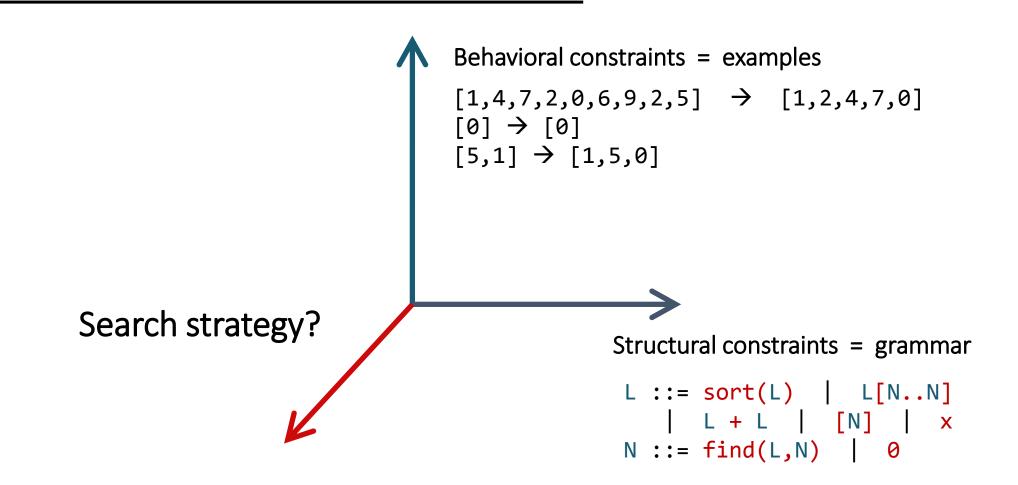
Lecture 3 Scaling Enumerative Search

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The problem statement



Enumerative search

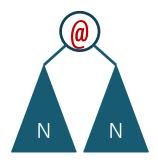
Explicit / Exhaustive Search

Idea: Generate programs from the grammar one by one and test them on the examples

How to make it scale

Prune

Discard useless subprograms





 $m * N^2$

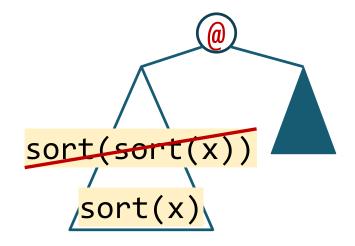
$$m * (N - 1)^2$$

Prioritize

Explore more promising candidates first

When can we discard a subprogram?

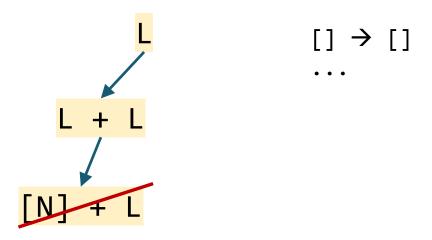
It's equivalent to something we have already explored



Equivalence reduction

(also: symmetry breaking)

No matter what we combine it with, it cannot satisfy the spec



Top-down propagation

Equivalent programs

```
X
                                                                                                                                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                                                                                                  \frac{1}{x} = \frac{x[0..0]}{x} + x = \frac{[0]}{x} = \frac{1}{x} = \frac{[0]}{x} = \frac{1}{x} = \frac{[0]}{x} = \frac{
 L ::= sort(L)
                                                     L[N..N]
                                                                                                                                                                                                                                                                                                              sort(sort(x)) sort(x + x) sort(x[0..0])
                                                                                                                                                                                             bottom_up
                                                      L + L
                                                                                                                                                                                                                                                                                                              sort([0]) \times [0..find(x,0)] \times [find(x,0)..0]
                                                       x[find(x,0)..find(x,0)] sort(x)[0..0]
N ::= find(L,N)
                                                                                                                                                                                                                                                                                                              x[0..0][0..0] (x + x)[0..0] [0][0..0]
                                                                                                                                                                                                                                                                                                              x + (x + x) x + [0] sort(x) + x x[0..0] + x
                                                                                                                                                                                                                                                                                                               (x + x) + x [0] + x x + x[0..0] x + sort(x)
```

Equivalent programs

```
0
                                                                                                                                                                                                                                               |x[0..0]| \times |x[0]| \times |x[0]| = |x| 
L ::= sort(L)
                                         L[N..N]
                                                                                                                                                                                                                                            sort(sort(x)) sort(x + x) sort(x[0..0])
                                                                                                                                                    bottom_up
                                          L + L
                                                                                                                                                                                                                                            sort([0]) \times [0..find(x,0)] \times [find(x,0)..0]
                                           \lceil N \rceil
                                                                                                                                                                                                                                             x[find(x,0)..find(x,0)] sort(x)[0..0]
N ::= find(L,N)
                                                                                                                                                                                                                                            x[0..0][0..0](x + x)[0..0][0][0..0]
                                                                                                                                                                                                                                             x + (x + x) x + [0] sort(x) + x x[0..0] + x
                                                                                                                                                                                                                                             (x + x) + x [0] + x x + x[0..0] x + sort(x)
```

