



暨南大學
JINAN UNIVERSITY

Lecture 2 – Supplement

-Cryptographic Algorithms and Protocols

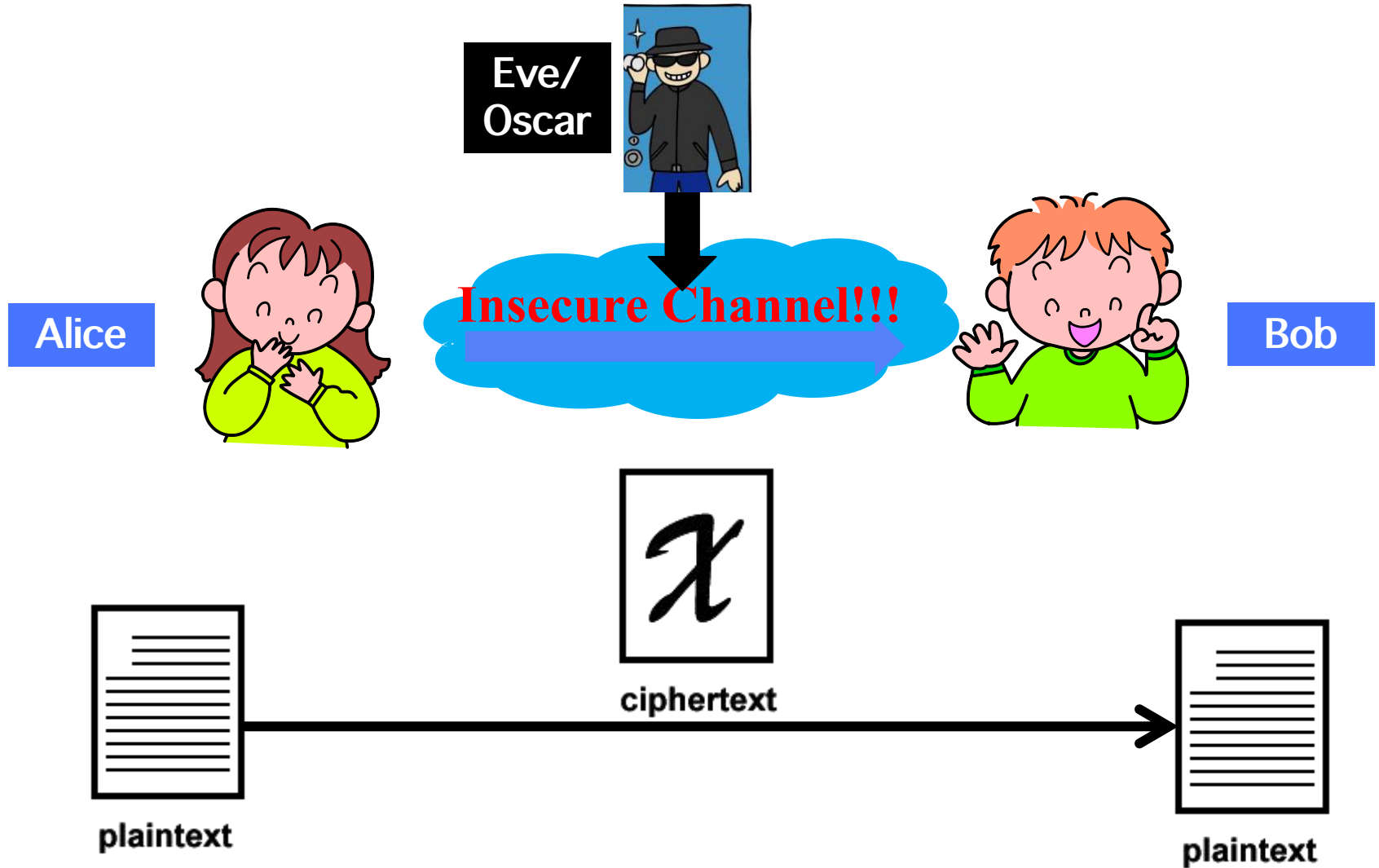
