

# Efficiency in Practice



Methods for reducing unnecessary work:

1. Avoid repeating the same calculations by storing the results of the calculations in auxiliary variables.
2. Avoid unnecessary copying of arrays into larger sizes by pre-allocating them.
3. Avoid unnecessary calculations by taking advantage of the characteristics of the input.

And always focus on those portions of code that are computationally intensive.

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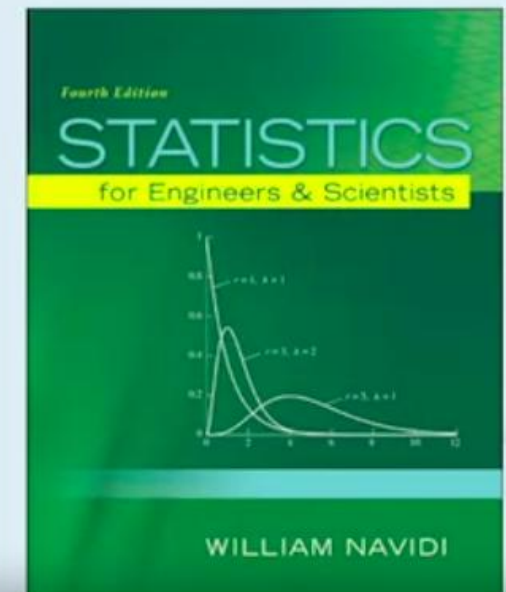
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4<sup>th</sup> Edition

By William Navidi

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here geared towards  
engineers and scientists.



