Hierarchical Imitation and Reinforcement Learning

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Abstract

We study how to effectively leverage expert feedback to learn sequential decision-making policies. We focus on problems with sparse rewards and long time horizons, which typically pose significant challenges in reinforcement learning. We propose an algorithmic framework, called hierarchical guidance, that leverages the hierarchical structure of the underlying problem to integrate different modes of expert interaction. Our framework can incorporate different combinations of imitation learning (IL) and reinforcement learning (RL) at different levels, leading to dramatic reductions in both expert effort and cost of exploration. Using long-horizon benchmarks, including Montezuma's Revenge, we demonstrate that our approach can learn significantly faster than hierarchical RL, and be significantly more label-efficient than standard IL. We also theoretically analyze labeling cost for certain instantiations of our framework.

1. Introduction

Learning good agent behavior from reward signals alone—the goal of reinforcement learning (RL)—is particularly difficult when the planning horizon is long and rewards are sparse. One successful method for dealing with such long horizons is imitation learning (IL) (Abbeel & Ng, 2004; Daumé et al., 2009; Ross et al., 2011; Ho & Ermon, 2016), in which the agent learns by watching and possibly querying an expert. One limitation of existing imitation learning approaches is that they may require a large amount of demonstration data in long-horizon problems.

The central question we address in this paper is: when experts are available, how can we most effectively leverage their feedback? A common strategy to improve sample ef-

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ficiency in RL over long time horizons is to exploit hierarchical structure of the problem (Sutton et al., 1998; 1999; Kulkarni et al., 2016; Dayan & Hinton, 1993; Vezhnevets et al., 2017; Dietterich, 2000). Our approach leverages hierarchical structure in imitation learning. We study the case where the underlying problem is hierarchical, and subtasks can be easily elicited from an expert. Our key design principle is an algorithmic framework called hierarchical guidance, in which feedback (labels) from the high-level expert is used to focus (guide) the low-level learner. The high-level expert ensures that low-level learning only occurs when necessary (when subtasks have not been mastered) and only over relevant parts of the state space. This differs from a naïve hierarchical approach which merely gives a subtask decomposition. Focusing on relevant parts of the state space speeds up learning (improves sample efficiency), while omitting feedback on the already mastered subtasks reduces expert effort (improves label efficiency).

We begin by formalizing the problem of hierarchical imitation learning (Section 3) and carefully separate out cost structures that naturally arise when the expert provides feedback at multiple levels of abstraction. We first apply hierarchical guidance to IL, derive hierarchically guided variants of behavior cloning and DAgger (Ross et al., 2011), and theoretically analyze the benefits (Section 4). We next apply hierarchical guidance to the hybrid setting with highlevel IL and low-level RL (Section 5). This architecture is particularly suitable in settings where we have access to high-level semantic knowledge, the subtask horizon is sufficiently short, but the low-level expert is too costly or unavailable. We demonstrate the efficacy of our approaches on a simple but extremely challenging maze domain, and on Montezuma's Revenge (Section 6). Our experiments show that incorporating a modest amount of expert feedback can lead to dramatic improvements in performance compared to pure hierarchical RL.¹

2. Related Work

For brevity, we provide here a short overview of related work, and defer to Appendix C for additional discussion.

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¹Code and experimental setups are available at https://sites.google.com/view/hierarchical-il-rl

Imitation Learning. One can broadly dichotomize IL into passive collection of demonstrations (behavioral cloning) versus active collection of demonstrations. The former setting (Abbeel & Ng, 2004; Ziebart et al., 2008; Syed & Schapire, 2008; Ho & Ermon, 2016) assumes that demonstrations are collected a priori and the goal of IL is to find a policy that mimics the demonstrations. The latter setting (Daumé et al., 2009; Ross et al., 2011; Ross & Bagnell, 2014; Chang et al., 2015; Sun et al., 2017) assumes an interactive expert that provides demonstrations in response to actions taken by the current policy. We explore extension of both approaches into hierarchical settings.

Hierarchical Reinforcement Learning. Several RL approaches to learning hierarchical policies have been explored, foremost among them the options framework (Sutton et al., 1998; 1999; Fruit & Lazaric, 2017). It is often assumed that a useful set of options are fully defined a priori, and (semi-Markov) planning and learning only occurs at the higher level. In comparison, our agent does not have direct access to policies that accomplish such subgoals and has to learn them via expert or reinforcement feedback. The closest hierarchical RL work to ours is that of Kulkarni et al. (2016), which uses a similar hierarchical structure, but no high-level expert and hence no hierarchical guidance.

Combining Reinforcement and Imitation Learning. The idea of combining IL and RL is not new (Nair et al., 2017; Hester et al., 2018). However, previous work focuses on flat policy classes that use IL as a "pre-training" step (e.g., by pre-populating the replay buffer with demonstrations). In contrast, we consider feedback at multiple levels for a hierarchical policy class, with different levels potentially receiving different types of feedback (i.e., imitation at one level and reinforcement at the other). Somewhat related to our hierarchical expert supervision is the approach of Andreas et al. (2017), which assumes access to symbolic descriptions of subgoals, without knowing what those symbols mean or how to execute them. Previous literature has not focused much on comparisons of sample complexity between IL and RL, with the exception of the recent work of Sun et al. (2017).

3. Hierarchical Formalism

For simplicity, we consider environments with a natural two-level hierarchy; the HI level corresponds to choosing subtasks, and the LO level corresponds to executing those subtasks. For instance, an agent's overall goal may be to leave a building. At the HI level, the agent may first choose the subtask "go to the elevator," then "take the elevator down," and finally "walk out." Each of these subtasks needs to be executed at the LO level by actually navigat-

ing the environment, pressing buttons on the elevator, etc.²

Subtasks, which we also call *subgoals*, are denoted as $g \in \mathcal{G}$, and the primitive actions are denoted as $a \in \mathcal{A}$. An agent (also referred to as learner) acts by iteratively choosing a subgoal g, carrying it out by executing a sequence of actions a until completion, and then picking a new subgoal. The agent's choices can depend on an observed state $s \in \mathcal{S}$. We assume that the horizon at the HI level is $H_{\rm HI}$, i.e., a trajectory uses at most $H_{\rm HI}$ subgoals, and the horizon at the LO level is $H_{\rm LO}$, i.e., after at most $H_{\rm LO}$ primitive actions, the agent either accomplishes the subgoal or needs to decide on a new subgoal. The total number of primitive actions in a trajectory is thus at most $H_{\rm FULL} := H_{\rm HI} H_{\rm LO}$.