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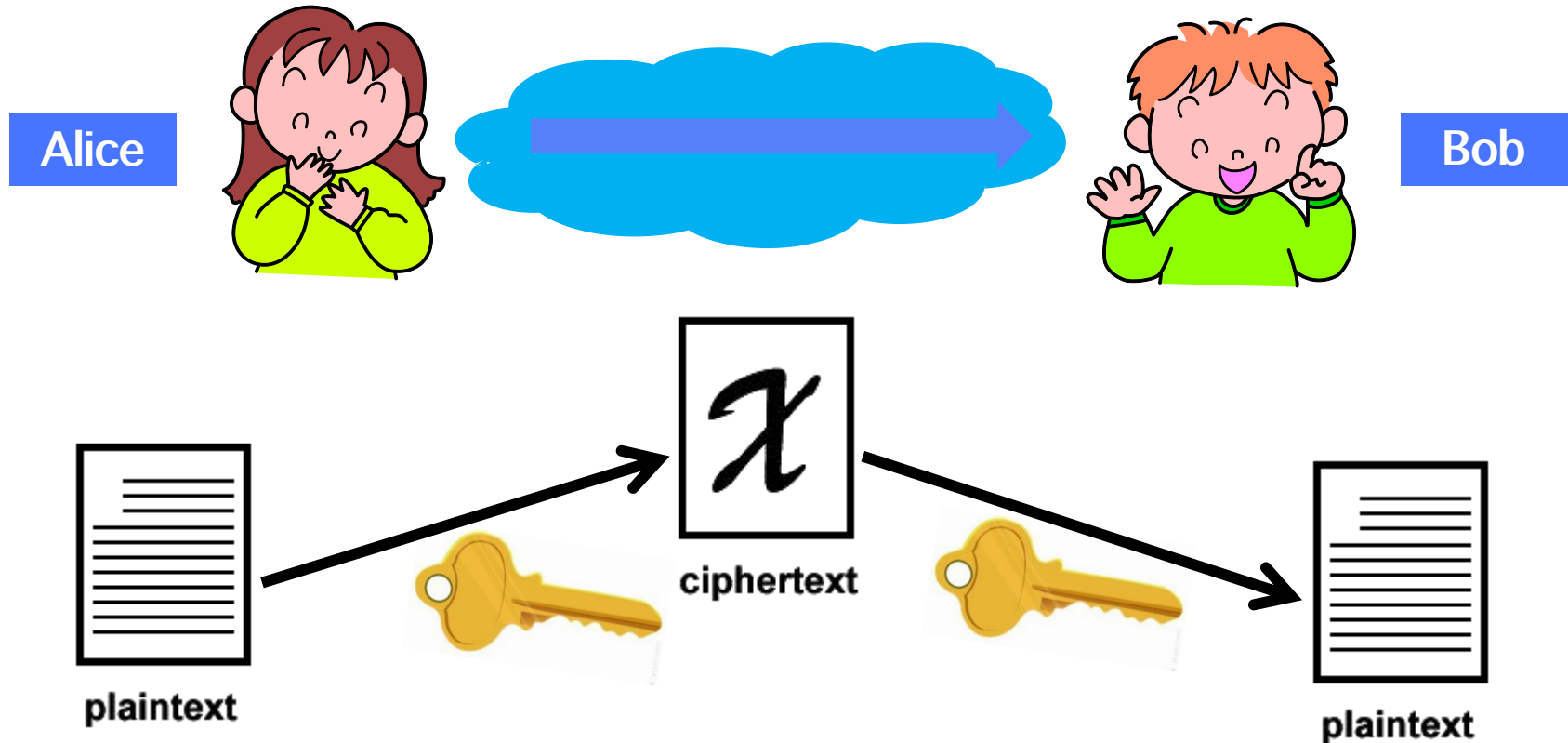
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Dept. Computer Science

