

SIM & Treynor-Black

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Single Index Model (Sharpe)

- ▶ Rendement

$$R_i(t) = \alpha_i + \beta_i R_M(t) + e_i(t)$$

- ▶ Espérance de rendement

$$E(R_i(t)) = \alpha_i + \beta_i E(R_M(t))$$

- ▶ Variance du rendement

$$\sigma_i^2 = \beta_i^2 \sigma_M^2 + \sigma(e_i)^2$$

- ▶ Covariance des rendements

$$\text{cov}(R_i, R_j) = \beta_i \beta_j \sigma_M^2$$

Portefeuille selon le SIM

Soit un portefeuille de n actifs avec $w_i = \frac{1}{n}$.

$$R_P(t) = \alpha_P + \beta_P R_M(t) + e_P(t)$$

$$\sigma_P^2 = \beta_P^2 \sigma_M^2 + \sigma(e_P)^2$$

Division du travail en Gestion de Portefeuille

- Espérance de rendement

$$E(R_i(t)) = \alpha_i + \beta_i E(R_M(t))$$

- Variance du rendement

$$\sigma_i^2 = \beta_i^2 \sigma_M^2 + \sigma(e_i)^2$$

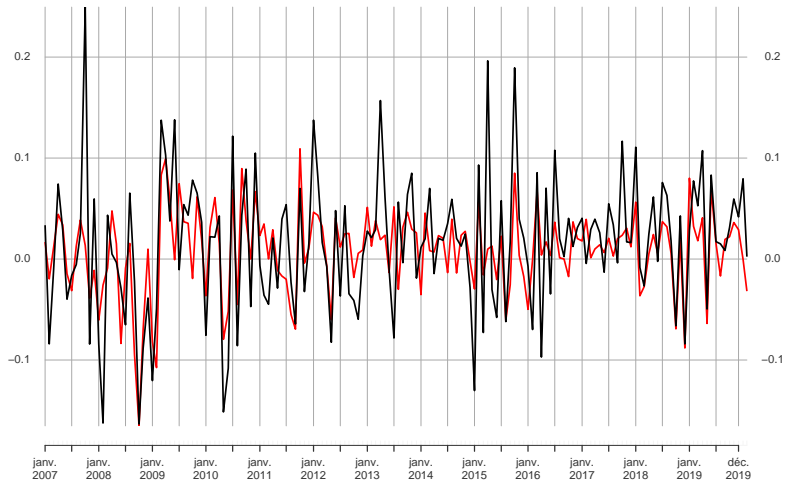
Allocation Treynor-Black

Voir note pour le détail des calculs.

Données

	AAPL	AMZN	MSFT	F	SPY	QQQ	XOM	MMM	HD	PG	KO
Observations	158.0000	158.0000	158.0000	158.0000	158.0000	158.0000	158.0000	158.0000	158.0000	158.0000	158.0000
NAs	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Minimum	-0.3296	-0.2540	-0.1634	-0.5788	-0.1652	-0.1558	-0.1423	-0.1498	-0.1652	-0.1161	-0.1668
Quartile 1	-0.0213	-0.0303	-0.0280	-0.0456	-0.0144	-0.0159	-0.0265	-0.0230	-0.0227	-0.0211	-0.0168
Median	0.0291	0.0256	0.0203	-0.0022	0.0128	0.0192	0.0022	0.0144	0.0178	0.0081	0.0104
Arithmetic Mean	0.0254	0.0298	0.0152	0.0115	0.0076	0.0123	0.0017	0.0079	0.0151	0.0074	0.0100
Geometric Mean	0.0214	0.0252	0.0130	0.0020	0.0067	0.0110	0.0004	0.0063	0.0133	0.0065	0.0090
Quartile 3	0.0792	0.0830	0.0545	0.0470	0.0324	0.0455	0.0411	0.0455	0.0608	0.0361	0.0405
Maximum	0.2377	0.5413	0.2495	1.2738	0.1091	0.1317	0.1128	0.1734	0.1605	0.1161	0.1419
SE Mean	0.0071	0.0079	0.0053	0.0120	0.0033	0.0040	0.0040	0.0045	0.0049	0.0034	0.0035
LCL Mean (0.95)	0.0114	0.0143	0.0047	-0.0121	0.0010	0.0044	-0.0062	-0.0010	0.0055	0.0006	0.0031
UCL Mean (0.95)	0.0394	0.0454	0.0257	0.0352	0.0142	0.0201	0.0095	0.0168	0.0248	0.0141	0.0170
Variance	0.0079	0.0098	0.0045	0.0226	0.0018	0.0025	0.0025	0.0032	0.0037	0.0019	0.0020
Stdev	0.0889	0.0990	0.0670	0.1504	0.0419	0.0502	0.0502	0.0566	0.0612	0.0430	0.0442
Skewness	-0.6572	0.7403	0.0788	3.6175	-0.7421	-0.6247	-0.3969	-0.3662	-0.3033	-0.2344	-0.2589
Kurtosis	1.9491	4.0251	0.8958	31.4460	1.5521	0.9798	0.0867	0.5184	0.4291	0.0619	1.1258

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Calcul de β

```
beta_roll <- removeNA(rollapply(data=monthly.ret$MSFT, Rb=r  
                                FUN=CAPM.beta, width=36, by
```



Calcul de α

```
alpha_roll <- removeNA(rollapply(data=monthly.ret$MSFT, Rb=
                                FUN=CAPM.alpha, width=36,
```



Bibliographie

Grinhold, R.C. and Kahn, R. Active Portfolio Management, McGraw-Hill, 2000