The hierarchical learning problem is to simultaneously learn a HI-level policy $\mu: \mathcal{S} \to \mathcal{G}$, called the *meta-controller*, as well as the subgoal policies $\pi_g: \mathcal{S} \to \mathcal{A}$ for each $g \in \mathcal{G}$, called *subpolicies*. The aim of the learner is to achieve a high reward when its meta-controller and subpolicies are run together. For each subgoal g, we also have a (possibly learned) termination function $\beta_g: \mathcal{S} \to \{True, False\}$, which terminates the execution of π_g . The hierarchical agent behaves as follows:

```
1: for h_{\rm HI}=1\dots H_{\rm HI} do

2: observe state s and choose subgoal g\leftarrow \mu(s)

3: for h_{\rm LO}=1\dots H_{\rm LO} do

4: observe state s

5: if \beta_g(s) then break

6: choose action a\leftarrow \pi_g(s)
```

The execution of each subpolicy π_g generates a LO-level trajectory $\tau=(s_1,a_1,\ldots,s_H,a_H,s_{H+1})$ with $H\leq H_{\text{LO}}$. The overall behavior results in a hierarchical trajectory $\sigma=(s_1,g_1,\tau_1,s_2,g_2,\tau_2,\ldots)$, where the last state of each LO-level trajectory τ_h coincides with the next state s_{h+1} in σ and the first state of the next LO-level trajectory τ_{h+1} . The subsequence of σ which excludes the LO-level trajectories τ_h is called the HI-level trajectory, $\tau_{\text{HI}}:=(s_1,g_1,s_2,g_2,\ldots)$. Finally, the full trajectory, τ_{FULL} , is the concatenation of all the LO-level trajectories.

We assume access to an expert, endowed with a meta-

²An important real-world application is in goal-oriented dialogue systems. For instance, a chatbot assisting a user with reservation and booking for flights and hotels (Peng et al., 2017; El Asri et al., 2017) needs to navigate through multiple turns of conversation. The chatbot developer designs the hierarchy of subtasks, such as *ask_user_goal*, *ask_dates*, *offer_flights*, *confirm*, etc. Each subtask consists of several turns of conversation. Typically a global state tracker exists alongside the hierarchical dialogue policy to ensure that cross-subtask constraints are satisfied.

³While we use the term state for simplicity, we do not require the environment to be fully observable or Markovian.

⁴The trajectory might optionally include a reward signal after each primitive action, which might either come from the environment, or be a pseudo-reward as we will see in Section 5.

controller μ^* , subpolicies π_g^* , and termination functions β_g^* , who can provide one or several types of supervision:

- HierDemo(s): hierarchical demonstration. The expert executes its hierarchical policy starting from s and returns the resulting hierarchical trajectory $\sigma^* = (s_1^*, g_1^*, \tau_1^*, s_2^*, g_2^*, \tau_2^*, \dots)$, where $s_1^* = s$.
- Label_{HI}($\tau_{\rm HI}$): HI-level labeling. The expert provides a good next subgoal at each state of a given HI-level trajectory $\tau_{\rm HI}=(s_1,g_1,s_2,g_2,\ldots)$, yielding a labeled data set $\{(s_1,g_1^{\star}),(s_2,g_2^{\star}),\ldots\}$.
- Label_{LO}($\tau;g$): LO-level labeling. The expert provides a good next primitive action towards a given subgoal g at each state of a given LO-level trajectory $\tau = (s_1, a_1, s_2, a_2, \ldots)$, yielding a labeled data set $\{(s_1, a_1^*), (s_2, a_2^*), \ldots\}$.
- Inspect_{LO}(τ ; g): LO-level inspection. Instead of annotating every state of a trajectory with a good action, the expert only verifies whether a subgoal g was accomplished, returning either *Pass* or *Fail*.
- Label_{FULL}(τ_{FULL}): full labeling. The expert labels the agent's full trajectory $\tau_{\text{FULL}} = (s_1, a_1, s_2, a_2, \dots)$, from start to finish, ignoring hierarchical structure, yielding a labeled data set $\{(s_1, a_1^*), (s_2, a_2^*), \dots\}$.
- Inspect_{FULL}(τ_{FULL}): *full inspection*. The expert verifies whether the agent's overall goal was accomplished, returning either *Pass* or *Fail*.

When the agent learns not only the subpolicies π_g , but also termination functions β_g , then Labello also returns good termination values $\omega^* \in \{\mathit{True}, \mathit{False}\}\$ for each state of $\tau = (s_1, a_1, \ldots)$, yielding a data set $\{(s_1, a_1^*, a_1^*), \ldots\}$.

Although HierDemo and Label can be both generated by the expert's hierarchical policy $(\mu^*, \{\pi_g^*\})$, they differ in the mode of expert interaction. HierDemo returns a hierarchical trajectory *executed by the expert*, as required for passive IL, and enables a hierarchical version of behavioral cloning (Abbeel & Ng, 2004; Syed & Schapire, 2008). Label operations provide labels *with respect to the learning agent's trajectories*, as required for interactive IL. Label_{FULL} is the standard query used in prior work on learning flat policies (Daumé et al., 2009; Ross et al., 2011), and Label_{HI} and Label_{LO} are its hierarchical extensions.

Inspect operations are newly introduced in this paper, and form a cornerstone of our interactive hierarchical guidance protocol that enables substantial savings in label efficiency. They can be viewed as "lazy" versions of the corresponding Label operations, requiring less effort. Our underlying assumption is that if the given hierarchical trajectory $\sigma = \{(s_h, g_h, \tau_h)\}$ agrees with the expert on HI level, i.e., $g_h = \mu^*(s_h)$, and LO-level trajectories pass the

Algorithm 1 Hierarchical Behavioral Cloning (h-BC)

```
1: Initialize data buffers \mathcal{D}_{\mathrm{HI}} \leftarrow \emptyset and \mathcal{D}_{g} \leftarrow \emptyset, g \in \mathcal{G}
2: for t = 1, \ldots, T do
3: Get a new environment instance with start state s
4: \sigma^{\star} \leftarrow \mathrm{HierDemo}(s)
5: for all (s_{h}^{\star}, g_{h}^{\star}, \tau_{h}^{\star}) \in \sigma^{\star} do
6: Append \mathcal{D}_{g_{h}^{\star}} \leftarrow \mathcal{D}_{g_{h}^{\star}} \cup \tau_{h}^{\star}
7: Append \mathcal{D}_{\mathrm{HI}} \leftarrow \mathcal{D}_{\mathrm{HI}} \cup \{(s_{h}^{\star}, g_{h}^{\star})\}
8: Train subpolicies \pi_{g} \leftarrow \mathrm{Train}(\pi_{g}, \mathcal{D}_{g}) for all g
9: Train meta-controller \mu \leftarrow \mathrm{Train}(\mu, \mathcal{D}_{\mathrm{HI}})
```

inspection, i.e., $\mathtt{Inspect}_{\mathtt{LO}}(\tau_h;g_h) = \mathit{Pass}$, then the resulting full trajectory must also pass the full inspection, $\mathtt{Inspect}_{\mathtt{FULL}}(\tau_{\mathtt{FULL}}) = \mathit{Pass}$. This means that a hierarchical policy need not always agree with the expert's execution at LO level to succeed in the overall task.

Besides algorithmic reasons, the motivation for separating the types of feedback is that different expert queries will typically require different amount of effort, which we refer to as cost. We assume the costs of the Label operations are $C_{\rm HI}^L$, $C_{\rm LO}^L$ and $C_{\rm FULL}^L$, the costs of each Inspect operation are $C_{\rm LO}^I$ and $C_{\rm LO}^I$. In many settings, LO-level inspection will require significantly less effort than LO-level labeling, i.e., $C_{\rm LO}^I \ll C_{\rm LO}^L$. For instance, identifying if a robot has successfully navigated to the elevator is presumably much easier than labeling an entire path to the elevator. One reasonable cost model, natural for the environments in our experiments, is to assume that Inspect operations take time O(1) and work by checking the final state of the trajectory, whereas Label operations take time proportional to the trajectory length, which is $O(H_{\rm HI})$, $O(H_{\rm LO})$ and $O(H_{\rm HI})$, for our three Label operations.

