

I. Environment Setup

Language: Python 3 (on VS code)**Library: numpy, PIL**

- II. Q1: Write a program which counts the Yokoi connectivity number on a downsampled image(lena.bmp).

step 1: down-sampling the original binarized lena.bmp from 512*512 to 64*64

```
def downSampling(image, rate):  
    '''  
    image: Image from PIL\n    rate: (int) down-sampling rate.  
    '''  
  
    width, height = image.size  
    new_width = width//rate  
    new_height = height//rate  
    new_image = Image.new("L", (new_width,new_height))  
  
    for x in range(new_width):  
        for y in range(new_height):  
            new_image.putpixel((x,y), image.getpixel((x*rate,y*rate)))  
  
    return new_image
```

step 2: implement Yokoi h function and f function

```
def Yokoi_h_function(b, c, d, e):  
    if(b==c and (d!=b or e!=b)):  
        return "q"  
    elif b==c and (d==b and e==b):  
        return "r"  
    elif b!=c:  
        return "s"  
  
def Yokoi_f_function(a1, a2, a3, a4):  
    if a1==a2==a3==a4=="r":  
        return 5  
    else:  
        return [a1, a2, a3, a4].count("q")
```

Step 3: traverse each element in the down-sampling image and count the connectivity number by h function and f function

```
def Yokoi(origin_image):  
    """  
    image: Image from PIL  
    """  
    width, height = origin_image.size  
    newList = [[ " " for i in range(width)] for j in range(height)]  
    for c in range(width):  
        for r in range(height):  
            if origin_image.getpixel((c,r)) != 0:  
                a1 = Yokoi_h_function(myGetPixel(origin_image,(c,r)), myGetPixel(origin_image,(c+1,r)),  
                                     myGetPixel(origin_image,(c+1,r-1)), myGetPixel(origin_image,(c,r-1)))  
                a2 = Yokoi_h_function(myGetPixel(origin_image,(c,r)), myGetPixel(origin_image,(c,r-1)),  
                                     myGetPixel(origin_image,(c-1,r-1)), myGetPixel(origin_image,(c-1,r)))  
                a3 = Yokoi_h_function(myGetPixel(origin_image,(c,r)), myGetPixel(origin_image,(c-1,r)),  
                                     myGetPixel(origin_image,(c-1,r+1)), myGetPixel(origin_image,(c,r+1)))  
                a4 = Yokoi_h_function(myGetPixel(origin_image,(c,r)), myGetPixel(origin_image,(c,r+1)),  
                                     myGetPixel(origin_image,(c+1,r+1)), myGetPixel(origin_image,(c+1,r)))  
                newList[r][c] = Yokoi_f_function(a1,a2,a3,a4)  
    return newList
```

I also implement myGetPixel function to detect out of range problem.

```
def myGetPixel(image, position):  
    x, y = position  
    width, height = image.size  
    if(0 <= x < width and 0 <= y < height):  
        return image.getpixel(position)  
    else:  
        return 0
```

Step 5: write the output list to a txt file

```
if __name__ == "__main__":  
    from PIL import Image  
    import numpy as np  
  
    originalImage = Image.open('binary.bmp')  
    downSamplingImage = downSampling(originalImage, 8)  
    output_list = Yokoi(downSamplingImage)  
    with open("Yokoi_connectivity.txt","w") as output_file:  
        for i in output_list:  
            for j in i:  
                output_file.write(str(j))  
            output_file.write('\n')
```

Result: 0s are also recorded.

11111111	1211111111112232221	111111111111	0 0
15555551	11555555511 2 11 11	115555555511	0
15555551	1 2115555112 21112221	15555555551	21
15555551	1 2 155112 2221511	155555555511	1
15555551	22 2112 22 121 0 0	1555555555511	0
15555551	1 2 21 2 1 1	1555555555551	0
15555551	12 1 121111 1321	15555555555511	
15111551	1322 1155551111	15555555555551	
111 1551	1 121555555511	155555555555511	
11 1551	21155555511	15511155555511	
21 1551	2 15555555111	1551 11555511	
1 1551	2 155555555511	1551 115551	1
1551	1121155555555551	1551 15511	12
1551	15555555555555511	1551 1111	111
1551	1 2221155555555555511	1151 11	1151
1551	2 22 1 15555555555555511	151 11111	1551
1551	2 1 115555555555555551	151 115551	11551
1551	2 115555555555555555111511155511	11511155511	115551
1551	12 1155555555555555555555555551		155551
1551	11 0 221555555555555555555555555112		1155551
1551	111 22 15555555555555555555555551 1		1555551
1551	1511 1 125112111112111555555555111		11555551
1551	15521 1 121 1 11 1 15555555111 0		15555551
1551	1151 132 2 1155555111 0		115555551
1551	151 0 322 115555111 121		155555551
1551	1221 2 1555551 131		1155555551
1551	2 0 1 115555511 1		1155555551
1551	2 0 0 1155555551 0		1 155555551
1551	2 11555555551		21155555551
1551	1 0 115555555551		15555555551
1551	1 11511115555521 1		115555555551
1551	1 1 11111 1155511 2		155555555551
1551	131 111 15111 2		155555555551
1551	121 0 1121 1 111 1 2		1155555555551
1551	11 111 1 221 11 1 2		1555555555551
1551	12 0 1 21 121 11 1111 2		1555555555551
1551	1 12 22 151111111551 2		11555555555551
1551	1 2 1555551115511 1		15555555555551
1551	2 0 0 22 12555551 15551 1		155555555555551
1551	1 1555511 11511 2		1155555555555551
1551	0 0 21 155551 1 151 2		1555555555555551
1551	2 15555112 151 2		1555555555555551
1551	1 1 1 1155555511111 2		1555555555555551
1551	2 22 111511111212 211555555555555551		211555555555555551
1551	0 1 12 151 2 1 15555555111555551		15555555111555551
1551	0 0 0 1111 121 155555551 1555551		155555551 1555551
1551	0 11111111 155555551 1555551		155555551 1555551
1551	0 115551 155555551 1555511		211111111 155511
1551	15551 211111111 155511		2 11 115511
11521	1 12 122155511 2111 15511		2111 15511
1 151 0	1 1 155555111 155111 1511		155111 1511
22 1511	1 15555555111 155551 1151		155551 1151
22 1511	1 11155555555511 155511 1511		155511 1511
2 151	0 1 155555555555511 15551 12151		15551 12151
2 1521	0 1 155555555555551 155511 1551		155511 1551
2 151	121 0 1555555555555551 115551 1511		111111151
2 1511	0 15555555555555551 111111151		111511
21 1511	11 11555555555555551 151		211
11 151	0 155555555555555551 1		1
11 151	0 1155555555555555551		
11 151	0 11555555555555555551		
11 151	0 15555555555555555551		
11 111	0 12111111111111111111		