Intuition on Cryptography



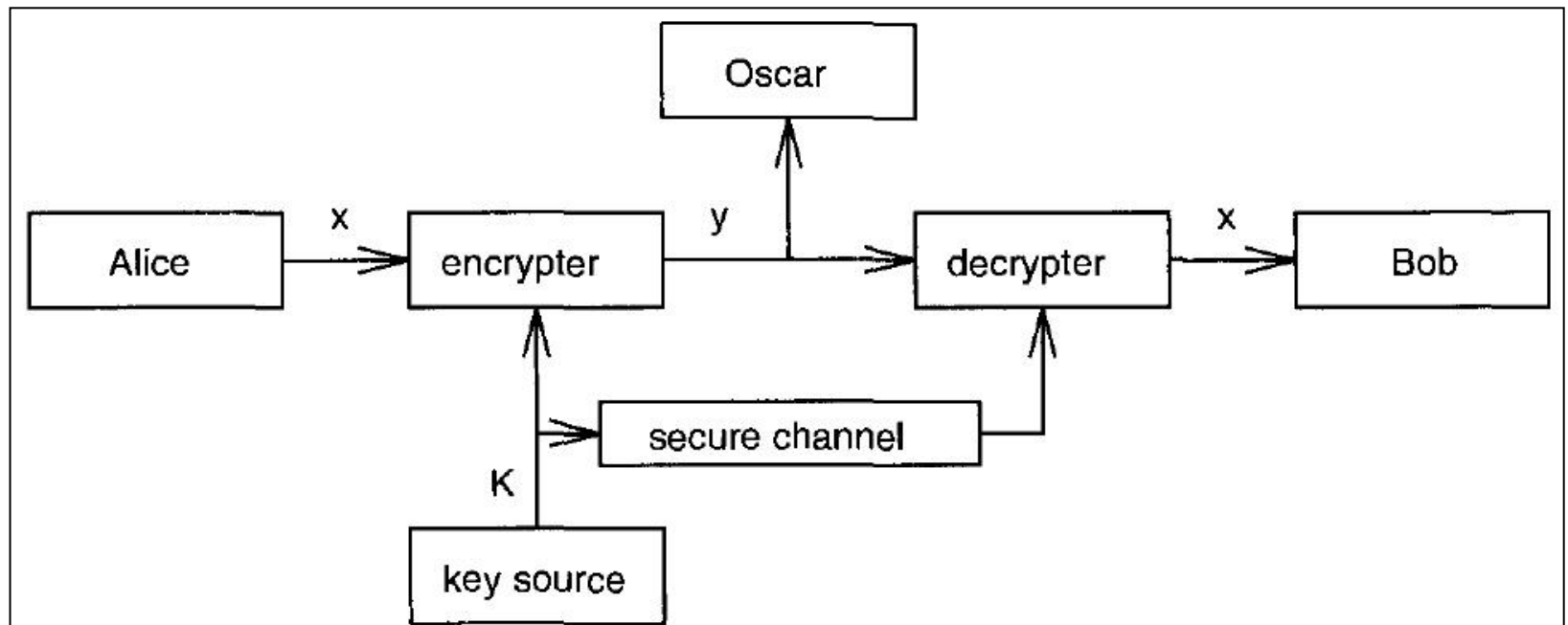
Symmetric-Key Cryptosystem (SKC)



Cryptographic Communication System

Protocol:

- A and B choose a random key K by a secure channel
- A wants to send a string message $\mathbf{x}=x_1x_2\dots x_n$
- A computes $y_i=e_K(x_i)$ and the resulting string $\mathbf{y}=y_1y_2\dots y_n$ is sent over the insecure channel
- B receives $\mathbf{y}=y_1y_2\dots y_n$ and decrypts $x_i=d_K(y_i)$ to obtain $\mathbf{x}=x_1x_2\dots x_n$



Statistical Properties of the English Language

Beker and Piper's Table for
Probabilities of occurrence of the 26 letters

letter	probability	letter	probability
A	.082	N	.067
B	.015	O	.075
C	.028	P	.019
D	.043	Q	.001
E	.127	R	.060
F	.022	S	.063
G	.020	T	.091
H	.061	U	.028
I	.070	V	.010
J	.002	W	.023
K	.008	X	.001
L	.040	Y	.020
M	.024	Z	.001

The thirty most common digrams:

TH, HE, IN, ER, AN, RE, ED, ON, ES, ST, EN, AT, TO, NT, HA, ND, OU, EA, NG, AS, OR, TI, IS, ET, IT, AR, TE, SE, HI, OF.

