

Hands on 3:

1:

$x=1; \rightarrow 1$

for $i=1:n \rightarrow n+1$

for $j=1:n \rightarrow n(n+1)$

$x=x+1; \rightarrow n^2$

The runtime would be calculated with following summation formula:

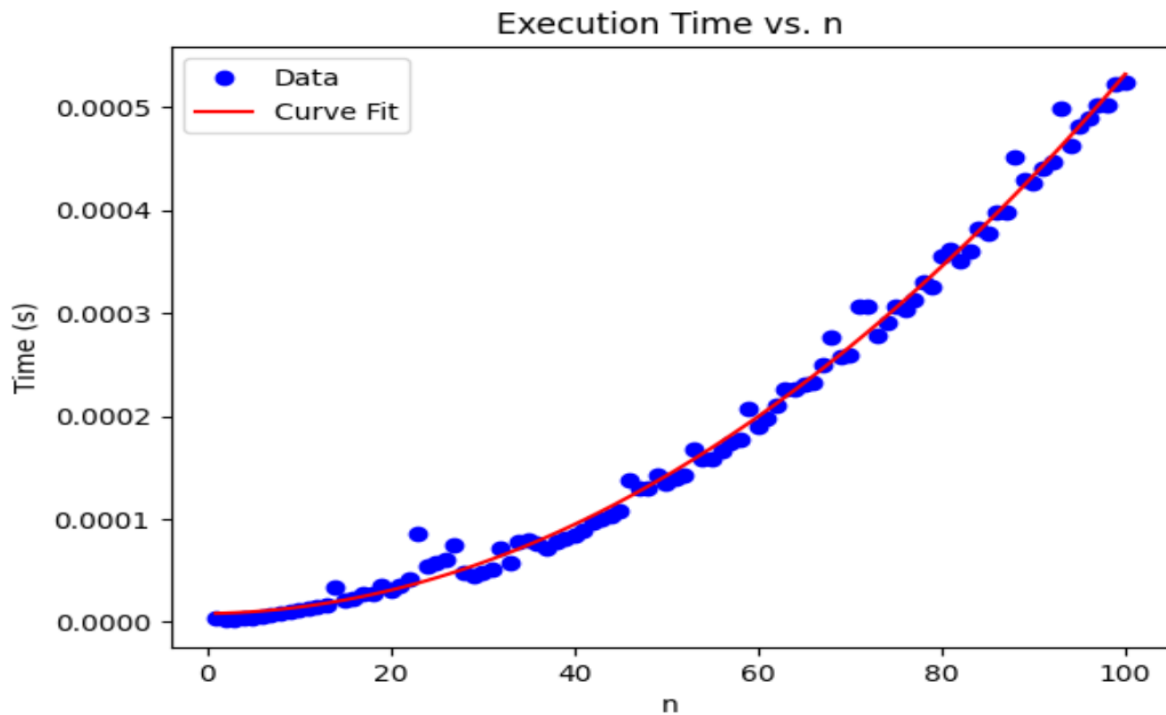
$$T(n) = 1 + \sum_{i=1}^{n+1} 1 \sum_{i=1}^n \sum_{j=1}^{n+1} 1 \sum_{i=1}^n \sum_{j=1}^n 1$$

$$\rightarrow t(n) = 1 + (n+1) + n(n+1) + n^2$$

$$\rightarrow T(n) = 2n^2 + 2n + 2$$

$O(n) = (n^2)$ [since the higher order term is (n^2) so the big O time complexity is (n^2)]

2:



3:

$$T(n) = an^2 + bn + c$$

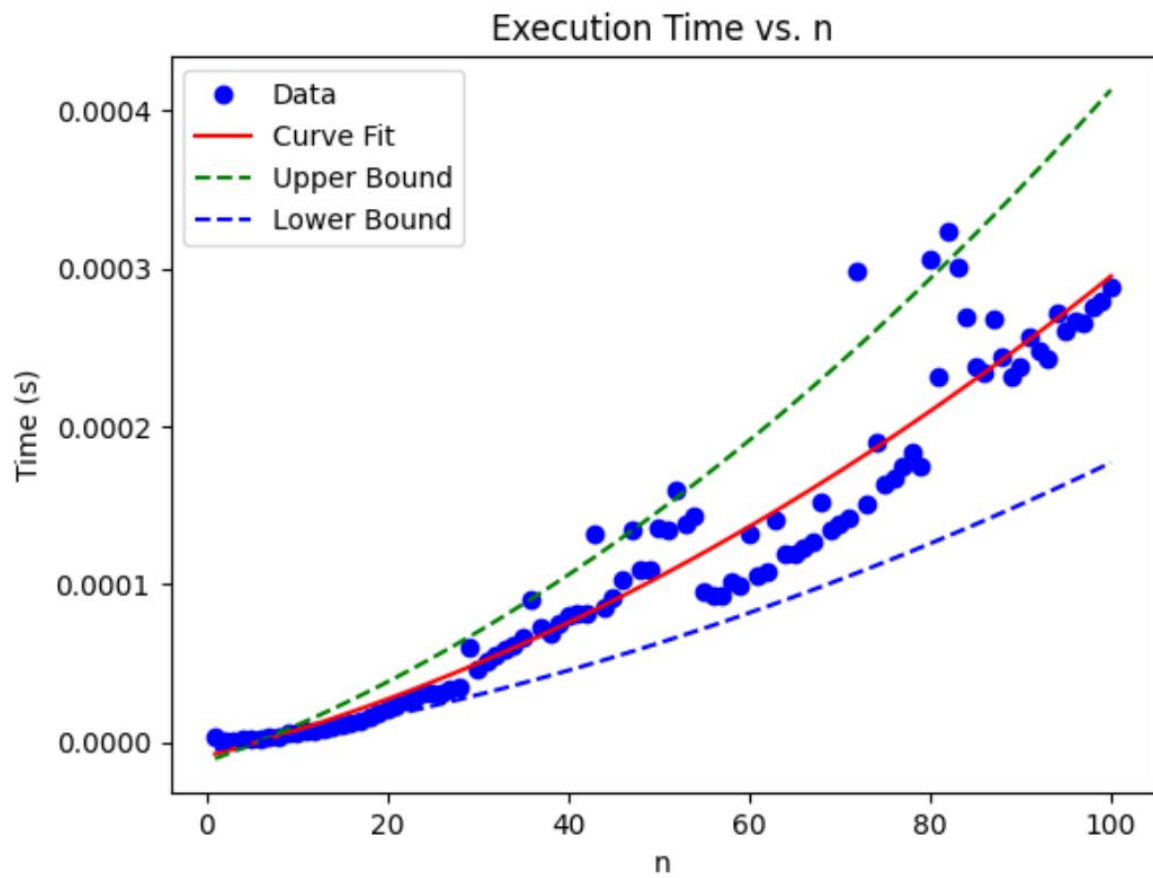
Upper bound: (n^2)

