

Haskell

The
INFDEV@HR
Team

Translating
Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Haskell

The INFDEV@HR Team

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notation and
IO monad

Overview

- Haskell can be translated mapped to Lambda Calculus as we did for F#
- It is slightly different than F# with respect to let-bindings

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Lazy
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The "do"
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Integers, booleans, floats, strings have the usual meaning, both in the lambda calculus, Haskell, and the languages you are used to:

```
((2 + 3) - 4)
```

```
(True && False)
```

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Lazy
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- Conditionals behave just like in the lambda calculus
- This means that they return the evaluation of either of the two branches
- This differs from imperative languages, where we just jump into either of the two branches

```
if (True && False) then  
  0  
else  
  1
```

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calculus to
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Lazy
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The "do"
notation and
IO monad

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```
if (True && False) then  
  0  
else  
  1
```

Lambda calculus

```
if (TRUE  $\wedge$  FALSE) then 0 else 1
```

```
((((( $\lambda p$  th  $e1 \rightarrow ((p$  th)  $e1$ )) (TRUE  $\wedge$  FALSE)) 0)  
  1)
```

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Lazy
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Functions look very similar, with \backslash instead of λ

```
(\x f -> (f x))
```

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Translating
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Lazy
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notation and
IO monad

Functions look very similar, with \backslash instead of λ

```
(\x f -> (f x))
```

Just like function application

```
(((\x f -> (f x)) 3) (\x -> (3 + x)))
```


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Lazy
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The "do"
notation and
IO monad

Haskell

```
(((\x f -> (f x)) 3) (\x -> (3 + x)))
```

Lambda calculus

```
(((\lambda x f \rightarrow (f x)) 3) (\lambda x \rightarrow (3 + x)))
```

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Lazy
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We can give names to functions, and code becomes much prettier as a result

```
let apply =  
  \ x f -> (f x) in  
((apply 3) (\x -> (3 + x)))
```

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calculus to
Haskell

Lazy
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The "do"
notation and
IO monad

Haskell

```
let apply =  
  \ x f -> (f x) in  
((apply 3) (\x -> (3 + x)))
```

Lambda calculus

```
let apply = ( $\lambda x f \rightarrow (f\ x)$ ) in ((apply 3) ( $\lambda x \rightarrow (3 + x)$ ))
```

```
(( $\lambda apply \rightarrow ((apply\ 3)\ (\lambda x \rightarrow (3 + x)))$ ) ( $\lambda x f \rightarrow (f\ x)$ ))
```

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- In Haskell, unlike F#, there is no distinction between `let` and `let rec`. Everything is `let rec`.
- `let-in` is used to define bindings locally into a function body
- Global `let` bindings are simply defined by defining the function name and can be used recursively

```
fact =  
  \ n ->  
    if (n == 0) then  
      1  
    else  
      ((fact (n - 1)) * n)  
  
(fact 2)
```

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Translating
Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Haskell

```
fact =  
  \ n ->  
    if (n == 0) then  
      1  
    else  
      ((fact (n - 1)) * n)  
  
(fact 2)
```

Lambda calculus

```
let fact = (fix (λf n→if (n = 0) then 1 else  
  ((f (n - 1)) × n))) in (fact 2)
```

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We can define tuples by just putting a comma between the values, with or without nesting for more than two values is done for us. Unlike F#, brackets are mandatory when defining tuples in Haskell

```
(1, True)
```

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```
(1, True)
```

Lambda calculus

```
(1, TRUE)
```

```
((((λx y→ (λf→((f x) y))) 1) TRUE)
```

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- Functions such as π_1 and π_2 , which both extract one item of a pair, also exist in Haskell
- They are called, respectively, `fst` and `snd`

```
(fst (1, True))
```

```
(snd (1, True))
```


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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Haskell

```
(fst (1, True))
```

```
(snd (1, True))
```

Lambda calculus

```
( $\pi_1$  (1, TRUE))
```

```
(( $\lambda p \rightarrow (p (\lambda x y \rightarrow x))$ ) (1, TRUE))
```

```
( $\pi_2$  (1, TRUE))
```

```
(( $\lambda p \rightarrow (p (\lambda x y \rightarrow y))$ ) (1, TRUE))
```

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Lazy
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- Haskell also offers built-in discriminated unions
- Functions such as `inl` and `inr`, which both embed one item into the union, also exist in Haskell
- They are called, respectively, `Left` and `Right`

```
(Left 1)
```

```
(Right True)
```

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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Haskell

```
(Left 1)
```

```
(Right True)
```

Lambda calculus

```
(inl 1)
```

```
((λx→ (λf g→(f x))) 1)
```

```
(inr TRUE)
```

```
((λy→ (λf g→(g y))) TRUE)
```

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Translating
Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

We can, of course, perform matches on discriminated unions

```
case (Left 1) of
  Left x ->
    (Left x)
  Right y ->
    (Right y)
```

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Translating
Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

We can, of course, perform matches on discriminated unions

```
case (Left 1) of
  Left x ->
    (Left x)
  Right y ->
    (Right y)
```

```
let i =
  case (Left 1) of
    Left x ->
      x
    Right y ->
      0
in
(i * 2)
```

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calculus to
Haskell

Lazy
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The "do"
notation and
IO monad

