Modelling and Simulation in Modern Science

or

The Hitch-hiker's guide to Model Land

or

The Cat That Looks Most Like A Dog

or

Escaping from Model Land

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Model worlds and the real world

This will be an introductory chapter

1.1 One real world; infinitely many model worlds

Though there is only one real world, there are many model worlds.

Model worlds include any and all representations, from the material or mathematical to the conceptual or artistic.

Model worlds may be complete and internally self-consistent, or more likely they may be incomplete and self-contradictory.

Each model is different, by virtue of abstracting different elements of the original real world.

The model-world, contained and defined by the model, then functions as a surrogate object for the purpose of recording or drawing certain conclusions about the real world, when the characteristics of the real world are inaccessible or unobservable.

Model worlds are constructed in lots of different ways:

• physical model of flood plain

- representational model eg OS map
- biological model eg mouse, e. coli
- conceptual model eg wave/particle
- statistical model
- simulation model eg climate, traffic
- 1.2 Motivation: Why do we construct model worlds? What is it all for?
- 1.3 Some consequences: teaser examples, for later indepth treatment (one per chapter???)
- 1.4 Solutions: teaser/summary

What do model worlds tell us?

Model: a thing or concept believed to have a correspondence with the real world, such that one may draw conclusions about properties of the real world by observing the model.

Model world: the world-in-the-model: the set of observable states of the model

[Does model-world have a hyphen or not?]

[define parameter, variable, etc]

2.1 Abstraction and simplification

Though there is only one real world, there are many model worlds. Model worlds include any and all representations, from the material or mathematical to the conceptual or artistic. Model worlds may be complete and internally self-consistent, or more likely they may be incomplete and self-contradictory. Each model is different, by virtue of abstracting different elements of the original real world. The model-world, contained and defined by the model, then functions as a surrogate object for the purpose of recording or drawing certain conclusions about the real world, when the characteristics of the real world are inaccessible or unobservable.

Some degree of abstraction and simplification is generally necessary for a model to be of value. An exact replica of the object of study would likely be no more accessible than the object itself, as is memorably described in Borges' 1946 short story "On Exactitude In Science" (quoted below). The important question is not the degree to which the map resembles the territory, but the useful information content of the map in terms of the kinds of questions we might wish to answer with it. If I am asking which is the best way to walk up a mountain, I may be interested in a contour map; if I am looking for a certain kind of fossil then I would prefer a geological map; if I would like to know where to find something to eat on my return, neither of the above will be of much use. Efforts to produce a larger, better, more detailed map sometimes arise from a genuine need for detail and sometimes instead from a lack of clarity about the question.

On Exactitude in Science

Box 2.1

'... In that Empire, the Art of Cartography attained such Perfection that the map of a single Province occupied the entirety of a City, and the map of the Empire, the entirety of a Province. In time, those Unconscionable Maps no longer satisfied, and the Cartographers Guilds struck a Map of the Empire whose size was that of the Empire, and which coincided point for point with it. The following Generations, who were not so fond of the Study of Cartography as their Forebears had been, saw that that vast map was Useless, and not without some Pitilessness was it, that they delivered it up to the Inclemencies of Sun and Winters. In the Deserts of the West, still today, there are Tattered Ruins of that Map, inhabited by Animals and Beggars; in all the Land there is no other Relic of the Disciplines of Geography."

Suárez Miranda, Viajes de varones prudentes, Libro IV, Cap. XLV, Lérida, 1658
Jorge Luis Borges, 1946, translated by XX

Abstracting the essential qualities of a situation in order to construct a model is something that we do routinely and unconsciously as a means of understanding the world from a limited perspective. There is a model, of sorts, in our expectation that the colour of a raincoat does not affect its waterproofing, or that the sun will rise in the east again tomorrow. These models might be based on long observation that A-follows-B or on a detailed logical explanation, or they may be some kind of unrationalised intuition. Scientific models are constructed in much the same way, either as a statistical relationship between observations of one set of events and another, or as a logical deduction given a set of starting points. Scientific models also arise from intuition, though rationalisations of that intuition are demanded as part of today's scientific method.