Equivalent programs

```
0
                                 x[0..0] \times x = x [0] find(x,0)
L ::= sort(L)
     L[N..N]
                                               sort(x + x)
                     bottom_up
     L + L
      [N]
                                           x[0..find(x,0)]
N ::= find(L,N)
                                 x + (x + x) x + [0] sort(x) + x
                                                                 x + sort(x)
                                             [0] + x
```

Bottom-up + equivalence reduction

```
bottom-up (\langle T, N, R, S \rangle, [i \rightarrow o]) {
  P := [t | t in T && t is nullary]
  while (true)
    P += grow(P);
    P := reduce(P);
    forall (p in P)
      if (whole(p) \&\& p([i]) = [o])
         return p;
reduce(P) {
  P' := []
  forall (p in P)
    r := exists p' in P': equiv(p, p');
    if !r
      P' += p;
  return P';
```

How do we implement equiv?

- In general undecidable
- For SyGuS problems: expensive
- Doing expensive checks on every candidate defeats the purpose of pruning the space!

Observational equivalence

```
bottom-up (⟨T, N, R, S⟩, [i → o])
{ ... }

equiv(p, p') {
   return p([i]) = p'([i])
}

sort(x) x[0..0] x + x [0] find(x,0)
```

In PBE, all we care about is equivalence on the given inputs!

- easy to check efficiently
- even more programs are equivalent

```
sort(x + x)
x[0..find(x,0)]
```

$$x + (x + x) x + [0] sort(x) + x$$
 $[0] + x$
 $x + sort(x)$

Observational equivalence

$$x + (x + x) x + [0] sort(x) + x$$
 $[0] + x$
 $x + sort(x)$

Observational equivalence

```
bottom-up (\langle T, N, R, S \rangle, [i \rightarrow o])
                                                       \lceil [0] \rightarrow [0] \rceil
{ ... }
                                                             0
equiv(p, p') {
  return p([i]) = p'([i])
                                                                    x[0..0]
```

Used in almost all PBE tools:

ESolver [Udupa et al. '13]

Escher [Albarghouthi et al. '13]

Lens [Phothilimthana et al. '16]

EUSolver [Alur et al. '17]

$$x + (x + x)$$

User-specifies equivalences

[Smith, Albarghouthi: unpublished]

```
Equivalences
                                             Term-rewriting system (TRS)
                                derived
sort(sort(1)) = sort(1) automatically
                                              1. sort(sort(1)) \rightarrow sort(1)
(1 + 1) + 1 = 1 + (1 + 1)
                                              2. (1 + 1) + 1 \rightarrow 1 + (1 + 1)
                                              3. n + 0 \rightarrow n
n = n + 0
                                              4. n + m \rightarrow_{(n > m)} m + n
n + m = m + n
   x 0
    sort(x) x[0..0] x + x [0] find(x,0)
    sort(sort(x)) rule 1 applies, not normal
```

Built-in equivalences

For a predefined set of operations, equivalence reduction can be hard-coded in the tool or built into the grammar

```
L ::= sort(L)

L[N..N]

L + L

[N]

X

N ::= find(L,N)

0
```

Used by **Leon** [Kneuss et al.'13], λ^2 [Feser et al.'15], ...

Equivalence reduction: comparison

Observational

- Very general, no user input required
- Finds more equivalences
- Can be costly (especially with many examples)
- If new examples are added, has to restart the search

User-specified

• Fast: no need to call reduce

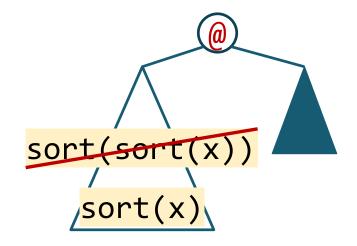
Built-in

- Even faster
- Restricted to built-in operators
- Only certain symmetries can be eliminated by modifying the grammar

Can any of them apply to top-down?

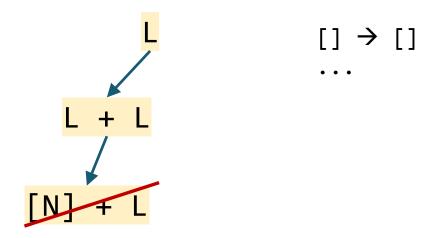
When can we discard a subprogram?

