40}{7})$
 $P_{4\Omega} = i^2 \cdot R = \frac{64}{49} \cdot 4 = 5.994 W$
 $= 2 \cdot (-\frac{34}{7}) = -\frac{68}{7} V$

c) $P = +V \cdot i = +4 \cdot (-\frac{68}{7}) = -11.1 W$
consumes power as power is positive
or because of current direction
and voltage polarity.

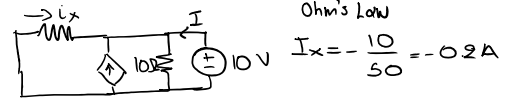


ii) V_{th} : KCL at node a
 $\frac{10 - V_a}{50} + 4i_x = \frac{V_a}{10} \Rightarrow$
 $\Rightarrow \frac{10 - V_a}{50} + 4 \frac{10 - V_a}{50} = \frac{V_a}{10}$
 $\Rightarrow 50 - 5V_a = 5V_a \Rightarrow V_a = 5V$
 $V_x = V_{th} = 5V$



KCL
 $\frac{10}{50} + 4 \cdot \frac{10}{50} = I_{sc} \Rightarrow I_{sc} = 1A$
 $R_{th} = \frac{V_{oc}}{I_{sc}} = \frac{5}{1} = 5\Omega$

Alternatively for R_{th} :

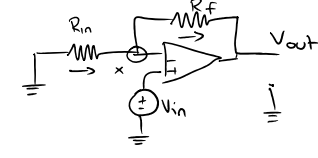


Ohm's Law
 $I_x = -\frac{10}{50} = -0.2 A$

iii) $P_{max} = \frac{V_m^2}{4R_{th}} = \frac{5^2}{4 \cdot 20} = 1.25 W$
 $I = \frac{10}{10} - i_x - 4i_x = 1 + 0.2 + 0.8 = 2A$
 $R_{th} = \frac{10}{I} = \frac{10}{2} = 5\Omega$

Question 2:

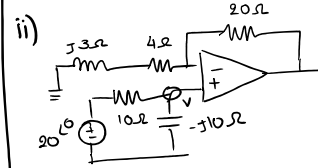
Circuit of non-inverting amplifier:



KCL at node x, $V_x = V_{in}$
 $\frac{0 - V_x}{R_{in}} = \frac{V_{in} - V_{out}}{R_f}$
 $\Rightarrow -R_f V_{in} = R_{in} V_{in} - R_{in} V_{out}$
 $\Rightarrow \frac{V_{out}}{V_{in}} = \frac{R_{in} + R_f}{R_{in}} \Rightarrow \frac{V_{out}}{V_{in}}$

ii) For again of 12, $\frac{R_f}{R_{in}} = 12 \rightarrow$ Resistors $10\Omega - 110\Omega$
 $50\Omega - 600\Omega$
 $20\Omega - 220\Omega$

iii) $\frac{R_f}{R_{in}} = 12$ Resistors $10\Omega - 120\Omega$
 $50\Omega - 600\Omega$
 $20\Omega - 240\Omega$



$Z = 10 - j10\Omega$
 $V = \frac{-j10}{10 - j10} \cdot 20 \angle 0^\circ =$
 $= 10 - j10 V = 10\sqrt{2} \angle -45^\circ V$

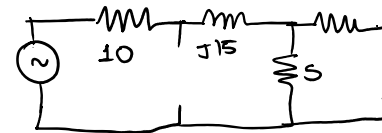
$\frac{V_{out}}{V_{in}} = 1 + \frac{Z_f}{Z_{in}} = 1 + \frac{16}{5} - \frac{12}{5} j$
 $V_{out} = (\frac{21}{5} - \frac{12}{5} j) V_{in} = (\frac{21}{5} - \frac{12}{5} j) (10 - j10)$
 $= 18 - j66 = 68.4 \angle -74.75^\circ V$



Question 3

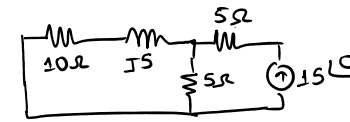
Must be superposition:

for $60 \cos 15t$ voltage source



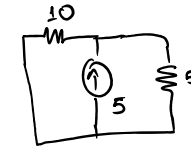
$Z = 15 + j15$ or voltage divider
 $I = \frac{60}{15 + j15} = \frac{4}{1 + j} = 2 - 2j$
 $V = 5 \cdot (2 - 2j) = 10 - j10 V$
 $= 14.14 \angle -45^\circ V$
 $= 14.14 \cos(15t - 45^\circ)$

b) Current source $15 \cos 5t$



$I = \frac{10 + j5}{15 + j15} \cdot 15$
 $= (\frac{7}{10} + j\frac{1}{10}) \cdot 15 = 10.6 \angle 8.13^\circ A$
 $V = 53.03 \angle 8.13^\circ V$
 $V_g(t) = 53.03 \cos(5t + 8.13^\circ) V$

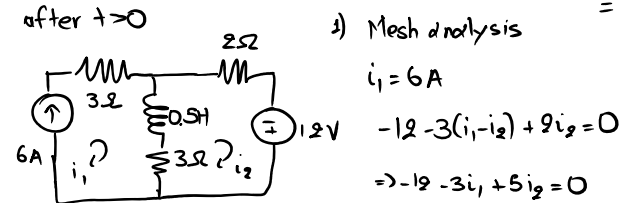
c) dc current source



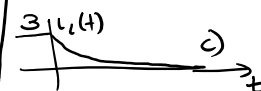
$I = \frac{10}{15} \cdot 5 = 3.33 A$
 $V = 5 \cdot 3.33 = 16.65 V$

