

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Hogeschool Rotterdam Rotterdam, Netherlands



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Introduction



Introduction

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

 ${\sf Introduction}$

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Lecture topics

- Course introduction
- Exam and practicum
- Semantics of traditional programming languages
- Basic lambda calculus



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Course introduction



Course introduction

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Course topics

- We will discuss a completely new paradigm for expressing programs
- This paradigm, functional programming, is based on different premises on computation
- It gives guarantees of correctness in complex places, like parallelism or separation of concerns
- It requires a radical conceptual shift in the way you think about programming



Course introduction

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Course topics

- We will begin with a short discussion on traditional programming language semantics
- We will then show the lambda calculus, which is the foundation for functional languages
- •
- We will then bridge the gap between theory and practice
- We will translate the lambda calculus into two mainstream functional languages: F# and Haskell
- This will cover a huge chunk of possible applications in countless other languages and libraries, from C# LINQ to Java streams, to Scala, Scheme, Closure, etc.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Examination



Examination

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Exam structure

- There is a theoretical exam, where you show understanding of the basic principles
- There is a practical exam, where you show understanding of their concrete applications



Examination

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Theoretical exam

- One question on a lambda calculus program execution
- One question on the type system of a lambda calculus program, F# program, or Haskell program
- Both questions must be answered correctly to get a voldoende



Examination

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Build, in groups of max four, an interpreter for a virtual machine according to the specifications given in the document that will be published during the course.

We will get together at the end of the course, and the teacher(s) will ask you to **individually** perform some activities on the code to prove understanding and familiarity.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Semantics of traditional programming languages



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

traditional programming languages

Basic lambda

- Traditional, imperative programming languages are based on sharing memory through instructions
- This means that subsequent instructions are not independent from each other
- Any function call makes use of the available memory



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction
Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

For example, consider the semantic rules that describe the working of ";"

First we run s_1 with the initial memory, then we run s_2 with the modified memory.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

introduction

 $\mathsf{E}{\times}\mathsf{amin}\,\mathsf{ation}$

Semantics of traditional programming languages

Basic lambda calculus

Closing up

For example, consider the semantic rules that describe the working of ";"

First we run s_1 with the initial memory, then we run s_2 with the modified memory.

$$\frac{\langle s_1, S, H \rangle \to \langle S_1, H_1 \rangle \land \langle s_2, S_1, H_1 \rangle \to \langle S_2, H_2 \rangle}{\langle (s_1; s_2), S, H \rangle \to \langle S_2, H_2 \rangle}$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

What does "first we run s_1 with the initial memory, then we run s_2 with the modified memory" imply?.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

Closing up

What does "first we run s_1 with the initial memory, then we run s_2 with the modified memory" imply?

- The same instructions, executed at different moments, will produce different results.
- Change the order of some method calls, and some weird dependence might cause bugs or break things.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Goals

- Our goal is to ensure that behaviour of code is consistent.
- Change the order of some method calls, and the results remain the same.
- This makes it easier to test, parallelize, and in general ensure correctness.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

How do we achieve this?



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

Closing up

How do we achieve this?

We give (shared) memory up: every piece of code is a function which output only depends on input.

This very important property is called **referential** transparency.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Basic lambda calculus



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Introduction

- The (basic) lambda calculus is an alternative mechanism to Turing Machines and the Von Neumann architecture.
- It is very different, but has equivalent expressive power.
- It is the foundation of all functional programming languages.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Substitution principle

- The (basic) lambda calculus is truly tiny when compared with its power.
- It is based on the substitution principle: calling a function with some parameters returns the function body with the variables replaced.
- There is no memory and no program counter: all we need to know is stored inside the body of the program itself.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

traditional programming languages

Basic lambda calculus

Closing up

A lambda calculus program (just *program* from now on) is made up of three syntactic elements:

- Variables: x, y, \dots
- Abstractions (function declarations with one parameter): $\lambda x \to t$ where x is a variable and t is the function body (a program).
- Applications (function calls with one argument): t u where t is the function being called (a program) and u is its argument (another program).



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

A simple example would be the identity function, which just returns whatever it gets as input

$$(\lambda x \rightarrow x)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

We can call this function with a variable as argument, by writing:

$$((\lambda x \rightarrow x) v)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

A lambda calculus program is computed by replacing lambda abstractions applied to arguments with the body of the lambda abstraction with the argument instead of the lambda parameter:



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

A lambda calculus program is computed by replacing lambda abstractions applied to arguments with the body of the lambda abstraction with the argument instead of the lambda parameter:

$$\overline{(\lambda x \to t) \ u \to_{\beta} t[x \mapsto u]}$$

 $t[x\mapsto u]$ means that we change variable x with u within t



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda calculus

$$((\lambda x \rightarrow x) v)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming

Basic lambda

$$((\lambda x \rightarrow x) v)$$

$$((\lambda x \rightarrow x) v)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming

Basic lambda

$$((\lambda x \rightarrow x) v)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

traditional programming languages

Basic lambda calculus

Closing up

$$((\lambda x \rightarrow x) v)$$

V



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Multiple applications where the left-side is not a lambda abstraction are solved in a left-to-right fashion:



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Multiple applications where the left-side is not a lambda abstraction are solved in a left-to-right fashion:

$$\frac{t \to_{\beta} t' \land u \to_{\beta} u' \land t' u' \to_{\beta} v}{t u \to_{\beta} v}$$



Introduction to functional programming and lambda calculus

The INFDEV@HR ____ Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Variables cannot be further reduced, that is they stay the same:



