

# Gestion de Portefeuille

## TP-5; Modèle de Black-Litterman

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- Effectuer une lecture attentive de l'article de He et Litterman.
- A partir de la note de cours, reproduire les autres exemples de l'article, comparer les résultats avec ceux obtenus avec le package BLCOP.
- Comparer avec une allocation MV classique.

Market data from He & Litterman paper

```
data =  
'1,0.4880,0.4780,0.5150,0.4390,0.5120,0.4910  
0.4880,1,0.6640,0.6550,0.3100,0.6080,0.7790  
0.4780,0.6640,1,0.8610,0.3550,0.7830,0.6680  
0.5150,0.6550,0.8610,1,0.3540,0.7770,0.6530  
0.4390,0.3100,0.3550,0.3540,1,0.4050,0.3060  
0.5120,0.6080,0.7830,0.7770,0.4050,1,0.6520  
0.4910,0.7790,0.6680,0.6530,0.3060,0.6520,1'  
  
Corrmat = matrix( as.double(spl( gsub('\n', ', ', data), ', ')),  
                  nrow = length(spl(data, '\n')), byrow=TRUE)  
  
stdevs = c(16.0, 20.3, 24.8, 27.1, 21.0, 20.0, 18.7)/100  
w.eq = c(1.6, 2.2, 5.2, 5.5, 11.6, 12.4, 61.5)/100  
# Prior covariance of returns  
Sigma = Corrmat * (stdevs %*% t(stdevs))
```

Equilibrium risk premium

```
# risk aversion parameter  
delta = 2.5  
Pi = delta * Sigma %*% w.eq
```

Summary market data

Assets	Std Dev	Weq	PI
Australia	16	1.6	3.9
Canada	20.3	2.2	6.9
France	24.8	5.2	8.4
Germany	27.1	5.5	9
Japan	21	11.6	4.3
UK	20	12.4	6.8
USA	18.7	61.5	7.6

Exemple 1

$$r_u = r_f + (r_u - r_f) \frac{w_f r_f + w_u r_u}{w_f + w_u} + 0.05 \frac{w_f r_f + w_u r_u + w_g r_g}{w_f + w_u} = r_f + (r_u - r_f) \frac{w_f r_f + w_u r_u}{w_f + w_u} + 0.05 \frac{w_f r_f + w_u r_u + w_g r_g}{w_f + w_u}$$

Après identification, on arrive à l'équation suivante:

```
## [1] 11.49351
```

Nous pouvons calculer maintenant  $r_u$  et  $r_f$

```
## [1] 7.6
```

```
## [1] 6
```

```
##      Australia      Canada      France      Germany      Japan      UK      USA
## [1,] 0.1143978 0.008153653 -0.3958454 0.579924 0.1806869 -0.1045678 0.6172508
```