# MATLAB and Implicit Looping

MATLAB invented by Cleve Moler to work with matrices and arrays

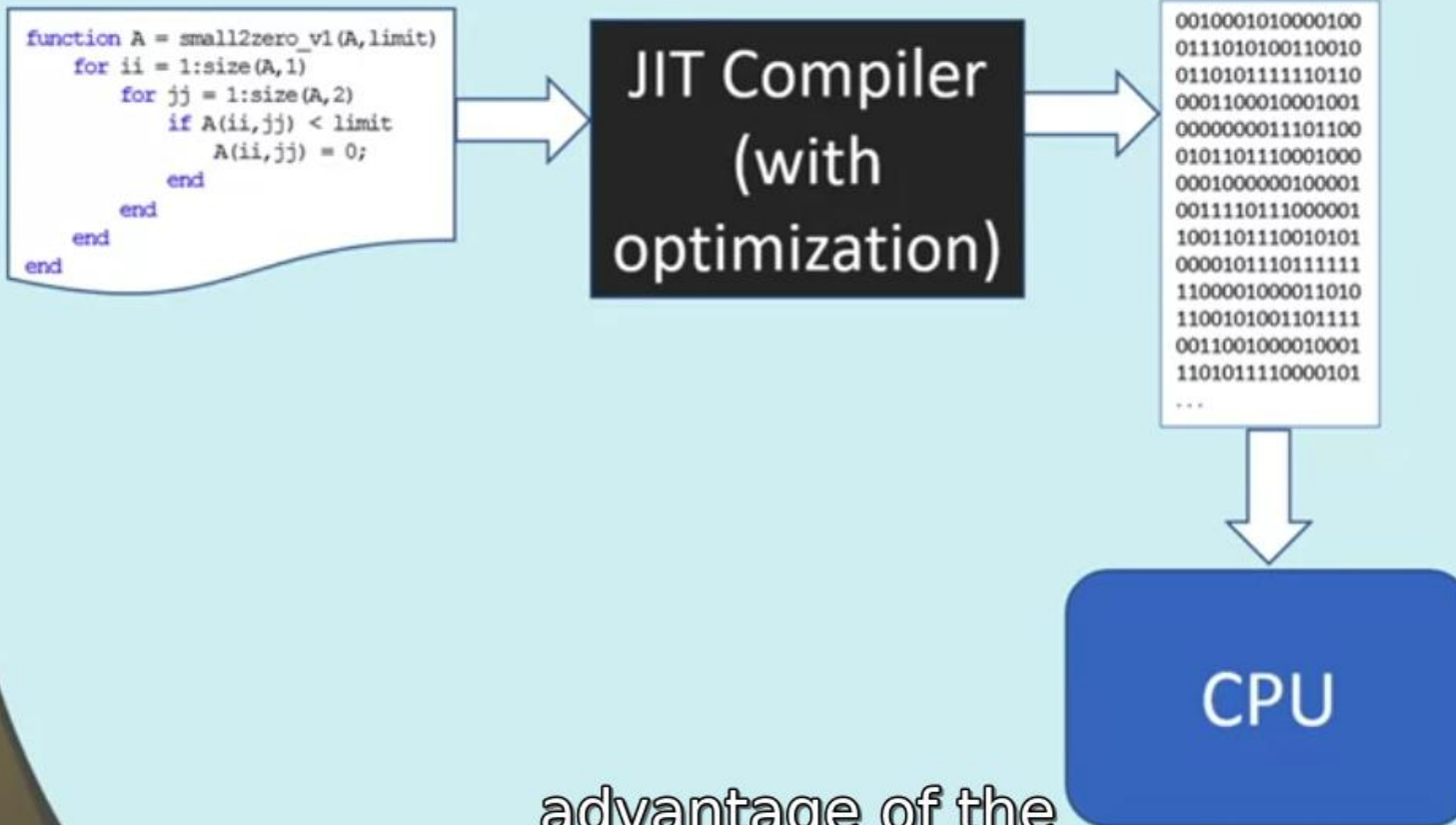
- Moler

- Expert in numerical computation
- Used the notation of numerical computation
- Notation implied loops that were not written out
- Computer language should incorporate that notation

- MATLAB gets implicit looping!

`*` `+` `-` `/` `&` `mean()` `sin()` `max()` `log()`  
`|` `~` `==` `tan()` `abs()` `sum()` `std()` `exp()` `nthroot`  
`min()` `det()` `cos()`

# Just-in-Time Compiling



advantage of the  
optimizations anyway,



# Just-in-Time Compiling

```
function A = small2zero_v1(A,limit)
    for ii = 1:size(A,1)
        for jj = 1:size(A,2)
            if A(ii,jj) < limit
                A(ii,jj) = 0;
            end
        end
    end
end
```

JIT Compiler

```
0010001010000100
0111010100110010
0110101111110110
0001100010001001
0000000011101100
0101101110001000
0001000000100001
0011110111000001
1001101110010101
0000101110111111
1100001000011010
1100101001101111
0011001000010001
1101011110000101
...
```

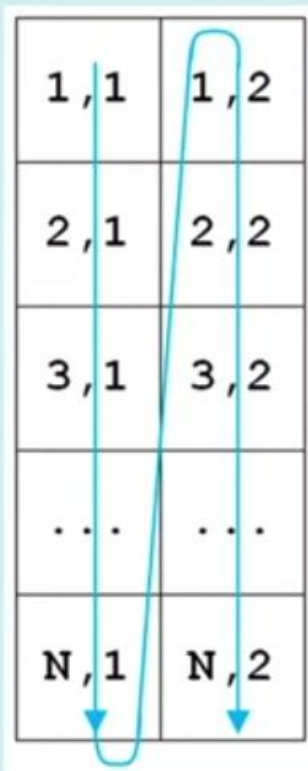
CPU

the function or give  
the command clear all,

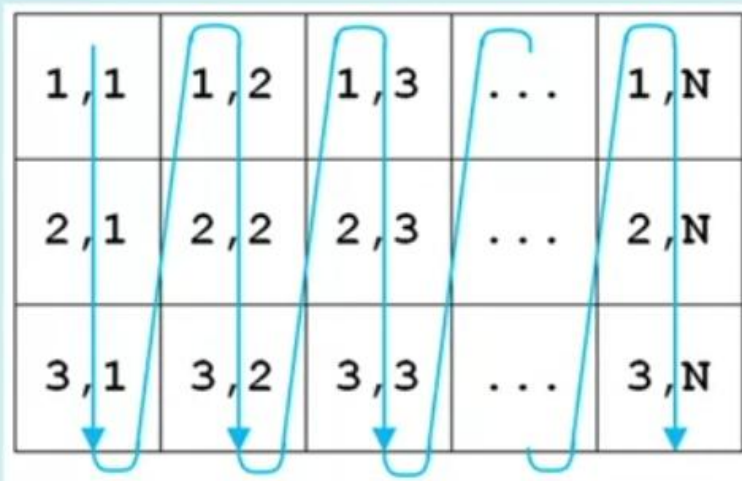
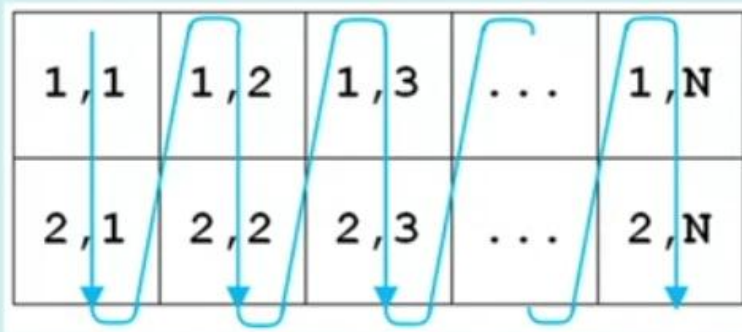
# Modes of Passing Arguments