The twelve most common trigrams:

THE, ING, AND, HER, ERE, ENT, THA, NTH, WAS, ETH, FOR, DTH.

Ciphertext-only attack on the Substitution Cipher

► See Example 2.11 on Pages 42-44.

Ciphertext from a substitution cipher:

Y I F Q F M Z R W Q F Y V E C F M D Z P C V M R Z W N M D Z V E J B T X C D D U M J
 N D I F E F M D Z C D M Q Z K C E Y F C J M Y R N C W J C S Z R E X C H Z U N M X Z
 N Z U C D R J X Y Y S M R T M E Y I F Z W D Y V Z V Y F Z U M R Z C R W N Z D Z J J
 X Z W G C H S M R N M D H N C M F Q C H Z J M X J Z W I E J Y U C F W D J N Z D I R

letter	frequency	letter	frequency
A	0	N	9
B	1	O	0
C	15	P	1
D	13	Q	4
E	7	R	10
F	11	S	3
G	1	T	2
H	4	U	5
I	5	V	5
J	11	W	8
K	1	X	6
L	0	Y	10
M	16	Z	20

Stage 2: Look at digrams, especially those of the form -Z or Z-.



$$d_K(W) = d.$$

Stage 1



$$d_K(Z) = e$$

C, D, F, J, M, R, Y
 t, a, o, i, n, s, h, r

Ciphertext-only attack on the Substitution Cipher

- ▶ See Example 2.11 on Pages 42-44.

Ciphertext from a substitution cipher:

YIFQFMZRWQFYVECFMDZPCVMRZWNMDZVEJBCTXCDUMJ
NDIFEFMDZCDMQZKCEYFCJMYRNCWJCSZREXCHZUNMXZ
NZUCDRJXYYSMRTMEYIFZWDYVZVYFZUMRZCRWNZDZJJ
XZWGCHSMRNMDHNCMFQCHZJMXJZWIEJYUCFWDJNZDIR



Our friend from Paris examined his empty glass with surprise, as if evaporation had taken place while he wasn't looking. I poured some more wine and he settled back in his chair, face tilted up towards the sun.¹

Attack on Shift Cipher

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>	<i>G</i>	<i>H</i>	<i>I</i>	<i>J</i>	<i>K</i>	<i>L</i>	<i>M</i>
0	1	2	3	4	5	6	7	8	9	10	11	12
<i>N</i>	<i>O</i>	<i>P</i>	<i>Q</i>	<i>R</i>	<i>S</i>	<i>T</i>	<i>U</i>	<i>V</i>	<i>W</i>	<i>X</i>	<i>Y</i>	<i>Z</i>
13	14	15	16	17	18	19	20	21	22	23	24	25

Jack



Key K = 1

MFUVTNFFUBUFJHIU

MEETING

letusmeetateight

Lucy




Ciphertext-only attack on the Affine cipher

- See Example 2.10 on Pages 41-42.

Ciphertext from an Affine cipher:

FMXVEDKAPHFERBNDKRXRSREFMORUDSDKDVSHVUFEDK
APRKDLYEVLRRHRH $e_K(x) = ax + b$

Beker and Piper's statistical table



letter	frequency	letter	frequency
A	2	N	1
B	1	O	1
C	0	P	2
D	7	Q	0
E	5	R	8
F	4	S	3
G	0	T	0
H	5	U	2
I	0	V	4
J	0	W	0
K	5	X	2
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M	2	Z	0

letter	probability	letter	probability
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M	.024	Z	.001

Ciphertext-only attack on the Affine cipher

► See Example 2.10 on Pages 41-42.