4. Hierarchically Guided Imitation Learning

Hierarchical guidance is an algorithmic design principle in which the feedback from high-level expert guides the low-level learner in two different ways: (i) the high-level expert ensures that low-level expert is only queried when necessary (when the subtasks have not been mastered yet), and (ii) low-level learning is limited to the relevant parts of the state space. We instantiate this framework first within passive learning from demonstrations, obtaining hierarchical behavioral cloning (Algorithm 1), and then within interactive imitation learning, obtaining hierarchically guided DAgger (Algorithm 2), our best-performing algorithm.

4.1. Hierarchical Behavioral Cloning (h-BC)

We consider a natural extension of behavioral cloning to the hierarchical setting (Algorithm 1). The expert provides a set of hierarchical demonstrations σ^\star , each consisting of LO-level trajectories $\tau_h^\star = \{(s_\ell^\star, a_\ell^\star)\}_{\ell=1}^{H_{\mathrm{HI}}}$ as well as a HI-level trajectory $\tau_{\mathrm{HI}}^\star = \{(s_h^\star, g_h^\star)\}_{h=1}^{H_{\mathrm{HI}}}$. We then run

Algorithm 2 Hierarchically Guided DAgger (hg-DAgger)

```
1: Initialize data buffers \mathcal{D}_{HI} \leftarrow \emptyset and \mathcal{D}_q \leftarrow \emptyset, g \in \mathcal{G}
 2: Run Hierarchical Behavioral Cloning (Algorithm 1)
          up to t = T_{\text{warm-start}}
 3: for t = T_{\text{warm-start}} + 1, \dots, T do
 4:
          Get a new environment instance with start state s
 5:
          Initialize \sigma \leftarrow \emptyset
 6:
          repeat
 7:
              g \leftarrow \mu(s)
              Execute \pi_g, obtain LO-level trajectory \tau
 8:
 9:
              Append (s, g, \tau) to \sigma
10:
               s \leftarrow the last state in \tau
          until end of episode
11:
12:
          Extract 	au_{\text{FULL}} and 	au_{\text{HI}} from \sigma
13:
          if Inspect_{FULL}(	au_{FULL}) = Fail then
14:
               \mathcal{D}^{\star} \leftarrow \texttt{Label}_{HI}(\tau_{HI})
              Process (s_h, g_h, \tau_h) \in \sigma in sequence as long as
15:
              g_h agrees with the expert's choice g_h^{\star} in \mathcal{D}^{\star}:
16:
                  if Inspect(	au_h;g_h)=\mathit{Fail} then
                      Append \mathcal{D}_{g_h} \leftarrow \mathcal{D}_{g_h} \cup \texttt{Label}_{\texttt{LO}}(	au_h; g_h)
17:
18:
19:
               Append \mathcal{D}_{HI} \leftarrow \mathcal{D}_{HI} \cup \mathcal{D}^*
           Update subpolicies \pi_g \leftarrow \text{Train}(\pi_g, \mathcal{D}_g) for all g
20:
21:
          Update meta-controller \mu \leftarrow \text{Train}(\mu, \mathcal{D}_{\text{HI}})
```

Train (lines 8–9) to find the subpolicies π_g that best predict a_ℓ^\star from s_ℓ^\star , and meta-controller μ that best predicts g_h^\star from s_h^\star , respectively. Train can generally be any supervised learning subroutine, such as stochastic optimization for neural networks or some batch training procedure. When termination functions β_g need to be learned as part of the hierarchical policy, the labels ω_g^\star will be provided by the expert as part of $\tau_h^\star = \{(s_\ell^\star, a_\ell^\star, \omega_\ell^\star)\}$. In this setting, hierarchical guidance is automatic, because subpolicy demonstrations only occur in relevant parts of the state space.

4.2. Hierarchically Guided DAgger (hg-DAgger)

Passive IL, e.g., behavioral cloning, suffers from the distribution mismatch between the learning and execution distributions. This mismatch is addressed by interactive IL algorithms, such as SEARN (Daumé et al., 2009) and DAgger (Ross et al., 2011), where the expert provides correct actions along the learner's trajectories through the operation \mathtt{Label}_{FULL} . A naïve hierarchical implementation would provide correct labels along the entire hierarchical trajectory via \mathtt{Label}_{HI} and \mathtt{Label}_{LO} . We next show how to use hierarchical guidance to decrease LO-level expert costs.

We leverage two HI-level query types: ${\tt Inspect_{LO}}$ and ${\tt Label_{HI}}$. We use ${\tt Inspect_{LO}}$ to verify whether the subtasks are successfully completed and ${\tt Label_{HI}}$ to check whether we are staying in the relevant part of the state space. The details are presented in Algorithm 2, which uses

DAgger as the learner on both levels, but the scheme can be adapted to other interactive imitation learners.

In each episode, the learner executes the hierarchical policy, including choosing a subgoal (line 7), executing the LO-level trajectories, i.e., rolling out the subpolicy π_q for the chosen subgoal, and terminating the execution according to β_q (line 8). Expert only provides feedback when the agent fails to execute the entire task, as verified by Inspect_{FULL} (line 13). When Inspect_{FULL} fails, the expert first labels the correct subgoals via Label_{HI} (line 14), and only performs LO-level labeling as long as the learner's meta-controller chooses the correct subgoal g_h (line 15), but its subpolicy fails (i.e., when Inspect₁₀ on line 16 fails). Since all the preceding subgoals were chosen and executed correctly, and the current subgoal is also correct, LO-level learning is in the "relevant" part of the state space. However, since the subpolicy execution failed, its learning has not been mastered yet. We next analyze the savings in expert cost that result from hierarchical guidance.

Theoretical Analysis. We analyze the cost of hg-DAgger in comparison with flat DAgger under somewhat stylized assumptions. We assume that the learner aims to learn the meta-controller μ from some policy class \mathcal{M} , and subpolicies π_g from some class Π_{LO} . The classes \mathcal{M} and Π_{LO} are finite (but possibly exponentially large) and the task is realizable, i.e., the expert's policies can be found in the corresponding classes: $\mu^* \in \mathcal{M}$, and $\pi_g^* \in \Pi_{\text{LO}}$, $g \in \mathcal{G}$. This allows us to use the *halving algorithm* (Shalev-Shwartz et al., 2012) as the online learner on both levels. (The implementation of our algorithm does not require these assumptions.)

The halving algorithm maintains a version space over policies, acts by a majority decision, and when it makes a mistake, it removes all the erring policies from the version space. In the hierarchical setting, it therefore makes at most $\log |\mathcal{M}|$ mistakes on the HI level, and at most $\log |\Pi_{LO}|$ mistakes when learning each π_g . The mistake bounds can be further used to upper bound the total expert cost in both hg-DAgger and flat DAgger. To enable an apples-to-apples comparison, we assume that the flat DAgger learns over the policy class $\Pi_{\text{FULL}} = \{ (\mu, \{\pi_q\}_{q \in \mathcal{G}}) : \mu \in \mathcal{M}, \pi_q \in \Pi_{\text{LO}} \},$ but is otherwise oblivious to the hierarchical task structure. The bounds depend on the cost of performing different types of operations, as defined at the end of Section 3. We consider a modified version of flat DAgger that first calls Inspect_{FULL}, and only requests labels (Label_{FULL}) if the inspection fails. The proofs are deferred to Appendix A.

