

## Assignment 2

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Q. 1) Design a NPDA for accepting the Language  $ww^R$  where  $w$  belongs to  $\{a, b\}^*$  and  $w^R$  is the reverse of string  $w$ .

→  $L = \{ww^R \mid w \in \{a, b\}^*\}$  where  $w^R$  is the Reverse string  $w$

- The NPDA will push characters from 'w' onto stack, and when it reaches the middle of the input, it will pop character off the stack to match with  $w^R$

- Formal definition of NPDA:-

$M = \langle Q, \Sigma, \Gamma, \delta, q_0, z_0, F \rangle$ , where.

- $Q = \{q_0, q_1, q_2, q_f\}$  : set of states.

- $\Sigma = \{a, b\}$  : input alphabet

- $\Gamma = \{a, b, z_0\}$  : stack alphabet (where  $z_0$  is the initial stack)

- $q_0$  = start state.

- $z_0$  = Initial stack symbol

- $F = \{q_f\}$  : set of accepting states

- Pushing Phase :- (w part)

- $\delta(q_0, a, z_0) = \{(q_0, a, z_0)\}$

- $\delta(q_0, b, z_0) = \{(q_0, b, z_0)\}$

- $\delta(q_0, a, a) = \{(q_0, aa)\}$

- $\delta(q_0, b, b) = \{(q_0, bb)\}$

- $\delta(q_0, a, b) = \{(q_0, ab)\}$

- $\delta(q_0, b, a) = \{(q_0, ba)\}$

- $\delta(q_0, \epsilon, z_0) = \{(q_1, z_0)\}$

- Popping phase. ( $w^R$  part)

- $\delta(q_1, a, a) = \{(q_1, \epsilon)\}$

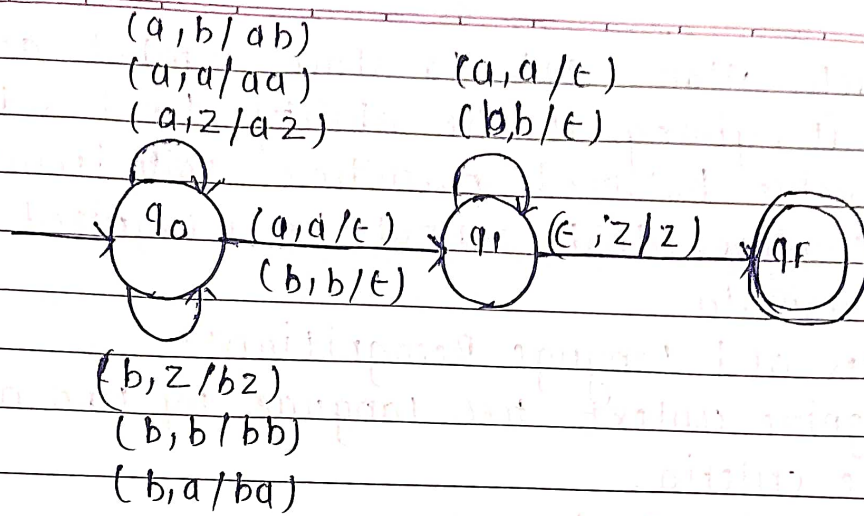
- $\delta(q_1, b, b) = \{(q_1, \epsilon)\}$

- $\delta(q_1, \epsilon, z_0) = \{(q_f, z_0)\}$

- Accepting state :-  $q_f$ .

- NPDA :-

$\epsilon$  - indicates pop operation.



∴ Required NPDA.

Q:2) Write a short note on recognition of language by PDA.

→ A Pushdown Automata (PDA) is a computational model used to recognize context-free language (CFL), which are generated by context-free grammar.

- PDA are an extension of finite automata equipped with an additional data structure: a stack which provides memory capability for storing symbols.
- This symbol enables PDAs to process nested and recursive patterns, making them suitable for recognising language that require more complex structure than regular language.

- Key Feature of PDA:-

A PDA is formally defined a 7-tuple  $M = (Q, \Sigma, \Gamma, \delta, q_0, z_0, F)$

where,  $Q$  is a set of states

$\Sigma$  is input symbol

$\Gamma$  is a stack alphabet

$\delta$  is a transition function

$q_0$  is the initial state

$z_0$  is the stack symbol

$F$  is the set of accepting state



The stack allows PDA to store symbol as it reads the input, giving it the ability to handle language that involve balanced parentheses, palindromes and nested structure which cannot be recognized by simpler finite automata.

### - PDA Types and Language Recognition:-

PDA recognize context free language by two main acceptance criteria.

#### 1. Acceptance by final state:-

The PDA accepts the input if, after reading the entire string, it reaches an accepting state  $F$ .

#### 2. Acceptance by Empty stack:-

The PDA accept the input if, after reading the entire string the stack is empty.

- A PDA is non-deterministic (NPDA) if it can choose bet<sup>n</sup> multiple transition at each step, which gives it more power than a deterministic PDA (DPDA). NPDA are equivalent in power to context-free grammar, meaning they can recognize all CFL's while DPDA cannot recognize all CFL's.

Q.3) Write and explain any 3 closure properties of CFL.

→ CFL have several closure properties, which means that applying certain operation on CFL result new language that is also context-free.

#### 1. Union:-

Property:- If  $L_1$  and  $L_2$  are CFL then  $L_1 \cup L_2$  is also CFL

Ex:-  $S_1 \rightarrow a S_1 b \mid \epsilon$

$S_2 \rightarrow b S_2 c \mid \epsilon$

Union :-  $S \rightarrow S_1 \mid S_2$

#### 2. Concatenation:-

Property:- if  $L_1$  and  $L_2$  are CFL, then  $L_1 L_2$  is also CFL.

### 3. Kleene Star:-

Property:- If  $L$  is a context-free language the  $L^*$  is also a CFL.