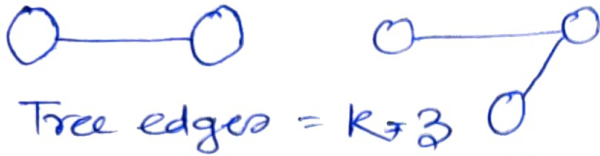


Introduction to algorithm and analysis
Assignment 9 solution

① Answer — (d)

Explanation — Tree edges are the edges that are part of DFS. If there are x tree edges in a tree, then, $x+1$ vertices in the tree.



Tree edges = $k+3$

vertices $n = 5$

Connected Components = 2

② Answer — b.

Explanation — (a) There can be more than one paths with same weight. Consider a path with one edge of weight 5 and another path with two edges of weights 2 and 3. Both the paths have same weights.

(b) Dijkstra and Bellman Ford Algo. both work fine for a graph with all +ve weights. but they are different algo. and may pick different edges for shortest paths.

③ Answer — c

④ Answer — c

⑤ Answer — d

Explanation — Dijkstra's algo. single source shortest path is not guaranteed to work for graphs with -ve weight edges, but it works for the given graph. Let us see.

Let us run the 1st pass

b 1

b is minimum, so shortest distance to b is 1

After 1st pass, distances are

c 3, e -2

e is minimum, so shortest distance to e is -2

After 2nd pass, distances are

c 3, f 0

f is minimum, so shortest distance to f is 0

After 3rd pass distance are

c 3, g 3.

Both are same, let us take g. so shortest distance to g is 3.

After 4th pass distances are

c 3, h 5,

c is minimum. so shortest distance to c is 3.

After 5th pass, distances are

h - 2

h is minimum. so shortest distance to h is -2

⑥ Answer - a

Explanation - the shortest path remains same. It is like if we change unit of distance from meter to kilometer the shortest path don't change

⑦ Answer - c

⑧ Answer - d

Explanation - (i) a b e g h f (visit a, explore all adjacents through b, and so on). In this b is adjacent e is picked 1st

(iii) a b f h g e (visit a, explore all adjacents through b, and so on) on this b's adjacents f is picked 1st.

(iv) a f g h b e (visit a, explore all adjacents through f and so on) on this f's adjacent g is picked 1st.

ii) a b f e h g can't be answer. as e is visited after f.

⑨ Answer - a

⑩ Answer - b.