Theorem 1. Given finite classes \mathcal{M} and Π_{LO} and realizable expert policies, the total cost incurred by the expert in hg-DAgger by round T is bounded by

$$TC_{\text{FULL}}^{I} + \left(\log_{2}|\mathcal{M}| + |\mathcal{G}_{opt}|\log_{2}|\Pi_{\text{LO}}|\right)\left(C_{\text{HI}}^{L} + H_{\text{HI}}C_{\text{LO}}^{I}\right) + \left(|\mathcal{G}_{opt}|\log_{2}|\Pi_{\text{LO}}|\right)C_{\text{LO}}^{L}, \tag{1}$$

⁵In our hierarchical imitation learning experiments, the termination functions are all learned. Formally, the termination signal ω_g , can be viewed as part of an augmented action at LO level.

where $\mathcal{G}_{opt} \subseteq \mathcal{G}$ is the set of the subgoals actually used by the expert, $\mathcal{G}_{opt} := \mu^*(\mathcal{S})$.

Theorem 2. Given the full policy class $\Pi_{\text{FULL}} = \{(\mu, \{\pi_g\}_{g \in \mathcal{G}}) : \mu \in \mathcal{M}, \pi_g \in \Pi_{\text{LO}}\}$ and a realizable expert policy, the total cost incurred by the expert in flat DAgger by round T is bounded by

$$TC_{\text{FULL}}^{I} + \left(\log_2 |\mathcal{M}| + |\mathcal{G}| \log_2 |\Pi_{\text{LO}}|\right) C_{\text{FULL}}^{L}.$$
 (2)

Both bounds have the same leading term, $TC^{I}_{\rm FULL}$, the cost of full inspection, which is incurred every round and can be viewed as the "cost of monitoring." In contrast, the remaining terms can be viewed as the "cost of learning" in the two settings, and include terms coming from their respective mistake bounds. The ratio of the cost of hierarchically guided learning to the flat learning is then bounded as

$$\frac{\text{Eq. (1)} - TC_{\text{FULL}}^{I}}{\text{Eq. (2)} - TC_{\text{FULL}}^{I}} \le \frac{C_{\text{HI}}^{L} + H_{\text{HI}}C_{\text{LO}}^{I} + C_{\text{LO}}^{L}}{C_{\text{FULL}}^{L}}, \quad (3)$$

where we applied the upper bound $|\mathcal{G}_{\mathrm{opt}}| \leq |\mathcal{G}|$. The savings thanks to hierarchical guidance depend on the specific costs. Typically, we expect the inspection costs to be O(1), if it suffices to check the final state, whereas labeling costs scale linearly with the length of the trajectory. The cost ratio is then $\propto \frac{H_{\mathrm{HI}} + H_{\mathrm{LO}}}{H_{\mathrm{HI}} H_{\mathrm{LO}}}$. Thus, we realize most significant savings if the horizons on each individual level are substantially shorter than the overall horizon. In particular, if $H_{\mathrm{HI}} = H_{\mathrm{LO}} = \sqrt{H_{\mathrm{FULL}}}$, the hierarchically guided approach reduces the overall labeling cost by a factor of $\sqrt{H_{\mathrm{FULL}}}$. More generally, whenever H_{FULL} is large, we reduce the costs of learning be at least a constant factor—a significant gain if this is a saving in the effort of a domain expert.

5. Hierarchically Guided IL/RL

Hierarchical guidance also applies in the hybrid setting with interactive IL on the HI level and RL on the LO level. The HI-level expert provides the hierarchical decomposition, including the pseudo-reward function for each subgoal, and is also able to pick a correct subgoal at each step. Similar to hg-DAgger, the labels from HI-level expert are used not only to train the meta-controller μ , but also to limit the LO-level learning to the relevant part of the state space. In Algorithm 3 we provide the details, with DAgger on HI level and Q-learning on LO level. The scheme can be adapted to other interactive IL and RL algorithms.

The learning agent proceeds by *rolling in* with its meta-controller (line 7). For each selected subgoal g, the subpolicy π_g selects and executes primitive actions via the

Algorithm 3 Hierarchically Guided DAgger/Q-learning (hg-DAgger/Q)

```
input Function pseudo(s; q) providing the pseudo-reward
input Predicate terminal(s; g) indicating the termination of g
input Annealed exploration probabilities \epsilon_g > 0, g \in \mathcal{G}
 1: Initialize data buffers \mathcal{D}_{\text{HI}} \leftarrow \emptyset and \mathcal{D}_g \leftarrow \emptyset, g \in \mathcal{G}
 2: Initialize subgoal Q-functions Q_g, g \in \mathcal{G}
 3: for t = 1, ..., T do
          Get a new environment instance with start state s
 5:
          Initialize \sigma \leftarrow \emptyset
 6:
          repeat
              s_{\text{HI}} \leftarrow s, \ g \leftarrow \mu(s) and initialize \tau \leftarrow \emptyset
 7:
 8:
 9:
                  a \leftarrow \epsilon_q-greedy(Q_q, s)
10:
                   Execute a, next state \tilde{s}, \tilde{r} \leftarrow \text{pseudo}(\tilde{s}; g)
11:
                   Update Q_g: a (stochastic) gradient descent step
                                      on a minibatch from \mathcal{D}_q
12:
                   Append (s, a, \tilde{r}, \tilde{s}) to \tau and update s \leftarrow \tilde{s}
               until terminal (s; g)
13:
14:
               Append (s_{\rm HI}, g, \tau) to \sigma
15:
           until end of episode
16:
           Extract 	au_{	ext{FULL}} and 	au_{	ext{HI}} from \sigma
17:
           if Inspect<sub>FULL</sub>(\tau_{\text{FULL}}) = Fail then
               \mathcal{D}^{\star} \leftarrow \texttt{Label}_{HI}(	au_{HI})
18:
19:
               Process (s_h, g_h, \tau_h) \in \sigma in sequence as long as
               g_h agrees with the expert's choice g_h^{\star} in \mathcal{D}^{\star}:
              Append \mathcal{D}_{g_h} \leftarrow \mathcal{D}_{g_h} \cup \tau_h
Append \mathcal{D}_{\text{HI}} \leftarrow \mathcal{D}_{\text{HI}} \cup \mathcal{D}^{\star}
20:
21:
               Append \mathcal{D}_{g_h} \leftarrow \mathcal{D}_{g_h} \cup \tau_h for all (s_h, g_h, \tau_h) \in \sigma
22:
23:
           Update meta-controller \mu \leftarrow \text{Train}(\mu, \mathcal{D}_{\text{HI}})
```

 ϵ -greedy rule (lines 9–10), until some termination condition is met. The agent receives some pseudo-reward, also known as intrinsic reward (Kulkarni et al., 2016) (line 10). Upon termination of the subgoal, agent's meta-controller μ chooses another subgoal and the process continues until the end of the episode, where the involvement of the expert begins. As in hg-DAgger, the expert inspects the overall execution of the learner (line 17), and if it is not successful, the expert provides HI-level labels, which are accumulated for training the meta-controller.