So $V_g(t) = 16.65 + 53.03 \cos(5t + 8.13^\circ) + 14.14 \cos(15t - 45^\circ)$

ii) Initial current of inductor $i_L(0) = 3A$ $e_L = \frac{1}{2} 0.5 \cdot 3^2 = \frac{9}{4} J$



or 2) $6 = \frac{V}{3} + \frac{V + 12}{2}$
 $\Rightarrow 36 = 2V + 3V + 36$
 $\Rightarrow V = 0$
 $i_L(t) = 3e^{-t/0.1} A, t \rightarrow sec = 3e^{-10t} A, t \rightarrow sec$
 $\tau = \frac{L}{R} = \frac{0.5}{5} = 0.1 s$

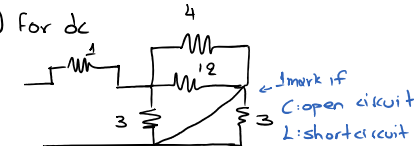


d) $V_{R2} = i_{R2} \cdot R = 3 \cdot i_L = 9e^{-10t} V, t \rightarrow sec$ 1 mark

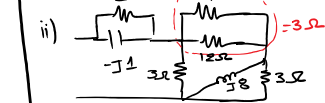
$V_{R1} = i_{R1} \cdot R = 6 \cdot 3 = 18V$ 1 mark

Question 4:

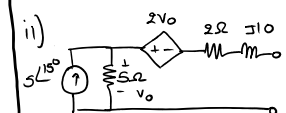
i) For dc



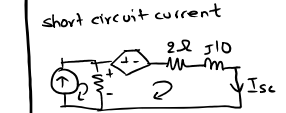
$R = 1 + 4 \parallel 12 \parallel 3 = 2.5\Omega$ 2 marks for all correct



$Z_{eq} = (1 \parallel 12) + 3 \parallel (3 + j10)$
 $= 0.5 - j0.5 + 3 \parallel (3 + j10)$
 $= 0.5 - j0.5 + 3 \parallel (5.63 + j9.98)$
 $= 0.5 - j0.5 + 1.97 + j0.11$
 $= 2.47 - j0.39 \Omega$



Open circuit voltage:
 $V_{th} = V_o$
 $V_o = 5 \cdot 5 \angle 15^\circ = 25 \angle 15^\circ$
 $V_{th} = 25 \angle 15^\circ V$



Short circuit current
 $-5(i_1 - i_2) + 2(5(i_1 - i_2) + 2i_2 + j10i_2) = 0$
 $-5i_1 + 5i_2 + 10i_1 - 10i_2 + 2i_2 + j10i_2 = 0$
 $\Rightarrow 5i_1 - 3i_2 + j10i_2 = 0$
 $\Rightarrow i_2(-3 + j10) = -5i_1$
 $\Rightarrow i_2 = \frac{25 \angle 15^\circ}{-3 + j10} = I_{sc}$

$Z_{th} = \frac{V_{th}}{I_{sc}} = \frac{25 \angle 15^\circ}{\frac{25 \angle 15^\circ}{-3 + j10}} = -3 + j10 \Omega$

iii) $Z_I = Z_{th}^*$ or conjugate of Z_{th} 2 marks

IGNORE THIS QUESTION

Question 5:

i) Load 1: 20kVA 0.8pf leading $\rightarrow 16 - j12 kVA$ 0.5 marks
Load 2: 6kW pf 0.6 lagging $\rightarrow 6 + j8 kVA$ 0.5 marks

Total complex power = $22 - j4 kVA$ 1 mark

Apparent power = $\sqrt{22^2 + 4^2} = 22.36 kVA$ 1 mark

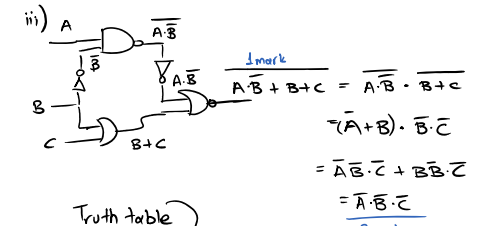
$I^* = \frac{S}{V} = \frac{22 - j4}{230} = 95.65 - j17.39$
 $I = 95.65 + j17.39 A$

$I_{rms} = 97.21 A$
 $S = V \cdot I \Rightarrow I = 22.36 kVA / 230 = 97.21 A$
 $pf = \frac{22}{22.36} = 0.983$ leading 1 mark

ii) $V_p = 500V$
 $V_s = 160V$
 $I_s = \frac{100}{10 + j10} = 5 - 5j = 7.07 \angle -45^\circ A$
 $I_p = 1 - 1j = 1.41 \angle -45^\circ A$

$S = V \cdot I^* = 100(5 + 5j) = 500 + j500 VA$
 $P = 500W, Q = 500VAR$

$S = 707 VA$
 $\% \text{ loading} = \frac{507}{2000} = 25.35\%$ if 25% 2 marks 1 mark



$A \oplus B = \overline{A \cdot B} + \overline{\overline{A} \cdot \overline{B}}$
 $A \oplus B + C = \overline{A \cdot B} + \overline{\overline{A} \cdot \overline{B}} + C$
 $= \overline{A \cdot B} + \overline{\overline{A} \cdot \overline{B} \cdot C}$

Truth table

A	B	C	Out
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

All others 0 2 marks