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Starting Values: $m=1.7$, $b=2.1$

Step 1: Calculate Predictions (\hat{y}) & Errors
where $\hat{y} = mx + b$

$$\text{Error}(e) = y - \hat{y} \text{ or } \hat{y} - y$$

And we have two points (1,3) and (3,6)

For point 1 (1,3)

$$\bullet \hat{y}_1 = (1.7)(1) + (2.1) = 3.8$$

$$\bullet \text{Error}(e) = 3.8 - 3 = 0.8$$

For point 2 (3,6)

$$\bullet \hat{y}_2 = (1.7)(3) + (2.1) = 5.1 + 2.1 = 7.2$$

$$\bullet e_2 = 7.2 - 6 = 1.2$$

Step 2: Calculate Gradients.

$$\bullet \frac{\partial J}{\partial m} = \frac{2}{n} \sum_{i=1}^n (\hat{y}_i - y_i)x_i \quad ; \quad \text{Gradient for } m \quad (\text{Sum of Error} \cdot x), \quad n=2$$

$$\frac{\partial J}{\partial m} = (0.8)(1) + (1.2)(3) = 0.8 + 3.6 = 4.4$$

$$\bullet \frac{\partial J}{\partial b} = \frac{2}{n} \sum_{i=1}^n (\hat{y}_i - y_i) \quad ; \quad \text{Gradient for } b \quad (\text{Sum of Errors}) \quad \text{and } n=2$$

$$\frac{\partial J}{\partial b} = 0.8 + 1.2 = 2.0$$

Step 3: Update Parameter

$$m_{\text{new}} = m_{\text{old}} - \alpha \frac{\partial J}{\partial m} \quad \text{as } \alpha = 0.1$$

$$b_{\text{new}} = b_{\text{old}} - \alpha \frac{\partial J}{\partial b}$$

$$\Rightarrow m_{\text{new}} = (1.7) - (0.1)(4.4) = 1.7 - 0.44 = 1.26$$

$$b_{\text{new}} = (2.1) - (0.1)(2.0) = 2.1 - 0.2 = 1.9$$