Hierarchical guidance impacts how the LO-level learners accumulate experience. As long as the meta-controller's subgoal g agrees with the expert's, the agent's experience of executing subgoal g is added to the experience replay buffer \mathcal{D}_g . If the meta-controller selects a "bad" subgoal, the accumulation of experience in the current episode is terminated. This ensures that experience buffers contain only the data from the relevant part of the state space.

Algorithm 3 assumes access to a real-valued function pseudo(s;g), providing the pseudo-reward in state s when executing g, and a predicate terminal(s;g), indicating the termination (not necessarily successful) of subgoal g. This setup is similar to prior work on hierarchical RL (Kulkarni et al., 2016). One natural defini-

⁶This is consistent with many hierarchical RL approaches, including options (Sutton et al., 1999), MAXQ (Dietterich, 2000), UVFA (Schaul et al., 2015a) and h-DQN (Kulkarni et al., 2016).

tion of pseudo-rewards, based on an additional predicate success(s;g) indicating a successful completion of subgoal g, is as follows:

```
\begin{cases} 1 & \text{if } \verb+success+(s;g) \\ -1 & \text{if } \neg \verb+success+(s;g) \text{ and } \verb+terminal+(s;g) \\ -\kappa & \text{otherwise}, \end{cases}
```

where $\kappa>0$ is a small penalty to encourage short trajectories. The predicates success and terminal are provided by an expert or learnt from supervised or reinforcement feedback. In our experiments, we explicitly provide these predicates to both hg-DAgger/Q as well as the hierarchical RL, giving them advantage over hg-DAgger, which needs to learn when to terminate subpolicies.

6. Experiments

We evaluate the performance of our algorithms on two separate domains: (i) a simple but challenging maze navigation domain and (ii) the Atari game Montezuma's Revenge.

6.1. Maze Navigation Domain

Task Overview. Figure 1 (left) displays a snapshot of the maze navigation domain. In each episode, the agent encounters a new instance of the maze from a large collection of different layouts. Each maze consists of 16 rooms arranged in a 4-by-4 grid, but the openings between the rooms vary from instance to instance as does the initial position of the agent and the target. The agent (white dot) needs to navigate from one corner of the maze to the target marked in yellow. Red cells are obstacles (lava), which the agent needs to avoid for survival. The contextual information the agent receives is the pixel representation of a bird's-eye view of the environment, including the partial trail (marked in green) indicating the visited locations.

Due to a large number of random environment instances, this domain is not solvable with tabular algorithms. Note that rooms are not always connected, and the locations of the hallways are not always in the middle of the wall. Primitive actions include going one step up, down, left or right. In addition, each instance of the environment is designed to ensure that there is a path from initial location to target, and the shortest path takes at least 45 steps ($H_{\rm FULL}=100$). The agent is penalized with reward -1 if it runs into lava, which also terminates the episode. The agent only receives positive reward upon stepping on the yellow block.

A hierarchical decomposition of the environment corresponds to four possible subgoals of going to the room immediately to the *north*, *south*, *west*, *east*, and the fifth possible subgoal *go_to_target* (valid only in the room containing the target). In this setup, $H_{\rm LO}\approx 5$ steps, and $H_{\rm HI}\approx 10$ –12 steps. The episode terminates after 100 prim-

itive steps if the agent is unsuccessful. The subpolicies and meta-controller use similar neural network architectures and only differ in the number of action outputs. (Details of network architecture are provided in Appendix B.)

Hierarchically Guided IL. We first compare our hierarchical IL algorithms with their flat versions. The algorithm performance is measured by success rate, defined as the average rate of successful task completion over the previous 100 test episodes, on random environment instances not used for training. The cost of each Label operation equals the length of the labeled trajectory, and the cost of each Inspect operation equals 1.

Both h-BC and hg-DAgger outperform flat imitation learners (Figure 2, left). hg-DAgger, in particular, achieves consistently the highest success rate, approaching 100% in fewer than 1000 episodes. Figure 2 (left) displays the median as well as the range from minimum to maximum success rate over 5 random executions of the algorithms.

Expert cost varies significantly between the two hierarchical algorithms. Figure 2 (middle) displays the same success rate, but as a function of the expert cost. hg-DAgger achieves significant savings in expert cost compared to other imitation learning algorithms thanks to a more efficient use of the LO-level expert through hierarchical guidance. Figure 1 (middle) shows that hg-DAgger requires most of its LO-level labels early in the training and requests primarily HI-level labels after the subgoals have been mastered. As a result, hg-DAgger requires only a fraction of LO-level labels compared to flat DAgger (Figure 2, right).

Hierarchically Guided IL/RL. We evaluate hg-DAgger/Q with deep double Q-learning (DDQN, Van Hasselt et al., 2016) and prioritized experience replay (Schaul et al., 2015b) as the underlying RL procedure. Each subpolicy learner receives a pseudo-reward of 1 for each successful execution, corresponding to stepping through the correct door (e.g., door to the north if the subgoal is north) and negative reward for stepping into lava or through other doors.

Figure 1 (right) shows the learning progression of hg-DAgger/Q, implying two main observations. First, the number of HI-level labels rapidly increases initially and then flattens out after the learner becomes more successful, thanks to the availability of Inspect_FULL operation. As the hybrid algorithm makes progress and the learning agent passes the Inspect_FULL operation increasingly often, the algorithm starts saving significantly on expert feedback. Second, the number of HI-level labels is higher than for both hg-DAgger and h-BC. Inspect_FULL returns Fail often, especially during the early parts of training. This is primarily due to the slower learning speed of *Q*-learning at the LO level, requiring more expert feedback at the HI

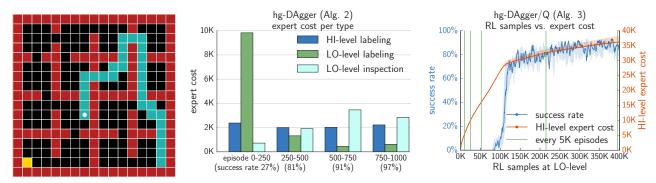


Figure 1. Maze navigation. (Left) One sampled environment instance; the agent needs to navigate from bottom right to bottom left. (Middle) Expert cost over time for hg-DAgger; the cost of Label operations equals the length of labeled trajectory, the cost of Inspect operations is 1. (Right) Success rate of hg-DAgger/Q and the HI-level label cost as a function of the number of LO-level RL samples.

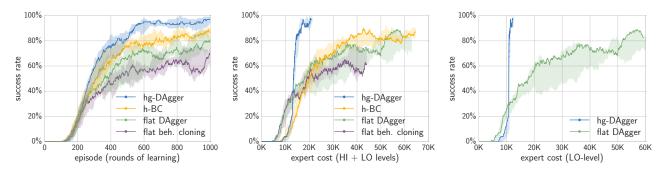


Figure 2. Maze navigation: hierarchical versus flat imitation learning. Each episode is followed by a round of training and a round of testing. The success rate is measured over previous 100 test episodes; the expert cost is as in Figure 1. (Left) Success rate per episode. (Middle) Success rate versus the expert cost. (Right) Success rate versus the LO-level expert cost.

level. This means that the hybrid algorithm is suited for settings where LO-level expert labels are either not available or more expensive than the HI-level labels. This is exactly the setting we analyze in the next section.