Discriminated unions, and their corresponding matches, can be nested as deep as we need

```
case (Left (Right True)) of
  Left x ->
    case x of
      Left x ->
        (Left x)
      Right y ->
        (Right y)

  Right y ->
    (Right y)
```

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calculus to
Haskell

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- Type annotation in haskell is quite different from F#
- A function type definition is separated from the function body definition

```
fact :: Integral -> Integral
fact = (\n ->
    if (n == 0) then
        1
    else
        ((fact (n - 1)) * n)
)
```

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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

- It is possible to use pattern matching to define functions instead of using a `match` or an `if-then-else`
- It is done just repeating the function definition with the specific arguments

```
length=(\[] -> 0)
length=(\(x:xs) -> (1 + (length xs)))
```


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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
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Since the type declaration is separated from the function body, type variables for generics can be written as normal variables

Note that in Haskell the type of a list is written as `[a]` where `a` is a concrete type or a type variable

```
length :: [a] -> Integral
length = (\[] -> 0)
length = (\(x:xs) -> (1 + (length xs)))
```

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Translating
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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Lazy evaluation

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calculus to
Haskell

Lazy
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- Haskell uses a mechanism of evaluation for expressions called *lazy evaluation*
- When binding an expression to a variable the expression is not evaluated immediately
- The binding contains a “recipe” to evaluate the expression
- The evaluation is delayed until the binding is actually used in the program
- Unevaluated values are called *thunks*

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calculus to
Haskell

Lazy
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The "do"
notation and
IO monad

Consider the following code:

```
let (x,y) =  
    ((length [1,2]), (reverse [1,2])) in  
    ...
```

- The variables `x` and `y` initially contain `thunks`, until at some point in the `in` body they are used
- If the values are never used, they will never be evaluated

Lazy evaluation

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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Consider the following code:

```
1 let
2   z = (length [1,2], reverse [1,2])
3   (n,s) = z
4 in ...
```

- At line 1 line `z` is simply a thunk
- At line 2 the compiler must know if `z` is actually a pair, because the pattern must match the `let` binding
- The compiler does not need to evaluate the content of the pair, just know if `z` is actually a pair
- Thus `(n,s)` becomes a pair of thunks, i.e. `z = (thunk,thunk)`

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Lambda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

Consider the following code:

```
1 let
2   z = (length [1,2], reverse [1,2])
3   (n,s) = z
4   (1::ss) = s
5 in ...
```

- At line 4 the compiler must know if `s` is a list with the number 1 as head to match the pattern
- The compiler needs to know if `s` is a list, thus it evaluates the result of `reverse` as a list with a thunk as a head and another thunk as a tail, so we have `thunk:thunk`
- The compiler needs to know if the head of `s` matches the number 1, thus we have `1:thunk`

Lazy evaluation

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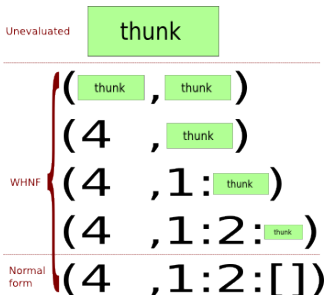
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Lazy
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IO monad

- The figure below shows the possible evaluation of $(2, [1,2])$
- WHNF = *Weak head normal form*, i.e. when the evaluation contains both values and thunks
- NF = *Normal form*, i.e. when the evaluation contains only values and no thunks



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calculus to
Haskell

Lazy
evaluation

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- In Haskell standard library we have a value called `undefined` which is used to capture errors in the program
- When the program evaluates `undefined`, it halts its execution and returns an error
- Now consider the following code:

```
let
  failMiserably = \x -> undefined
  (x,y) = (4,failMiserably "Please crash")
in
  x
```

Does it crash?

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Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

```
1 let
2   failMiserably = \x -> undefined
3   (x,y) = (4,failMiserably "Please crash")
4 in
5   x
```

The answer is no!

- At line 3 $(x,y) = (\text{thunk}, \text{thunk})$
- At line 5 the expression only uses x , thus only 4 is evaluated.
- y is still a thunk, so the program will never know that it contains undefined
- You might have an evaluation that actually failed but you will never know because of the lazy evaluation!

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Translating
Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

The "do" notation and IO monad

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Lambda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
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- Haskell, unlike F#, is a pure functional language
- This means we cannot make calls to imperative functions just like in F#. For example we cannot call something like `printf` because that is an imperative function
- How can we print a value to the standard output?

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Haskell

Lazy
evaluation

The "do"
notation and
IO monad

- In Haskell the main function always comes with a do notation
- For example:

```
main = do
  putStr("Velociraptor\n")
  print (velociraptor 30.0 10)
```

The code allows you to print things on the shell

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Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

You are cheating!!! That is imperative code!!! So all this course is about nothing because you cannot have pure functional programming!

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calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

You are cheating!!! That is imperative code!!! So all this course is about nothing because you cannot have pure functional programming!

- No. The do notation is syntax to hide a functional structure called *Monad*
- We do not have time to explain monads in detail in this course, but they are structures that only use lambdas and a composition of lambdas to produce a result.
- It is possible to express imperative behaviours only with monads.
- If you are interested take a look at the State monad.
- In particular the IO Monad allows you to handle side effects, thus print on the shell

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Translating
Lamda
calculus to
Haskell

Lazy
evaluation

The "do"
notation and
IO monad

The best of luck, and thanks for the
attention!