It's equivalent to something we have already explored



Equivalence reduction

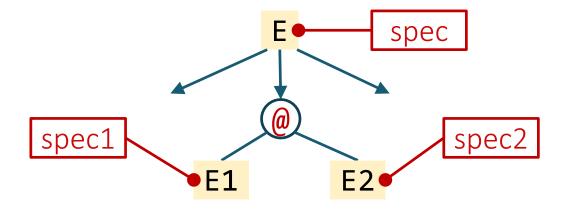
No matter what we combine it with, it cannot fit the spec



Top-down propagation

Top-down propagation

Idea: once we pick the production, infer specs for subprograms

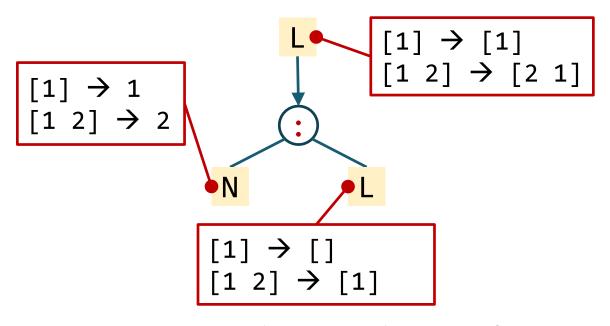


If $spec1 = \bot$, discard E1 @ E2 altogether!

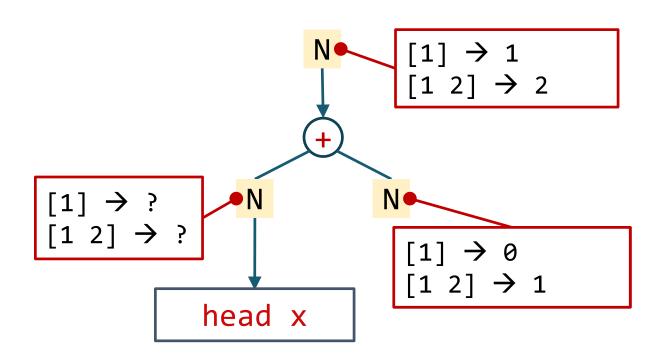
For now: spec = examples

When is TDP possible?

Depends on @!