In Appendix B.1, we compare hg-DAgger/Q with hierarchical RL (h-DQN, Kulkarni et al., 2016), concluding that h-DQN, even with significantly more LO-level samples, fails to reach success rate comparable to hg-DAgger/Q. Flat Q-learning also fails in this setting, due to a long planning horizon and sparse rewards (Mnih et al., 2015).

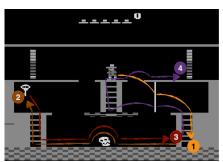
6.2. Hierarchically Guided IL/RL vs Hierarchical RL: Comparison on Montezuma's Revenge

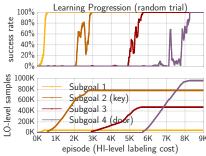
Task Overview. Montezuma's Revenge is among the most difficult Atari games for existing deep RL algorithms, and is a natural candidate for hierarchical approach due to the sequential order of subtasks. Figure 3 (left) displays the environment and an annotated sequence of subgoals. The four designated subgoals are: go to bottom of the right stair, get the key, reverse path to go back to the right stair, then go to open the door (while avoiding obstacles throughout).

The agent is given a pseudo-reward of 1 for each subgoal

completion and -1 upon loss of life. We enforce that the agent can only have a single life per episode, preventing the agent from taking a shortcut after collecting the key (by taking its own life and re-initializing with a new life at the starting position, effectively collapsing the task horizon). Note that for this setting, the actual game environment is equipped with two positive external rewards corresponding to picking up the key (subgoal 2, reward of 100) and using the key to open the door (subgoal 4, reward of 300). Optimal execution of this sequence of subgoals requires more than 200 primitive actions. Unsurprisingly, flat RL algorithms often achieve a score of 0 on this domain (Mnih et al., 2015; 2016; Wang et al., 2016).

hg-DAgger/Q versus h-DQN. Similar to the maze domain, we use DDQN with prioritized experience replay at the LO level of hg-DAgger/Q. We compare its performance with h-DQN using the same neural network architecture as Kulkarni et al. (2016). Figure 3 (middle) shows the learning progression of our hybrid algorithm. The HI-level horizon $H_{\rm HI}=4$, so meta-controller is learnt from fairly few samples. Each episode roughly corresponds to one Label_{HI} query. Subpolicies are learnt in the order of subgoal execution as prescribed by the expert.





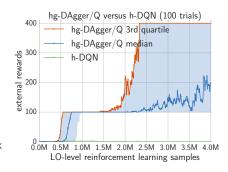


Figure 3. Montezuma's revenge: hg-DAgger/Q versus h-DQN. (Left) Screenshot of Montezuma's Revenge in black-and-white with color-coded subgoals. (Middle) Learning progression of hg-DAgger/Q in solving the first room of Montezuma's Revenge for a typical successful trial. Subgoal colors match the left pane; success rate is the fraction of times the LO-level RL learner achieves its subgoal over the previous 100 attempts. (Right) Learning performance of hg-DAgger/Q versus h-DQN (median and inter-quartile range).

We introduce a simple modification to *Q*-learning on the LO level to speed up learning: the accumulation of experience replay buffer does not begin until the first time the agent encounters positive pseudo-reward. During this period, in effect, only the meta-controller is being trained. This modification ensures the reinforcement learner encounters at least some positive pseudo-rewards, which boosts learning in the long horizon settings and should naturally work with any off-policy learning scheme (DQN, DDQN, Dueling-DQN). For a fair comparison, we introduce the same modification to the h-DQN learner (otherwise, h-DQN failed to achieve any reward).

To mitigate the instability of DQN (see, for example, learning progression of subgoal 2 and 4 in Figure 3, middle), we introduce one additional modification. We terminate training of subpolicies when the success rate exceeds 90%, at which point the subgoal is considered learned. Subgoal success rate is defined as the percentage of successful subgoal completions over the previous 100 attempts.

Figure 3 (right) shows the median and the inter-quartile range over 100 runs of hg-DAgger/Q and hg-DQN.⁷ The LO-level sample sizes are not directly comparable with the middle panel, which displays the learning progression for a random successful run, rather than an aggregate over multiple runs. In all of our experiments, the performance of the imitation learning component is stable across many different trials, whereas the performance of the reinforcement learning component varies substantially. Subgoal 4 (door) is the most difficult to learn due to its long horizon whereas subgoals 1–3 are mastered very quickly, especially compared to h-DQN. Our algorithm benefits from hierarchical guidance and accumulates experience for each subgoal only within the relevant part of the state space, where the subgoal is part of an optimal trajectory. In contrast, h-DQN

may pick bad subgoals and the resulting LO-level samples then "corrupt" the subgoal experience replay buffers and substantially slow down convergence.⁸

The number of HI-level labels in Figure 3 (middle) can be further reduced by using a more efficient RL procedure than DDQN at the LO level. In the specific example of Montezuma's Revenge, the actual human effort is in fact much smaller, since the human expert needs to provide a sequence of subgoals only once (together with simple subgoal detectors), and then HI-level labeling can be done automatically. The human expert only needs to understand the high level semantics, and does not need to be able to play the game.

7. Conclusion

We have presented *hierarchical guidance* framework and shown how it can be used to speed up learning and reduce the cost of expert feedback in hierarchical imitation learning and hybrid imitation—reinforcement learning.

Our approach can be extended in several ways. For instance, one can consider weaker feedback such as preference or gradient-style feedback (Fürnkranz et al., 2012; Loftin et al., 2016; Christiano et al., 2017), or a weaker form of imitation feedback, only saying whether the agent action is correct or incorrect, corresponding to bandit variant of imitation learning (Ross et al., 2011).

Our hybrid IL/RL approach relied on the availability of a subgoal termination predicate indicating when the subgoal is achieved. While in many settings such a termination predicate is relatively easy to specify, in other settings this predicate needs to be learned. We leave the question of learning the termination predicate, while learning to act from reinforcement feedback, open for future research.

⁷In Appendix B, we present additional plots, including 10 best runs of each algorithm, subgoal completion rate over 100 trials, and versions of Figure 3 (middle) for additional random instances.

⁸In fact, we further reduced the number of subgoals of h-DQN to only two initial subgoals, but the agent still largely failed to learn even the second subgoal (see the appendix for details).

Acknowledgments

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A. Proofs

Proof of Theorem 2. The first term TC_{FULL}^I should be obvious as the expert inspects the agent's overall behavior in each episode. Whenever something goes wrong in an episode, the expert labels the whole trajectory, incurring C_{FULL}^L each time. The remaining work is to bound the number of episodes where agent makes one or more mistakes. This quantity is bounded by the number of total mistakes made by the halving algorithm, which is at most the logarithm of the number of candidate functions (policies), $\log |\Pi_{\text{FULL}}| = \log \left(|\mathcal{M}||\Pi_{\text{Lo}}|^{|\mathcal{G}|}\right) = \log |\mathcal{M}| + |\mathcal{G}| \log |\Pi_{\text{Lo}}|$. This completes the proof.