- Call by value
  - Copy of argument is placed on the stack.
  - Changes to argument in function leave actual argument unchanged
  - Copying large arrays takes lots of time and lots of memory
- Call by reference
  - Pointer to argument is placed on the stack.
- Reverting to call by value during function execution
  - Execution halts while argument is copied to stack

Let's see an example.



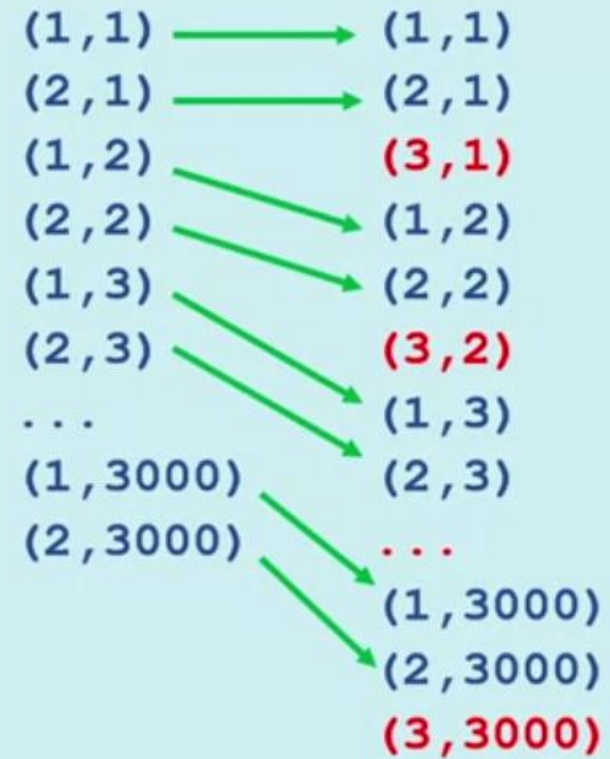
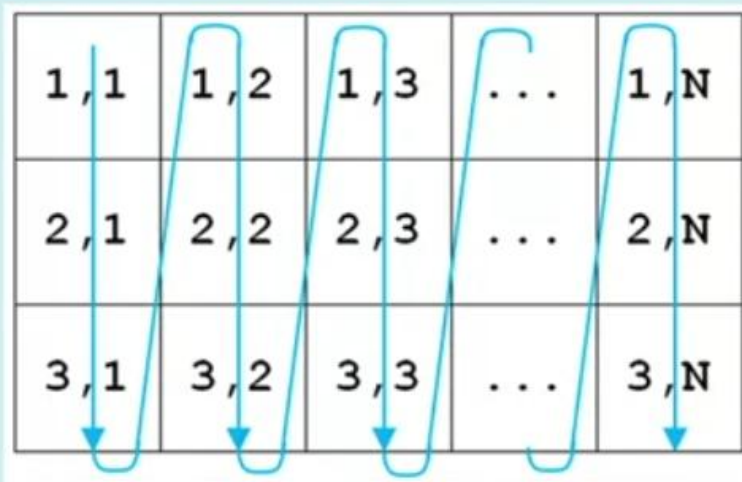
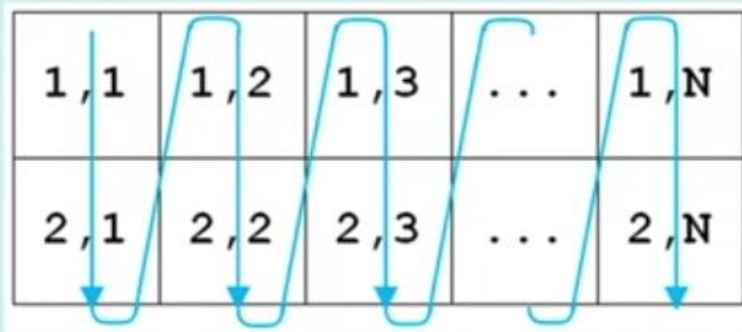
(1,1)	(1,1)
(2,1)	(2,1)
(3,1)	(3,1)
...	...
(3000,1)	(3000,1)
(1,2)	(1,2)
(2,2)	(2,2)
(3,2)	(3,2)
...	...
(3000,2)	(3000,2)
	(1,3)
	(2,3)
	(3,3)
	...
	(3000,3)