Q: when would we infer 1.2.
Great for injective functions

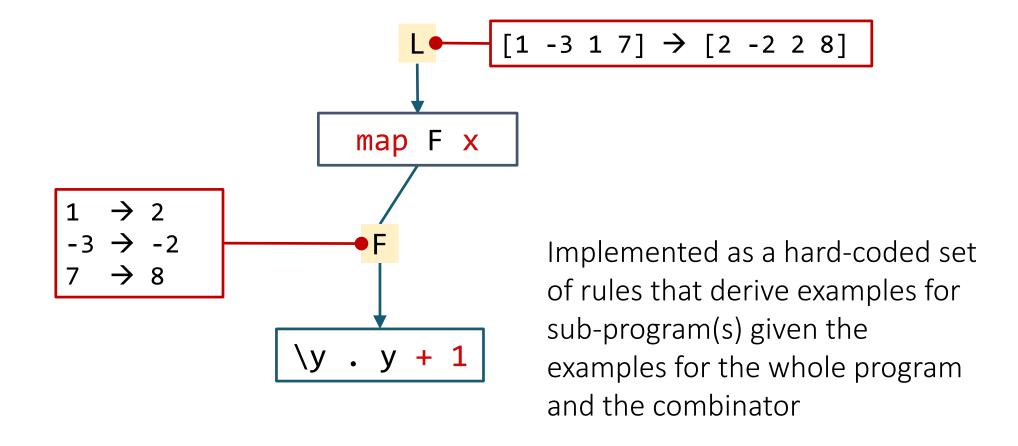


λ^2 : TDP for list combinators

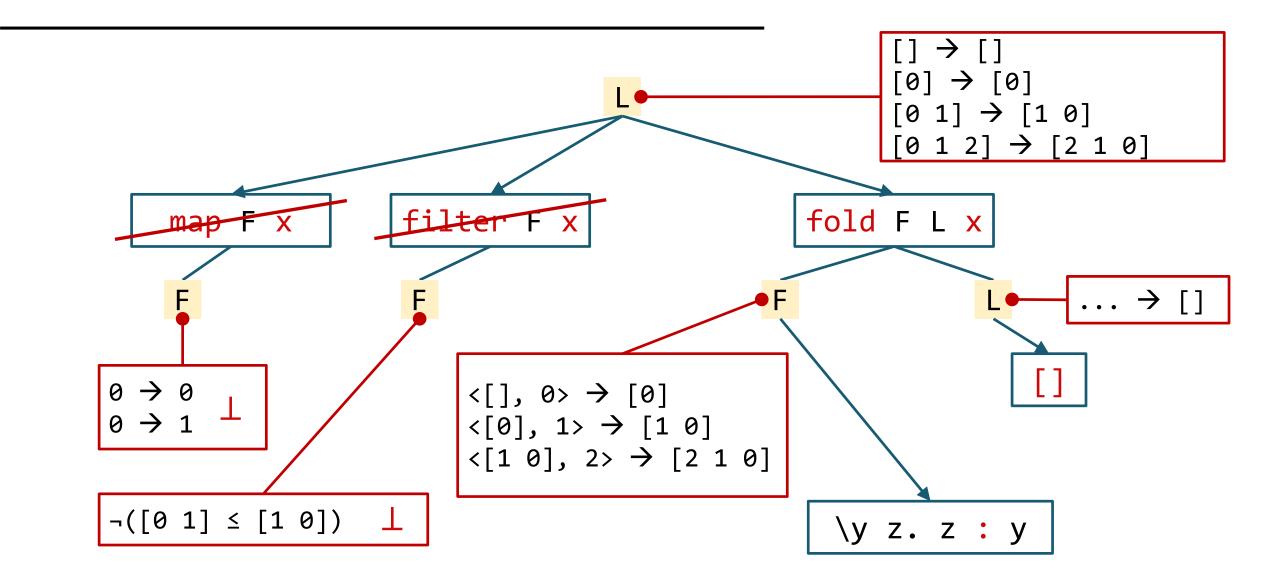
[Feser, Chaudhuri, Dillig '15]

```
map f x
                     map (\y . y + 1) [1, -3, 1, 7] \rightarrow [2, -2, 2, 8]
filter f x
                     filter (\y . y > 0) [1, -3, 1, 7] \rightarrow [1, 1, 7]
fold f acc x fold (\y z . y + z) 0 [1, -3, 1, 7] \rightarrow 6
                      fold (\y z . y + z) \emptyset [] \rightarrow \emptyset
```

λ^2 : TDP for list combinators



λ²: TDP for list combinators



Condition abduction

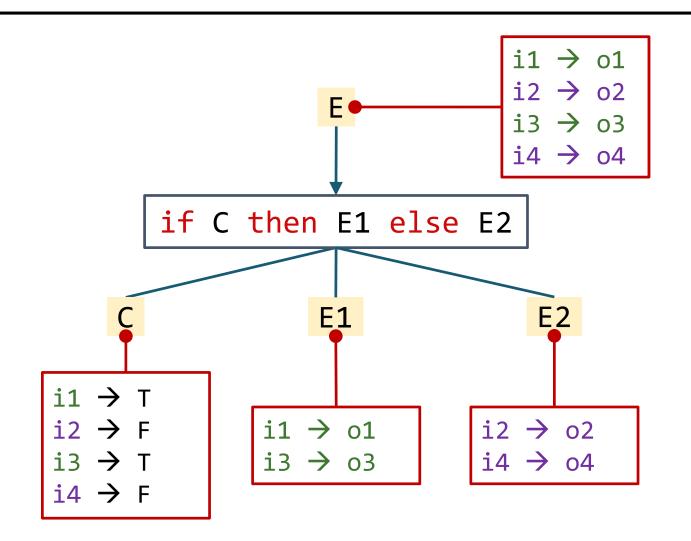
Smart way to synthesize conditionals

Used in many tools (under different names):

- FlashFill [Gulwani '11]
- Escher [Albarghouthi et al. '13]
- Leon [Kneuss et al. '13]
- Synquid [Polikarpova et al. '13]
- EUSolver [Alur et al. '17]

In fact, an instance of TDP!

Condition abduction



Q: How does EUSolver decide how to split the inputs?

Q: How does EUSolver generate C?

EUSover

Q1: What does EUSolver use as behavioral constraints? Structural constraint? Search strategy?

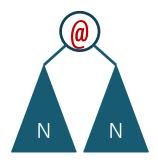
Q2: What are the main two pruning/decomposition techniques EUSolver uses to speed up the search? What enables these technique?

Q3: What would be a naive alternative to decision tree learning for synthesizing branch conditions? What are the disadvantages of this alternative?

How to make it scale

Prune

Discard useless subprograms





 $m * N^2$

$$m * (N - 1)^2$$

Prioritize

Explore more promising candidates first

Next week

Topics:

- Prioritization and Stochastic Search
- Representation-Based Synthesis

Paper: Gulwani: <u>Automating string processing in spreadsheets</u> using input-output examples

- Review due Wednesday
- Link to PDF on the course wiki
- Submit through EasyChair

Project: come talk to me about the topic!

Monday 4-5pm