Proof of Theorem 1. Similar to the proof of Theorem 2, the first term TC_{FULL}^{I} is obvious. The second term corresponds to the situation where Inspect_{FULL} finds issues. According to Algorithm 2, the expert then labels the subgoals and also inspects whether each subgoal is accomplished successfully, which incurs $C_{\rm HI}^L + H_{\rm HI} C_{\rm LO}^I$ cost each time. The number of times that this situation happens is bounded by (a) the number of times that a wrong subgoal is chosen, plus (b) the number of times that all subgoals are good but at least one of the subpolicies fails to accomplish the subgoal. Situation (a) occurs at most $\log |\mathcal{M}|$ times. In situation (b), the subgoals chosen in the episode must come from \mathcal{G}_{opt} , and for each of these subgoals the halving algorithm makes at most $\log |\Pi_{LO}|$ mistakes. The last term corresponds to cost of Labello operations. This only occurs when the meta-controller chooses a correct subgoal but the corresponding subpolicy fails. Similar to previous analysis, this situation occurs at most $\log |\Pi_{LO}|$ for each "good" subgoal $(g \in \mathcal{G}_{opt})$. This completes the proof.

B. Additional Experimental Details

In our experiments, *success rate* and *external rewards* are reported as the trailing average over previous 100 episodes of training. For hierarchical imitation learning experiments in maze navigation domain, the success rate is only measured on separate test environments not used for training.

In addition to experimental results, in this section we describe our mechanism for subgoal detection / terminal predicate for Montezuma's Revenge and how the Maze Navigation environments are created. Network architectures from our experiments are in Tables 1 and 2.

B.1. Maze Navigation Domain

We compare hg-DAgger/Q with the hierarchical reinforcement learning baseline (h-DQN, Kulkarni et al., 2016) with the same network architecture for the meta-controller and subpolicies as hg-DAgger/Q and similarly enhanced *Q*-learning procedure.

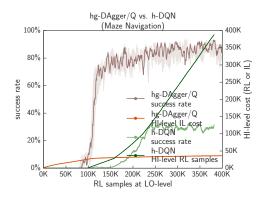


Figure 4. Maze navigation: hybrid IL-RL (full task) versus h-DQN (with 50% head-start).

Similar to the Montezuma's Revenge domain, h-DQN does not work well for the maze domain. At the HI level, the planning horizon of 10–12 with 4–5 possible subgoals in each step is prohibitively difficult for the HI-level reinforcement learner and we were not able to achieve non-zero rewards within in any of our experiments. To make the comparison, we attempted to provide additional advantage to the h-DQN algorithm by giving it some head-start, so we ran h-DQN with 50% reduction in the horizon, by giving the hierarchical learner the optimal execution of the first half of the trajectory. The resulting success rate is in Figure 4. Note that the hybrid IL-RL does not get the 50% advantage, but it still quickly outperforms h-DQN, which flattens out at 30% success rate.

B.1.1. Creating Maze Navigation Environments

We create 2000 maze navigation environments, 1000 of which are used for training and 1000 maps are used for testing. The comparison results for maze navigation (e.g., Figure 2) are all based on randomly selected environments among 1000 test maps. See Figure 5 for additional examples of the environments created. For each map (environment instance), we start with a 17×17 grid, which are divided into 4×4 room structure. Initially, no door exists in between rooms. To create an instance of the maze navigation environment, the goal block (yellow) and the starting position are randomly selected (accepted as long as they are not the same). Next, we randomly select a wall separating two different room and replace a random red block (lava) along this wall with a door (black cell). This process continues until two conditions are satisfied:

- There is a feasible path between the starting location and the goal block (yellow)
- The minimum distance between start to goal is at least 40 steps. The optimal path can be constructed using

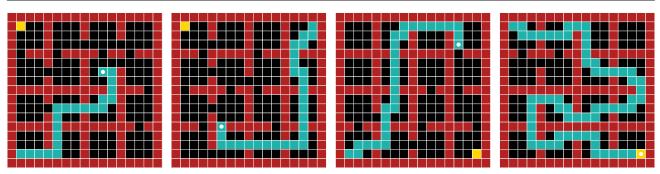


Figure 5. Maze navigation. Sample random instances of the maze domain (different from main text). The 17×17 pixel representation of the maze is used as input for neural network policies.

graph search

Each of the 2000 environments create must satisfy both conditions. The expert labels for each environment come from optimal policy computed via value iteration (which is fast based on tabular representation of the given grid world).

B.1.2. Hyperparameters for Maze Navigation

The network architecture used for maze navigation is described in Table 1. The only difference between subgoal policy networks and metacontroller network is the number of output class (4 actions versus 5 subgoals). For our hierarchical imitation learning algorithms, we also maintain a small network along each subgoal policy for subgoal termination classification (one can also view the subgoal termination classifier as an extra head of the subgoal policy network).

The contextual input (state) to the policy networks consists of 3-channel pixel representation of the maze environment. We assign different (fixed) values to goal block, agent location, agent's trail and lava blocks. In our hierarchical imitation learning implementations, the base policy learner (DAgger and behavior cloning) update the policies every 100 steps using stochastic optimization. We use Adam optimizer and learning rate of 0.0005.

Table 1. Network Architecture—Maze Domain

Convolutional Layer Convolutional Layer Max Pooling Layer	32 filters, kernel size 3, stride 1 32 filters, kernel size 3, stride 1 pool size 2
4: Convolutional Layer5: Convolutional Layer6: Max Pooling Layer	64 filters, kernel size 3, stride 1 64 filters, kernel size 3, stride 1 pool size 2
7: Fully Connected Layer	256 nodes, relu activation
8: Output Layer	softmax activation (dimension 4 for subpolicy,

dimension 5 for meta-controller)

B.2. Montezuma's Revenge

Although the imitation learning component tends to be stable and consistent, the samples required by the reinforcement learners can vary between experiments with identical hyperparameters. In this section, we report additional results of our hybrid algorithm for the Montezuma's Revenge domain.

For the implementation of our hybrid algorithm on the game Montezuma's Revenge, we decided to limit the computation to 4 million frames for the LO-level reinforcement learners (in aggregate across all 4 subpolicies). Out of 100 experiments, 81 out of 100 successfully learn the first 3 subpolicies, 89 out of 100 successfully learn the first 2 subpolicies. The last subgoal (going from the bottom of the stairs to open the door) proved to be the most difficult and almost half of our experiments did not manage to finish learning the fourth subpolicy within the 4 million frame limit (see Figure 7 middle pane). The reason mainly has to do with the longer horizon of subgoal 4 compared to other three subgoals. Of course, this is a function of the design of subgoals and one can always try to shorten the horizon by introducing intermediate subgoals.

However, it is worth pointing out that even as we limit the h-DQN baseline to only 2 subgoals (up to getting the key), the h-DQN baseline generally tends to underperform our proposed hybrid algorithm by a large margin. Even with the given advantage we confer to our implementation of h-DQN, all of the h-DQN experiments failed to successfully master the second subgoal (getting the key). It is instructive to also examine the sample complexity associated with getting the key (the first positive external reward, see Figure 7 right pane). Here the horizon is sufficiently short to appreciate the difference between having expert feedback at the HI level versus relying only on reinforcement learning to train the meta-controller.