Lower bound: (n)

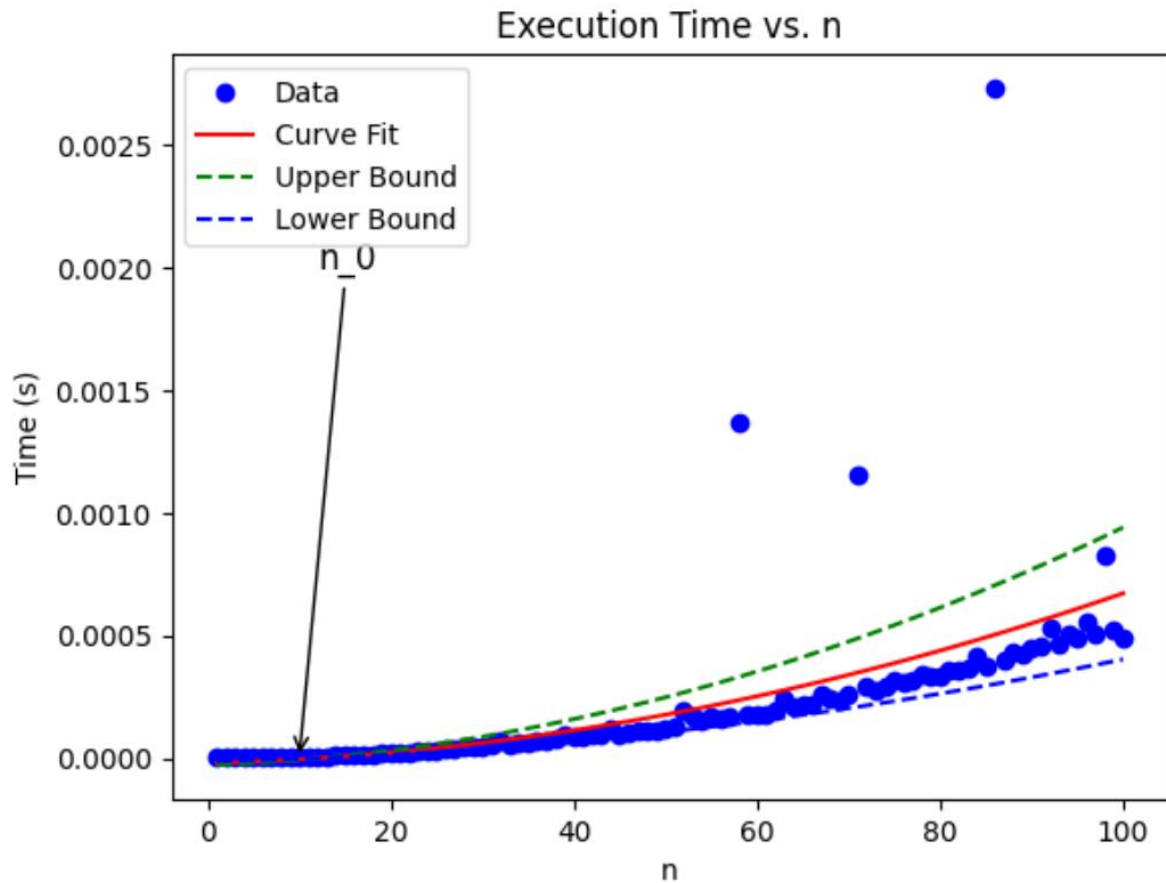
Big-O- (n^2)

Big-Theta- (n^2)

Big omega- (n^2)



4



4. By zooming the plot, at $n=10$ the upper bound is getting deviated from the fitted curve. So $n_0=10$ at which the algorithm's behavior becomes relevant or significant.

4: Yes, The runtime will be increased, The added statement $y=i+j$ will double the runtime by adding (n^n) to the run time

i.e $T(n) = 1 + (n+1) + n(n+1) + (n^2) + (n^2)$

5:

No, even the runtime increased there will be no change in the result as the equation stays quadratic. For Big-O notation we consider higher order terms and constants are ignored so it stays $O(n^2)$.