2.2 Model world quantities

2.2.1 How the real world influences the model world, and vice-versa

Quantities in the model world are usually named after their real-world counterparts, but just as the map is not the territory, neither are the labels the objects. Thus, care is needed to ensure that even those model world quantities (variables) thought to have a strong relationship with the real world quantities (measurables) are not accidentally or implicitly given real-world status.

2.2.2 Real world -> model world

In some cases, the undisputed reality of real-world quantities such as the freezing point of water or the acceleration due to gravity give them a very high epistemic status in the mind of the scientific modeller, such that they are given fixed, known values. By contrast, it is acceptable (often unavoidable) to calibrate lower-status parameters such as a cloud fraction or leaf area index by altering or tuning their values (within a range deemed to be reasonable) to give the best possible correspondence of the output with observation. This makes sense in that we "know the answer" for the real-world freezing point of water in a way that we don't for other parameters, but we are

still mistaking the map for the territory: why do we think we "know the answer" in the model world? It could be the case that the freezing point of water in our model world is actually 1 degree different from the real-world value, in the sense that a freezing point of water chosen to be 1 degree rather than zero could give output which corresponds more closely to observation.

The freezing point of water, as far as I am aware, is hard-coded into all global climate models as zero degrees Celsius. But after many real-years of work, thousands of model-years of simulation and calibrating many other parameters, models still differ by a few degrees in their global mean temperature (IPCC fig 9.8, 2013). Most presentations subtract off the difference, implying that the net effects of all processes must be linear with regard to temperature, and effectively varying the freezing point of water by a couple of degrees Celsius.

2.2.3 Model world -> real world (eg implied volatility, climate sensitivity)

At other times, the relationship goes the other way: quantities which have been given a definition or meaning solely as a result of their usefulness in the model world become applied to the real world as well. In climate research, one example is the "climate sensitivity": the amount by which the global mean temperature increases given a doubling in the radiative forcing applied. The concept is already theory-laden: it is assumed that the relationship is logarithmic and only the constant of proportionality need be determined (as an aside, it is also insensitive to the systematic differences in global mean temperature mentioned above).

2.2.4 No true parameter set exists

2.3 Complexity. Subtractability. Noise/music.

2.4 Dynamical (process-based) models versus statistical models

- 2.4.1 ?explainability? and interpretability
- 2.4.2 Horses and Hawkmoths
- 2.4.3 Note on ?machine learning??

Butterflies and Hawkmoths

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3.5 Consequences of the Hawkmoth Effect

- 3.5.1 Things which are not included may not be negligible
- 3.5.2 Models cannot be monotonically improved

3.6 Mathematical treatment (easily skippable!)

Andronov/Pontryagin 1937, Anosov, etc. Shadowing timescales and numerical approximations. Solution of PDEs. Ergodicity, existence/timescales of attractors, ?statistical stability??

The Cat that looks most like a Dog

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Escaping from Model Land

Chapter overview

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5.1 Statements made about real world need to refer to the real world

5.2 Evaluation against past data

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- 5.2.2 Big Data
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5.3 Use of expert judgement

Making decisions based on models

- 6.1 The aim: getting ?the right answer? or supporting a decision?
- **6.1.1 Properties of good decisions**
- **6.1.2** Sometimes the skill of the model is unimportant (Mali farmers; Start; horoscopes; biodynamic planting?)
- 6.1.3 Sometimes the confidence, even where reported honestly, is recalibrated by the audience (?ninety per cent? =/= 90%)
- 6.2 Evaluation of models, evaluation of forecasts

Conclusions and consequences

- 7.1 The unreasonable effectiveness of mathematics in the natural sciences?
- 7.2 Modelling for decision support
- 7.3 Alternative strategies, find positive/constructive note to end on.

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