The stark difference in learning performance (see Figure 7 right) comes from the fact that the HI-level expert advice effectively prevents the LO-level reinforcement learners from

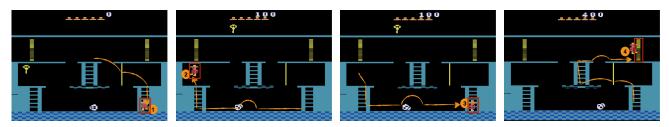


Figure 6. Montezuma's Revenge: Screenshots of the environment with 4 designated subgoals in sequence.

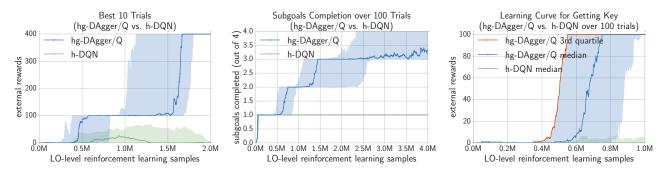


Figure 7. Montezuma's revenge: hybrid IL-RL versus hierarchical RL. (Left) Median reward, min and max across the best 10 trials. The agent completes the first room in less than 2 million samples. The shaded region corresponds to min and max of the best 10 trials. (Middle) Median, first and third quartile of subgoal completion rate across 100 trials. The shaded region corresponds to first and third quartile. (Right) Median, first and third quartile of reward across 100 trials. The shaded region corresponds to first and third quartile. h-DQN only considers the first two subgoals to simplify the learning task.

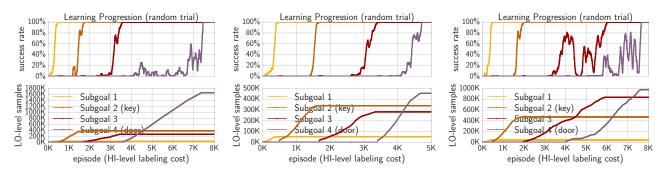


Figure 8. Montezuma's revenge: Learning progression of Algorithm 3 in solving the entire first room. The figures show three randomly selected successful trials.

accumulating bad experience, which is frequently the case for h-DQN. The potential corruption of experience replay buffer also implies at in our considered setting, learning with hierarchical DQN is no easier compared to flat DQN learning. Hierarchical DQN is thus susceptible to collapsing into the flat learning version.

B.2.1. SUBGOAL DETECTORS FOR MONTEZUMA'S REVENGE

In principle, the system designer would select the hierarchical decomposition that is most convenient for giving feedback. For Montezuma's Revenge, we set up four subgoals and automatic detectors that make expert feedback trivial. The subgoals are landmarks that are described by

small rectangles. For example, the door subgoal (subgoal 4) would be represented by a patch of pixel around the right door (see Figure 6 right). We can detect the correct termination / attainment of this subgoal by simply counting the number of pixels inside of the pre-specified box that has changed in value. Specifically in our case, subgoal completion is detected if at least 30% of pixels in the landmark's detector box changes.

B.2.2. HYPERPARAMETERS FOR MONTEZUMA'S REVENGE

Neural network architecture used is similar to (Kulkarni et al., 2016). One difference is that we train a separate neural network for each subgoal policy, instead of main-

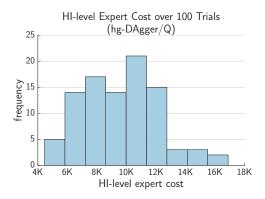


Figure 9. Montezuma's Revenge: Number of HI-level expert labels. Distribution of Hi-level expert labels needed across 100 trials; the histogram excludes 6 outliers whose number of labels exceeds 20K for ease of visualization

Table 2. Network Architecture—Montezuma's Revenge

1: Conv. Layer	32 filters, kernel size 8, stride 4, relu
2: Conv. Layer	64 filters, kernel size 4, stride 2, relu
3: Conv. Layer	64 filters, kernel size 3, stride 1, relu
4: Fully Connected	512 nodes, relu,
Layer	normal initialization with std 0.01
5: Output Layer	linear (dimension 8 for subpolicy, dimension 4 for meta-controller)

taining a subgoal encoding as part of the input into a policy neural network that shares representation for multiple subgoals jointly. Empirically, sharing representation across multiple subgoals causes the policy performance to degrade we move from one learned subgoal to the next (a phenomenon of catastrophic forgetting in deep learning literature). Maintaining each separate neural network for each subgoal ensures the performance to be stable across subgoal sequence. The metacontroller policy network also has similar architecture. The only difference is the number of output (4 output classes for metacontroller, versus 8 classes (actions) for each LO-level policy).

For training the LO-level policy with Q-learning, we use DDQN (Van Hasselt et al., 2016) with prioritized experience replay (Schaul et al., 2015b) (with prioritization exponent $\alpha=0.6$, importance sampling exponent $\beta_0=0.4$). Similar to previous deep reinforcement learning work applied on Atari games, the contextual input (state) consists of four consecutive frames, each converted to grey scale and reduced to size 84×84 pixels. Frame skip parameter as part of the Arcade Learning Environment is set to the default value of 4. The repeated action probability is set to 0, thus the Atari environment is largely deterministic. The experience memory has capacity of 500K. The target net-

work used in *Q*-learning is updated every 2000 steps. For stochastic optimization, we use rmsProp with learning rate of 0.0001, with mini-batch size of 128.

C. Additional Related Work

Imitation Learning. Another dichotomy in imitation learning, as well as in reinforcement learning, is that of value-function learning versus policy learning. The former setting (Abbeel & Ng, 2004; Ziebart et al., 2008) assumes that the optimal (demonstrated) behavior is induced by maximizing an unknown value function. The goal then is to learn that value function, which imposes a certain structure onto the policy class. The latter setting (Daumé et al., 2009; Ross et al., 2011; Ho & Ermon, 2016) makes no such structural assumptions and aims to directly fit a policy whose decisions well imitate the demonstrations. This latter setting is typically more general but often suffers from higher sample complexity. Our approach is agnostic to this dichotomy and can accommodate both styles of learning. Some instantiations of our framework allow for deriving theoretical guarantees, which rely on the policy learning setting. Sample complexity comparison between imitation learning and reinforcement learning has not been studied much in the literature, perhaps with the exception of the recent analysis of AggreVaTeD (Sun et al., 2017).

Hierarchical Reinforcement Learning. Feudal RL is another hierarchical framework that is similar to how we decompose the task hierarchically (Dayan & Hinton, 1993; Dietterich, 2000; Vezhnevets et al., 2017). In particular, a feudal system has a manager (similar to our HIlevel learner) and multiple submanagers (similar to our LOlevel learners), and submanagers are given pseudo-rewards which define the subgoals. Prior work in feudal RL use reinforcement learning for both levels; this can require a large amount of data when one of the levels has a long planning horizon, which we demonstrate in our experiments. In contrast, we propose a more general framework where imitation learners can be used to substitute reinforcement learners to substantially speed up learning, whenever the right level of expert feedback is available. Hierarchical policy classes have been additional studied by He et al. (2010), Hausknecht & Stone (2016), Zheng et al. (2016), and Andreas et al. (2017).

Learning with Weaker Feedback. Our work is motivated by efficient learning under weak expert feedback. When we only receive demonstration data at the high level, and must utilize reinforcement learning at the low level, then our setting can be viewed as an instance of learning under weak demonstration feedback. The primary other way to elicit weaker demonstration feedback is with preference-based or gradient-based learning, studied by Fürnkranz et al. (2012), Loftin et al. (2016), and Christiano et al. (2017).