Ciphertext from an Affine cipher:

FMXVEDKAPHFERBNDKRXRSREFMORUDSDKDVSHVUFEDK
APRKDLYEVLRRHHRH

$$e_K(x) = ax + b$$

~~Try 1:~~ R is the encryption of e and D is the encryption of t

$$\begin{cases} e_K(4) = 17 \\ e_K(19) = 3 \end{cases} \quad \begin{cases} 4a + b = 17 \\ 19a + b = 3 \end{cases} \Rightarrow a = 6, b = 19 \text{ (in } \mathbb{Z}_{26})$$

$\gcd(a, 26) = 2 > 1$

~~Try 2:~~ R is the encryption of e and E is the encryption of $t \Rightarrow a = 13$

~~Try 3:~~ R is the encryption of e and H is the encryption of $t \Rightarrow a = 8$

~~Try~~ 4: R is the encryption of e and K is the encryption of t

$$\Rightarrow a = 3, b = 5 \quad \Rightarrow d_K(y) = 9y - 19$$

\Rightarrow algorithms are quite general definition so far arithmetic processes

Permutation Cipher - Example 2.7

Suppose $m = 6$ and the key is the following permutation π :

x	1	2	3	4	5	6
$\pi(x)$	3	5	1	6	4	2

we see that the permutation π^{-1} is the following:

x	1	2	3	4	5	6
$\pi^{-1}(x)$	3	6	1	5	2	4

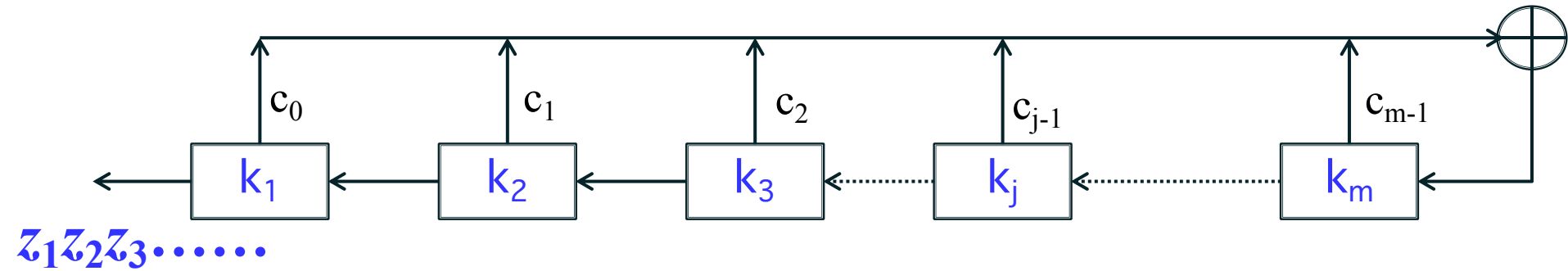
$$K_{\pi} = \begin{pmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{pmatrix}$$

Plaintext: shesellsseashellsbytheseashore.