(1,1)  
 (2,1)  
 (1,2)  
 (2,2)  
 (1,3)  
 (2,3)  
 ...  
 (1,3000)  
 (2,3000)


(1,1)  
 (2,1)  
 (3,1)  
 (1,2)  
 (2,2)  
 (3,2)  
 ...  
 (1,3)  
 (2,3)  
 (3,3)  
 ...  
 (1,3000)  
 (2,3000)  
 (3,3000)






# Index Re-ordering

```
for ii = 1:M
    for jj = 1:N
        A(ii,jj) = . . .
    end
end
```



```
for ii = 1:N
    for jj = 1:M
        A(jj,ii) = . . .
    end
end
```

1,1	1,2	1,3
2,1	2,2	2,3
3,1	3,2	3,3
...	...	...
N,1	N,2	N,3

  
**3,000**  
 (1,1)  
 (2,1)  
 (3,1)  
 ...  
 (3000,1)  
 (1,2)  
 (2,2)  
 (3,2)  
 ...  
 (3000,2)  
 (1,3)  
 (2,3)  
 (3,3)  
 ...  
 (3000,3)

stride

# Index Re-ordering

```
for ii = 1:M
    for jj = 1:N
        A(ii,jj) = . . .
    end
end
```

row-major  
order

```
for ii = 1:N
    for jj = 1:M
        A(jj,ii) = . . .
    end
end
```

column-major  
order



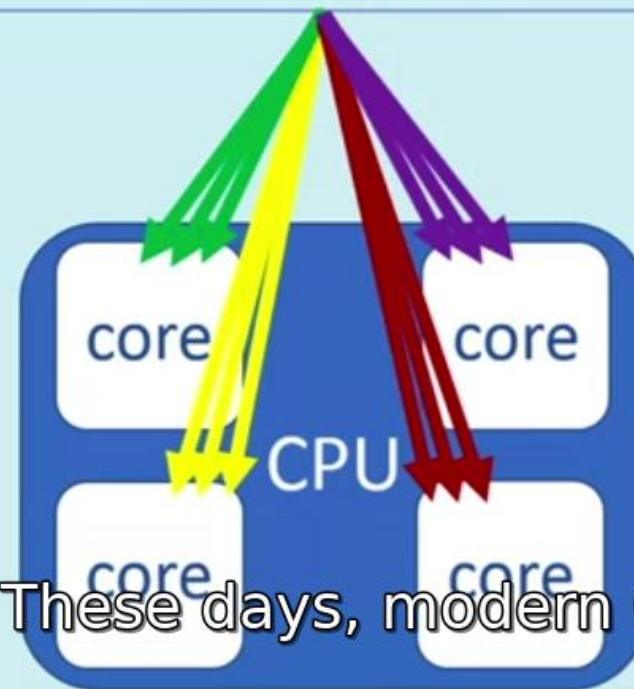
# parfor

`parfor` stands for “parallel for-loop”

```
parfor i = 1:12
```

```
    a(i) = max(abs(eig(rand(500)))));
```

```
end
```



These days, modern CPUs

# parfor

`parfor` stands for “parallel for-loop”

```
parfor i = 1:12
```

```
    a(i) = max(abs(eig(rand(500)))));
```

```
end
```



# parfor

`parfor` stands for “parallel for-loop”

```
parfor i = 1:12
```

```
    a(i) = max(abs(eig(rand(500)))));
```

```
end
```

solved repeatedly on  
randomly generated data,

Command Window

`fx >>`

Editor - /Users/fitzpajm/MATLAB-Drive/MATLAB Course 2/Lesson...

```
eigen_for.m x eigen_parfor.m x +
1 function a = eigen_for(A3D)
2   a = zeros(1, size(A3D, 1));
3   for ii = 1: length(a)
4       a(ii) = max(abs(eig(squeeze(A3D(ii, :, :)))));
5   end
```

Eigenvalues are an important  
concept in linear algebra,



# Lesson 4

- First three lectures: Algorithms and complexity
- Fourth lecture: Eliminating unnecessary work
- Fifth lecture:
  - Vectorization
  - Logical indexing
  - Avoiding function calls
  - Call-by-reference
  - Reduction of array re-allocation

efficient index ordering,