

# Software Engineering 1

Herkansing OP4 - 2017

## 1 Question 1 (4 pts.)

**Grading:** Full points for all correct steps and result. -1 for each wrong step. Zero points with 4 or more errors.

Given the following lambda program, complete the empty beta reduction steps for this program.

```
((((λf g→(f (g x))) (λx y→y)) (λx→x)) A)
```

### 1.1 Answer 1

```
((((λf g→(f (g x))) (λx y→y)) (λx→x)) A)
```

```
(( (λf g→(f (g x))) (λx y→y)) (λx→x)) A)
```

```
(( (λg→( (λx y→y) (g x))) (λx→x)) A)
```

```
(( (λg→((λx y→y) (g x))) (λx→x)) A)
```

```
(( (λx y→y) ( (λx→x) x)) A)
```

```
(( (λx y→y) ((λx→x) x)) A)
```

```
(( (λx y→y) x) A)
```

```
(( (λx y→y) x) A)
```

```
((λy→y) A)
```

```
((λy→y) A)
```

```
A
```

## 2 Question 2 (4 pts.)

**Grading:** Full points for all correct steps and result. -1 for each wrong step. Zero points with 4 or more errors.

Given the following lambda calculus program complete the typing derivation for the program.

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→((g (f t)) l))
```

## 2.1 Answer 2

$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) \ (g:(\text{List} \rightarrow \text{List} \rightarrow \text{List})) \ (t:\text{Tuple}) \ (l:\text{List}) \rightarrow ((g \ (f \ t)) \ l))$$

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→((g (f t)) l))
```

$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) \ (g:(\text{List} \rightarrow \text{List} \rightarrow \text{List})) \ (t:\text{Tuple}) \ (l:\text{List}) \rightarrow ((g \ ( \text{Tuple} \rightarrow \text{List} \ t)) \ l))$$
$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) (g:(\text{List} \rightarrow \text{List} \rightarrow \text{List})) (t:\text{Tuple}) (l:\text{List}) \rightarrow ((g ((\text{Tuple} \rightarrow \text{List}) t)) l))$$

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→(( (List→List→List) ((Tuple→List) t)) l))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List) →
  (((List→List→List) ((Tuple→List) t)) l))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→(((List→List→List) ((Tuple→List)
Tuple)) l))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List) →
  (((List→List→List) ((Tuple→List) Tuple)) l))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→(((List→List→List) ((Tuple→List)
    Tuple)) List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→(((List→List→List)
((Tuple→List) Tuple) ) List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→(((List→List→List) List) List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→( ((List→List→List) List) List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→(List→List) List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→ ((List→List) List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List)→ List)
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) (l:List) → List)
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple)→ (List→List))
```

```
(λ(f:(Tuple→List)) (g:(List→List→List)) (t:Tuple) → (List→List))
```

$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) \ (g:(\text{List} \rightarrow \text{List} \rightarrow \text{List})) \rightarrow (\text{Tuple} \rightarrow \text{List} \rightarrow \text{List}))$$
$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) (g:(\text{List} \rightarrow \text{List} \rightarrow \text{List})) \rightarrow (\text{Tuple} \rightarrow \text{List} \rightarrow \text{List}))$$
$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) \rightarrow ((\text{List} \rightarrow \text{List} \rightarrow \text{List}) \rightarrow \text{Tuple} \rightarrow \text{List} \rightarrow \text{List}))$$
$$(\lambda(f:(\text{Tuple} \rightarrow \text{List})) \rightarrow ((\text{List} \rightarrow \text{List} \rightarrow \text{List}) \rightarrow \text{Tuple} \rightarrow \text{List} \rightarrow \text{List}))$$
$$((\text{Tuple} \rightarrow \text{List}) \rightarrow (\text{List} \rightarrow \text{List} \rightarrow \text{List}) \rightarrow \text{Tuple} \rightarrow \text{List} \rightarrow \text{List})$$