Partition: shesel | lsseas | hellsb | ythese | ashore

Encryption: EESLSH | SALSES | LSHBLE | HSYEET | HRAEOS

General LFSR of Binary Stream Ciphers



$$z_{i+m} = \sum_{j=0}^{m-1} c_j z_{i+j} \bmod 2$$

Stream Ciphers - Example 2.8

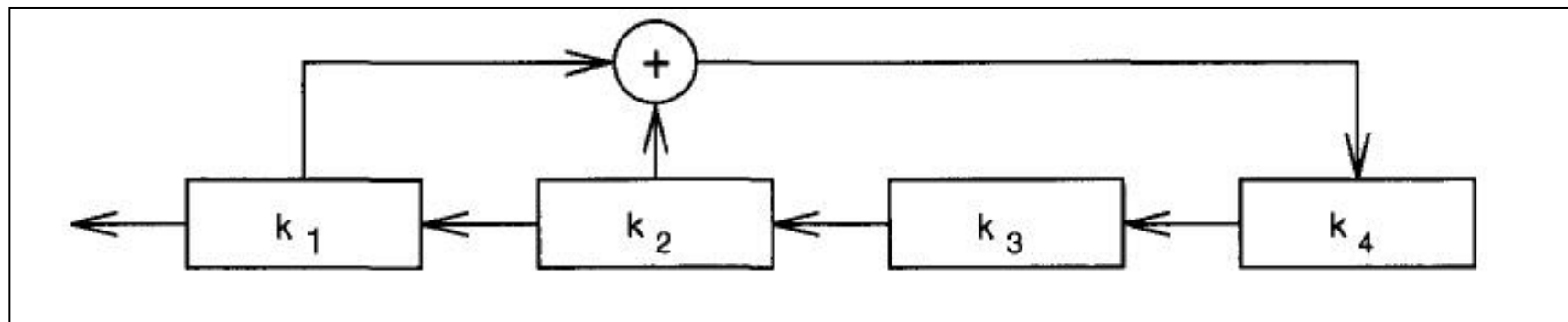
Suppose $m = 4$ and the keystream is generated using the linear recurrence

$$z_{i+4} = (z_i + z_{i+1}) \bmod 2,$$

$i \geq 1$. If the keystream is initialized with any vector other than $(0, 0, 0, 0)$, then we obtain a keystream of period 15. For example, starting with $(1, 0, 0, 0)$, the keystream is

$100010011010111 \dots$

Any other non-zero initialization vector will give rise to a cyclic permutation of the same keystream. \square



Known-plaintext attack on the LFSR Stream cipher

Oscar has a plaintext string $x_1 x_2 \cdots x_n$

and the corresponding ciphertext string $y_1 y_2 \cdots y_n$

Encryption rule: $y_i = (x_i + z_i) \bmod 2$.

Keystream generator: $z_{m+i} = \sum_{j=0}^{m-1} c_j z_{i+j} \bmod 2$
 $(z_1, \dots, z_m) = (k_1, \dots, k_m)$

KEY?

$k_1, k_2, \dots, k_m; c_0, c_1, \dots, c_{m-1}$

Then he can compute the keystream bits $z_i = (x_i + y_i) \bmod 2$

 $(k_1, k_2, \dots, k_m) = (z_1, z_2, \dots, z_m)$

Known-plaintext attack on the LFSR Stream cipher

$$c_0, c_1, \dots, c_{m-1} \quad ?$$

$$z_{m+i} = \sum_{j=0}^{m-1} c_j z_{i+j} \bmod 2$$

$$(z_{m+1}, z_{m+2}, \dots, z_{2m}) = (c_0, c_1, \dots, c_{m-1}) \begin{pmatrix} z_1 & z_2 & \dots & z_m \\ z_2 & z_3 & \dots & z_{m+1} \\ \vdots & \vdots & & \vdots \\ z_m & z_{m+1} & \dots & z_{2m-1} \end{pmatrix}$$



$$(c_0, c_1, \dots, c_{m-1}) = (z_{m+1}, z_{m+2}, \dots, z_{2m}) \begin{pmatrix} z_1 & z_2 & \dots & z_m \\ z_2 & z_3 & \dots & z_{m+1} \\ \vdots & \vdots & & \vdots \\ z_m & z_{m+1} & \dots & z_{2m-1} \end{pmatrix}^{-1}$$

Autokey Cipher - Example 2.9

Suppose the key is $K = 8$, and the plaintext is

Plaintext: rendezvous.

Integers of Plaintext: 17 4 13 3 4 25 21 14 20 18

Keystream: 8 17 4 13 3 4 25 21 14 20

```
graph TD; P1[17] --> K1[8]; P2[4] --> K2[17]; P3[13] --> K3[4]; P4[3] --> K4[13]; P5[4] --> K5[3];
```

Encryption: 25 21 17 16 7 3 20 9 8 12

Ciphertext: ZVRQH DUJIM.