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

Variables cannot be further reduced, that is they stay the same:

$$x \to_{\beta} x$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

We can encode functions with multiple parameters by nesting lambda abstractions:

$$(\lambda x y \rightarrow (x y))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

traditional programming languages

Basic lambda calculus

Closing up

The parameters are then given one at a time:

$$(((\lambda x y \rightarrow (x y)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

$$(((\lambda x y \rightarrow (x y)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

$$(((\lambda x y \rightarrow (x y)) A) B)$$

$$(((\lambda x y \rightarrow (x y)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda calculus

$$((\lambda x y \rightarrow (x y)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

programming languages

Basic lambda calculus

$$((\lambda x y \rightarrow (x y)) A) B)$$

$$((\lambda y \rightarrow (A y)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda calculus

$$((\lambda y \rightarrow (A y)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

traditional programming languages

Basic lambda calculus

$$((\lambda y \rightarrow (A y)) B)$$

$$((\lambda y \rightarrow (A y)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

 $((\lambda y \rightarrow (A y)) B)$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

$$((\lambda y \rightarrow (A y)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Example executions of (apparently) nonsensical programs

- We will now exercise with the execution of various lambda programs.
- Try to guess what the result of these programs is, and then we shall see what would have happened.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

Closing up

What is the result of this program execution?

$$(((\lambda x y \rightarrow (x y)) (\lambda z \rightarrow (z z))) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

$$(((\lambda x y \rightarrow (x y)) (\lambda z \rightarrow (z z))) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

traditional programming languages

Basic lambda calculus

$$(((\lambda x y \rightarrow (x y)) (\lambda z \rightarrow (z z))) A)$$

$$(((\lambda x y \rightarrow (x y)) (\lambda z \rightarrow (z z))) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$(((\lambda x y \rightarrow (x y)) (\lambda z \rightarrow (z z))) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

programming languages Basic lambda

calculus

$$(((\lambda x y \rightarrow (x y)) (\lambda z \rightarrow (z z))) A)$$

$$((\lambda y \rightarrow ((\lambda z \rightarrow (z z)) y)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda y \rightarrow ((\lambda z \rightarrow (z z)) y)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming

languages

Basic lambda
calculus

$$((\lambda y \rightarrow ((\lambda z \rightarrow (z z)) y)) A)$$

$$((\lambda y \rightarrow ((\lambda z \rightarrow (z z)) y)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda y \rightarrow ((\lambda z \rightarrow (z z)) y)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

 ${\tt Introduction}$

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda y \rightarrow ((\lambda z \rightarrow (z z)) y)) A)$$

$$((\lambda z \rightarrow (z z)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

 $\mathsf{E}{\times}\mathsf{amin}\,\mathsf{ation}$

Semantics of traditional programming languages

Basic lambda

$$((\lambda z \rightarrow (z z)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

 ${\tt Introduction}$

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda z \rightarrow (z z)) A)$$

$$((\lambda z \rightarrow (z z)) A)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda z \rightarrow (z z)) A)$$

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

 ${\tt Introduction}$

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

$$((\lambda z \rightarrow (z z)) A)$$

(A A)

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

What is the result of this program execution? Watch out for the scope of the two "x" variables!

$$(((\lambda x x \rightarrow (x x)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

$$(((\lambda x x \rightarrow (x x)) A) B)$$

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming

languages

Basic lambda
calculus

$$(((\lambda x x \rightarrow (x x)) A) B)$$

$$(((\lambda x x \rightarrow (x x)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

$$(((\lambda x \times (x \times)) \land) \land B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

traditional programming languages

Basic lambda calculus

$$(((\lambda x x \rightarrow (x x)) A) B)$$

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional

programming languages Basic lambda

cal culus

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

 ${\tt Introduction}$

Course introduction

Examination

Semantics of traditional programming

languages

Basic lambda
calculus

$$((\lambda x \rightarrow (x x)) B)$$

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination
Semantics of

traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) B)$$

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

The first "x" gets replaced with "A", but the second "x" shadows it!

$$(((\lambda x x \rightarrow (x x)) A) B)$$

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda calculus

Closing up

A better formulation, less ambiguous, would turn:

$$(((\lambda x x \rightarrow (x x)) A) B)$$

...into:

(((
$$\lambda y x \rightarrow (x x)$$
) A) B)



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$(((\lambda y x \rightarrow (x x)) A) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of

traditional programming languages

Basic lambda calculus

$$(((\lambda y x \rightarrow (x x)) A) B)$$

$$(((\lambda y \times (x \times)) \land) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda y \times (x \times x)) \land B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional

programming languages Basic lambda

calculus

$$((\lambda y \times (x \times x)) \land B)$$

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

programming languages Basic lambda

Basic lambd

$$((\lambda x \rightarrow (x x)) B)$$

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) B)$$

Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) B)$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction Examination

Examinatio

Semantics of traditional programming languages

Basic lambda

Closing up

What is the result of this program execution? Is there even a result?

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda calculus

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

programming languages Basic lambda

calculus

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$

$$(\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

programming languages Basic lambda

calculus

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of

traditional programming languages

Basic lambda calculus

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$

$$(\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x))$$



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

$$((\lambda x \rightarrow (x x)) (\lambda x \rightarrow (x x)))$$

It never ends! Like a while true: .



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Ok, I know what you are all thinking: what is this for sick joke? This is no real programming language!

- We have some sort of functions and function calls
- We do not have booleans and if's
- We do not have integers and arithmetic operators
- We do not have a lot of things!



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Surprise!

With nothing but lambda programs we will show how to build all of these features and more.



Introduction to functional programming and lambda calculus

The INFDEV@HR Team

Introduction

Course

introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

Stay tuned.

This will be a marvelous voyage.

This is it!

to functional programming and lambda calculus

Introduction

The INFDEV@HR Team

Introduction

Course introduction

Examination

Semantics of traditional programming languages

Basic lambda

Closing up

The best of luck, and thanks for the attention!